SAS/STAT® 15.1 User's Guide

The SURVEYIMPUTE Procedure

This document is an individual chapter from *SAS/STAT® 15.1 User's Guide*.

The correct bibliographic citation for this manual is as follows: SAS Institute Inc. 2018. *SAS/STAT® 15.1 User's Guide*. Cary, NC: SAS Institute Inc.

SAS/STAT® 15.1 User's Guide

Copyright © 2018, SAS Institute Inc., Cary, NC, USA

All Rights Reserved. Produced in the United States of America.

For a hard-copy book: No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, or otherwise, without the prior written permission of the publisher, SAS Institute Inc.

For a web download or e-book: Your use of this publication shall be governed by the terms established by the vendor at the time you acquire this publication.

The scanning, uploading, and distribution of this book via the Internet or any other means without the permission of the publisher is illegal and punishable by law. Please purchase only authorized electronic editions and do not participate in or encourage electronic piracy of copyrighted materials. Your support of others' rights is appreciated.

U.S. Government License Rights; Restricted Rights: The Software and its documentation is commercial computer software developed at private expense and is provided with RESTRICTED RIGHTS to the United States Government. Use, duplication, or disclosure of the Software by the United States Government is subject to the license terms of this Agreement pursuant to, as applicable, FAR 12.212, DFAR 227.7202-1(a), DFAR 227.7202-3(a), and DFAR 227.7202-4, and, to the extent required under U.S. federal law, the minimum restricted rights as set out in FAR 52.227-19 (DEC 2007). If FAR 52.227-19 is applicable, this provision serves as notice under clause (c) thereof and no other notice is required to be affixed to the Software or documentation. The Government's rights in Software and documentation shall be only those set forth in this Agreement.

SAS Institute Inc., SAS Campus Drive, Cary, NC 27513-2414

November 2018

SAS® and all other SAS Institute Inc. product or service names are registered trademarks or trademarks of SAS Institute Inc. in the USA and other countries. ® indicates USA registration.

Other brand and product names are trademarks of their respective companies.

SAS software may be provided with certain third-party software, including but not limited to open-source software, which is licensed under its applicable third-party software license agreement. For license information about third-party software distributed with SAS software, refer to http://support.sas.com/thirdpartylicenses.

Chapter 116
The SURVEYIMPUTE Procedure

Contents

Overview: SURVEYIMPUTE Procedure **9580**
Getting Started: SURVEYIMPUTE Procedure **9581**
Syntax: SURVEYIMPUTE Procedure **9587**
- PROC SURVEYIMPUTE Statement 9587
- BY Statement 9596
- CELLS Statement 9596
- CLASS Statement 9597
- CLUSTER Statement 9598
- ID Statement 9598
- IMPJOINT Statement 9598
- OUTPUT Statement 9599
- REPWEIGHTS Statement 9601
- STRATA Statement 9601
- VAR Statement 9602
- WEIGHT Statement 9602

Details: SURVEYIMPUTE Procedure **9603**
- Definitions 9603
- Specifying the Sample Design 9604
- Missing Values 9606
- Missing Data Patterns 9607
- Random Number Generation 9608
- Fully Efficient Fractional Imputation 9608
- Two-Stage Fully Efficient Fractional Imputation 9613
- Fractional Hot-Deck Imputation 9625
- Hot-Deck Imputation 9636
- Replication Variance Estimation 9639
- Output Data Sets 9645
- Displayed Output 9646
- ODS Table Names 9649

Examples: SURVEYIMPUTE Procedure **9649**
- Example 116.1: Approximate Bayesian Bootstrap Imputation 9649
- Example 116.2: Fully Efficient Fractional Imputation 9656
- Example 116.3: Fully Efficient Fractional Imputation, Fay's Balanced Repeated Replication, and Domain Analysis 9659
- Example 116.4: Fractional Hot-Deck Imputation for Mixed Variables 9667

References **9675**

Overview: SURVEYIMPUTE Procedure

The SURVEYIMPUTE procedure imputes missing values of an item in a data set by replacing them with observed values from the same item. The principles by which the imputation is performed are particularly useful for survey data. PROC SURVEYIMPUTE also computes replicate weights (such as jackknife weights) that account for the imputation and that can be used for replication-based variance estimation for complex surveys. The procedure implements a fractional hot-deck imputation technique (Kim and Fuller 2004; Fuller 2009; Kim and Shao 2014) in addition to some traditional hot-deck imputation techniques (Andridge and Little 2010).

Nonresponse is a common problem in almost all surveys of human populations. Estimators that are based on survey data that include nonresponse can suffer from nonresponse bias if the nonrespondents are different from the respondents. Estimators that use complete cases (only the observed units) might also be less precise. Imputation techniques are important tools for reducing nonresponse bias and producing efficient estimators.

The main objectives of any imputation technique are to eliminate the nonresponse bias and to provide an imputed data set that results in consistent analyses conducted with the imputed data. In addition, a variance estimator must be available that accounts for both the sampling variance and the imputation variance. Imputation techniques use implicit or explicit models. Some model-based imputation techniques include multiple imputation, mean imputation, and regression imputation. For more information about multiple imputation in SAS/STAT, see Chapter 79, "The MI Procedure," and Chapter 80, "The MIANALYZE Procedure."

Imputation techniques that do not use explicit models include hot-deck imputation, cold-deck imputation, and fractional imputation. PROC SURVEYIMPUTE implements imputation techniques that do not use explicit models. It also produces replicate weights that can be used with any survey analysis procedure in SAS/STAT to estimate both the sampling variability and the imputation variability.

Hot-deck imputation is the most commonly used imputation technique for survey data. A donor is selected for a recipient unit, and the observed values of the donor are imputed for the missing items of the recipient. Although the imputation method is straightforward, the variance estimator that accounts for imputation variance might not be simple and is often ignored in practice. PROC SURVEYIMPUTE does not create imputation-adjusted replicate weights for hot-deck imputation.

Fractional hot-deck imputation (Kalton and Kish 1984; Fay 1996; Kim and Fuller 2004; Fuller and Kim 2005), also known as fractional imputation (FI), is a variation of hot-deck imputation in which one missing item for a recipient is imputed from multiple donors. Each donor donates a fraction of the original weight of the recipient such that the sum of the fractional weights from all the donors is equal to the original weight of the recipient. For fully efficient fractional imputation (FEFI), all observed values in an imputation cell are used as donors for a recipient unit in that cell (Kim and Fuller 2004).

The SURVEYIMPUTE procedure implements single and multiple hot-deck imputation, FEFI and FHDI. Available donor selection techniques include simple random selection with or without replacement, probability proportional to weights selection (Rao and Shao 1992), and approximate Bayesian bootstrap selection (Rubin and Schenker 1986).

The remaining sections of this chapter are organized as follows:

- "Getting Started: SURVEYIMPUTE Procedure" on page 9581 introduces PROC SURVEYIMPUTE with an example.

- "Syntax: SURVEYIMPUTE Procedure" on page 9587 describes the syntax of the procedure.
- "Details: SURVEYIMPUTE Procedure" on page 9603 summarizes the imputation techniques that PROC SURVEYIMPUTE uses.
- "Examples: SURVEYIMPUTE Procedure" on page 9649 includes some additional examples of useful applications.

Getting Started: SURVEYIMPUTE Procedure

This example shows how you can use PROC SURVEYIMPUTE to impute missing values and compute imputation-adjusted statistics for sample survey data. The example uses simulated data from a customer satisfaction survey for a student information system (SIS), which is a software product that provides modules for student registration, class scheduling, attendance, grade reporting, and other functions.

The software company conducted a survey of school personnel who use the SIS. A probability sample of SIS users was selected from the study population, which included SIS users at middle schools and high schools in three states, Georgia, South Carolina, and North Carolina. The sample design for this survey was a two-stage stratified design. A first-stage sample of schools was selected from the list of schools in the three states that use the SIS. The list of schools, which are the primary sampling units (PSU), was stratified by state and by customer status (whether the school was a new user or a renewal user of the system). Within the strata, schools were selected with probability proportional to size and with replacement, where the size measure was school enrollment. From each sample school, five staff members were randomly selected with replacement as the second-stage units to complete the SIS satisfaction questionnaire. These staff members include both teachers and administrators.

The SAS data set SIS_Survey_Sub contains the survey results and the sample design information that is needed to analyze the data. The data set contains the following items:

- State: state where the school is located
- NewUser: 1 if the school is a new user of SIS or 0 if not
- School: school identification (PSU)
- SamplingWeight: sampling weight
- Department: 0 for teachers and 1 for administrators
- Response: coded from 1 to 5, where 1 represents "Very Unsatisfied" and 5 represents "Very Satisfied"

```
data SIS_Survey_Sub;
   input State $ NewUser School SamplingWeight Department Response @@;
   datalines;
GA 1  1 25 1 1  GA 1  1 25 1 2  GA 1  1 25 1 2  GA 1  1 15 . .  GA 1  1 15 0 3
GA 1  2 25 . 3  GA 1  2 25 1 1  GA 1  2 25 . 1  GA 1  2 15 0 .  GA 1  2 15 0 1
GA 1  3 25 1 .  GA 1  3 25 1 4  GA 1  3 25 1 4  GA 1  3 15 . 5  GA 1  3 15 0 .
GA 1  4 25 0 3  GA 1  4 25 0 4  GA 1  4 25 0 .  GA 1  4 15 1 3  GA 1  4 15 1 5
```

```
GA 1  5 25 0 3  GA 1  5 25 0 2  GA 1  5 25 0 2  GA 1  5 15 1 4  GA 1  5 15 1 .
GA 1  6 25 0 4  GA 1  6 25 0 .  GA 1  6 25 0 3  GA 1  6 15 1 .  GA 1  6 15 1 4
GA 1  7 25 0 .  GA 1  7 25 0 .  GA 1  7 25 0 3  GA 1  7 15 0 5  GA 1  7 15 0 1
GA 1  8 25 1 2  GA 1  8 25 1 4  GA 1  8 25 1 4  GA 1  8 15 0 4  GA 1  8 15 0 .
GA 1  9 25 1 4  GA 1  9 25 1 .  GA 1  9 25 1 .  GA 1  9 15 0 5  GA 1  9 15 . 5
GA 1 10 25 0 4  GA 1 10 25 0 4  GA 1 10 25 0 4  GA 1 10 15 0 4  GA 1 10 15 0 3
GA 0 11 25 . 5  GA 0 11 25 1 2  GA 0 11 25 1 .  GA 0 11 15 . 3  GA 0 11 15 1 3
GA 0 12 25 1 4  GA 0 12 25 1 2  GA 0 12 25 1 2  GA 0 12 15 1 5  GA 0 12 15 1 .
GA 0 13 25 1 3  GA 0 13 25 1 1  GA 0 13 25 1 1  GA 0 13 15 0 1  GA 0 13 15 0 4
GA 0 14 25 1 .  GA 0 14 25 1 3  GA 0 14 25 1 .  GA 0 14 15 1 4  GA 0 14 15 1 2
GA 0 15 25 1 .  GA 0 15 25 1 5  GA 0 15 25 1 5  GA 0 15 15 1 4  GA 0 15 15 1 .
GA 0 16 25 0 5  GA 0 16 25 0 2  GA 0 16 25 0 2  GA 0 16 15 0 .  GA 0 16 15 0 2
GA 0 17 25 0 1  GA 0 17 25 0 1  GA 0 17 25 0 1  GA 0 17 15 0 2  GA 0 17 15 0 3
GA 0 18 25 1 4  GA 0 18 25 1 4  GA 0 18 25 1 4  GA 0 18 15 0 .  GA 0 18 15 0 .
GA 0 19 25 0 3  GA 0 19 25 0 5  GA 0 19 25 . 5  GA 0 19 15 0 4  GA 0 19 15 0 5
GA 0 20 25 1 1  GA 0 20 25 1 4  GA 0 20 25 1 4  GA 0 20 15 0 .  GA 0 20 15 0 .
GA 0 21 25 1 2  GA 0 21 25 1 2  GA 0 21 25 1 2  GA 0 21 15 0 3  GA 0 21 15 0 3
NC 1 22 30 1 3  NC 1 22 30 . 3  NC 1 22 30 1 3  NC 1 22 20 . 4  NC 1 22 20 1 4
NC 1 23 30 0 3  NC 1 23 30 0 3  NC 1 23 30 0 .  NC 1 23 20 0 5  NC 1 23 20 0 .
NC 1 24 30 . 4  NC 1 24 30 0 .  NC 1 24 30 . .  NC 1 24 20 1 .  NC 1 24 20 1 4
NC 1 25 30 0 3  NC 1 25 30 0 3  NC 1 25 30 0 3  NC 1 25 20 1 2  NC 1 25 20 1 2
NC 1 26 30 . 5  NC 1 26 30 1 5  NC 1 26 30 1 5  NC 1 26 20 1 1  NC 1 26 20 1 .
NC 1 27 30 1 .  NC 1 27 30 1 1  NC 1 27 30 . 1  NC 1 27 20 0 1  NC 1 27 20 . 1
NC 1 28 30 0 .  NC 1 28 30 0 .  NC 1 28 30 . 3  NC 1 28 20 1 3  NC 1 28 20 1 .
NC 1 29 30 1 1  NC 1 29 30 . 1  NC 1 29 30 1 .  NC 1 29 20 1 5  NC 1 29 20 1 5
NC 1 30 30 0 1  NC 1 30 30 0 1  NC 1 30 30 0 1  NC 1 30 20 1 2  NC 1 30 20 1 2
NC 1 31 30 0 3  NC 1 31 30 0 3  NC 1 31 30 0 3  NC 1 31 20 1 2  NC 1 31 20 1 2
NC 1 32 30 0 5  NC 1 32 30 . .  NC 1 32 30 0 5  NC 1 32 20 . 2  NC 1 32 20 0 2
NC 1 33 30 1 3  NC 1 33 30 1 3  NC 1 33 30 1 3  NC 1 33 20 0 1  NC 1 33 20 0 1
NC 1 34 30 0 3  NC 1 34 30 0 .  NC 1 34 30 0 .  NC 1 34 20 0 .  NC 1 34 20 0 5
NC 0 35 35 0 4  NC 0 35 35 0 2  NC 0 35 35 0 2  NC 0 35 20 1 3  NC 0 35 20 1 3
NC 0 36 35 0 2  NC 0 36 35 0 .  NC 0 36 35 0 .  NC 0 36 20 1 2  NC 0 36 20 . .
NC 0 37 35 1 4  NC 0 37 35 1 1  NC 0 37 35 1 1  NC 0 37 20 1 5  NC 0 37 20 1 5
NC 0 38 35 1 3  NC 0 38 35 . 3  NC 0 38 35 1 3  NC 0 38 20 . 2  NC 0 38 20 0 2
NC 0 39 35 0 3  NC 0 39 35 0 .  NC 0 39 35 . .  NC 0 39 20 0 .  NC 0 39 20 0 3
NC 0 40 35 1 4  NC 0 40 35 1 2  NC 0 40 35 1 2  NC 0 40 20 0 1  NC 0 40 20 0 1
SC 1 41 50 . 2  SC 1 41 50 0 5  SC 1 41 50 0 5  SC 1 41 40 1 .  SC 1 41 40 1 .
SC 1 42 50 1 3  SC 1 42 50 1 1  SC 1 42 50 1 1  SC 1 42 40 1 4  SC 1 42 40 1 4
SC 1 43 50 0 .  SC 1 43 50 0 .  SC 1 43 50 0 .  SC 1 43 40 0 .  SC 1 43 40 0 .
SC 1 44 50 0 .  SC 1 44 50 0 .  SC 1 44 50 0 3  SC 1 44 40 1 3  SC 1 44 40 1 .
SC 0 45 55 1 1  SC 0 45 55 1 .  SC 0 45 55 1 4  SC 0 45 48 1 4  SC 0 45 48 1 4
SC 0 46 55 1 5  SC 0 46 55 1 3  SC 0 46 55 1 3  SC 0 46 48 . 1  SC 0 46 48 0 1
SC 0 47 55 0 .  SC 0 47 55 0 2  SC 0 47 55 0 2  SC 0 47 48 0 2  SC 0 47 48 . 2
;
```

The following statements request the imputation of missing values for Department and Response by using the fully efficient fractional imputation (FEFI) method:

```
proc surveyimpute data=SIS_Survey_Sub method=fefi varmethod=jackknife;
   class Department Response;
   var Department Response;
   strata State NewUser;
   cluster School;
   weight SamplingWeight;
   output out=SIS_Survey_Imputed outjkcoefs=SIS_JKCoefs;
run;
```

The PROC SURVEYIMPUTE statement invokes the procedure. The DATA= option in the PROC SURVEYIMPUTE statement specifies the input data set containing the missing values, the METHOD=FEFI option requests the fully efficient fractional imputation method, and the VARMETHOD= option requests the imputation-adjusted jackknife replicate weights. The CLASS statement specifies the classification variables. The STRATA, CLUSTER, and WEIGHT statements specify the strata, clusters (PSUs), and weight variables. The VAR statement specifies the variables to be imputed (Department and Response). By default, both the variables Department and Response are imputed jointly. Therefore, the missing values for Department will be imputed conditionally on the observed levels of Response, and the missing values for Response will be imputed conditionally on the observed levels of Department. Observations that contain missing values for both Department and Response will be imputed by using the joint observed levels of Department and Response. The OUT= option in the OUTPUT statement names a SAS data set to save the imputed data. The OUTJKCOEFS= option in the OUTPUT statement names a SAS data set to save the jackknife coefficients.

