

The Categorical Might of PROC FREQ

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ABSTRACT

PROC FREQ is essential to anybody using Base SAS® for analyzing categorical data. This paper presents the various utilities of the FREQ procedure that enable in effective data analysis. The cases presented include a range of utilities such as finding counts, percentages, unique levels or records, Pearson chi-square test, Fisher's test, McNemar test, Cochran-Armitage trend test, binomial proportions test, relative risk, and odds ratio. In addition, this paper will show the ODS features available to effectively display your results. All the cases presented in this paper will prove the categorical might of PROC FREQ beyond doubt.

INTRODUCTION

PROC FREQ is one of the most commonly used procedure in SAS® and primarily used for analyzing categorical data. The FREQ procedure can generate one-way to n-way frequency and contingency tables along with various statistical measures of interest. The objective of this paper is to present some of the common utilities of PROC FREQ with regards to data manipulation and statistical analysis which will eventually prove the categorical might of this procedure. The utilities are applied to a dummy data set and presented as cases to easily discern their applicability. It is recommended to refer the PROC FREQ in SAS® procedure manual for complete list of available utilities which will further prove the usefulness of FREQ procedure.

The syntax of FREQ procedure with the summarized statement description is shown in Table 1. The snapshot of the two dummy data sets named MALTS and DOSES used in this paper is presented in Tables 2A and 2B respectively.

<u>Syntax</u>	<u>Statement Description</u>
PROC FREQ < options > ; BY variables ; EXACT <i>statistic-options</i> < / computation-options > ; OUTPUT <OUT=SAS-data-set > <i>output-options</i> ; TABLES <i>requests</i> < / options > ; TEST <i>options</i> ; WEIGHT <i>variable</i> < / option > ;	-provides separate analysis for each BY group -requests exact tests -requests an output data set -specifies tables and requests analyses -requests test for measure of association and agreement -identifies a weight variable

Table 1. PROC FREQ Syntax and the Summary of Statement Description

SITE	ENRLDATE	BIOPSYDT	CPSLIDES	oprej	Reader 1	Reader 2	lcrej	sex	agecat	ages	id
1	8/30/2010	7/24/2012	2	0	1	1	1	F	3	2	110
1	8/30/2010	3/15/2011	2	0	0	0	1	M	1	1	112
1	9/8/2010	6/7/2012	2	0	0	1	0	M	1	1	113
1	9/8/2010	6/18/2012	2	0	1	1	0	M	1	1	113
1	9/8/2010	6/28/2012	5	0	0	1	0	M	1	1	113
1	9/27/2010	12/15/2011	2	1	0	0	1	M	1	1	119

Table 2A Snapshot of MALTS Dataset

levels	event	count
0	No	20
0	Yes	0
1	No	18
1	Yes	2
2	No	21
2	Yes	3
3	No	16
3	Yes	5

Table 2B Snapshot of DOSES Dataset

Case 1: One-Way Frequency Table

Code 1 is the simplest statement of PROC FREQ procedure. This code will produce one-way frequency table for each variable in the most recently created data set. Code 2 follows the general syntax structure of PROC FREQ with

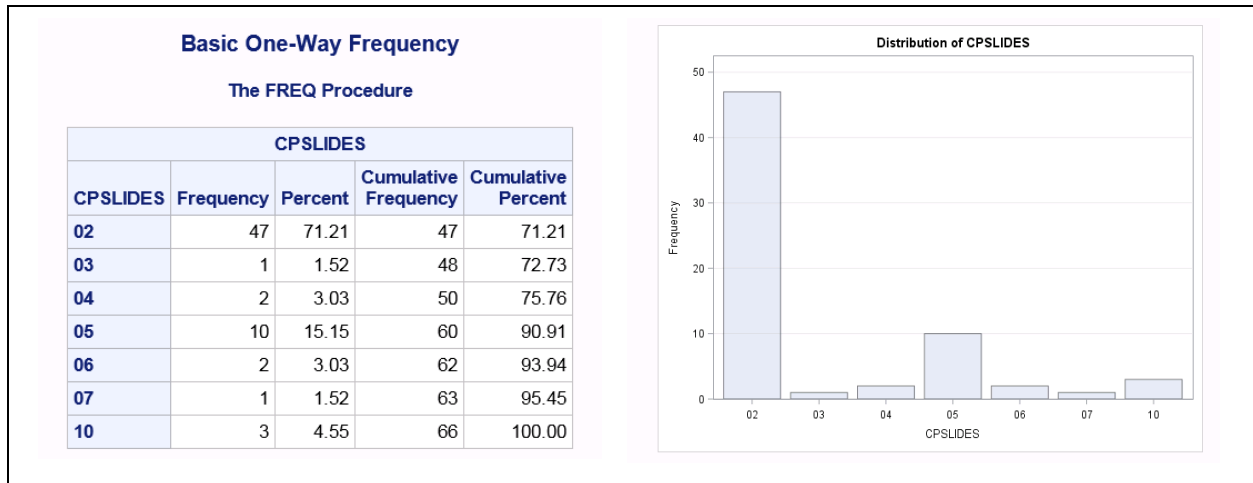
the TABLES statement. The TITLE statement which displays the title of the output can be outside or within the PROC FREQ construct. The PLOTS option with FREQPLOT requests frequency plots from ODS graphics. The output for code 2 is shown in Display 1.

Code 1

```
proc freq;
run;
```

Code 2

```
proc freq data=malts;
  title "Basic One-Way Frequency";
  tables cpslides/plots=freqplot;
run;
```



Display 1. Output of PROC FREQ Procedure of Code 2 for One-Way Frequency Table

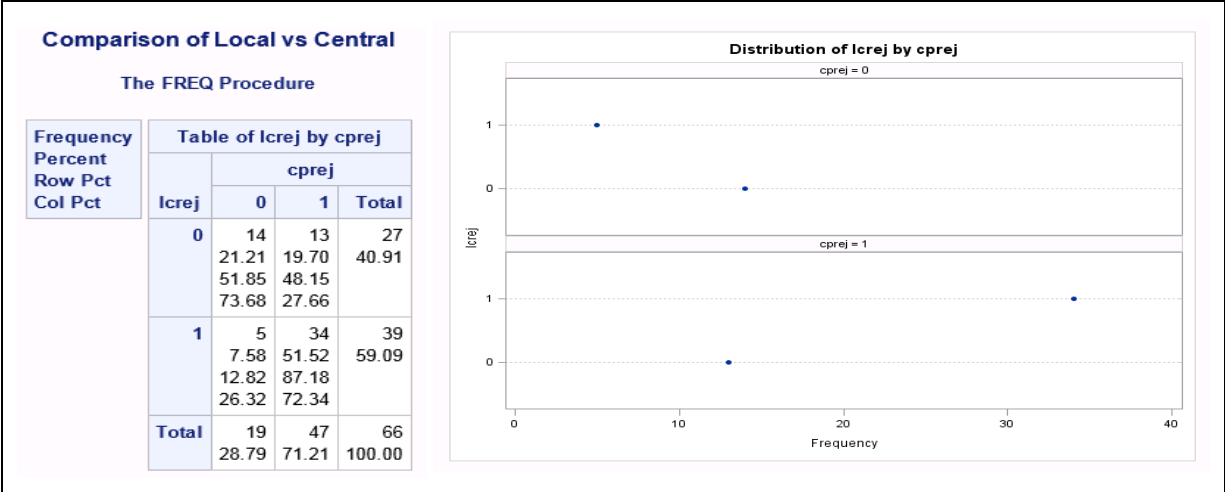
Case 2: Two-Way Frequency Tables

The TABLES statement in PROC FREQ generates one-way to n-way frequency tables. For requesting a two-way crosstabulation table, an asterisk is used between the two variables of interest as shown in code 3 (lcrej*cprej). Note that the first variable forms the rows (lcrej) whereas the second variable forms the columns (cprej) of the crosstabulation table. Note that multiple TABLES statements can be executed within the PROC FREQ procedure as shown in Code 3 with three different TABLE statements executed.