Summary information about the data, CLASS levels, and survey design is shown in Figure 116.1. The "Imputation Information" table summarizes the imputation information. The "Number of Observations" table displays the number of observations that PROC SURVEYIMPUTE reads and uses. This table also displays the sum of weights that are read and used. The sum of weights read (6,468) can be used as an estimator of the population size. For example, the 235 observation units in the SIS_Survey_Sub data set represent 6,468 teachers and administrative staff in the population. The "Class Level Information" table shows that Department has two levels and Response has five levels. The "Design Summary" table shows that 47 schools are selected in the sample from six strata.

Figure 116.1 Summary Information

The SURVEYIMPUTE Procedure

Imputation Information	
Data Set	WORK.SIS_SURVEY_SUB
Weight Variable	SamplingWeight
Stratum Variables	State
	NewUser
Cluster Variable	School
Imputation Method	FEFI
Replication Method	JACKKNIFE
Number of Replicates	47

Number of Observations Read	235
Number of Observations Used	235
Sum of Weights Read	6468
Sum of Weights Used	6468

Class Level Information		
Class	**Levels**	**Values**
Department	2	0 1
Response	5	1 2 3 4 5

Design Summary	
Number of Strata	6
Number of Clusters	47

The "Missing Data Patterns" table in Figure 116.2 lists distinct missing data patterns along with their corresponding frequencies and weighted percentages. An "X" means that the variable is observed in the corresponding group, and a "." means that the variable is missing. The table also displays group-specific variable means. In this hypothetical example, five respondents have unit nonresponse (both variables in the VAR statement contain missing values), 73 respondents have item nonresponse (only one variable in the VAR statement contains a missing value), and 157 respondents have complete response (no variables in the VAR statement contain missing values). Among the 73 item nonrespondents, for 52 respondents, Department is observed but Response is not observed; for 21 respondents, Response is observed but Department is not observed. The estimated percentages in the sample for unit nonresponse, item nonresponse, and complete response are 2.1%, 31.1%, and 66.8%, respectively.

Figure 116.2 Missing Data Patterns

Missing Data Patterns

Group	Department	Response	Freq	Sum of Weights	Unweighted Percent	Weighted Percent
1	X	X	157	4272	66.81	66.05
2	X	.	52	1480	22.13	22.88
3	.	X	21	586	8.94	9.06
4	.	.	5	130	2.13	2.01

Missing Data Patterns

Group Means

Group	Department 0	Department 1	Response 1	Response 2	Response 3	Response 4	Response 5
1	0.440309	0.559691	0.184457	0.206695	0.265684	0.209738	0.133427
2	0.641892	0.358108	.	.	.	.	.
3	.	.	0.261092	0.235495	0.230375	0.085324	0.187713
4	.	.	.	.	.	.	.

The "Imputation Summary" table in Figure 116.3 lists the number of nonmissing observations, missing observations, and imputed observations. There are 78 observations that have missing values for at least one variable, and all 78 missing observations are imputed.

Figure 116.3 Imputation Summary

Imputation Summary

Observation Status	Number of Observations	Sum of Weights
Nonmissing	157	4272
Missing	78	2196
Missing, Imputed	78	2196
Missing, Not Imputed	0	0

The output data set SIS_Survey_Imputed contains the observed data and the imputed values for Department and Response. In addition, this data set contains the imputation-adjusted full-sample weight (ImpWt), observation unit identification (UnitId), recipient index (ImpIndex), and imputation-adjusted jackknife replicate weights (ImpRepWt_1, . . . , ImpRepWt_47).

Suppose you want to compute frequency tables by using the imputed data set. The following statements request one-way tables for Department and Response and a two-way table for Department by Response.

The analyses include the imputed values and account for both the design variance and the imputation variance.

```
proc surveyfreq data=SIS_Survey_Imputed varmethod=jackknife;
   table department response  department*response;
   weight ImpWt;
   repweights ImpRepWt: / jkcoefs=SIS_JKCoefs;
run;
```

The DATA= option in the PROC SURVEYFREQ statement specifies the input data set for analysis, SIS_Survey_Imputed, which contains the observed values and the imputed values for Department and Response. The FEFI technique uses multiple donor cells for a missing item. Therefore, the number of rows in the SIS_Survey_Imputed data set is greater than the number of rows in the observed data set, SIS_Survey_Sub. Each row in the SIS_Survey_Sub data set represents an observation unit, but this is not true for the SIS_Survey_Imputed data set. Therefore, it is very important to use only the weighted statistics from SIS_Survey_Imputed. The WEIGHT statement specifies the weight variable ImpWt, which is adjusted for the FEFI method. The imputation-adjusted jackknife replicate weights are saved in the variables ImpRepWt_1, . . . , ImpRepWt_47 in the SIS_Survey_Imputed data set. The REPWEIGHTS statement names the replicate weight variables and the jackknife coefficients data set, SIS_JKCOEFS. You should not use the unadjusted full-sample weights (SamplingWeight) or unadjusted replicate weights along with the imputed data.

Figure 116.4 displays some summary information. Note that the sum of weights in Figure 116.4 matches the sum of weights read from Figure 116.1, but the number of observations in Figure 116.4 (509) does not match the number of observations from Figure 116.1 (235). The sum of weights from both PROC SURVEYIMPUTE and PROC SURVEYFREQ represents the population size. The number of observations in Figure 116.1 represents the number of observation units, but the number of observations in Figure 116.4 represents the number of rows in the data set that include the observed units and the imputed rows. The number of replicates is 47, which is the same as the number of schools (PSUs).

Figure 116.4 One-Way Table

The SURVEYFREQ Procedure

Data Summary	
Number of Observations	509
Sum of Weights	6468

Variance Estimation	
Method	Jackknife
Replicate Weights	SIS_SURVEY_IMPUTED
Number of Replicates	47

Figure 116.5 displays one-way tables for Department and Response. The Frequency column does not represent frequencies for observation units from the SIS_Survey_Sub data set. These frequencies represent the frequency of data lines in the SIS_Survey_Sub data set, which also include the imputed rows. The Weighted Frequency, Std Err of Wgt Freq, Percent, and Std Err of Percent columns use the imputation-adjusted full-sample weight and replicate weights. You should use the weighted statistics from these columns. For example, an estimated 49.47% of SIS users are teachers, with a standard error of 6.64%. An estimate of "Very Satisfied" users is 14.19%, with a standard error of 3.77%.

Figure 116.5 One-Way Table

Table of Department

Department	Frequency	Weighted Frequency	Std Err of Wgt Freq	Percent	Std Err of Percent
0	278	3200	429.52229	49.4729	6.6407
1	231	3268	429.52229	50.5271	6.6407
Total	509	6468	0	100.0000	

Table of Response

Response	Frequency	Weighted Frequency	Std Err of Wgt Freq	Percent	Std Err of Percent
1	100	1256	291.92305	19.4153	4.5133
2	103	1371	361.02585	21.1976	5.5817
3	112	1710	305.26968	26.4371	4.7197
4	100	1213	283.69298	18.7598	4.3861
5	94	917.82544	243.87967	14.1903	3.7706
Total	509	6468	0	100.0000	

Figure 116.6 displays the two-way table for Department by Response. The Weighted Frequency, Std Err of Wgt Freq, Percent, and Std Err of Percent columns use the imputation-adjusted full-sample weight and replicate weights. You should use the weighted statistics from these columns. Among the school personnel, an estimated 8.10% are teachers who are "Very Satisfied", and 6.09% are administrators who are "Very Satisfied". The standard errors are 3.11% and 2.43%, respectively.

Figure 116.6 Crosstabulation

Table of Department by Response

Department	Response	Frequency	Weighted Frequency	Std Err of Wgt Freq	Percent	Std Err of Percent
0	**1**	57	637.83724	246.18741	9.8614	3.8062
	2	55	743.50947	334.28335	11.4952	5.1683
	3	64	951.95811	258.23015	14.7180	3.9924
	4	49	342.84458	150.44168	5.3006	2.3259
	5	53	523.75680	200.99126	8.0977	3.1075
	Total	278	3200	429.52229	49.4729	6.6407
1	**1**	43	617.94159	209.04386	9.5538	3.2320
	2	48	627.55128	185.53346	9.7024	2.8685
	3	48	757.99401	237.82609	11.7191	3.6770
	4	51	870.53830	262.37514	13.4592	4.0565
	5	41	394.06863	156.95381	6.0926	2.4266
	Total	231	3268	429.52229	50.5271	6.6407
Total	**1**	100	1256	291.92305	19.4153	4.5133
	2	103	1371	361.02585	21.1976	5.5817
	3	112	1710	305.26968	26.4371	4.7197
	4	100	1213	283.69298	18.7598	4.3861
	5	94	917.82544	243.87967	14.1903	3.7706
	Total	509	6468	0	100.0000	

Syntax: SURVEYIMPUTE Procedure

The following statements are available in the SURVEYIMPUTE procedure. Items within < > are optional.

```
PROC SURVEYIMPUTE <options> ;
    BY variables ;
    CELLS variables ;
    CLASS variable <(options)> <... variable <(options)>> </ options> ;
    CLUSTER variables ;
    ID variable ;
    IMPJOINT <variables> ;
    OUTPUT <OUT=SAS-data-set><OUTJKCOEFS=SAS-data-set><keyword=name
            ... keyword=name> ;
    REPWEIGHTS variables ;
    STRATA variables </ option> ;
    VAR variable <(options)> <... variable <(options)>> </ options> ;
    WEIGHT variable ;
```

The PROC SURVEYIMPUTE and VAR statements are required.

The following sections describe the PROC SURVEYIMPUTE statement and then describe the other statements in alphabetical order.

PROC SURVEYIMPUTE Statement

PROC SURVEYIMPUTE < *options* > ;

The PROC SURVEYIMPUTE statement invokes the SURVEYIMPUTE procedure. The DATA= option identifies the data set to be analyzed. Table 116.1 summarizes the options available in the PROC SURVEYIMPUTE statement.

Table 116.1 Options Available in the PROC SURVEYIMPUTE Statement

Option	Description
DATA=	Names the input data set
METHOD=	Specifies the imputation method
NDONORS=	Specifies the number of donors for a recipient
NOPRINT	Suppresses all displayed output
ORDER=	Specifies the sort order of CLASS variables
RATE=	Specifies the sampling rate for the primary sampling units
SEED=	Specifies the random number seed
TOTAL=	Specifies the total number of primary sampling units
VARMETHOD=	Specifies the variance estimation method

You can specify the following *options*.

DATA=*SAS-data-set*
names the SAS data set that contains the data to be analyzed. If you omit the DATA= option, PROC SURVEYIMPUTE uses the most recently created SAS data set.

METHOD=FEFI | FHDI | HOTDECK | HD < (*method-option***) >**
specifies the imputation method to impute missing values for all variables in the VAR statement.

Table 116.2 summarizes the available *method-options*.

Table 116.2 Imputation Methods

METHOD=	Imputation Method	*Method-Options*
FEFI	Fully efficient fractional imputation method	ABSEMWTCONV= MAXDONORCELLS= MAXEMITER= RELEMWTCONV=
FHDI	Fractional hot-deck imputation method	ABSEMWTCONV= DISP=MEAN DISP=SSCP MAXDONORCELLS= MAXEMITER= RELEMWTCONV= REPWTADJ=RATIO REPWTADJ=NEIGHBOR REPWTADJ=NONE SELECTION=PPSPERPATN SELECTION=PPSPEROBS
HOTDECK | HD	Approximate Bayesian bootstrap Simple random sampling without replacement Simple random sampling with replacement Weighted selection	SELECTION=ABB SELECTION=SRSWOR SELECTION=SRSWR SELECTION=WEIGHTED

By default, if all variables that you specify in the VAR statement are also specified in the CLASS statement, then METHOD=FEFI. Otherwise, the default imputation method is METHOD=HOTDECK. You can specify the following values:

FEFI < (*method-options***) >**
requests the fully efficient fractional imputation (FEFI) method. For more information, see the section "Fully Efficient Fractional Imputation" on page 9608.

You can specify the following *method-options*:

ABSEMWTCONV=*r*
specifies the absolute weighted convergence criterion. The expectation maximization (EM) algorithm stops when the maximum absolute difference between the fractional weights from the previous iteration and the fractional weights from the current iteration is less than *r*. The

default value of *r* is 0.00001. For more information, see the section "FEFI Algorithm" on page 9608.

MAXDONORCELLS=*i*
specifies the maximum number (*i*) of donor cells allowed for a recipient unit. If the maximum number of donor cells exceeds MAXDONORCELLS=, then no imputation is performed. By default, MAXDONORCELLS=5000.

MAXEMITER=*i*
specifies the maximum number (*i*) of iterations for the expectation maximization (EM) algorithm. By default, MAXEMITER=100.

RELEMWTCONV=*r*
specifies a relative weighted convergence criterion. The expectation maximization (EM) algorithm stops when the maximum absolute relative difference between the weights from the previous iteration and the weights from the current iteration is less than *r*. For more information, see the section "FEFI Algorithm" on page 9608. The default value of *r* is 0.001.

FHDI < (*method-options***) >**
requests the fractional hot-deck imputation (FHDI) method. For more information, see the section "Fractional Hot-Deck Imputation" on page 9625.

You can specify the following *method-options* in parentheses:

ABSEMWTCONV=*r*
specifies the absolute weighted convergence criterion. The expectation maximization (EM) algorithm stops when the maximum absolute difference between the first-stage fractional weights from the previous iteration and the first-stage fractional weights from the current iteration is less than *r*. For more information, see the section "FEFI Algorithm" on page 9608. The default value of *r* is 0.00001.

DISP=*stat*
displays the weighted mean or the crossproduct of the weighted mean sum of squares for variables that are specified in the VAR statement but not in the CLASS statement.

You can specify one of the following *stats*:

MEAN displays the weighted mean.

SSCP displays both the weighted mean and the crossproduct of the weighted mean sum of squares.

Displayed statistics are from both two-stage FEFI and FHDI because PROC SURVEYIMPUTE must perform two-stage FEFI in order to determine the donor sets for FHDI. The closer the means and crossproducts for FHDI are to the ones for two-stage FEFI, the more confidence you can have that FHDI is as efficient as FEFI.

MAXDONORCELLS=*i*
specifies the maximum number (*i*) of second-stage donor cells allowed for a recipient unit. If the maximum number of second-stage donor cells exceeds *i*, then no imputation is performed. By default, MAXDONORCELLS=5000.

MAXEMITER=*i*
specifies the maximum number (*i*) of iterations for the expectation maximization (EM) algorithm for the first-stage FEFI. By default, MAXEMITER=100.

RELEMWTCONV=*r*
specifies the relative weighted convergence criterion. The expectation maximization (EM) algorithm for the first-stage FEFI stops when the maximum absolute relative difference between the weights from the previous iteration and the weights from the current iteration is less than *r*. For more information, see the section "FEFI Algorithm" on page 9608. The default value of *r* is 0.001.

REPWTADJ=*replicate-adjustment-option*
adjusts the replicate weights for FHDI. For more information, see the section "Replicate Weight Adjustments for FHDI" on page 9643. You can specify one of the following values for *replicate-adjustment-option*:

NEIGHBOR adjusts replicate weights by using the sum of replicate fractional weights in neighborhoods that are defined by the full sample fractional weights from two-stage FEFI.