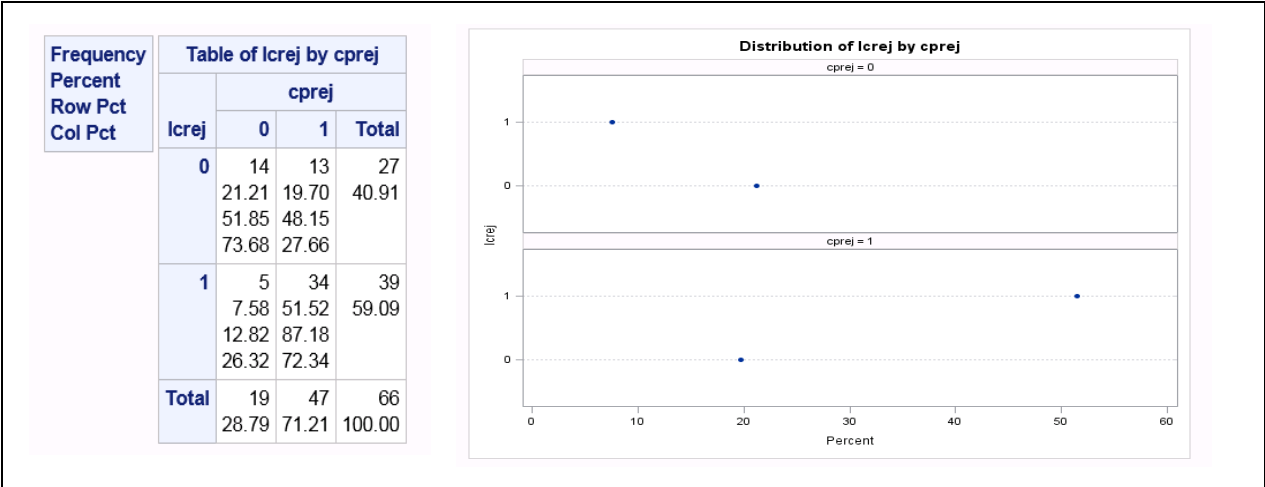
Code 3

```
proc freq data=malts;
  title "Comparison of Local vs Central";
  tables lcrej*cprej /plots=freqplot(type=dotplot); ** first **;
  tables lcrej*cprej /plots=freqplot(type=dotplot scale=percent); ** second **;
  tables lcrej*cprej /out=out_2way nocol nocum nopercnt; ** third **;
run;
```

For the first TABLES statement in Code 3, we have explicitly specified the type of frequency plot, which in this case is DOTPLOT. The output for the first TABLES statement is presented in Display 2. In Display 2, the horizontal axis of the dot plot has frequency and this can be changed to percent by using SCALE=PERCENT as shown in the second TABLES statement in Code 3. Display 3 presents the output with percent on the horizontal axis. Displays 2 and 3 both have row variable (lcrej) on the vertical axis.



Display 2. Output of First TABLES Statement in Code 3 for Two-Way Frequency Tables



Display 3. Output of Second TABLES Statement in Code 3 for Two-Way Frequency Tables

For the third TABLES statement, the OUTPUT statements generate an external SAS data set (out_2way) with frequency and percent of total frequency as presented in Display 4. Also, NOCOL, NOCUM and NOPERCENT suppresses display of column percentages, cumulative and percentages respectively. The NOROW and NOFREQ options can be used to suppress the display of row percentages and frequency. The OUTPCT option can be used to include row, column and two-way table percentages in the output data set.

Frequency Row Pct	Table of lcrej by cprej			Frequency Count	Percent of Total Frequency
	lcrej	cprej			
		0	1		
0	14	13	27	21.212121212	
	51.85	48.15		19.696969697	
1	5	34	39	7.5757575758	
	12.82	87.18		51.515151515	
Total	19	47	66		

Display 4. Output of Third TABLES Statement in Code 3 for Two-Way Frequency Tables

Case 3: Three-Way Frequency Tables

A third dimension can be added to the TABLES statement and in this situation the first dimension becomes the strata with the second and third forming the row and column respectively. The code is presented in Code 4 with results displayed in Display 5. Another way to accomplish this tri-dimensional scenario is shown in Code 5 with the use of a BY statement. Sorting the data by strata variable ("site" in Code 5) is mandatory when this approach is followed. The output of Code 5 is displayed in Display 6.

Code 4

```
proc freq data=malts;
  tables site*lcrej*cprej;
run;
```

Code 5

```
proc sort data=malts out=malts1;
  by site;
run;
proc freq data=malts1;
  tables lcrej*cprej;
  by site; ** strata variable **;
run;
```

Frequency Percent Row Pct Col Pct	Table 1 of lcrej by cprej Controlling for SITE=01				Frequency Percent Row Pct Col Pct	Table 2 of lcrej by cprej Controlling for SITE=02				Frequency Percent Row Pct Col Pct	Table 3 of lcrej by cprej Controlling for SITE=03										
	lcrej	cprej				lcrej	cprej				lcrej	cprej									
		0	1	Total			0	1	Total			0	1	Total							
0	5	2	7	41.67	16.67	58.33	71.43	28.57	62.50	50.00	0	4	3	7	36.36	27.27	63.64	57.14	42.86	100.00	42.86
1	3	2	5	25.00	16.67	41.67	60.00	40.00	37.50	50.00	1	0	4	4	0.00	36.36	36.36	0.00	100.00	0.00	57.14
Total	8	4	12	66.67	33.33	100.00	Total	3	18	21	14.29	85.71	100.00	Total	4	7	11	36.36	63.64	100.00	

Display 5. Output of Code 4 for Three-Way Frequency Tables

The FREQ Procedure				The FREQ Procedure				The FREQ Procedure													
SITE=01				SITE=02				SITE=03													
Frequency Percent Row Pct Col Pct	Table of lcrej by cprej			Frequency Percent Row Pct Col Pct	Table of lcrej by cprej			Frequency Percent Row Pct Col Pct	Table of lcrej by cprej												
	lcrej	cprej			lcrej	cprej			lcrej	cprej											
		0	1			Total	0			1	Total	0	1	Total							
0	5	2	7	41.67	16.67	58.33	71.43	28.57	62.50	50.00	0	4	3	7	36.36	27.27	63.64	57.14	42.86	100.00	42.86
1	3	2	5	25.00	16.67	41.67	60.00	40.00	37.50	50.00	1	0	4	4	0.00	36.36	36.36	0.00	100.00	0.00	57.14
Total	8	4	12	66.67	33.33	100.00	Total	3	18	21	14.29	85.71	100.00	Total	4	7	11	36.36	63.64	100.00	

Display 6. Output of Code 5 for Three-Way Frequency Tables Using the BY Statement

The output presented in displays 5 and 6 are the same with only difference being in their appearance. Code 5 displays each table on a separate page with a dashed line separating each stratum. It is also important to note that a simple OUT statement in these two cases will give percent which are based on different denominators. In the case of

BY statement, the percent is based on each stratum as opposed to the total. The OUTPCT along with the OUT option in the TABLES statement can generate all the relevant statistics.