NONE does not adjust the replicate weights for the selection of donors after two-stage FEFI.

RATIO adjusts replicate weights by using the ratio of replicate fractional weights and the full sample fractional weights from two-stage FEFI.

By default, REPWTADJ=NEIGHBOR.

SELECTION=*selection-option*
specifies how to perform the probability proportional to size (PPS) with replacement selection. For more information, see "Second-Stage Selection" in section "Fractional Hot-Deck Imputation Algorithm" on page 9628. You can specify one of the following *selection-options*:

PPSPEROBS performs independent selection of second-stage donor cells for every observation unit that is a recipient for the second-stage imputation.

PPSPERPATN performs one selection of second-stage donor cells for all observation units that are recipients for the second-stage imputation and have the same first-stage FEFI levels.

By default, SELECTION=PPSPERPATN for METHOD=FHDI.

HOTDECK < (SELECTION=*selection-option***) >**
HD < (SELECTION=*selection-option***) >**
requests the hot-deck imputation method. For more information, see the section "Hot-Deck Imputation" on page 9636.

By default, SELECTION=SRSWR for METHOD=HOTDECK if you do not use the WEIGHT statement, and SELECTION=WEIGHTED for METHOD=HOTDECK if you use the WEIGHT statement. You can specify one of the following donor selection *selection-options*:

ABB
requests donor selection by using the approximate Bayesian bootstrap method. For more information, see the section "Approximate Bayesian Bootstrap" on page 9638.

SRSWOR
requests donor selection by using simple random samples without replacement. For more information, see the section "Simple Random Samples without Replacement" on page 9638.

SRSWR
requests donor selection by using simple random samples with replacement. For more information, see the section "Simple Random Samples with Replacement" on page 9638.

WEIGHTED
requests donor selection by using probability proportional to respondent weights with replacement. For more information, see the section "Weighted Selection" on page 9639.

NDONORS=*r*
specifies the number of donor units *r*, where *r* is either of the following:

- the number of donor units to be used to impute every recipient unit when METHOD=HOTDECK
- the maximum number of second-stage donor cells to be used to impute second-stage missing items conditional on the first-stage FEFI levels when METHOD=FHDI

If you specify NDONORS=0 for METHOD=HOTDECK, then no imputation is performed.

When METHOD=FEFI, the SURVEYIMPUTE procedure performs fully efficient fractional imputation, for which the NDONORS= option does not apply.

By default, NDONORS=1 for METHOD=HOTDECK and NDONORS=10 for METHOD=FHDI.

NOPRINT
suppresses all displayed output. This option temporarily disables the Output Delivery System (ODS); for more information about ODS, see Chapter 20, "Using the Output Delivery System."

ORDER=DATA | FORMATTED | FREQ | INTERNAL
specifies the sort order for the levels of the classification variables (which are specified in the CLASS statement).

This option applies to the levels for all classification variables, except when you use the (default) ORDER=FORMATTED option with numeric classification variables that have no explicit format. In that case, the levels of such variables are ordered by their internal value.

The ORDER= option can take the following values:

Value of ORDER=	Levels Sorted By
DATA	Order of appearance in the input data set
FORMATTED	External formatted value, except for numeric variables with no explicit format, which are sorted by their unformatted (internal) value
FREQ	Descending frequency count; levels with the most observations come first in the order
INTERNAL	Unformatted value

By default, ORDER=FORMATTED. For ORDER=FORMATTED and ORDER=INTERNAL, the sort order is machine-dependent.

For more information about sort order, see the chapter on the SORT procedure in the *Base SAS Procedures Guide* and the discussion of BY-group processing in *SAS Language Reference: Concepts*.

RATE=*value* | *SAS-data-set*

R=*value* | *SAS-data-set*

specifies the sampling rate, which PROC SURVEYIMPUTE uses to compute a finite population correction for bootstrap replicate weights. This option is ignored for the BRR and jackknife replication methods.

If your sample design has multiple stages, you should specify the *first-stage sampling rate*, which is the ratio of the number of primary sampling units (PSUs) that are selected to the total number of PSUs in the population.

You can specify the sampling rate in either of the following ways:

value specifies a nonnegative number to use for a nonstratified design or for a stratified design that has the same sampling rate in each stratum.

SAS-data-set specifies a *SAS-data-set* that contains the stratification variables and the sampling rates for a stratified design that has different sampling rates in the strata. You must provide the sampling rates in the data set variable named _RATE_.

The sampling rates must be nonnegative numbers. You can specify *value* as a number between 0 and 1. Or you can specify *value* in percentage form as a number between 1 and 100, and PROC SURVEYIMPUTE converts that number to a proportion. The procedure treats the value 1 as 100% instead of 1%.

For more information, see the section "Population Totals and Sampling Rates" on page 9605.

If you do not specify the RATE= or TOTAL= option, then the bootstrap replicate weights do not include a finite population correction. You cannot specify both the TOTAL= option and the RATE= option in the same PROC SURVEYIMPUTE statement.

SEED=*number*

specifies the initial random number generation seed for selecting donor units for METHOD=HOTDECK or for selecting second-stage donor cells for METHOD=FHDI. The *number* should be a positive integer. If you do not specify this option or if *number* is 0, PROC SURVEYIMPUTE uses the time of day from the computer's clock to obtain the initial seed. For more information, see the section "Random Number Generation" on page 9608.

TOTAL=*value* | *SAS-data-set*

specifies the total number of primary sampling units (PSUs) in the population. PROC SURVEYIMPUTE uses the *value* to compute a finite population correction for bootstrap replicate weights. This option is ignored for the BRR and jackknife replication methods.

You can specify the total number of PSUs in either of the following ways:

value specifies a positive number to use for a nonstratified design or for a stratified design that has the same population total in each stratum.

SAS-data-set specifies a *SAS-data-set* that contains the stratification variables and the population totals for a stratified design that has different population totals in the strata. You must provide the stratum totals in the data set variable named _TOTAL_.

The stratum totals must be positive numbers.

For more information, see the section "Population Totals and Sampling Rates" on page 9605.

If you do not specify the TOTAL= or RATE= option, then the bootstrap replicate weights do not include a finite population correction. You cannot specify both the TOTAL= option and the RATE= option in the same PROC SURVEYIMPUTE statement.

VARMETHOD=*method* **<(***method-options***)>**
REPWEIGHTSTYPE=*method* **<(***method-options***)>**
computes imputation-adjusted replicate weights.

Table 116.3 summarizes the available *methods* and *method-options*.

Table 116.3 Replicate Weights Options

method	**Replicate Weights Method**	*method-options*
BOOTSTRAP	Bootstrap	MH=*number* REPS=*number*
BRR	Balanced repeated replication	FAY <=*value*> HADAMARD=*SAS-data-set* PRINTH REPS=*number*
JACKKNIFE	Jackknife	None
NONE	No replicate weight computation	None

By default, VARMETHOD=JACKKNIFE when METHOD=FEFI or METHOD=FHDI, and VARMETHOD=NONE when METHOD=HOTDECK.

You can specify the following *methods*:

BOOTSTRAP <(*method-options***)>**
computes imputation-adjusted bootstrap replicate weights. The bootstrap method requires at least two primary sampling units (PSUs) in each stratum for stratified designs unless you provide replicate weights by using a REPWEIGHTS statement. For more information, see the section "Bootstrap Method" on page 9639.

You can specify the following *method-options*:

MH=*value* **|** **(***values***)**
specifies the number of PSUs to select for the bootstrap replicate samples. You can provide bootstrap stratum sample sizes m_h by specifying a list of *values*. Alternatively, you can provide a single bootstrap sample size *value* to use for all strata or for a nonstratified design. For more information, see the section "Bootstrap Method" on page 9639.

Each bootstrap sample size, m_h, must be a positive integer and must be less than n_h, which is the total number of PSUs in stratum h. By default, $m_h = n_h - 1$ for a stratified design. For a nonstratified design, the bootstrap sample size *value* must be less than n (the total number of PSUs in the sample). By default, $m = n - 1$ for a nonstratified design. You can provide the bootstrap sample size by specifying one of the following forms:

MH=*value*
specifies a single bootstrap sample size *value* to use for all strata or for a nonstratified design.

MH=(*values***)**
specifies a list of stratum bootstrap sample size *values*. You can separate the values by using blanks or commas, and you must enclose the list of values in parentheses. The number of values must not be less than the number of strata in the DATA= input data set.

The order of the stratum sample size values must match the order of the stratum levels in the DATA= input data set. Each stratum sample size value must be a positive integer and must be less than the total number of PSUs in the corresponding stratum.

REPS=*number*
specifies the *number* of replicates for bootstrap variance estimation, where *number* must be an integer greater than 1. Increasing the number of replicates improves the estimation precision but also increases the computation time. By default, REPS=250.

BRR < (*method-options***) >**
computes the imputation-adjusted balanced repeated replication (BRR) weights. The BRR method requires a stratified sample design with two primary sampling units (PSUs) in each stratum. If you specify the VARMETHOD=BRR option, you must also use a STRATA statement unless you provide replicate weights by using a REPWEIGHTS statement. For more information, see the section "Balanced Repeated Replication (BRR) Method" on page 9640.

You can specify the following *method-options* in parentheses after the VARMETHOD=BRR option:

FAY < =*value* **>**
requests Fay's method, which is a modification of the BRR method. For more information, see the section "Unadjusted Fay's BRR Replicate Weights" on page 9641.

You can specify the *value* of the Fay coefficient, which is used in converting the original sampling weights to replicate weights. The Fay coefficient must be a nonnegative number less than 1. By default, the value of the Fay coefficient is 0.5.

HADAMARD=*SAS-data-set*

H=*SAS-data-set*
names a SAS data set that contains the Hadamard matrix for BRR replicate construction. If you do not provide a Hadamard matrix by using this *method-option*, PROC SURVEYIMPUTE generates an appropriate Hadamard matrix for replicate construction. For more information, see the sections "Balanced Repeated Replication (BRR) Method" on page 9640 and "Hadamard Matrix" on page 9641.

If a Hadamard matrix of a particular dimension exists, it is not necessarily unique. Therefore, if you want to use a specific Hadamard matrix, you must provide the matrix as a SAS data set in the HADAMARD= *method-option*.

In the HADAMARD= input data set, each variable corresponds to a column of the Hadamard matrix, and each observation corresponds to a row of the matrix. You can use any variable names in the HADAMARD= data set. All values in the data set must equal either 1 or –1. You must ensure that the matrix you provide is indeed a Hadamard matrix—that is, $\mathbf{A}'\mathbf{A} = R\mathbf{I}$, where $\mathbf{A}$ is the Hadamard matrix of dimension R and $\mathbf{I}$ is an identity matrix. PROC SURVEYIMPUTE does not check the validity of the Hadamard matrix that you provide.

The HADAMARD= input data set must contain at least H variables, where H denotes the number of first-stage strata in your design. If the data set contains more than H variables, PROC SURVEYIMPUTE uses only the first H variables. Similarly, the HADAMARD= input data set must contain at least H observations.

If you do not specify the REPS= *method-option*, then the number of replicates is equal to the number of observations in the HADAMARD= input data set. If you specify the number of replicates—for example, REPS=*nreps*—then the procedure uses the first *nreps* observations in the HADAMARD= data set to construct the replicates.

You can specify the PRINTH *method-option* to display the Hadamard matrix that the procedure uses to construct replicates for BRR.

PRINTH

displays the Hadamard matrix that is used to construct replicates for BRR. When you provide the Hadamard matrix in the HADAMARD= *method-option*, PROC SURVEYIMPUTE displays only the rows and columns that are actually used to construct replicates. For more information, see the sections "Balanced Repeated Replication (BRR) Method" on page 9640 and "Hadamard Matrix" on page 9641.

The PRINTH *method-option* is not available when you use a REPWEIGHTS statement to provide replicate weights, because the procedure does not use a Hadamard matrix in this case.

REPS=*number*

specifies the number of replicates for BRR variance estimation. The value of *number* must be an integer greater than 1.

If you do not provide a Hadamard matrix by using the HADAMARD= *method-option*, the number of replicates should be greater than the number of strata and should be a multiple of 4. For more information, see the section "Balanced Repeated Replication (BRR) Method" on page 9640. If a Hadamard matrix cannot be constructed for the REPS= value that you specify, the value is increased until a Hadamard matrix of that dimension can be constructed. Therefore, it is possible for the actual number of replicates used to be larger than the REPS= value that you specify.

If you provide a Hadamard matrix by using the HADAMARD= *method-option*, the value of REPS= must not be greater than the number of rows in the Hadamard matrix. If you provide a Hadamard matrix and do not specify the REPS= *method-option*, the number of replicates equals the number of rows in the Hadamard matrix.

If you do not specify the REPS= or HADAMARD= *method-option* and do not include a REPWEIGHTS statement, the number of replicates equals the smallest multiple of 4 that is greater than the number of strata.

If you provide replicate weights by using a REPWEIGHTS statement, PROC SURVEYIMPUTE does not use the REPS= *method-option*. When you use a REPWEIGHTS statement, the number of replicates equals the number of REPWEIGHTS variables.

JACKKNIFE
JK
computes the imputation-adjusted jackknife replicate weights. For more information, see the section "Jackknife Method" on page 9642.

NONE
does not compute replicate weights.

BY Statement

BY *variables* **;**

You can specify a BY statement in PROC SURVEYIMPUTE to obtain separate analyses of observations in groups that are defined by the BY variables. When a BY statement appears, the procedure expects the input data set to be sorted in order of the BY variables. If you specify more than one BY statement, only the last one specified is used.

If your input data set is not sorted in ascending order, use one of the following alternatives:

- Sort the data by using the SORT procedure with a similar BY statement.
- Specify the NOTSORTED or DESCENDING option in the BY statement in the SURVEYIMPUTE procedure. The NOTSORTED option does not mean that the data are unsorted but rather that the data are arranged in groups (according to values of the BY variables) and that these groups are not necessarily in alphabetical or increasing numeric order.
- Create an index on the BY variables by using the DATASETS procedure (in Base SAS software).

Note that using a BY statement provides completely separate imputation within the BY groups. For more information about BY-group processing, see the discussion in *SAS Language Reference: Concepts*. For more information about the DATASETS procedure, see the discussion in the *Base SAS Procedures Guide*.

CELLS Statement

CELLS *variables* **;**

The CELLS statement names the variables that identify the imputation cells. The imputation cells divide the data into groups of similar units. The combination of levels of CELLS variables defines the imputation cells. If you do not use this statement, then all observation units are assumed to be in one imputation cell.

CLASS Statement

CLASS *variable* < (*options*) > . . . < *variable* < (*options*) > > < / *options* > ;

The CLASS statement names the classification variables for the analysis. Most *options* can be specified either as individual variable *options* or as global *options*. You can specify *options* for each variable by enclosing the options in parentheses after the variable name. You can also specify global *options* for the CLASS statement by placing the *options* after a slash (/). Global *options* are applied to every variable that is specified without an *option* in the CLASS statement. However, individual CLASS variable *options* override the global *options*.

You can specify the following *options* either as global options or as individual options:

DESCENDING
DESC

reverses the sort order of the classification variable. If you specify both the DESCENDING and ORDER= options, PROC SURVEYIMPUTE orders the categories according to the ORDER= option and then reverses that order.

ORDER=DATA | FORMATTED | FREQ | INTERNAL

specifies the sort order for the levels of classification variables.

The following table shows how PROC SURVEYIMPUTE interprets values of the ORDER= option:

Value of ORDER=	Levels Sorted By
DATA	Order of appearance in the input data set
FORMATTED	External formatted values, except for numeric variables with no explicit format, which are sorted by their unformatted (internal) values
FREQ	Descending frequency count; levels with more observations come earlier in the order
INTERNAL	Unformatted value

By default, ORDER=FORMATTED. For ORDER=FORMATTED and ORDER=INTERNAL, the sort order is machine-dependent. When ORDER=FORMATTED is in effect for numeric variables for which you have supplied no explicit format, the levels are ordered by their internal values. For ORDER=FREQ, the frequency counts are unweighted. For more information about sort order, see the chapter on the SORT procedure in the *Base SAS Procedures Guide* and the discussion of BY-group processing in *SAS Language Reference: Concepts*.

TRUNCATE < =*n* >

specifies the length *n* of CLASS variable values to use in determining CLASS variable levels. The default is to use the full formatted length of the CLASS variable. If you specify the TRUNCATE option without the length *n*, the first 16 characters of the formatted values are used. When formatted values are longer than 16 characters, you can use this option to revert to the levels as determined in releases before SAS 9. The TRUNCATE option is available only as a global option.

CLUSTER Statement

CLUSTER *variables* **;**

The CLUSTER statement names variables that identify the first-stage clusters in a clustered sample design. First-stage clusters are also known as primary sampling units (PSUs). The combinations of categories of CLUSTER variables define the clusters in the sample. If you also use the STRATA statement, clusters are nested within strata.

If your sample design has clustering at multiple stages, you should specify only the first-stage clusters (PSUs) in the CLUSTER statement. For more information, see the section "Specifying the Sample Design" on page 9604.

If you provide replicate weights in a REPWEIGHTS statement, you do not need to use a CLUSTER statement.

The CLUSTER *variables* are one or more variables in the DATA= input data set. These variables can be either character or numeric, but PROC SURVEYIMPUTE treats them as categorical variables. The formatted values of the CLUSTER variables determine the cluster variable levels. Thus, you can use formats to group values into levels. For more information, see the discussion of the FORMAT procedure in the *Base SAS Procedures Guide* and the discussions of the FORMAT statement and SAS formats in *SAS Formats and Informats: Reference*.

You can use multiple CLUSTER statements to specify CLUSTER variables. PROC SURVEYIMPUTE uses variables from all CLUSTER statements to create clusters.

ID Statement

ID *variable* **;**

The ID statement names a *variable* in the DATA= input data set to identify observation units. When you use an OUTPUT statement, the OUT= data set includes the ID variable. PROC SURVEYIMPUTE uses the ID variable values to identify the donor observations. If you do not use an ID statement, the procedure creates a new variable named UnitID that uses the observation numbers to identify the donor observations.

IMPJOINT Statement

IMPJOINT < *variables* > **;**

The IMPJOINT statement specifies the names of variables that are to be imputed jointly for the fully efficient fractional imputation (FEFI) method. If you do not use the IMPJOINT statement, then all the variables that you specify in the VAR statement are imputed jointly. You can use multiple IMPJOINT statements. The levels of the variables in the IMPJOINT statement describe a nonparametric imputation model for the expectation maximization (EM) step for the fractional imputation.

If you use the following IMPJOINT statements, then the variables y1, y2, and y3 are imputed jointly, and the variables y4 and y5 are imputed jointly:

```
IMPJOINT y1 y2 y3;
IMPJOINT y4 y5;
```

Analysis variables, which you specify in the VAR statement, can appear in only one IMPJOINT statement. However, auxiliary variables that you do not specify in the VAR statement can be specified in multiple IMPJOINT statements.

If you do not specify any variable names in the IMPJOINT statement, then every variable in the VAR statement is imputed marginally.

The IMPJOINT statement is ignored when you specify the METHOD=HOTDECK or METHOD=FHDI option in the PROC SURVEYIMPUTE statement.

OUTPUT Statement

OUTPUT < **OUT=***SAS-data-set* > < **OUTJKCOEFS=***SAS-data-set* > < *keyword***=***name* . . . *keyword***=***name* >
;

The OUTPUT statement creates a SAS data set that contains the imputed data. You must use the OUTPUT statement to store the imputed data in a SAS data set. If you use multiple OUTPUT statements, then PROC SURVEYIMPUTE uses only the first OUTPUT statement and ignores the rest. The OUTPUT OUT= data set contains all the variables from the DATA= input data set, imputed values for missing values for the variables in the VAR statement, and some observation-level quantities. These quantities can include the fractionally adjusted weights, replicate weights, recipient numbers, and donor identifications.

You can specify the following in the OUTPUT statement:

OUT=*SAS-data-set*
names the output data set. If you use the OUTPUT statement but omit the OUT= option, then the output data set is named by using the DATA*n* convention. For more information, see the section "OUT= Output Data Set" on page 9645.

OUTJKCOEFS=*SAS-data-set*
names a SAS data set that contains the jackknife coefficients for VARMETHOD=JACKKNIFE.

keyword < *=name* >
specifies the quantities to include in the output data set and optionally names the new variables that contain the quantities. Specify a *keyword* for each desired quantity (see the following list of *keywords*), optionally followed by an equal sign and a variable name to contain the quantity. If you specify a *keyword* without a variable *name*, then PROC SURVEYIMPUTE uses default names. You can specify the following *keywords*:

DONORID< **=***name* >
requests a name for the identification variable for the donor units. If you do not specify this keyword, the donor IDs are not saved in the output data set. If you specify this keyword but do not specify a *name*, then the donor IDs are stored in a new variable named DonorID. This keyword is available only when METHOD=HOTDECK.

FRACTIONALWEIGHTS=*name*

includes the fractional weights of donor cells in the output data set and specifies the corresponding variable *name*. If you do not specify this keyword, the fractional weights are not saved in the output data set. This keyword is available when METHOD=FEFI or METHOD=FHDI.

IMPADJWEIGHTS=*name*

includes the imputation-adjusted weights in the output data set and specifies the corresponding variable *name*. The imputation-adjusted weights are computed by multiplying the base weights by the fractional weights. If you do not specify this keyword, then the imputation-adjusted weights are stored in a new variable named ImpWt. This keyword is available when METHOD=FEFI or METHOD=FHDI.

IMPSTATUS=*name*

includes an imputation status index with the values shown in Table 116.4.

Table 116.4 Imputation Status Index

Index	Imputation Status
0	All items are observed
1	All missing items are imputed
2	No missing items are imputed
3	Some missing items are imputed but some missing items are not imputed
4	Invalid observation; observation is not used in the imputation

OBSID=*name*

includes an index variable to contain the unique numeric identification of every unit from the input data set in the output data and specifies the corresponding variable *name*. If you do not specify this keyword, then the default unit ID is stored in a new variable named UnitID. The OBSID= option is not applicable when the ID statement is specified.

IMPINDEX=*name*

includes the imputation index in the output data set and specifies the corresponding variable *name*. The imputation index can be 0 (which indicates a nonmissing unit) or any positive integer (which represents multiple donor units for a recipient unit). If you do not specify this keyword, then the imputation index is stored in a new variable named ImpIndex.

OUTCONTLEVELS < =YES | NO >

specifies whether to include in the OUTPUT OUT= data set the imputed values for the variables that are specified in the CLEVVAR= option in the VAR statement or the imputed levels for the imputation bins (when the CLEVELS= option is specified in the VAR statement). This option does not apply when METHOD=HOTDECK.

By default, the imputed values for the variables that are specified in the CLEVVAR= option or the imputed levels for the imputation bins are included in the OUTPUT OUT= data. Optionally, you can specify the following keywords:

YES includes the imputed values for CLEVVAR= variables or the imputed levels for the imputation bins (when the CLEVELS= option is used) in the OUTPUT OUT= data set.

NO does not include the imputed values for CLEVVAR= variables or the imputed levels for the imputation bins in the OUTPUT OUT= data set.

REPWEIGHTS Statement

REPWEIGHTS *variables* **;**

The REPWEIGHTS statement names variables that provide replicate weights.

If you use a REPWEIGHTS statement and you specify METHOD=HOTDECK in the PROC SURVEYIMPUTE statement, the procedure does not adjust the replicate weights.

If you use a REPWEIGHTS statement and you specify METHOD=FEFI or METHOD=FHDI in the PROC SURVEYIMPUTE statement, the procedure adjusts the replicate weights.

Each REPWEIGHTS variable should contain the weights for a single replicate, and the number of replicates should equal the number of REPWEIGHTS variables. The REPWEIGHTS variables must be numeric, and the variable values must be nonnegative numbers.

If you provide replicate weights in a REPWEIGHTS statement, you do not need to use a CLUSTER or STRATA statement.

If you use a REPWEIGHTS statement but do not use a WEIGHT statement, PROC SURVEYIMPUTE uses the average of each observation's replicate weights as the observation's weight.

STRATA Statement

STRATA *variables* < / *option* > **;**

The STRATA statement names one or more *variables* that form the strata in a stratified sample design. The combinations of levels of STRATA variables define the strata in the sample, where strata are nonoverlapping subgroups that were sampled independently.

If your sample design has stratification at multiple stages, you should identify only the first-stage strata in the STRATA statement. For more information, see the section "Specifying the Sample Design" on page 9604.

If you provide replicate weights in a REPWEIGHTS statement, you do not need to use a STRATA statement.

The STRATA *variables* are one or more variables in the DATA= input data set. These variables can be either character or numeric, but PROC SURVEYIMPUTE treats them as categorical variables. The formatted values of the STRATA variables determine the STRATA variable levels. Thus, you can use formats to group values into levels. For more information, see the discussion of the FORMAT procedure in the *Base SAS Procedures Guide* and the discussions of the FORMAT statement and SAS formats in the *SAS Formats and Informats: Reference*.

You can specify the following *option* in the STRATA statement after a slash (/):

LIST
displays a "Stratum Information" table, which lists all strata together with the corresponding values of the STRATA variables. This table provides the number of observations, the number of clusters, and the

sum of weights in each stratum, as well as the sampling fraction if you specify the RATE= or TOTAL= option.

VAR Statement

VAR *variable* < (*options*) > < . . . *variable* < (*options*) > > < / *global-options* > **;**

The VAR statement names the analysis variables to be imputed. The analysis variables can be either character or numeric. The categorical variables in the VAR statement, which can be either character or numeric, must also be specified in the CLASS statement. Only variables that you specify in the VAR statement are imputed. If you specify METHOD=FEFI or METHOD=FHDI, then you must also specify a CLEVELS= or CLEVVAR= option for all numeric variables that are not specified in the CLASS statement.

A *variable* in the VAR statement should not appear in any of the BY, CLUSTER, REPWEIGHTS, STRATA, and WEIGHT statements.

You can specify the following *global-options* or *options* in the VAR statement:

CLEVELS=*k*
specifies the number of levels by which to categorize numeric variables that are in the VAR statement but not in the CLASS statement. The procedure divides the range of these variables into *k* equally spaced bins. You can specify the CLEVELS= option either as a *global-option* or as an individual *option*.

CLEVVAR=*variable*
specifies a variable that contains the bins for a numeric variable that is specified in the VAR statement but not in the CLASS statement. Both the CLEVVAR= *variable* and the numeric variable to which the CLEVVAR=*variable* applies to should have the same missing values.

WEIGHT Statement

WEIGHT *variable* **;**

The WEIGHT statement names the variable that contains the sampling weights. This variable must be numeric, and the sampling weights must be positive numbers. If an observation has a weight that is nonpositive or missing, then PROC SURVEYIMPUTE omits that observation from the analysis. For more information, see the section "Missing Values" on page 9606.

If you do not use a WEIGHT statement but you provide replicate weights in a REPWEIGHTS statement, PROC SURVEYIMPUTE uses the average of each observation's replicate weights as the observation's weight.

If you use neither a WEIGHT statement nor a REPWEIGHTS statement, PROC SURVEYIMPUTE assigns all observations a weight of 1.

Details: SURVEYIMPUTE Procedure

Definitions

The following definitions are used in this chapter:

- *Analysis variables:* The variables whose missing values are imputed. These variables are specified in the VAR statement.
- *Augmented (output) data:* The data set that contains both observed data and imputed data.
- *Auxiliary variables:* The variables that are used to impute other variables. Missing values in the auxiliary variables are not imputed. Auxiliary variables are specified in the IMPJOINT statement or CELLS statement, but not in the VAR statement.
- *Discretized variable:* The variable that contains the discretized levels of a continuous variable. These levels are used as imputation bins for the continuous variable. See also *imputation bins*.
- *Donor cell:* The collection of donor units that have the same observed levels for all items. Donor cells that have the same observed levels as the observed levels for the nonmissing items in a recipient unit are used to impute the missing values in that recipient unit.
- *Donor unit:* The observation unit that provides a value for imputation.
- *Fractional replicate weight:* The fraction of weight that a donor cell contributes to the recipient unit in a replicate sample. Fractional replicate weights are proportions that lie between 0 and 1.
- *Fractional weight:* The fraction of weight that a donor cell contributes to the recipient unit. Fractional weights are proportions that lie between 0 and 1.
- *Fully efficient fractional weight:* The fractional weight from the fully efficient fractional imputation.
- *Imputation-adjusted replicate weight:* The fraction of the recipient weight that a donor cell contributes to the recipient unit in a replicate sample.
- *Imputation-adjusted weight:* The fraction of the recipient weight that a donor cell contributes to the recipient unit.
- *Imputation bins:* A partition of the range of observed values for a continuous variable on which the first-stage imputation is applied. See also *discretized variables*.
- *Imputation cell:* A partition of the input data within which imputation is performed independently.
- *Observation row:* The same as the *observation unit* for observation units that have no missing values. Otherwise, an observation row is one realization of imputed values. Each row in the output data set represents one observation row.
- *Observation unit:* "An object on which a measurement is taken." (Lohr 2010).
- *Recipient unit:* The *observation unit* that contains missing values.

- *Sampling unit:* An object that can be selected in a sample. Probabilities of selection are assigned to the sampling units.
- *Set of donor cells:* The set of all possible configurations (vectors of observed values) that a particular observation unit that has missing items can take for a particular imputation model. Each configuration represents a donor cell. See also *donor cells*.

Specifying the Sample Design

PROC SURVEYIMPUTE produces replicate weights that are based on the sample design that is used to collect the survey data. You can use PROC SURVEYIMPUTE for single-stage or multistage designs, with or without stratification, and with or without unequal weighting. To create imputation-adjusted replicate weights for your survey data, you need to provide sample design information to PROC SURVEYIMPUTE. This information can include design (or variance) strata, clusters, and sampling weights. You provide sample design information by specifying the STRATA, CLUSTER, WEIGHT, and REPWEIGHTS statements and the RATE= or TOTAL= option in the PROC SURVEYIMPUTE statement.

If you use the REPWEIGHTS statement to provide replicate weights, you do not need to use a STRATA or CLUSTER statement. Otherwise, you should use STRATA and CLUSTER statements whenever your design includes stratification and clustering. If your design includes unequal sampling weights, you should use the WEIGHT statement.

For a multistage sample design, PROC SURVEYIMPUTE uses only the first stage of the sample design to create replicate weights. Therefore, the required input includes only the first-stage cluster (PSU) identification and first-stage stratum identification. You do not need to input design information about any additional stages of sampling.

Stratification

If your sample design is stratified at the first stage of sampling, use the STRATA statement to name the variables that form the strata. The combinations of categories of STRATA variables define the strata in the sample, where strata are nonoverlapping subgroups that were sampled independently. If your sample design has stratification at multiple stages, then identify only the first-stage strata in the STRATA statement.

If you use a REPWEIGHTS statement to provide replicate weights, you do not need to use a STRATA statement. Otherwise, you should use a STRATA statement whenever your design includes stratification. If you do not use a STRATA statement or a REPWEIGHTS statement, then PROC SURVEYIMPUTE assumes there is no stratification at the first stage; that is, the procedure assumes that all observation units are in the same stratum.

Clustering

If your sample design selects clusters at the first stage of sampling, use the CLUSTER statement to name the variables that identify the first-stage clusters, which are also called primary sampling units (PSUs). The combinations of categories of CLUSTER variables define the clusters in the sample. If there is a STRATA statement, clusters are nested within strata. If your sample design has clustering at multiple stages, you should specify only the first-stage clusters (PSUs) in the CLUSTER statement. PROC SURVEYIMPUTE assumes that each cluster that is defined by the variables in the CLUSTER statement represents a PSU in the sample.

If you use a REPWEIGHTS statement to provide replicate weights, you do not need to use a CLUSTER statement. Otherwise, you should use a CLUSTER statement whenever your design includes clustering at the first stage of sampling. If you do not use a CLUSTER statement, then PROC SURVEYIMPUTE treats each observation as a PSU.

Weighting

If your sample design includes unequal weighting, use the WEIGHT statement to name the variable that contains the sampling weights. Sampling weights must be positive numbers. If an observation has a weight that is nonpositive or missing, then PROC SURVEYIMPUTE omits that observation from the analysis. For more information, see the section "Missing Values" on page 9606.