Case 4: Table Display Options

So far in this paper, tables were displayed in default cross tabulation format. The tables can be displayed in column format using the LIST and CROSSLIST options. The application for this is shown in Code 6 and note that both these options are specified in separate TABLES statement. Both the LIST and CROSSLIST options cannot be specified in the same TABLES statement. The output shown in Display 7 shows the results of using these two options. The LIST option displays the cumulative frequency and cumulative percent whereas CROSSLIST option displays row and column percent. Also, the CROSSLIST option generates totals and rows with zero frequencies included. Use the NOPARSE option to suppress the display of zero frequency when using CROSSLIST as shown in Code 7. The output for Code 7 is not presented since it is the same output with zero frequency rows excluded.

Code 6

```
proc freq data=malts;
title "Gender by Age Category";
tables sex*agecat /list;
tables sex*agecat /crosstlist;
run;
```

Code 7

```
proc freq data=malts;
title "Gender by Age Category";
tables sex*agecat /crosstlist noparse;
run;
```

Gender by Age Category						Table of sex by agecat					
The FREQ Procedure						sex	agecat	Frequency	Percent	Row Percent	Column Percent
sex	agecat	Frequency	Percent	Cumulative Frequency	Cumulative Percent	F	1	0	0.00	0.00	0.00
							2	15	22.73	28.30	75.00
							3	38	57.58	71.70	100.00
							Total	53	80.30	100.00	
						M	1	8	12.12	61.54	100.00
							2	5	7.58	38.46	25.00
							3	0	0.00	0.00	0.00
							Total	13	19.70	100.00	
						Total	1	8	12.12		100.00
							2	20	30.30		100.00
							3	38	57.58		100.00
							Total	66	100.00		

Display 7. Output of Code 6 Using LIST and CROSSLIST Options

Case 5: Unique Levels

In data analysis, it is always of interest to find distinct levels of a variable and we often see the usage of PROC SQL and PROC SORT with NODUPKEY options. PROC FREQ with NEVELS options can cater to this need in multiple ways as shown in codes 8 and 9.

Code 8

```
proc freq data=malts nlevels;
title "Unique Levels";
tables sex agecat;
run;
```

Code 9

```
proc freq data=malts nlevels;
title "Unique Levels";
tables _char_/noprint;
tables _numeric_/noprint;
tables enrldate--cpslides/noprint;
run;
```

Code 8 will generate the number of levels for variables sex and agecat along with one-way frequency table as shown in Display 8. To suppress the one-way frequency table, use the NOPRINT option as used in Code 9. If one is interested to just know the number of levels for all character variables, all numeric variables or selection of orderly variables in the data set, use _CHAR_, _NUMERIC_ and VARxx—VARyy options in the TABLES statement as shown in Code 9. Display 8 shows the output for codes 8 and 9 and note that for Code 9 only the snapshot is

presented. If the TABLES statement is excluded when using the NLEVELS option, then levels for all variables in the data set will be displayed.

Unique Levels				
The FREQ Procedure				
Number of Variable Levels				
Variable	Levels			
agecat	3			
sex	2			

agecat	Frequency	Percent	Cumulative Frequency	Cumulative Percent
1	8	12.12	8	12.12
2	20	30.30	28	42.42
3	38	57.58	66	100.00

sex	Frequency	Percent	Cumulative Frequency	Cumulative Percent
F	53	80.30	53	80.30
M	13	19.70	66	100.00

Unique Levels				
The FREQ Procedure				
Number of Variable Levels				
Variable	Label	Levels	Missing Levels	Nonmissing Levels
SITE	SITE	5	0	5
PROT	PROT	1	0	1
PATID		36	0	36
PROJID	PROJID	51	0	51
CPSSLIDES	CPSSLIDES	7	0	7
ENRLDATE		43	0	43
BIOPSYDT	BIOPSYDT	63	0	63

Display 8. Output of Code 8 and 9 Using NLEVELS Option

Case 6: Binomial Proportions Test

A Binomial proportions test is performed to investigate if observed test results differ from what was expected and is used when a study has two possible outcomes such as success/failure, yes/no, present/absent and so forth.

Code 10

```
proc freq data=malts order=freq;
  tables cprej / binomial;
  title 'Binomial Default';
run;
```

Code 11

```
proc freq data=malts order=freq;
  tables cprej / binomial(p=0.9);
  tables cprej / binomial(p=0.9 ac wilson exact) alpha=.1;
  title 'Binomial with Additional Options';
run;
```

Code 10 shows the basic code for the binomial proportions test. The TABLES statement provides a one-way frequency table for the variable cprej and the BINOMIAL option generates the binomial proportion, confidence limits, and test. By default, PROC FREQ provides Wald and Exact (Clopper-Pearson) confidence limits for the binomial proportion. The BINOMIAL option also produces an asymptotic equality Wald test that the proportion equals 0.5. The output is shown in Display 9 titled “Binomial Default”.

The defaults of the BINOMIAL option can be modified using the options shown in Code 11. The first TABLES statement in Code 11 tests the hypothesis for proportion equal to 0.9 ($P=0.9$) with rest of the default options in place. In the second TABLES statement, we are testing the proportion for 0.9 at 90% confidence interval using the option $P=0.9$ and $ALPHA=0.1$ respectively. In addition, the AC, WILSON, and EXACT binomial-options generates Agresti-Coull, Wilson (score), and exact (Clopper-Pearson) confidence limits types respectively. The output for both the TABLES statement of Code 11 is displayed in Display 9 titled “Binomial with Additional Options”.

The ORDER=FREQ option in the PROC FREQ statement implies that the levels of the variable cprej is ordered in the descending frequency count. By default, the variable levels are listed in ascending order of unformatted variable values. Table 3 provides the options for the ORDER statement and this option can also be used to display values in the output as per the needs.

The exact p-values can be generated by specifying the BINOMIAL option in the EXACT statement. PROC FREQ can also do tests of noninferiority, superiority and equivalence for the binomial proportion in addition to equality tests. The continuity corrected confidence limits can also be requested in PROC FREQ. For more details, please refer to the SAS documentation on PROC FREQ.

Value of ORDER =	Values Ordered By
DATA	orders values according to their order in the input data set
FORMATTED	orders values by their formatted values (in ascending order). This order is dependent on the operating environment.
FREQ	orders values by their descending frequency counts
INTERNAL	orders values by their unformatted values, which yields the same order that the SORT procedure does. This order is dependent on the operating environment.