If you do not use a WEIGHT statement but you include a REPWEIGHTS statement, PROC SURVEYIMPUTE uses the average of each observation's replicate weights as the observation's weight. If you use neither a WEIGHT statement nor a REPWEIGHTS statement, PROC SURVEYIMPUTE assumes that all observations have a weight of 1.

Population Totals and Sampling Rates

To include a finite population correction (*fpc*) in the bootstrap replicate weights, you can specify either the sampling rate or the population total by using the RATE= or TOTAL= option, respectively, in the PROC SURVEYIMPUTE statement. You cannot specify both of these options in the same PROC SURVEYIMPUTE statement. The procedure does not use a finite population correction for BRR or jackknife variance estimation.

If you do not specify the RATE= or TOTAL= option, the bootstrap replicate weights do not include a finite population correction. For fairly small sampling fractions, this correction is often ignored. For more information, see Cochran (1977) and Kish (1965).

If your design has multiple stages of selection and you are specifying the RATE= option, you should use the first-stage sampling rate, which is the ratio of the number of PSUs in the sample to the total number of PSUs in the population. If you are specifying the TOTAL= option for a multistage design, you should use the total number of PSUs in the population.

For a nonstratified sample design, or for a stratified sample design that has the same sampling rate or same population total in all strata, you can use the RATE=*value* or TOTAL=*value* option. If your sample design is stratified with different sampling rates or population totals in different strata, use the RATE=*SAS-data-set* or TOTAL=*SAS-data-set* option to name a SAS data set that contains the stratum sampling rates or totals. This data set is called a *secondary data set*, as opposed to the *primary data set* that you specify by using the DATA= option.

The secondary data set must contain all the stratification variables that are listed in the STRATA statement and all the variables in the BY statement. Furthermore, the BY groups must appear in the same order as in the primary data set. If there are formats associated with the STRATA variables and BY variables, then the formats must be consistent in the primary and secondary data sets. If you specify the TOTAL=*SAS-data-set* option, the secondary data set must have a variable named _TOTAL_ that contains the stratum population totals. If you specify the RATE=*SAS-data-set* option, the secondary data set must have a variable named _RATE_ that contains the stratum sampling rates. If the secondary data set contains more than one observation for any one stratum, the procedure uses the first value of _TOTAL_ or _RATE_ for that stratum and ignores the rest.

The *value* in the RATE= option or the values of _RATE_ in the secondary data set must be nonnegative numbers. You can specify *value* as a number between 0 and 1. Or you can specify *value* in percentage form

as a number between 1 and 100, and PROC SURVEYIMPUTE converts that number to a proportion. The procedure treats the value 1 as 100% instead of 1%.

If you specify the TOTAL=*value* option, *value* must not be less than the sample size. If you provide stratum population totals in a secondary data set, these values must not be less than the corresponding stratum sample sizes.

Replicate Weights

If you have replicate weights available for your survey data, use the REPWEIGHTS statement to name the variables that contain the replicate weights. Replicate weights must be positive numbers. If an observation has a replicate weight that is nonpositive or missing, then PROC SURVEYIMPUTE does not perform any imputation. For more information, see the section "Missing Values" on page 9606.

Missing Values

You might have missing values in your data set for several reasons. Some common reasons are data entry error, ineligible items or units, and nonresponse. You should complete your data preparation (identify data entry error or ineligibility) and adjustment (fill in deterministic values or edits) before using the SURVEYIMPUTE procedure. Use PROC SURVEYIMPUTE to impute missing values that arise only from nonresponse. If you have observations that have missing values in variables that are not specified in the VAR statement, then the procedure does not impute those observations. The following subsections describe how PROC SURVEYIMPUTE treats missing values in the variables that are specified in some statements.

WEIGHT Statement Variable

If an observation has a missing value or a nonpositive value for the variable in the WEIGHT statement, then PROC SURVEYIMPUTE excludes that observation from the analysis. However, if you use the OUTPUT statement, the observation is included in the output data set.

REPWEIGHTS Statement Variables

If you provide replicate weights by using a REPWEIGHTS statement, the values for all variables in that statement must be nonmissing and nonnegative. PROC SURVEYIMPUTE does not perform the analysis when any replicate weight value is missing or nonpositive.

Variables in the CLUSTER and STRATA Statements

An observation is excluded from the analysis if it has a missing value for any variable in a CLUSTER or STRATA statement. However, if you use the OUTPUT statement, the observation is included in the output data set.

Variables in the CELLS Statement

An observation is excluded from the imputation if it has a missing value for any variable in the CELLS statement. However, if you specify the VARMETHOD=JK option in the PROC SURVEYIMPUTE statement, then the observation unit is used to create replicate weights, unless the observation unit has missing values in any of the variables in the STRATA, CLUSTER, or WEIGHT statement. If you use the OUTPUT statement, the observation is also included in the output data set.

Auxiliary Variables in the IMPJOINT Statement

Variables that you specify in the IMPJOINT statement but do not specify in the VAR statement are used as auxiliary variables in the imputation. If you have missing values in the auxiliary variables, then that observation unit is not used in the imputation. However, if you specify the VARMETHOD=JK option in the PROC SURVEYIMPUTE statement, then the observation unit is used to create replicate weights, unless the observation unit has missing values in any of the variables in the STRATA, CLUSTER, or WEIGHT statement. If you use the OUTPUT statement, the observation unit is also included in the output data set.

Variable in the ID Statement

If an observation unit has a missing value for the variable in the ID statement, then that observation is used in the imputation unless it also has missing values for variables in the STRATA, CLUSTER, or WEIGHT or CELLS statement. If the observation is selected as a donor unit for a recipient unit, then the donor identification for that recipient unit will also be missing.

Missing Data Patterns

The SURVEYIMPUTE procedure displays the missing data patterns in groups in a "Missing Data Patterns" table; the groups are based on whether the analysis variables are observed or missing. The input data set does not need to be sorted in any order.

For example, when a data set contains variables Z_1, Z_2, and Z_3 (in that order), up to eight groups of observations can be formed from the data set. Figure 116.7 displays the eight groups of observations and an unique missing pattern for each group.

Figure 116.7 Missing Data Patterns

Missing Data Patterns

Group	Z1	Z2	Z3
1	X	X	X
2	X	X	.
3	X	.	X
4	X	.	.
5	.	X	X
6	.	X	.
7	.	.	X
8	.	.	.

An "X" in Figure 116.7 means that the variable is observed, and a "." means that the variable is missing.

The order of the groups is determined by the order in which you list the variables in the VAR statement. If you specify a different order of variables in the VAR statement, then the results are different even if the other specifications remain the same.

Random Number Generation

The donor selection methods available in PROC SURVEYIMPUTE use random numbers in their selection algorithms. PROC SURVEYIMPUTE uses a uniform random number function to generate streams of pseudorandom numbers from an initial starting point, or seed. You can use the SEED= option to specify the initial seed. You can specify the same SEED= value (along with the same options and the same input data) to reproduce the imputation. If you do not specify the SEED= option, PROC SURVEYIMPUTE uses the time of day from the computer's clock to obtain the initial seed. For information about specifying the initial seed, see the SEED= option.

PROC SURVEYIMPUTE uses the Mersenne twister random number generator. The Mersenne twister generator (Matsumoto and Nishimura 1998) has a very long period ($2^{19937}-1$) and good statistical properties. The algorithm is a twisted generalized feedback shift register. This is the same random number generator that PROC SURVEYSELECT uses by default and that the RAND function provides for the uniform distribution. For more information, see *SAS Functions and CALL Routines: Reference*.

Fully Efficient Fractional Imputation

The fully efficient fractional imputation (FEFI) method uses multiple donor units for a recipient unit. The observation unit that contains the missing values is known as the recipient unit, and the observation unit that provides the value for imputation is known as the donor unit. The number of donor units for a recipient unit is equal to the number of observed levels for the missing items, given the observed levels for the nonmissing items of the recipient unit. Each donor donates a fraction of the original weight of the recipient unit such that the sum of the fractional weights from all the donors is equal to the original weight of the recipient. The fraction of the recipient weight that a donor unit contributes to the recipient unit is known as the *fractional weight*. The method is called fully efficient because it does not introduce additional variability that is caused by the selection of donor units (Kim and Fuller 2004). One disadvantage of the FEFI method is that it can greatly increase the size of the imputed data set. For more information, see Kalton and Kish (1984), Fuller (2009, Section 5.2.2), and Kim and Shao (2014, Section 4.6).

FEFI Algorithm

Suppose you want to impute P items jointly (by using the IMPJOINT statement in PROC SURVEYIMPUTE). Let $\mathbf{Z}_i = (Z_{i1}, \ldots, Z_{iP})$ be the true response for the P items for unit i. $\mathbf{Z}_i$ is completely known if all P items are observed for unit i. However, the true response might not be known for some units because of item nonresponse. Let Z_{ij} be categorical and have J levels for item j. Denote $\mathbf{Z}_{i,\text{obs}}$ as the observed part and $\mathbf{Z}_{i,\text{miss}}$ as the missing part of $\mathbf{Z}_i$. Let $\pi(\kappa_1\kappa_2\cdots\kappa_P)$ be the population proportion that falls in category $(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2, \cdots, Z_{iP} = \kappa_P)$. Assume that it is possible to estimate the population proportion from the observed sample. That is, for example, the conditional probability, $P(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2 | Z_{i3} = \kappa_3, \ldots, Z_{iP} = \kappa_p)$, in the observed data is the same as the conditional probability in the data where $(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2)$ are missing. The conditional probabilities are estimated by

$$\hat{P}(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2 | Z_{i3} = \kappa_3, \ldots, Z_{iP} = \kappa_p) = \left\{ \sum_{\kappa_1\kappa_2} \hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P) \right\}^{-1} \hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P)$$

where

$$\hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P) = \left\{\sum_i w_i\right\}^{-1} \sum_i w_i I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

is the estimated joint probability, $I(.)$ is an indicator function, and w_i is the observation weight for unit i.

The FEFI method uses an EM-by-weighting algorithm similar to that of Ibrahim (1990). The detailed algorithm is described in Kim and Fuller (2013). The following steps describe the imputation technique. If you do not specify imputation cells by using the CELLS statement, PROC SURVEYIMPUTE uses the entire data set as one imputation cell. If you specify imputation cells, then all the probabilities in these steps are computed by using observations from the same imputation cell as the recipient unit. To simplify notation, subscripts are not used for imputation cells in the following description.

For given i, let $\mathbf{Z}_{i,\text{obs}}$ and $\mathbf{Z}_{i,\text{miss}}$ be the observed part and the missing part, respectively, of unit i. Let $\mathcal{A}_c$ be the index set for the complete respondents. Suppose you want to impute the missing part of $\mathbf{Z}_i$, $\mathbf{Z}_{i,\text{miss}}$. The index set $d_i = \{k : k \in \mathcal{A}_c \wedge \mathbf{Z}_{k,\text{obs}} = \mathbf{Z}_{i,\text{obs}}\}$ contains the indexes for the all possible donor units for $\mathbf{Z}_i$. Let $l = 1, 2, \ldots, M_l$ be all the observed combinations of $\{\mathbf{Z}_{k,\text{miss}} : k \in d_i\}$. The set of all observed combinations for unit i defines the donor cells (all possible realizations) for unit i. Let $\mathbf{Z}_{i,\text{miss}[l]}$ be the lth imputed value of $\mathbf{Z}_{i,\text{miss}}$. You must assume that at least one imputed value is available; otherwise the observation is not imputed.

1. *Initialization:* For each observation that has missing items, determine the number of donor cells by using the number of unique combinations of observed levels for the missing items for the responding units in the imputation cell. Compute the initial fractional weight from donor cell l to unit i, $w_{il(0)}$, by

   $$w_{il(0)} = \left\{\sum_{k=1}^{M_l} \tilde{\pi}_{(0)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[k]})\right\}^{-1} \tilde{\pi}_{(0)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[l]})$$

   where $l = 1, 2, \ldots, M_l$ is the number of donor cells and

   $$\tilde{\pi}_{(0)}(\kappa_1\cdots\kappa_P) = \left\{\sum_{i\in\mathcal{A}_c} w_i\right\}^{-1} \sum_{i\in\mathcal{A}_c} w_i I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

   The sum of the fractional weights over all the donor cells is 1 for every observation unit; that is, $\sum_l w_{il(0)} = 1$, for all i. The lth imputed row for unit i is created by keeping the observed items unchanged, replacing the missing items with the observed levels from the lth donor cell, and computing the fractional weight by $w_i w_{il(0)}$. Only the complete respondents are used to compute the fractional weights in this step. If unit i has no missing items, then $w_{i1(0)} = 1$. The initial FEFI data set contains all the observed units, the imputed rows for observation that had missing items, and the corresponding fractional weights.

2. *M-step:* The tth M-step computes the joint probabilities by using the fractional weights from the (t–1)th E-step,

   $$\tilde{\pi}_{(t)}(\kappa_1\cdots\kappa_P) = \left\{\sum_i\sum_l w_i w_{il(t-1)}\right\}^{-1} \sum_i\sum_l w_i w_{il(t-1)} I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

   for all i, all l, and $t > 0$. Note that for $t > 0$, $\tilde{\pi}_{(t)}$ uses all observation units, including observations where missing items are imputed in the initialization step.

3. *E-step:* The tth E-step computes the fractional weights by using the joint probabilities $\tilde{\pi}_{(t)}(\kappa_1 \cdots \kappa_P)$ from the tth M-step. The tth fractional weight for unit i and donor cell l is given by

$$w_{il(t)} = \left\{ \sum_{k=1}^{M_l} \tilde{\pi}_{(t)}(\mathbf{Z}_{i,\mathrm{obs}}, \mathbf{Z}_{i,\mathrm{miss}[k]}) \right\}^{-1} \tilde{\pi}_{(t)}(\mathbf{Z}_{i,\mathrm{obs}}, \mathbf{Z}_{i,\mathrm{miss}[l]})$$

4. *Repetition:* The EM-steps are repeated for $t = 1, 2, \ldots,$ until the changes in fractional weights over all observation units between two successive EM-steps are negligible or the maximum number of EM repetitions is reached.

   The maximum absolute difference convergence criterion, ϵ_{AD}, at step t is defined as

$$\max_{i,l} |w_{il(t)} - w_{il(t-1)}| \leq \epsilon_{\mathrm{AD}}$$

   The maximum absolute relative difference convergence criterion, ϵ_{RD}, at step t is defined as

$$\max_{i,l} |w_{il(t)} - w_{il(t-1)}| / w_{il(t-1)} \leq \epsilon_{\mathrm{RD}}$$

   where $w_{il(t-1)} > 0$.

The replicate weights are created by computing a replicated version of $\tilde{\pi}_{(t)}(\kappa_1\kappa_2 \cdots \kappa_p)$, $\tilde{\pi}^{(k)}_{(t)}(\kappa_1\kappa_2 \cdots \kappa_p)$, and by repeating the EM-by-weighting algorithm as described earlier. For the kth replicate sample, $\tilde{\pi}^{(k)}_{(t)}(\kappa_1\kappa_2 \cdots \kappa_p)$ is computed by

$$\tilde{\pi}^{(k)}_{(t)}(\kappa_1 \cdots \kappa_P) = \left\{ \sum_i \sum_l w_i^{(k)} w_{il(t-1)}^{(k)} \right\}^{-1} \sum_i \sum_l w_i^{(k)} w_{il(t-1)}^{(k)} I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

Example of FEFI

The small data set shown in Figure 116.8 is used to illustrate the imputation technique. The data set contains nine observation units, and each unit has two items (X and Y). The variable Unit contains the observation identification. In this example, X is missing for units 5 and 9, and Y is missing for units 2 and 9.

Figure 116.8 Sample Data with Missing Items

Unit	X	Y
1	0	0
2	0	.
3	0	1
4	0	0
5	.	1
6	1	0
7	1	1
8	1	1
9	.	.

The following SAS statements request joint imputation of X and Y by using the FEFI method. These statements also request imputation-adjusted replicate weights for the jackknife replication method. The CLASS statement specifies that both X and Y are CLASS variables. The OUTPUT statement stores the imputed values in the data set Imputed and stores the jackknife coefficients in the data set Ojkc. The FRACTIONALWEIGHTS= option in the OUTPUT statement saves the fractional weights in the Imputed data set.

```
proc surveyimpute data=test varmethod=jackknife;
   class x y;
   var x y;
   id Unit;
   output out=Imputed fractionalweights=FracWgt outjkcoefs=Ojkc;
run;
```

The initial fractional weights, FracWgt, after the initialization step are displayed in Figure 116.9.

- Observation unit 1 has no missing value. Therefore, the ImpIndex value is 0, the FracWgt value is 1, and the values of X and Y are the same as the observed values for observation unit 1 in Figure 116.9. Because all observation units have a weight of 1, the fractional weights, FracWgt, and the imputation-adjusted weights, ImpWt, are the same for all rows.

- Observation unit 2 has a missing Y. The observed level for X for unit 2 is 0. For X = 0, two levels for Y are observed: Y = 0, which has a proportion (FracWgt) of 0.67, and Y = 1, which has a proportion of 0.33. Therefore, observation unit 2 receives two donor cells (ImpIndex = 1 and ImpIndex = 2), whose initial fractional weights are 0.67 and 0.33, respectively. Because X is observed, the X values in both rows for unit 2 are the same as the observed value. However, the first recipient row for unit 2 has an imputed Y value of 0, the second recipient row for unit 2 has an imputed Y value of 1, and each has a corresponding initial fractional weight.

- Observation unit 5 has a missing X. The observed level for Y for unit 5 is 1. To impute X, note that two levels of X are observed when Y = 1: X = 0 with a proportion of 0.33 and X = 1 with a proportion of 0.67. The two recipient rows for observation unit 5 contain the initial fractional weights in the FracWgt column and the imputed X values.

- Observation unit 9 has missing values for both X and Y. From the observed data, X and Y can take the following values: (X = 0, Y = 0) with probability 0.33, (X = 0, Y = 1) with probability 0.17, (X = 1, Y = 0) with probability 0.17, and (X = 1, Y = 1) with probability 0.33. The four imputed rows (ImpIndex 1, ImpIndex 2, ImpIndex 3, and ImpIndex 4) for observation unit 9 represent the four observed combinations for X and Y along with their initial fractional weights.

The resulting data set contains 14 rows. There are six rows for fully observed units (ImpIndex = 0), two rows for unit 2, two rows for unit 5, and four rows for unit 9. The sum of initial fractional weights is 1 for all units.

Figure 116.9 Fractional Imputation after Initialization

Unit	ImpIndex	ImpWt	FracWgt	X	Y
1	0	1.00000	1.00000	0	0
2	1	0.66667	0.66667	0	0
2	2	0.33333	0.33333	0	1
3	0	1.00000	1.00000	0	1
4	0	1.00000	1.00000	0	0
5	1	0.33333	0.33333	0	1
5	2	0.66667	0.66667	1	1
6	0	1.00000	1.00000	1	0
7	0	1.00000	1.00000	1	1
8	0	1.00000	1.00000	1	1
9	1	0.33333	0.33333	0	0
9	2	0.16667	0.16667	0	1
9	3	0.16667	0.16667	1	0
9	4	0.33333	0.33333	1	1

The EM algorithm repeats the computation of the joint probabilities and the fractional weights until convergence. The fractional weights, FracWgt, after the EM step and the imputation-adjusted replicate weights (ImpRepWt_1, . . . , ImpRepWt_9) are displayed in Figure 116.10.

Figure 116.10 Fractional Imputation after the EM

Unit	ImpIndex	ImpWt	FracWgt	X	Y	ImpRepWt_1	ImpRepWt_2	ImpRepWt_3	ImpRepWt_4
1	0	1.00000	1.00000	0	0	0.00000	1.12500	1.12500	1.12500
2	1	0.58601	0.58601	0	0	0.46072	0.00000	1.12498	0.46072
2	2	0.41399	0.41399	0	1	0.66428	0.00000	0.00002	0.66428
3	0	1.00000	1.00000	0	1	1.12500	1.12500	0.00000	1.12500
4	0	1.00000	1.00000	0	0	1.12500	1.12500	1.12500	0.00000
5	1	0.41399	0.41399	0	1	0.49821	0.37510	0.00002	0.49821
5	2	0.58601	0.58601	1	1	0.62679	0.74990	1.12498	0.62679
6	0	1.00000	1.00000	1	0	1.12500	1.12500	1.12500	1.12500
7	0	1.00000	1.00000	1	1	1.12500	1.12500	1.12500	1.12500
8	0	1.00000	1.00000	1	1	1.12500	1.12500	1.12500	1.12500
9	1	0.32330	0.32330	0	0	0.22659	0.32143	0.48214	0.22659
9	2	0.22840	0.22840	0	1	0.32669	0.21434	0.00001	0.32669
9	3	0.12500	0.12500	1	0	0.16071	0.16071	0.16071	0.16071
9	4	0.32330	0.32330	1	1	0.41101	0.42851	0.48214	0.41101

ImpRepWt_5	ImpRepWt_6	ImpRepWt_7	ImpRepWt_8	ImpRepWt_9
1.12500	1.12500	1.12500	1.12500	1.12500
0.75009	0.65906	0.62682	0.62682	0.65877
0.37491	0.46594	0.49818	0.49818	0.46623
1.12500	1.12500	1.12500	1.12500	1.12500
1.12500	1.12500	1.12500	1.12500	1.12500
0.00000	0.46601	0.66443	0.66443	0.46623
0.00000	0.65899	0.46057	0.46057	0.65877
1.12500	0.00000	1.12500	1.12500	1.12500
1.12500	1.12500	0.00000	1.12500	1.12500
1.12500	1.12500	1.12500	0.00000	1.12500
0.42862	0.41563	0.41109	0.41109	0.00000
0.21424	0.29384	0.32672	0.32672	0.00000
0.16071	0.00000	0.16071	0.16071	0.00000
0.32143	0.41553	0.22648	0.22648	0.00000

Two-Stage Fully Efficient Fractional Imputation

The two-stage fully efficient fractional imputation method uses multiple donor units for a recipient unit. Each donor donates a fraction of the original weight of the recipient unit such that the sum of the fractional weights from all the donors is equal to the original weight of the recipient. The fraction of the recipient weight that a donor unit contributes to the recipient unit is known as the *fractional weight*. The method is called fully efficient because it does not introduce additional variability that is caused by the selection of donor units (Kim and Fuller 2004). Two-stage FEFI has two hierarchical imputation stages. One disadvantage of the two-stage FEFI method is that it can greatly increase the size of the imputed data set.

Two-stage FEFI is useful when you want to impute variables that have many unique observed values. FEFI creates many imputed rows if the variable that you are imputing has many unique observed values. Two-stage FEFI imputes these variables conditional on the imputed levels from the first-stage FEFI. Thus, two-stage FEFI often uses fewer imputed rows compared to a similar first-stage FEFI.

Variables that have many observed levels are grouped into imputation bins. The first-stage imputation is performed for all categorical variables by using the FEFI method. The categorical variables include the character variables, the CLASS variables that you also specify in the VAR statement, and the variables that contain the imputation bins of the continuous variables.

The second-stage imputation is performed for the continuous variables within each first-stage donor cell. Observations that contain missing values in any of the continuous items are the recipients, and observations that contain observed values for these missing items are the donors. The second-stage donor cells are defined by the unique combinations of the observed values for the continuous variables within the first-stage donor cells.

Imputation-adjusted replicate weights are computed by repeating both the first-stage and second-stage imputation in every replicate sample independently.

The method is similar to Im, Kim, and Fuller (2015).

Two-Stage FEFI Algorithm

Suppose you want to impute P items jointly. Let $\mathbf{X}_i = (X_{i1}, \ldots, X_{iP_1})$ be the response for P_1 items in unit i, and let $\mathbf{Y}_i = (Y_{i1}, \ldots, Y_{iP_2})$ be the response for P_2 items in unit i, where $P = P_1 + P_2$. Let X_{ij} be categorical with J levels for item j, and let Y_{ij} be continuous. Further assume that $\tilde{\mathbf{Y}} = (\tilde{Y}_{i1}, \ldots, \tilde{Y}_{iP_2})$ contains the discretized levels (imputation bins) for Y, where $\tilde{Y}_{ij}$ has J levels. Define $Z_{ij} = (X_{ij}, \tilde{Y}_{ij})$. Then Z_{ij} is categorical and has J levels for item j. Denote $\mathbf{Z}_{i,\text{obs}}$ as the observed part and $\mathbf{Z}_{i,\text{miss}}$ as the missing part of $\mathbf{Z}_i$.

Let $\pi(\kappa_1\kappa_2\cdots\kappa_P)$ be the population proportion that falls in category $\kappa_1\kappa_2\cdots\kappa_P$. Assume that it is possible to estimate the population categories from the observed sample. For example, the conditional probability, $P(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2 | Z_{i3} = \kappa_3, \ldots, Z_{iP} = \kappa_p)$, is the same for the observed data as it is for the data where $(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2)$ are missing. The initial conditional probabilities are estimated by

$$\hat{P}(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2 | Z_{i3} = \kappa_3, \ldots, Z_{iP} = \kappa_p) = \left\{ \sum_{\kappa_1\kappa_2} \hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P) \right\}^{-1} \hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P)$$

where

$$\hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P) = \left\{ \sum_i w_i \right\}^{-1} \sum_i w_i I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

is the estimated joint probability, $I(.)$ is an indicator function, and w_i is the observation weight for unit i.

Let $l = 1, 2, \ldots, M_{il_1}$ be all the observed combinations of $\mathbf{Z}_{k:k\notin i,\text{miss}}$ in the sample. Let $\mathbf{Z}_{i,\text{miss}[l]}$ be the lth realization of $\mathbf{Z}_{i,\text{miss}}$ in the sample. You must assume that at least one realization is available; otherwise, the observation is not imputed.

The two-stage FEFI method first computes the fully efficient fractional weights by using an EM-by-weighting algorithm like that of Kim and Fuller (2013) to impute the missing values in $\mathbf{Z}_i$. The missing values in $\mathbf{Y}_i$ are imputed in the second-stage imputation. Two-stage FEFI weights for imputing $\mathbf{Y}_i$ are computed independently in every imputed level of $\mathbf{Z}_{i,\text{miss}[l]}$, where $l = 1, \ldots, M_{l_1}$ is the number of first-stage donor cells.

The following steps describe the two-stage FEFI technique. If you do not use the CELL statement to specify imputation cells, PROC SURVEYIMPUTE uses the entire data set as one imputation cell. If you specify

imputation cells, then all the probabilities are computed by using observations from the same imputation cell as the recipient unit. To simplify notation, subscripts are not used for imputation cells in the following description. Imputation cells are defined for the first-stage imputation. Steps 1 to 4 describe the first-stage FEFI for the categorical variables, which also include the imputation bins for the continuous variables. Step 5 describes the second-stage FEFI.

1. *Initialization*: For each observation that has missing items, determine the number of first-stage donor cells. The first-stage donor cells are determined by using the number of unique combinations of observed levels in $\mathbf{Z}_i$ for imputing the missing items in $\mathbf{Z}_i$. Only the responding units in the imputation cell are used to determine the number of first-stage donor cells. Compute the initial fractional weight from donor cell l to unit i, $w_{il(0)}$, by

$$w_{il(0)} = \left\{ \sum_{k=1}^{M_{il_1}} \tilde{\pi}_{(0)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[k]}) \right\}^{-1} \tilde{\pi}_{(0)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[l]})$$

where $l = 1, 2, \ldots, M_{l_1}$ is the number of first-stage donor cells and

$$\tilde{\pi}_{(0)}(\kappa_1, \ldots, \kappa_P) = \left\{ \sum_{i \in \mathcal{A}_c} w_i \right\}^{-1} \sum_{i \in \mathcal{A}_c} w_i I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

The sum of the fractional weights over all the donor cells is 1 for every observation unit; that is, $\sum_l w_{il(0)} = 1$ for all i. The lth imputed row for unit i is created by keeping the observed items unchanged, replacing the missing items with the observed levels from the lth donor cell, and computing the fractional weight by $w_i w_{il(0)}$. Only the complete observations (observations that have no missing items) are used to compute the fractional weights in this step. If unit i has no missing items, then $w_{i1(0)} = 1$. The initial FEFI data set contains all the observed units, the imputed rows for observations that have missing items, and the corresponding fractional weights.

2. *M-step*: The tth maximization step (M-step) computes the joint probabilities by using the fractional weights from the (t–1)th expectation-step,

$$\tilde{\pi}_{(t)}(\kappa_1, \ldots, \kappa_P) = \left\{ \sum_i \sum_l w_i w_{il(t-1)} \right\}^{-1} \sum_i \sum_l w_i w_{il(t-1)} I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

for all i, all l, and $t > 0$. Note that for $t > 0$, $\tilde{\pi}_{(t)}$ uses all observation units, including observations that have missing items that are imputed in the initialization step.

3. *E-step*: The tth expectation (E-step) computes the fractional weights by using the joint probabilities $\tilde{\pi}_{(t)}(\kappa_1, \ldots, \kappa_P)$ from the tth M-step. The tth fractional weight for unit i and donor cell l is given by

$$w_{il(t)} = \left\{ \sum_{k=1}^{M_{il_1}} \tilde{\pi}_{(t)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[k]}) \right\}^{-1} \tilde{\pi}_{(t)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[l]})$$

4. *Repetition*: The expectation maximization steps (EM-steps, steps 2 and 3) are repeated for $t = 1, 2, \ldots,$ until the changes in fractional weights over all observation units between two successive EM-steps are negligible or the maximum number of EM repetitions is reached.

The maximum absolute difference convergence criterion, ϵ_{AD}, at step t is defined as

$$\max_{i,l}|w_{il(t)} - w_{il(t-1)}| \leq \epsilon_{\mathrm{AD}}$$

The maximum absolute relative difference convergence criterion, ϵ_{RD}, at step t is defined as

$$\max_{i,l}|w_{il(t)} - w_{il(t-1)}|/w_{il(t-1)} \leq \epsilon_{\mathrm{RD}}$$

where $w_{il(t-1)} > 0$.

5. *Second-stage imputation*: The second-stage imputation replaces the missing values in the continuous variables by using the observed values within each selected first-stage donor cell. This step is similar to step 1 but is applied to impute the continuous variables.

   For a particular observation unit i, let $\mathbf{Z}_{i,\mathrm{dcell}[l_1]} = (\mathbf{Z}_{i,\mathrm{obs}}, \mathbf{Z}_{i,\mathrm{mis}[l_1]})$ be the l_1th donor cell from the first-stage imputation, where l_1 ranges from 1 to M_{l_1}. For each observation unit, i, the possible number of second-stage donor cells is equal to the number of unique combinations of the observed levels for the missing items in $\mathbf{Y}_i$ from the responding units in the first-stage donor cell l_1.

   Let $\pi_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1}\cdots\kappa_{P_2|l_1})$ be the population proportion that falls in category $\kappa_{1|l_1}\kappa_{2|l_1}\cdots\kappa_{P_2|l_1}$. Assume that it is possible to estimate the population categories from the observed sample. For example, the conditional probability, $P(Y_{i1|l_1} = \kappa_{1|l_1}, Y_{i2|l_1} = \kappa_{2|l_1}|Y_{i3|l_1} = \kappa_{3|l_1}, \ldots, Y_{iP_2|l_1} = \kappa_{P_2|l_1})$, is the same for the observed data as it is for the data in which $(Y_{i1|l_1} = \kappa_{1|l_1}, Y_{i2|l_1} = \kappa_{2|l_1})$ are missing. The conditional probabilities are estimated by

$$\hat{P}(Y_{i1|l_1} = \kappa_{1|l_1}, Y_{i2|l_1} = \kappa_{2|l_1}|Y_{i3|l_1} = \kappa_{3|l_1}, \ldots, Y_{iP_2|l_1} = \kappa_{P_2|l_1}) = \left\{\sum_{\kappa_{1|l_1}\kappa_{2|l_1}} \hat{\pi}_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1}\cdots\kappa_{P_2|l_1})\right\}^{-1} \hat{\pi}_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1}\cdots\kappa_{P_2|l_1})$$

   where

$$\hat{\pi}_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1}\cdots\kappa_{P_2|l_1}) = \left\{\sum_{i\in\mathbf{Z}_{i,\mathrm{dcell}[l_1]}} w_i\right\}^{-1} \sum_{i\in\mathbf{Z}_{i,\mathrm{dcell}[l_1]}} w_i I(Y_{i1|l_1} = \kappa_{1|l_1}, \ldots, Y_{iP_2|l_1} = \kappa_{P_2|l_1})$$

   is the estimated joint probability, $I(.)$ is an indicator function, and w_i is the observation weight for unit i.