Table 3. Options for the Values of ORDER Statement

Binomial Default		Binomial with Additional Options																																																																									
The FREQ Procedure		The FREQ Procedure																																																																									
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Display 9. Output of Code 10 and 11 for Binomial Proportions Test

Case 7: Chi-Square Test

Chi-square test is used to analyze categorical data mainly with respect to goodness-of-fit, equality of two proportions or association of two categorical variables. PROC FREQ can perform these inferential statistics and the corresponding code is presented in Code 12. In Code 12, the CHISQ option generates a chi-square goodness-of-fit test for the frequency table of variable agecat. By default, the CHISQ option provides a one-way Pearson chi-square goodness of fit test. To generate a one-way likelihood ratio chi-square test, the CHISQ(LRCHI) can be used instead of the CHISQ option. Exact P-values for these two statistics can be obtained using the EXACT statement with CHISQ and LRCHI options respectively.

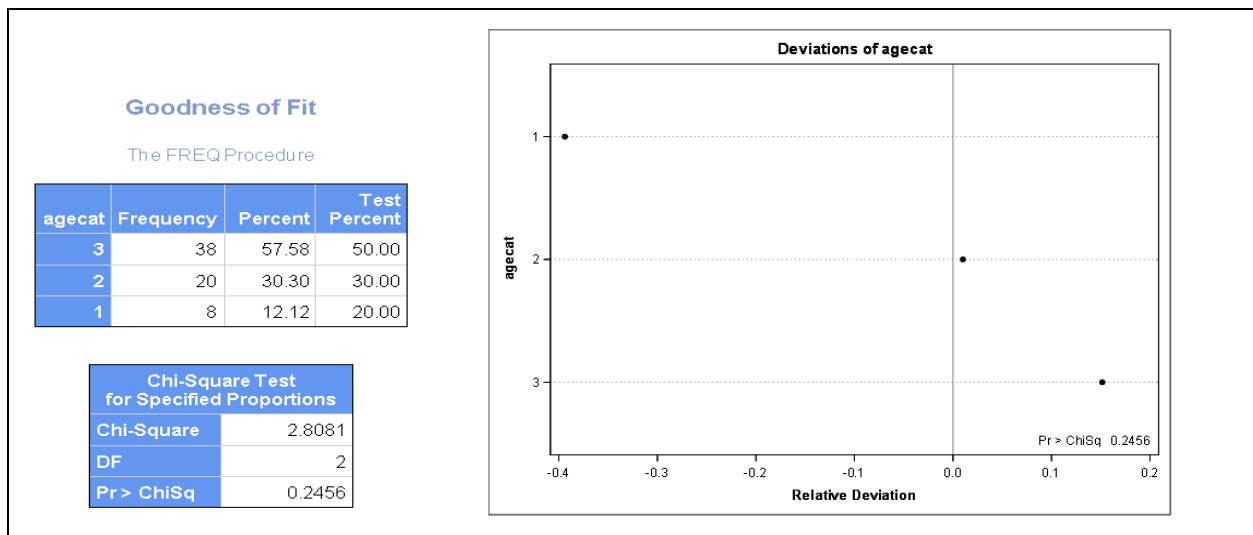
The NOCUM option in the TABLES statement suppresses the cumulative numbers while the TESTP= option specifies the hypothesized percentages for the chi-square test (50%, 30% and 20%). It is important to note that the TESTP= percentages are listed in the order specified using the ORDER option. In this case, ORDER=FREQ implies that the levels of the variable agecat is ordered in the descending frequency count. In this example, we have presented the output in a RTF file. Note the usage of ODS RTF in generating the RTF file and closing of ODS

destination using ODS RTF CLOSE statements. The style used in generating this RTF report is SASWEB which is an inbuilt template from SAS.

Code 12

```
ods rtf file="C:\Jinson\SAS\SESUG2018\Freq\gof.rtf" style=sasweb;
ods graphics on;
proc freq data=malts order=freq;
  tables agecat / nocum chisq testp=(50 30 20)
             plots(only)=deviationplot(type=dotplot);
  title 'Goodness of Fit';
run;
ods graphics off;
ods rtf close;
```

The snapshot in display 10 is output from Code 12. The PLOTS= option produces a deviation plot, which is associated with the CHISQ option and displays the relative deviations from the test frequencies. The TYPE=DOTPLOT option produces a dot plot instead of the default bar chart.



Display 10. Output of Code 12 for Goodness of Fit Test

In Display 10, we see both the Percent and Test Percent for the goodness of fit test. The p-value of 0.2456 for this analysis indicates that the sample distribution is not significantly different at an alpha level of 0.05 than the assumed distribution of 50%, 30% and 20% in agecat levels 3, 2 and 1 respectively.

The chi-square test for association or equality of proportions is presented in Code 13. In the case of two-way tables, the chi-square tests the null hypothesis of no association between row and column variables.

Code 13

```
ods pdf file="C:\Jinson\SAS\SESUG2018\Freq\assoc.pdf" style=journal;
proc freq data=malts order=data;
  tables cprej*ages / expected cellchi2 norow nocol chisq;
  output out=outchisq n nmiss pchi lrchi;
  title 'Chi-Square Tests for Association or Equality of Proportions';
run;
ods pdf close;
```

PROC FREQ computes Pearson chi-square, likelihood ratio chi-square and Mantel Haenszel chi-square statistic for each two-way table. In addition, it provides phi coefficient, contingency coefficient and Cramer's V which are all based on Pearson chi-square statistic. For 2 x 2 tables, the CHISQ options also produces the Fisher's Exact and continuity-

adjusted chi-square statistic. In Code 13, we are generating the output in a PDF file with STYLE=JOURNAL as compared to RTF file with STYLE=SASWEB in Code 12.

The additional options used in Code 13 is described in Table 4 with Display 11 showing all the generated statistics. From the output in Display 11, the p-value of 0.7838 for the non-directional test results in the acceptance of the null hypothesis of no association. The directional test (left-sided and right-sided) also shows the lack of significance. If the objective is to determine what the association is then we look at row and column percentages based on the research question. Display 12 shows the screen shot of the output data set which includes all the specified statistics in the OUTPUT statement.

Options	Description
EXPECTED	Displays expected cell frequencies
CELLCHI2	Displays the cell contribution to the overall chi-square
NOROW	Suppresses the display of row percent
NOCOL	Suppresses the display of column percent
CHISQ	Produces chi-square tests
OUTPUT	Creates an output dataset (in code 13, outchisq) with the specified statistics
N	Number of non-missing observations
NMISS	Number of missing observations
PCHI	Pearson chi-square statistics
LRCHI	Likelihood ratio chi-square statistics

Table 4. Options Used in Code 13

Chi-Square Tests for Association or Equality of Proportions				Statistics for Table of cprej by ages																																																																																			
<p>The FREQ Procedure</p> <p>Table of cprej by ages</p> <table border="1"> <thead> <tr> <th>cprej</th> <th colspan="2">ages</th> <th>Total</th> </tr> <tr> <th>Frequency</th> <th>2</th> <th>1</th> <th></th> </tr> </thead> <tbody> <tr> <td>Expected</td> <td>10</td> <td>9</td> <td>19</td> </tr> <tr> <td>Cell Chi-Square</td> <td>10.939</td> <td>8.0606</td> <td></td> </tr> <tr> <td>Percent</td> <td>0.0807</td> <td>0.1095</td> <td></td> </tr> <tr> <td></td> <td>15.15</td> <td>13.64</td> <td>28.79</td> </tr> <tr> <td></td> <td>28</td> <td>19</td> <td>47</td> </tr> <tr> <td></td> <td>27.061</td> <td>19.939</td> <td></td> </tr> <tr> <td></td> <td>0.0326</td> <td>0.0443</td> <td></td> </tr> <tr> <td></td> <td>42.42</td> <td>28.79</td> <td>71.21</td> </tr> <tr> <td>Total</td> <td>38</td> <td>28</td> <td>66</td> </tr> <tr> <td></td> <td>57.58</td> <td>42.42</td> <td>100.00</td> </tr> </tbody> </table>				cprej	ages		Total	Frequency	2	1		Expected	10	9	19	Cell Chi-Square	10.939	8.0606		Percent	0.0807	0.1095			15.15	13.64	28.79		28	19	47		27.061	19.939			0.0326	0.0443			42.42	28.79	71.21	Total	38	28	66		57.58	42.42	100.00	<table border="1"> <thead> <tr> <th>Statistic</th> <th>DF</th> <th>Value</th> <th>Prob</th> </tr> </thead> <tbody> <tr> <td>Chi-Square</td> <td>1</td> <td>0.2670</td> <td>0.6053</td> </tr> <tr> <td>Likelihood Ratio Chi-Square</td> <td>1</td> <td>0.2657</td> <td>0.6062</td> </tr> <tr> <td>Continuity Adj. Chi-Square</td> <td>1</td> <td>0.0584</td> <td>0.8090</td> </tr> <tr> <td>Mantel-Haenszel Chi-Square</td> <td>1</td> <td>0.2630</td> <td>0.6081</td> </tr> <tr> <td>Phi Coefficient</td> <td></td> <td>-0.0636</td> <td></td> </tr> <tr> <td>Contingency Coefficient</td> <td></td> <td>0.0635</td> <td></td> </tr> <tr> <td>Cramer's V</td> <td></td> <td>-0.0636</td> <td></td> </tr> </tbody> </table>				Statistic	DF	Value	Prob	Chi-Square	1	0.2670	0.6053	Likelihood Ratio Chi-Square	1	0.2657	0.6062	Continuity Adj. Chi-Square	1	0.0584	0.8090	Mantel-Haenszel Chi-Square	1	0.2630	0.6081	Phi Coefficient		-0.0636		Contingency Coefficient		0.0635		Cramer's V		-0.0636	
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Display 11. Output of Code 13 for Test of Association

	Number of Subjects in the Stratum	Number of Missing Subjects	Chi-Square	DF for Chi-Square	P-value for Chi-Square	Likelihood Ratio Chi-Square	DF for Likelihood Ratio Chi-Square	P-value Likelihood Chi-Square
1	66	0	0.2670141198	1	0.6053417953	0.2657474995	1	0.6061

Display 12. Screen Shot of the Dataset Created Using the OUTPUT Statement in Code 13

Case 8: Fisher's Exact Test

Fisher's exact test was mentioned in Case 7 as a default output in 2 x 2 tables. Fisher's exact test is the most widely accepted test for 2 x 2 tables because it is not based on an asymptotic distribution and is appropriate for small and sparse data. When the expected count in table cells are small, the CHISQ option will give a warning stating that the asymptotic chi-square test may not be valid. In such cases, it is recommended to perform the exact tests. Code 14 shows the various ways you can perform the Fisher's Exact Test and the results are shown in in Display 13. From the output, we can see that these three separate runs will deliver the same output.

Code 14

<pre>proc freq data=malts; title 'Fisher Option'; tables lcrej*cprej/ nopercnt fisher; run;</pre>	<pre>proc freq data=malts; title 'Exact Option'; tables lcrej*cprej/ nopercnt exact; run;</pre>	<pre>proc freq data=malts; title 'Chisq Option'; tables lcrej*cprej/ nopercnt chisq; run;</pre>
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Display 13. Output of Code 14 for Fisher's Exact Test

The Fisher's exact tests provides the table probability, two-sided p-value, left-sided p-value and right-sided p-value. Note that the table probability is test statistic for Fisher's exact test and this equals the hypergeometric probability of the observed table. For a 2 x 2 table, the first cell (1,1) completely determines table when the marginal row and column sums are fixed and this frequency is explicitly displayed in the output results for Fisher's exact test. The one-sided p-values are all defined in terms of the frequency of the first cell.

The results in display 13 shows that p-value =0.0009 for non-directional test which provides a strong evidence of $I_{c_{rej}}=0$ being different than $I_{c_{rej}}=1$. Also, the directional right-sided test with p-value=0.0008 supports the alternate hypothesis - the probability of $c_{prej}=0$ is greater when $I_{c_{rej}}=0$ than $I_{c_{rej}}=1$.

Fisher's test can be applied to R x C tables and this is also known as Freeman-Halton test and this executed by using the network algorithm developed by Mehta and Patel. More details on this can be obtained from the SAS documentation on PROC FREQ.

Case 9: Monte Carlo Estimates for Exact Tests

Exact p-values can be requested for many statistical tests in the FREQ procedure as mentioned before. For large problems, computing exact p-values may be prohibitively expensive with regards to time and computational resources. In PROC FREQ, you can use a Monte Carlo approach to randomly generate tables that satisfy the null hypothesis for the test and evaluate the test statistic on those tables. Many of the tests in PROC FREQ supports the MC option in the EXACT statement for computing Monte Carlo estimates. To describe the precision of each Monte Carlo estimate, the FREQ procedure provides the asymptotic standard error and $100(1-\alpha)$ % confidence limits which can also be used for comparative purposes.

Codes 15 and 16 shows the Monte Carlo simulation and the standard run for Fisher's exact test respectively with the resulting output in Display 14. The exact p-value from Monte Carlo is 0.0879 whereas the exact p-value from a standard run is 0.0906. Note the following, random number seed was not provided in the code and therefore you may get a different result each time you run the code. The random number seed can be fixed using the SEED option along with the MC option in the EXACT statement. By default, the EXACT statement generates 10,000 random tables that have the same row and column sum as the observed table and this can be changed per need using the N option as shown in code 15 (N=20,000).

Code 15

```
/*Monte Carlo Simulation for Fisher's Exact Test*/  
proc freq data=malts;  
  tables agecat*cprej;  
  exact Fisher / mc n=20000;  
  title "Monte Carlo Estimates for Fishers's Exact Test";  
run;
```

Code 16

```
/*Fisher's Exact Test*/  
proc freq data=malts;  
  tables agecat*cprej;  
  exact Fisher;  
  title "Fisher's Exact Test";  
run;
```

It is important to note that the MC option is available for all EXACT statistic-options except BINOMIAL. It is also important to note that ALPHA, N, SEED options in the EXACT statement will invoke the MC option.