   Let $l = 1, 2, \ldots, M_{il_2|l_1}$ be all the observed combinations of $\mathbf{Y}_{k:k\in\mathbf{Z}_{i,\mathrm{dcell}[l_1]},k\neq i,\mathrm{miss}}$ in the sample. Let $\mathbf{Y}_{i,\mathrm{miss}[l]}$ be the lth realization of $\mathbf{Y}_{i,\mathrm{miss}}$ in the sample. You must assume that at least one realization is available; otherwise, missing values in the continuous items for the observation are not imputed.

   Compute the second-stage fractional weight from the second-stage donor cell l_2 conditional on the first-stage donor cell l_1 for unit i, $w_{il_2|l_1}$:

$$w_{il_2|l_1} = \left\{\sum_{k=1}^{M_{il_2|l_1}} \tilde{\pi}_{2|l_1}(\mathbf{Y}_{i,\mathrm{obs}}, \mathbf{Y}_{i,\mathrm{miss}[k]})\right\}^{-1} \tilde{\pi}_{2|l_1}(\mathbf{Y}_{i,\mathrm{obs}}, \mathbf{Y}_{i,\mathrm{miss}[l_2]})$$

   where $l = 1, 2, \ldots, M_{il_2|l_1}$ is the number of second-stage donor cells and

$$\tilde{\pi}_{2|l_1}(\kappa_1, \ldots, \kappa_{P_2}) = \left\{\sum_{i\in\mathbf{Z}_{i,\mathrm{dcell}[l_1]}} w_i\right\}^{-1} \sum_{i\in\mathbf{Z}_{i,\mathrm{dcell}[l_1]}} w_i I(Y_{i1|l_1} = \kappa_1, \ldots, Y_{iP_2|l_1} = \kappa_{P_2})$$

The sum of the second-stage fractional weights over all second-stage donor cells is 1 for every observation unit; that is, $\sum_{l_2} w_{il_2|l_1} = 1$ for all l_1 and i. The l_2th second-stage imputed row in the l_1th first-stage imputed row for unit i is created by keeping the observed items unchanged, replacing the missing items in $\mathbf{Y}_i$ with the observed values from the l_2th second-stage donor cell, and computing the two-stage fractional weight by $w_{il_1l_2} = w_{il_1} w_{il_2|l_1}$, where w_{il_1} is the first-stage fractional weight for the first-stage donor cell l_1. The maximum number of donor cells for unit i is $M_{il_1} M_{il_2|l_1}$. Only the complete observations are used to compute the second-stage fractional weights.

The imputation-adjusted replicate weights are created by using the following:

1. The first-stage FEFI is repeated by using replicate weights in every replicate sample.
2. The second-stage replicate fractional weights for the kth replicate are computed by using the estimated joint probabilities from the kth replicate sample:

$$\hat{\pi}^{(k)}_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1}\cdots\kappa_{P_2|l_1}) = \left\{ \sum_{i\in\mathbf{Z}_{i,\mathrm{dcell}[l_1]}} w_i^{(k)} \right\}^{-1} \sum_{i\in\mathbf{Z}_{i,\mathrm{dcell}[l_1]}} w_i^{(k)} I(Y_{i1|l_1} = \kappa_{1|l_1}, \ldots, Y_{iP_2|l_1} = \kappa_{P_2|l_1})$$

where $w_i^{(k)}$ are the unadjusted replicate weights.

Example of Two-Stage FEFI

The small data set shown in Figure 116.11 is used to illustrate the imputation technique. The data set contains 18 observation units, and each unit has four items (X, CX, Y, and CY). The variable Unit contains the observation identification. Variables CX and CY contains the imputation bins for variables X and Y, respectively. In this example, X and CX are missing for units 14 and 18, and Y and CY are missing for units 5 and 18.

Figure 116.11 Sample Data with Missing Items

Unit	X	CX	Y	CY
1	0.3	0	-0.54	0
2	0.2	0	-0.77	0
3	1.7	0	-0.59	0
4	1.7	0	-0.59	0
5	1.0	0	.	.
6	1.8	0	-0.03	1
7	2.0	0	0.95	1
8	1.9	0	0.78	1
9	6.7	1	-0.15	0
10	6.0	1	-1.01	0
11	3.3	1	-1.86	0
12	7.3	1	-0.21	0
13	6.7	1	0.80	1
14	.	.	1.23	1
15	2.9	1	0.65	1
16	9.6	1	0.95	1
17	10.0	1	0.13	1
18	.	.	.	.

The following statements request joint imputation of X and Y by using the two-stage FEFI method. Two CLEVVAR= options specify variables CX and CY, which contain the imputation bins for variables X and Y, respectively. The following statements also request imputation-adjusted replicate weights for the jackknife replication method. The OUTPUT statement stores the imputed values in the Imputed data set and stores the jackknife coefficients in the OJKC data set. The FRACTIONALWEIGHTS= option in the OUTPUT statement saves the fractional weights in the Imputed data set.

```
proc surveyimpute data=Example method=fefi;
   var X (clevvar=CX) Y (clevvar=CY);
   output out=Imputed fractionalweights=FracWt outjkcoefs=OJKC;
run;
```

The first-stage FEFI imputes the imputation bin variables CX and CY by using the FEFI method. The imputed data set after the first-stage imputation is displayed in Figure 116.12. Variables X and Y are not imputed in the first-stage imputation.

Figure 116.12 First-Stage Fractional Imputation

Unit	ImpIndex	ImpWt	FracWt	X	CX	Y	CY
1	0	1.0000	1.0000	0.3	0	-0.54	0
2	0	1.0000	1.0000	0.2	0	-0.77	0
3	0	1.0000	1.0000	1.7	0	-0.59	0
4	0	1.0000	1.0000	1.7	0	-0.59	0
5	1	0.5360	0.5360	1.0	0	.	0
5	2	0.4640	0.4640	1.0	0	.	1
6	0	1.0000	1.0000	1.8	0	-0.03	1
7	0	1.0000	1.0000	2.0	0	0.95	1
8	0	1.0000	1.0000	1.9	0	0.78	1
9	0	1.0000	1.0000	6.7	1	-0.15	0
10	0	1.0000	1.0000	6.0	1	-1.01	0
11	0	1.0000	1.0000	3.3	1	-1.86	0
12	0	1.0000	1.0000	7.3	1	-0.21	0
13	0	1.0000	1.0000	6.7	1	0.80	1
14	1	0.4640	0.4640	.	0	1.23	1
14	2	0.5360	0.5360	.	1	1.23	1
15	0	1.0000	1.0000	2.9	1	0.65	1
16	0	1.0000	1.0000	9.6	1	0.95	1
17	0	1.0000	1.0000	10.0	1	0.13	1
18	1	0.2668	0.2668	.	0	.	0
18	2	0.2310	0.2310	.	0	.	1
18	3	0.2353	0.2353	.	1	.	0
18	4	0.2668	0.2668	.	1	.	1

The first-stage FEFI is described as follows:

- Observation unit 1 has no missing value. Therefore, the ImpIndex value is 0; the FracWt value is 1; and the values of X, CX, Y, and CY are the same as the observed values for observation unit 1 in Figure 116.12. Because all observation units have a weight of 1, the fractional weights (FracWt) and the imputation-adjusted weights (ImpWt) are the same for all rows.

- Observation unit 5 has missing values in Y and CY. In the first-stage, only CY is imputed conditional on the observed level of CX. The observed level for CX for observation unit 5 is 0. For CX=0, two levels for CY are observed: CY=0, and CY=1. Therefore, observation unit 5 receives two donor cells (ImpIndex=1 and ImpIndex=2). The fractional weights for these two donor cells are computed by applying FEFI on variables CX and CY. For more information about FEFI, see the section "Example of FEFI" on page 9610. The fractional weights after the first-stage imputation are 0.536 and 0.464. Because CX is observed, CX values in both rows for observation unit 5 are the same as the observed value. However, the first recipient row for observation unit 5 has an imputed CY value of 0, the second recipient row for observation unit 5 has an imputed CY value of 1, and each of these rows has a corresponding fractional weight. Because no imputation is performed for Y in the first-stage, both rows for observation unit 5 contain missing values for Y.

- Observation unit 14 has missing values in X and CX. In the first-stage, only CX is imputed conditional on the observed level of CY. The observed level of CY for unit 14 is 1. For CY=1, two levels for CX are observed: CX=0, and CX=1. Therefore, observation unit 14 receives two donor cells (ImpIndex=1 and ImpIndex=2). The fractional weights for these two donor cells are computed by applying FEFI on variables CX and CY. For more information about FEFI, see the section "Example of FEFI" on page 9610. The fractional weights after the first-stage imputation are 0.464 and 0.536. Because CY is observed, CY values in both rows for unit 14 are the same as the observed value. However, the first recipient row for unit 14 has an imputed CX value of 0, the second recipient row for unit 14 has an imputed CX value of 1, and each of these rows has a corresponding fractional weight. Because no imputation is performed for X in the first-stage, both rows for unit 14 contain missing values for X.

- Observation unit 18 has missing values in all variables X, CX, Y, and CY. Only variables CX and CY are imputed in the first-stage. From the observed data, CX and CY can take the following values (CX=0, CY=0), (CX=0, CY=1), (CX=1, CY=0), and (CX=1, CY=1). The four imputed rows (ImpIndex 1, ImpIndex 2, ImpIndex 3, and ImpIndex 4) for observation unit 18 represent the four observed combinations for CX and CY along with their fractional weights. The fractional weights for these four donor cells are computed by applying FEFI on variables CX and CY. For more information about FEFI, see the section "Example of FEFI" on page 9610.

The second-stage FEFI imputes the missing values in X and Y conditional on the imputed levels for imputation bin variables CX and CY from the first-stage imputation. The imputed data set after the second-stage imputation is displayed in Figure 116.13. Variables X and Y are imputed in the second stage.

Figure 116.13 Two-Stage Fractional Imputation

Unit	ImpIndex	ImpWt	FracWt	X	CX	Y	CY
1	0	1.0000	1.0000	0.3	0	-0.54	0
2	0	1.0000	1.0000	0.2	0	-0.77	0
3	0	1.0000	1.0000	1.7	0	-0.59	0
4	0	1.0000	1.0000	1.7	0	-0.59	0
5	1	0.1340	0.1340	1.0	0	-0.77	0
5	2	0.1340	0.1340	1.0	0	-0.54	0
5	3	0.2680	0.2680	1.0	0	-0.59	0
5	4	0.1547	0.1547	1.0	0	-0.03	1
5	5	0.1547	0.1547	1.0	0	0.78	1
5	6	0.1547	0.1547	1.0	0	0.95	1
6	0	1.0000	1.0000	1.8	0	-0.03	1
7	0	1.0000	1.0000	2.0	0	0.95	1
8	0	1.0000	1.0000	1.9	0	0.78	1
9	0	1.0000	1.0000	6.7	1	-0.15	0
10	0	1.0000	1.0000	6.0	1	-1.01	0
11	0	1.0000	1.0000	3.3	1	-1.86	0
12	0	1.0000	1.0000	7.3	1	-0.21	0
13	0	1.0000	1.0000	6.7	1	0.80	1
14	1	0.1547	0.1547	1.8	0	1.23	1
14	2	0.1547	0.1547	1.9	0	1.23	1
14	3	0.1547	0.1547	2.0	0	1.23	1
14	4	0.1340	0.1340	2.9	1	1.23	1
14	5	0.1340	0.1340	6.7	1	1.23	1
14	6	0.1340	0.1340	9.6	1	1.23	1
14	7	0.1340	0.1340	10.0	1	1.23	1
15	0	1.0000	1.0000	2.9	1	0.65	1
16	0	1.0000	1.0000	9.6	1	0.95	1
17	0	1.0000	1.0000	10.0	1	0.13	1
18	1	0.0667	0.0667	0.2	0	-0.77	0
18	2	0.0667	0.0667	0.3	0	-0.54	0
18	3	0.1334	0.1334	1.7	0	-0.59	0
18	4	0.0770	0.0770	1.8	0	-0.03	1
18	5	0.0770	0.0770	1.9	0	0.78	1
18	6	0.0770	0.0770	2.0	0	0.95	1
18	7	0.0588	0.0588	3.3	1	-1.86	0
18	8	0.0588	0.0588	6.0	1	-1.01	0
18	9	0.0588	0.0588	6.7	1	-0.15	0
18	10	0.0588	0.0588	7.3	1	-0.21	0
18	11	0.0667	0.0667	2.9	1	0.65	1
18	12	0.0667	0.0667	6.7	1	0.80	1
18	13	0.0667	0.0667	9.6	1	0.95	1
18	14	0.0667	0.0667	10.0	1	0.13	1

The second-stage FEFI is described as follows:

- Observation unit 1 has no missing value. Therefore, the ImpIndex value is 0; the FracWt value is 1; and the values of X, CX, Y, and CY are the same as the observed values for observation unit 1 in Figure 116.13. Because all observation units have a weight of 1, the fractional weights (FracWt) and the imputation-adjusted weights (ImpWt) are the same for all rows.

- Observation unit 5 has missing values in Y and CY. The variable CY has two imputed levels (0 and 1) from the first-stage imputation. The observed level of CX for observation unit 5 is 0.

  The row that contains Unit 5 and ImpIndex=1 in Figure 116.12 has CX=0 and CY=0. Units 1, 2, 3, and 4 in the complete data have CX=0 and CY=0. These units are possible donors for a missing Y when CX=0 and CY=0. The four donor units have three unique values for Y: –0.54, –0.59, and –0.77. These three unique values define three donor cells to impute Y when CX=0 and CY=0. The missing value in Y for CX=0 and CY=0 is replaced by all three possible observed values. Because the weight for the donor cell that is defined by Y=–0.59 is double the weight for the other two donor cells, the imputed row that contains Y = –0.59 is assigned a second-stage fractional weight of 1/2 and the other two rows are each assigned a second-stage fractional weight of 1/4. The second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.54) for CX=0, CY=0, and ImpIndex=1 to obtain the two-stage FEFI weight.

  The row that contains Unit 5 and ImpIndex=2 in Figure 116.12 has CX=0 and CY=1. Units 6, 7, and 8 in the complete data have CX=0 and CY=1. These units are donors for missing Y when CX=0 and CY=1. The three donor units have three unique values for Y: –0.03, 0.95, and 0.78. These three unique values define three donor cells for imputing Y when CX=0 and CY=1. The missing value in Y for CX=0 and CY=1 is replaced by all three possible observed values. Because all three donor cells have equal weights, all three imputed rows are assigned a second-stage fractional weight of 1/3. The second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.46) for CX=0, CY=1, and ImpIndex=2 to obtain the two-stage FEFI weight.

  Therefore, after two-stage FEFI, missing values in Y are replaced by six imputed values that have fractional weights proportional to the observed weighted frequencies of the second-stage donor cells conditional on the first-stage FEFI.

- Observation unit 14 has missing values in X and CX. The variable CX has two imputed levels (0 and 1) from the first-stage imputation. The observed level for CY for unit 14 is 1.

  The row that contains Unit 14 and ImpIndex=1 in Figure 116.12 has CX=0 and CY=1. Units 6, 7, and 8 in the complete data have CX=0 and CY=1. These units are possible donors for missing X when CX=0 and CY=1. The three donor units have three unique values for X: 1.8, 1.9, and 2.0. These three unique values define three donor cells for imputing X when CX=0 and CY=1. The missing value in X for CX=0 and CY=1 is replaced by all three possible observed values. Because all three donor cells have equal weights, all three imputed rows are assigned a second-stage fractional weight of 1/3. The second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.46) for CX=0, CY=1, and ImpIndex=1 to obtain the two-stage FEFI weight.

  The row that contains Unit 14 and ImpIndex=2 in Figure 116.12 has CX=1 and CY=1. Units 13, 15, 16 and 17 in the complete data have CX=1 and CY=1. These units are donors for missing X when CX=1 and CY=1. The four donor units have four unique values for X: 2.9, 6.7, 9.6, and 10.0. These four unique values define four donor cells for imputing X when CX=1 and CY=1. The missing value in X for CX=1 and CY=1 is replaced by all four possible observed values. Because all four donor cells have equal weights, all four imputed rows are assigned a second-stage fractional weight of 1/4. The

second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.54) for CX=1 CX=1 to obtain the two-stage FEFI weight.