Monte Carlo Estimates for Fishers's Exact Test

The FREQ Procedure

Frequency Percent Row Pct Col Pct	Table of agecat by cprej		
	agecat	cprej	
		0	1
1	5 7.58 62.50 26.32	3 4.55 37.50 6.38	8 12.12
2	4 6.06 20.00 21.05	16 24.24 80.00 34.04	20 30.30
3	10 15.15 26.32 52.63	28 42.42 73.68 59.57	38 57.58
Total	19 28.79	47 71.21	66 100.00

Statistics for Table of agecat by cprej

Statistic	DF	Value	Prob
Chi-Square	2	5.3017	0.0706
Likelihood Ratio Chi-Square	2	4.8294	0.0894
Mantel-Haenszel Chi-Square	1	1.9628	0.1612
Phi Coefficient		0.2834	
Contingency Coefficient		0.2727	
Cramer's V		0.2834	

Fisher's Exact Test	
Table Probability (P)	0.0074

Monte Carlo Estimate for the Exact Test	
Pr <= P	0.0879
99% Lower Conf Limit	0.0827
99% Upper Conf Limit	0.0930
Number of Samples	20000
Initial Seed	868999001

Sample Size = 66

Fisher's Exact Test

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	agecat	cprej	
		0	1
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Cramer's V		0.2834	

Fisher's Exact Test	
Table Probability (P)	0.0074
Pr <= P	0.0906

Sample Size = 66

Display 14. Output of Code 15 and 16 for Exact Tests Using Monte Carlo (MC) Option

Case 10: Relative Risks and Odds Ratio

The research question may involve finding the existence of association and the magnitude of association in a 2 x 2 table. Relative risks and odds ratio can be requested by either using the MEASURES or RELRISK option. Relative risks are mainly used in prospective studies whereas odds ratio is widely applied in case-control studies. Note that the odds ratio can also be used in prospective studies. These two statistics can be generated by either using the aggregated data or the raw form. Display 15 shows the code used for aggregating the data and the associated output data set. In this example we are generating the counts for each of the cells involved (total of 4). In Code 17, the WEIGHT statement is used to associate the counts (i.e. frequency) to each of the cells. In Code 18, the data is directly read from raw data sets to generate the required statistics of relative risk and odds ratio. The WEIGHTS option can be used for weighting individual records and is very common in survey data where one is involved with respondent weighting, demographic weighting and so forth.

The MEASURES options generate a whole range of statistics that describe the association between the row and column variable of the contingency table in addition to relative risks and odds ratio of 2 x 2 table. All these statistics are displayed in Display 16 and authors recommend you refer SAS documentation for the definition and applicability of these statistics. Display 16 shows the output using aggregated as well as raw data and note that the results are expectedly identical.

<pre>/*data set for creating the counts*/ proc freq data=malts; table cprej*sex /out=rowcols; run;</pre>	<table border="1"> <thead> <tr> <th></th> <th>cprej</th> <th>sex</th> <th>Frequency Count</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>0</td> <td>F</td> <td>12</td> </tr> <tr> <td>2</td> <td>0</td> <td>M</td> <td>7</td> </tr> <tr> <td>3</td> <td>1</td> <td>F</td> <td>41</td> </tr> <tr> <td>4</td> <td>1</td> <td>M</td> <td>6</td> </tr> </tbody> </table>		cprej	sex	Frequency Count	1	0	F	12	2	0	M	7	3	1	F	41	4	1	M	6
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2	0	M	7																		
3	1	F	41																		
4	1	M	6																		

Display 15. Creation of Aggregated Data

Code 17

```
/*with weighting variable*/
proc freq data=rowcols;
  tables sex*cprej / chisq measures;
  weight count;
run;
```

Code 18

```
/*without weighting variable*/
proc freq data=malts;
  tables sex*cprej / chisq measures;
run;
```

RR and OR with Weighting Variable				RR and OR without Weighting Variable																																																																																																																											
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<table border="1"> <thead> <tr> <th colspan="4">Odds Ratio and Relative Risks</th> </tr> <tr> <th>Statistic</th> <th>Value</th> <th colspan="2">95% Confidence Limits</th> </tr> </thead> <tbody> <tr> <td>Odds Ratio</td> <td>0.2509</td> <td>0.0707</td> <td>0.8898</td> </tr> <tr> <td>Relative Risk (Column 1)</td> <td>0.4205</td> <td>0.2072</td> <td>0.8533</td> </tr> <tr> <td>Relative Risk (Column 2)</td> <td>1.6761</td> <td>0.9153</td> <td>3.0692</td> </tr> </tbody> </table>	Odds Ratio and Relative Risks				Statistic	Value	95% Confidence Limits		Odds Ratio	0.2509	0.0707	0.8898	Relative Risk (Column 1)	0.4205	0.2072	0.8533	Relative Risk (Column 2)	1.6761	0.9153	3.0692	<table border="1"> <thead> <tr> <th colspan="4">Odds Ratio and Relative Risks</th> </tr> <tr> <th>Statistic</th> <th>Value</th> <th colspan="2">95% Confidence Limits</th> </tr> </thead> <tbody> <tr> <td>Odds Ratio</td> <td>0.2509</td> <td>0.0707</td> <td>0.8898</td> </tr> <tr> <td>Relative Risk (Column 1)</td> <td>0.4205</td> <td>0.2072</td> <td>0.8533</td> </tr> <tr> <td>Relative Risk (Column 2)</td> <td>1.6761</td> <td>0.9153</td> <td>3.0692</td> </tr> </tbody> </table>	Odds Ratio and Relative Risks				Statistic	Value	95% Confidence Limits		Odds Ratio	0.2509	0.0707	0.8898	Relative Risk (Column 1)	0.4205	0.2072	0.8533	Relative Risk (Column 2)	1.6761	0.9153	3.0692																																																																																						
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Display 16. Output of Code 17 and 18 for Relative Risks and Odds Ratio

If a significant association exist between row and column variables, then we look at the odds ratio. From the output in Display 16, if we assume cprej=0 indicates failure, then the odds ratio can be interpreted as the odds of failure is 0.2509 times as likely for sex=F than for sex=M.

The relative risk is dependent on the orientation of columns in two-way table. In this example, if the objective is to determine the risk of failure (column 1, cprej=0) then we would report the Relative Risk (Column1). The interpretation in this case would be that relative risk of failure is 0.4205 for sex=F than for sex=M. The output can be limited to just odds ratio and relative risk by using the RELRISK or OR or ODDSRATIO options instead of the MEASURES option. The default confidence interval for both relative risk and odds ratio is the Wald confidence limits, but Wald Modified, Score, Likelihood ratio confidence limits can also be requested. For stratified analysis, the CMH option can be used to compute the Cochran-Mantel-Haenszel statistics. The CMH options also provides the adjusted Mantel-Haenszel and logit estimates of the odds ratio and relative risks. The Breslow-Day test for the homogeneity of odds ratio is also generated with CMH option.

Case 11: McNemar's Test

McNemar's Test is employed when the data from matched pair of subjects with a dichotomous response needs to be analyzed. It is critical to note that observations from matched pair data sets are not independent and McNemar's test accounts for this scenario. The null hypothesis tested in McNemar's test is that there is no difference in marginal proportions. PROC FREQ computes the McNemar's test for 2 x 2 tables with a TEST AGREE statement as shown in Code 19 with results in Display 17.

Code 19

```
proc freq data=malts;
  tables cprej*lcprej;
  test agree;
  title 'McNemars Test';
run;
```

McNemars Test				
The FREQ Procedure				
Frequency Percent Row Pct Col Pct	Table of cprej by lcprej			
	cprej	lcprej		Total
		0	1	
	0	14 21.21 73.68 51.85	5 7.58 26.32 12.82	19 28.79
	1	13 19.70 27.66 48.15	34 51.52 72.34 87.18	47 71.21
	Total	27 40.91	39 59.09	66 100.00
Statistics for Table of cprej by lcprej				
				Sample Size = 66

McNemar's Test	
Statistic (S)	3.5556
DF	1
Pr > S	0.0593

Simple Kappa Coefficient	
Kappa	0.4090
ASE	0.1128
95% Lower Conf Limit	0.1879
95% Upper Conf Limit	0.6300

Test of H0: Kappa = 0	
ASE under H0	0.1188
Z	3.4433
One-sided Pr > Z	0.0003
Two-sided Pr > Z	0.0006

Display 17. Output of Code 19 for McNemar's Test

In the case presented here, we are testing the null hypothesis that the distribution is same across cprej and lcprej. The output in Display 17 shows p-value >.05 resulting in the acceptance of null hypothesis of no difference in marginal proportions. The AGREE option also generates Kappa coefficient which is not relevant to matched pair data. To obtain exact p-value for McNemar's test, we can specify the MCNEM option in the EXACT statement.

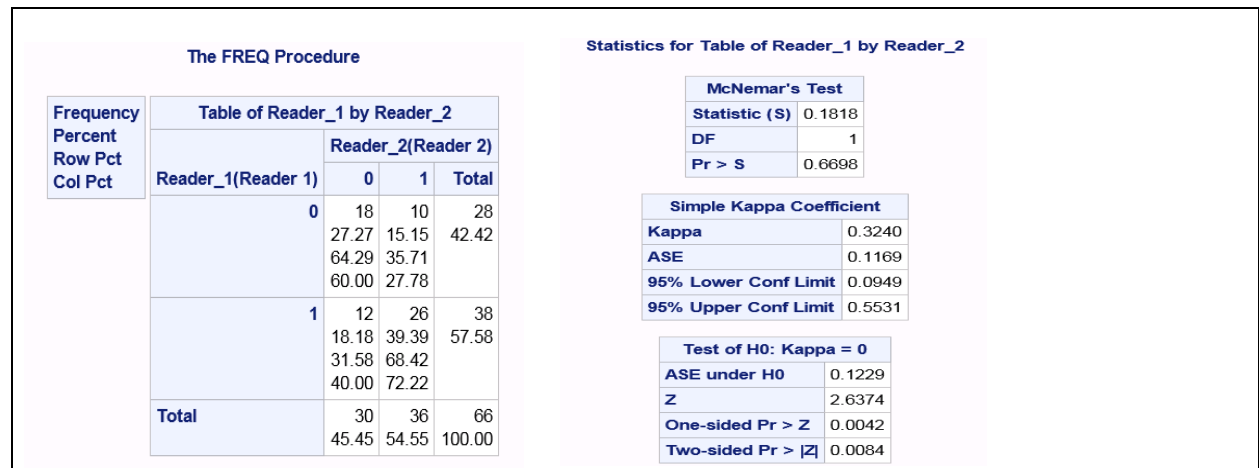
Case 12: Agreement Tests

Agreement tests are carried out when the research objective is to evaluate the levels of agreements between raters on the same subject. The AGREE option in the TABLES statement and the KAPPA option in the TEST statement can be used to perform the agreement tests as shown in Code 20. The Kappa coefficient indicates the level of agreement

with 1=perfect, 0=exact and negative numbers indicating less agreement than the expected. The null hypothesis in this case is $\text{Kappa}=0$, which indicates the agreement is purely by chance.

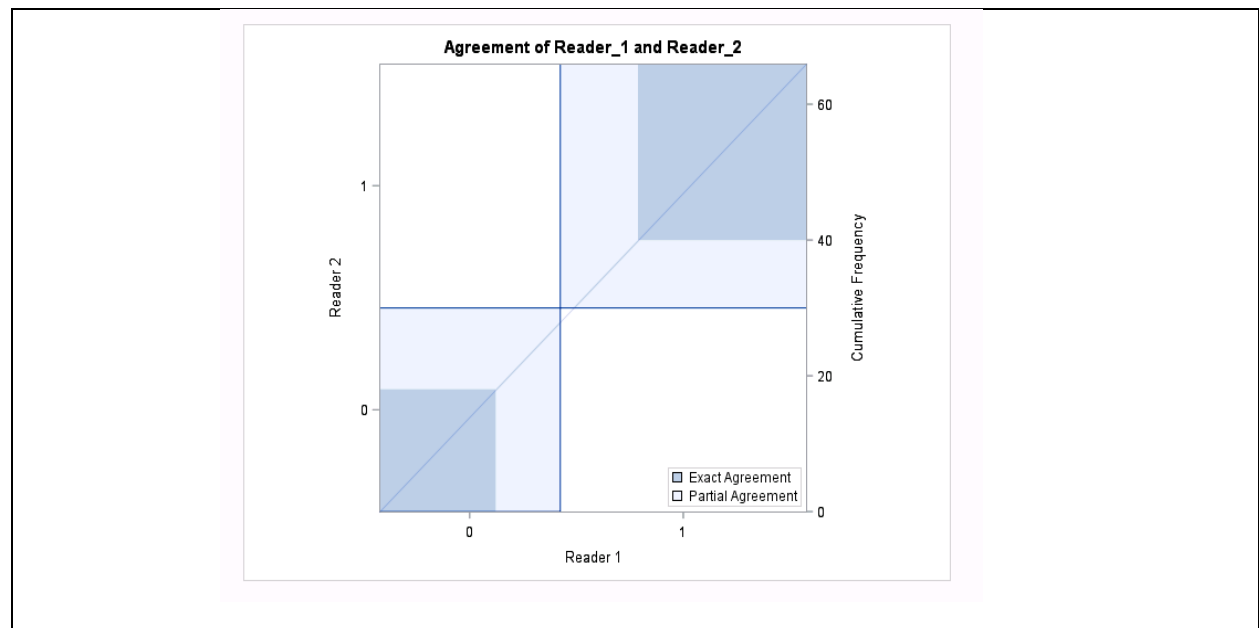
Code 20

```
proc freq data=malts;
  tables reader_1*reader_2/agree;
  title 'Agreement Test';
  test kappa;
run;
```



Display 18. Output of Code 20 for Agreement Tests

In this example, we are testing the level of agreement between readers 1 and 2 and the output is shown in Display 18. Since this is a test of whether the marginal proportions differ, we can refer to McNemar's test which suggests it as non-significant. The Kappa coefficient is equal to 0.3240 which indicates some agreement between the readers. Also, the hypothesis test and the confidence interval (0.0949, 0.5531) confirms the rejection of null hypothesis of no agreement which suggests that Kappa in fact is greater than 0. The AGREE option also generates the Kappa plot which is shown in Display 19.



Display 19. Kappa Plot Using the AGREE option

The Kappa plot is a plot of agreement which shows agreement and distribution simultaneously. The perfect agreement in the plot is shown by dark blue shades. The plot also shows that there is more agreement for readers score of 1 than 0. It is important to be aware that the plot is based on marginal values.

Case 13: Cochran-Armitage Trend Test

Cochran Armitage Trend Test is used to test an underlying trend. The test is used to find the existence of an association between a variable with two categories and an ordinal variable with multiple categories. This is commonly used in dose response studies to investigate the effect of increasing dosage on a subject with respect to adverse effects. The null hypothesis tests for absence of linear trend in the binomial proportions across increasing levels of the ordinal variable.

Code 21

```
/*Asymptotic*/  
proc freq data=doses;  
  title "Asymptotic Method";  
  tables event*levels /  
  trend plots=mosaicplot;  
  weight count;  
run;
```

Code 22

```
/*Exact*/  
proc freq data=doses;  
  title "Exact Method";  
  tables event*levels /  
  trend plots=mosaicplot;  
  exact trend;  
  weight count;  
run;
```

Code 23

```
/*Monte Carlo*/  
proc freq data=doses;  
  title "Simulation(Monte Carlo) Method";  
  tables event*levels / trend plots=mosaicplot;  
  exact trend / mc alpha=.05 maxtime=30 seed=8766;  
  weight count;  
run;
```

As done in previous cases, PROC FREQ can perform the asymptotic, exact and simulation estimation (Monte Carlo) for the Cochran Armitage trend test as presented in Code 21, Code 22 and Code 23 respectively. For this example, the dummy data set shown in Table 2B is used. In this data, we have events of interest (event), levels of the ordinal variable (levels) and count as the number of subjects for event-level combination. In all the three codes (21,22,23) presented we use the TREND option to perform the trend test. In codes 22 and 23, we use the EXACT statement to generate exact p-values. In Code 23, the ALPHA option specifies the significance level and note the default for Monte Carlo estimates is 0.01. The MAXTIME option is used to specify the maximum clock time in seconds to compute the p-value. The SEED option specifies the initial seed for random number generation for Monte Carlo estimation. Note that we could have used the MAXTIME option in Code 22 to limit the computation time. The PLOT=MOSAICPLOT helps in analyzing the trend in the proportion of events with respect to increasing levels. The output for the three codes is shown in Display 20.

Display 20 shows one sided (left sided) p-values of 0.0102, 0.0140 and 0.0136 for the three methods, which indicate that the probability of the event being equal to 1 (event=1) increase as dose increases. The mosaic plot with levels on the horizontal axis and events on the vertical axis aids in visualizing this trend hypothesis. Since we are dealing with ordinal variables, we could have requested for Pearson and Spearman correlation coefficients to detect associations using the MEASURES option.

Asymptotic Method

The FREQ Procedure

Frequency Percent Row Pct Col Pct	Table of event by levels					
	event	levels				Total
		0	1	2	3	
No	20 23.53 26.67 100.00	18 21.18 24.00 90.00	21 24.71 28.00 87.50	16 18.82 21.33 76.19	75 88.24	
Yes	0 0.00 0.00 0.00	2 2.35 20.00 10.00	3 3.53 30.00 12.50	5 5.88 50.00 23.81	10 11.76	
Total	20 23.53	20 23.53	24 28.24	21 24.71	85 100.00	

Exact Method

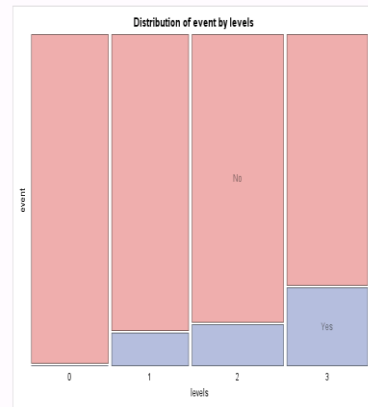
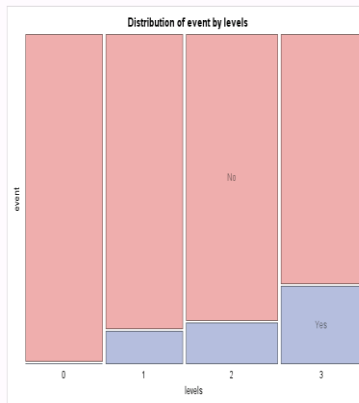
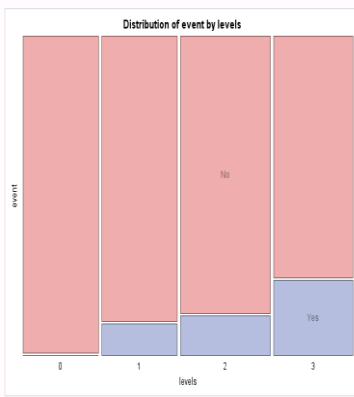
The FREQ Procedure

Frequency Percent Row Pct Col Pct	Table of event by levels					
	event	levels				Total
		0	1	2	3	
No	20 23.53 26.67 100.00	18 21.18 24.00 90.00	21 24.71 28.00 87.50	16 18.82 21.33 76.19	75 88.24	
Yes	0 0.00 0.00 0.00	2 2.35 20.00 10.00	3 3.53 30.00 12.50	5 5.88 50.00 23.81	10 11.76	
Total	20 23.53	20 23.53	24 28.24	21 24.71	85 100.00	

Simulation(Monte Carlo) Method

The FREQ Procedure

Frequency Percent Row Pct Col Pct	Table of event by levels					
	event	levels				Total
		0	1	2	3	
No	20 23.53 26.67 100.00	18 21.18 24.00 90.00	21 24.71 28.00 87.50	16 18.82 21.33 76.19	75 88.24	
Yes	0 0.00 0.00 0.00	2 2.35 20.00 10.00	3 3.53 30.00 12.50	5 5.88 50.00 23.81	10 11.76	
Total	20 23.53	20 23.53	24 28.24	21 24.71	85 100.00	



Statistics for Table of event by levels

Cochran-Armitage Trend Test	
Statistic (Z)	-2.3195
One-sided Pr < Z	0.0102
Two-sided Pr > Z	0.0204

Sample Size = 85

Statistics for Table of event by levels

Cochran-Armitage Trend Test	
Statistic (Z)	-2.3195
Asymptotic Test	
One-sided Pr < Z	0.0102
Two-sided Pr > Z	0.0204
Exact Test	
One-sided Pr <= Z	0.0140
Two-sided Pr >= Z	0.0214

Sample Size = 85

Statistics for Table of event by levels

Cochran-Armitage Trend Test	
Statistic (Z)	-2.3195
One-sided Pr < Z	0.0102
Two-sided Pr > Z	0.0204

Monte Carlo Estimates for the Exact Test

One-sided Pr <= Z	
Estimate	0.0136
95% Lower Conf Limit	0.0113
95% Upper Conf Limit	0.0159
Two-sided Pr >= Z	
Estimate	0.0220
95% Lower Conf Limit	0.0191
95% Upper Conf Limit	0.0249
Number of Samples	10000
Initial Seed	8766

Sample Size = 85

Display 20. Output of Codes 21, 22 and 23 for Cochran-Armitage Trend Test

CONCLUSION

PROC FREQ has plethora of options to carry out various data management and statistical tasks. This paper has presented only 13 cases of using PROC FREQ in a categorical setting and it has far more capabilities which can be referred in the SAS documentation. From the categorical perspective, PROC FREQ can identify outliers, assess inter-rater agreement, determine odds ratio, relative risk, risk difference, evaluate data quality and lot more. In addition, when used with Output Delivery System (ODS), it can produce presentation quality graphics and tables. It is no doubt that PROC FREQ is one of the most trustworthy workhorse in SAS tool box.

REFERENCES

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