Therefore, after two-stage FEFI, missing values in X are replaced by seven imputed values that have fractional weights proportional to the observed weighted frequencies of the second-stage donor cells conditional on the first-stage FEFI.

- Observation unit 18 has missing values in all four variables X, CX, Y, and CY. The variable CX has two imputed levels (0 and 1), and the variable CY has two imputed levels (0 and 1) from the first-stage imputation.

  The row that contains Unit 18 and ImpIndex=1 in Figure 116.12 has CX=0 and CY=0. Units 1, 2, 3, and 4 in the complete data have CX=0 and CY=0. These units are possible donors for missing X and Y when CX=0 and CY=0. The four donor units have three unique values for (X, Y): (0.3, –0.54), (0.2, –0.77), and (1.7, –0.59). These three unique values define three donor cells for imputing (X, Y) when CX=0 and CY=0. The missing value in (X, Y) for CX=0 and CY=0 is replaced by all three values. Because the weight for the donor cell that is defined by (X, Y) = (1.7, –0.59) is double the weight for the other two donor cells, the imputed row that contains X = 1.7 and Y = –0.59 is assigned a second-stage fractional weight of 1/2 and the other two rows each are assigned a second-stage fractional weight of 1/4. The second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.27) for CX=0, CY=0, and ImpIndex=1 to obtain the two-stage FEFI weight.

  The row that contains Unit 18 and ImpIndex=2 in Figure 116.12 has CX=0 and CY=1. Units 6, 7, and 8 in the complete data have CX=0 and CY=1. These units are donors for the missing (X, Y) when CX=0 and CY=1. The three donor units have three unique values for (X, Y): (1.8, -0.3), (1.9, 0.78), and (2.0, 0.95). These three unique values define three donor cells for imputing (X, Y) when CX=0 and CY=1. The missing value in (X, Y) for CX=0 and CY=1 is replaced by all three possible observed values. Because all three donor cells have equal weights, all three imputed rows are assigned a second-stage fractional weight of 1/3. The second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.23) for CX=0 and CX=1 to obtain the two-stage FEFI weight.

  Missing values in (X, Y) in rows that contain Unit 18, ImpIndex=3, and ImpIndex=4 in Figure 116.12 are imputed similarly.

  Thus, after two-stage FEFI, missing values in (X, Y) are replaced by 14 imputed values that have fractional weights proportional to the observed weighted frequencies of the second-stage donor cells conditional on the first-stage FEFI.

The resulting data set has 42 rows. Fifteen rows for fully observed units (ImpIndex = 0), six rows for unit 5, seven rows for unit 14, and fourteen rows for unit 18. The sum of the fractional weights is 1 for all units. The imputation-adjusted replicate weights are computed by applying the first-stage and the second-stage imputation independently in each replicate sample as discussed in the previous list. The imputed data set along with first four imputation-adjusted replicate weights is displayed in Figure 116.14.

Figure 116.14 Two-Stage Fractional Imputation with the Imputation-Adjusted Replicate Weights

Unit	ImpIndex	ImpWt	FracWt	X	CX	Y	CY	ImpRepWt_1	ImpRepWt_2	ImpRepWt_3	ImpRepWt_4
1	0	1.0000	1.0000	0.3	0	-0.54	0	0	1.0588	1.0588	1.0588
2	0	1.0000	1.0000	0.2	0	-0.77	0	1.0588	0	1.0588	1.0588
3	0	1.0000	1.0000	1.7	0	-0.59	0	1.0588	1.0588	0	1.0588
4	0	1.0000	1.0000	1.7	0	-0.59	0	1.0588	1.0588	1.0588	0
5	1	0.1340	0.1340	1.0	0	-0.77	0	0.1637	0	0.1637	0.1637
5	2	0.1340	0.1340	1.0	0	-0.54	0	0	0.1637	0.1637	0.1637
5	3	0.2680	0.2680	1.0	0	-0.59	0	0.3274	0.3274	0.1637	0.1637
5	4	0.1547	0.1547	1.0	0	-0.03	1	0.1893	0.1893	0.1893	0.1893
5	5	0.1547	0.1547	1.0	0	0.78	1	0.1893	0.1893	0.1893	0.1893
5	6	0.1547	0.1547	1.0	0	0.95	1	0.1893	0.1893	0.1893	0.1893
6	0	1.0000	1.0000	1.8	0	-0.03	1	1.0588	1.0588	1.0588	1.0588
7	0	1.0000	1.0000	2.0	0	0.95	1	1.0588	1.0588	1.0588	1.0588
8	0	1.0000	1.0000	1.9	0	0.78	1	1.0588	1.0588	1.0588	1.0588
9	0	1.0000	1.0000	6.7	1	-0.15	0	1.0588	1.0588	1.0588	1.0588
10	0	1.0000	1.0000	6.0	1	-1.01	0	1.0588	1.0588	1.0588	1.0588
11	0	1.0000	1.0000	3.3	1	-1.86	0	1.0588	1.0588	1.0588	1.0588
12	0	1.0000	1.0000	7.3	1	-0.21	0	1.0588	1.0588	1.0588	1.0588
13	0	1.0000	1.0000	6.7	1	0.80	1	1.0588	1.0588	1.0588	1.0588
14	1	0.1547	0.1547	1.8	0	1.23	1	0.1656	0.1656	0.1656	0.1656
14	2	0.1547	0.1547	1.9	0	1.23	1	0.1656	0.1656	0.1656	0.1656
14	3	0.1547	0.1547	2.0	0	1.23	1	0.1656	0.1656	0.1656	0.1656
14	4	0.1340	0.1340	2.9	1	1.23	1	0.1405	0.1405	0.1405	0.1405
14	5	0.1340	0.1340	6.7	1	1.23	1	0.1405	0.1405	0.1405	0.1405
14	6	0.1340	0.1340	9.6	1	1.23	1	0.1405	0.1405	0.1405	0.1405
14	7	0.1340	0.1340	10.0	1	1.23	1	0.1405	0.1405	0.1405	0.1405
15	0	1.0000	1.0000	2.9	1	0.65	1	1.0588	1.0588	1.0588	1.0588
16	0	1.0000	1.0000	9.6	1	0.95	1	1.0588	1.0588	1.0588	1.0588
17	0	1.0000	1.0000	10.0	1	0.13	1	1.0588	1.0588	1.0588	1.0588
18	1	0.0667	0.0667	0.2	0	-0.77	0	0.0764	0	0.0764	0.0764
18	2	0.0667	0.0667	0.3	0	-0.54	0	0	0.0764	0.0764	0.0764
18	3	0.1334	0.1334	1.7	0	-0.59	0	0.1528	0.1528	0.0764	0.0764
18	4	0.0770	0.0770	1.8	0	-0.03	1	0.0884	0.0884	0.0884	0.0884
18	5	0.0770	0.0770	1.9	0	0.78	1	0.0884	0.0884	0.0884	0.0884
18	6	0.0770	0.0770	2.0	0	0.95	1	0.0884	0.0884	0.0884	0.0884
18	7	0.0588	0.0588	3.3	1	-1.86	0	0.0662	0.0662	0.0662	0.0662
18	8	0.0588	0.0588	6.0	1	-1.01	0	0.0662	0.0662	0.0662	0.0662
18	9	0.0588	0.0588	6.7	1	-0.15	0	0.0662	0.0662	0.0662	0.0662
18	10	0.0588	0.0588	7.3	1	-0.21	0	0.0662	0.0662	0.0662	0.0662
18	11	0.0667	0.0667	2.9	1	0.65	1	0.0750	0.0750	0.0750	0.0750
18	12	0.0667	0.0667	6.7	1	0.80	1	0.0750	0.0750	0.0750	0.0750
18	13	0.0667	0.0667	9.6	1	0.95	1	0.0750	0.0750	0.0750	0.0750
18	14	0.0667	0.0667	10.0	1	0.13	1	0.0750	0.0750	0.0750	0.0750

Fractional Hot-Deck Imputation

The fractional hot-deck imputation (FHDI) method uses multiple donor units for a recipient unit. Each donor donates a fraction of the original weight of the recipient unit such that the sum of the fractional weights from all the donors is equal to the original weight of the recipient. The fraction of the recipient weight that a donor unit contributes to the recipient unit is known as the *fractional weight*. The donors are selected by using probability proportional to size (PPS) selection in which the two-stage FEFI weights are used as the size measure.

FHDI is useful for reducing the size of the imputed data when two-stage FEFI creates many imputed rows. FHDI follows the same imputation steps as those of two-stage FEFI, but FHDI selects a subset of second-stage donor cells from all possible second-stage donor cells for the imputation.

Similar to two-stage FEFI, variables that have many unique observed levels are grouped into imputation bins. The first imputation stage is performed for all categorical variables by using the FEFI method. The categorical variables include the character variables, the CLASS variables that you also specify in the VAR statement, and the variables that contain the imputation bins of the continuous variables.

The second imputation stage is performed for the continuous variables within each first-stage donor cell. Observations that contain missing values for any of the continuous items are considered to be the recipients, and observations that contain observed values for all items are the donors. The second-stage donor cells are defined by the unique vectors of the observed values for the continuous variables within the first-stage donor cells.

If you specify NDONORS=m_2, then m_2 second-stage donor cells are selected within each first-stage donor cell, provided that more than m_2 second-stage donor cells are available for the continuous variables in that donor cell. Second-stage donor cells are selected within each first-stage donor cell by using PPS selection with replacement, where the fractional weights of the second-stage donor cells are used as the size measures. If the number of second-stage donor cells in a first-stage donor cell is less than or equal to m_2, then all available second-stage donor cells are used to impute the missing values for the continuous variables in that first-stage donor cell.

If no second-stage selection is performed, then the second-stage fractional weights are the same as the fractional weights from two-stage FEFI. If a second-stage selection is performed, then the second-stage fractional weights are computed by multiplying the first-stage fractional weights by the number of times a second-stage donor cell is selected divided by the second-stage sample size.

Imputation-adjusted replicate weights are computed by repeating both the first-stage and second-stage imputation in every replicate sample independently.

Selection of donor cells is not repeated in the creation of replicate samples. The donor cells that are selected in the full sample are retained in all replicate samples, and the replicate weights are adjusted to compensate for the selection of donor cells in both stages. If no selection is performed in either stage in the full sample (FEFI is used in both stages), then the replicate weights are not adjusted further.

The method is similar to Im, Kim, and Fuller (2015).

For more information about replication-weight adjustment, see the section "Replicate Weight Adjustments for FHDI" on page 9643.

Fractional Hot-Deck Imputation Notations and Assumptions

Suppose you want to impute P items jointly. Let $\mathbf{X}_i = (X_{i1}, \ldots, X_{iP_1})$ be the response for P_1 items in unit i, and let $\mathbf{Y}_i = (Y_{i1}, \ldots, Y_{iP_2})$ be the response for P_2 items in unit i, where $P = P_1 + P_2$. Let X_{ij} be categorical with J_j levels for item j, and let Y_{ij} be continuous. Further assume that $\tilde{\mathbf{Y}} = (\tilde{Y}_{i1}, \ldots, \tilde{Y}_{iP_2})$ contains the discretized levels (imputation bins) for $\mathbf{Y}$, where $\tilde{Y}_{ij}$ has J_j levels. Define $Z_{ij} = (X_{ij}, \tilde{Y}_{ij})$. Then Z_{ij} is categorical and has J_j levels for item j. Denote $\mathbf{Z}_{i,\text{obs}}$ as the observed part and $\mathbf{Z}_{i,\text{miss}}$ as the missing part of $\mathbf{Z}_i$.

Let $\pi(\kappa_1\kappa_2\cdots\kappa_P)$ be the population proportion that falls in category $Z_1 = \kappa_1, Z_2 = \kappa_2, \cdots Z_P = \kappa_P$. FEFI computes the fractional weights by using conditional probabilities of observing an imputed value in the data in which the observed levels for the nonmissing items in the recipient unit are equal to the observed levels for the same items in the donor units. For example, consider observation unit i in which items Z_{i1} and Z_{i2} are missing and items $Z_{i3} = \kappa_3$, $Z_{i4} = \kappa_4$, ..., and $Z_{iP} = \kappa_P$ are observed. The initial fractional weight for imputing (Z_{i1}, Z_{i2}) with (κ_1, κ_2) is computed by using the estimated conditional probability of observing $(Z_{i1}, Z_{i2}) = (\kappa_1, \kappa_2)$ when $(Z_{i3}, Z_{i4}, \ldots, Z_{iP}) = (\kappa_3, \kappa_4, \ldots, \kappa_P)$ in the complete data. The initial conditional probabilities are estimated by

$$\hat{P}(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2 | Z_{i3} = \kappa_3, \ldots, Z_{iP} = \kappa_p) = \left\{ \sum_{\kappa_1=1}^{J_1} \sum_{\kappa_2=1}^{J_2} \hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P) \right\}^{-1} \hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P)$$

where

$$\hat{\pi}(\kappa_1\kappa_2\cdots\kappa_P) = \left\{ \sum_{i\in\mathcal{A}_c} w_i \right\}^{-1} \sum_{i\in\mathcal{A}_c} w_i I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

is the estimated joint probability, $I(.)$ is an indicator function, w_i is the sampling weight for observation unit i, and $\mathcal{A}_c$ is the set of indices for observation units without any missing items.

The first-stage FEFI replaces the missing items in $\mathbf{Z}_i = (\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{mis}})$ by using observed values from all donor cells for observation unit i. The l_1th imputed value $\mathbf{Z}_{i,\text{dcell}[l_1]} = (\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{mis}[l_1]})$ uses the observed values from the l_1th donor cell (realization), where l_1 ranges from 1 to M_{l_1}.

The second-stage FEFI imputes the missing values in the continuous variables Y_{ij} where $j = 1, 2, \ldots, P_2$. The second-stage imputation is conditional on the imputed levels from the first-stage imputation. For observation unit i and first-stage donor cell l_1, the number of second-stage donor cells is equal to the number of unique combinations of the observed levels for the missing items in $\mathbf{Y}_i = (\mathbf{Y}_{i,\text{obs}}, \mathbf{Y}_{i,\text{mis}})$ among the responding units in the first-stage donor cell l_1. Unlike the first-stage imputation, the second-stage imputation does not depend on the observed levels for the nonmissing items in $\mathbf{Y}_i = (\mathbf{Y}_{i,\text{obs}}, \mathbf{Y}_{i,\text{mis}})$.

The second-stage fractional weights are computed by using the estimated probability of observing an imputed value for continuous variables conditional on the first-stage imputed level. For example, consider observation unit i in which items Y_{i1} and Y_{i2} are missing. Assume that the l_1th first-stage donor cell containing observation units that have $Z_1 = \kappa_1$, $Z_2 = \kappa_2$, ..., and $Z_P = \kappa_P$ provides the l_1th imputed value for the first-stage imputation for observation unit i. The second-stage fractional weight for imputing (Y_{i1}, Y_{i2}) with $(\kappa_{21}, \kappa_{22})$ in the first-stage donor cell l_1 is computed by using the estimated conditional probability of observing $(Y_{i1}, Y_{i2}) = (\kappa_{21}, \kappa_{22})$ by using the nonmissing units in the l_1th first-stage donor cell.

The conditional probabilities are estimated by

$$\hat{P}(Y_{i1} = \kappa_{21}, Y_{i2} = \kappa_{22} | Z_1 = \kappa_1, \ldots, Z_P = \kappa_P) = \hat{\pi}(\kappa_{21}\kappa_{22}|l_1) = \left\{\sum_{i \in \mathcal{A}_c} w_i I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_p)\right\}^{-1} \sum_{i \in \mathcal{A}_c} w_i I(Y_{i1} = \kappa_{21}, Y_{i2} = \kappa_{22}, Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_p)$$

The second-stage FEFI replaces the missing values in $\mathbf{Y}_i = (\mathbf{Y}_{i,\text{obs}}, \mathbf{Y}_{i,\text{miss}})$ when $(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$ by using all observed values for $\mathbf{Y}_{i,\text{miss}}$ from observation rows that contain $(Z_1 = \kappa_1, \ldots, Z_P = \kappa_P)$. Each second-stage imputed value (configuration) defines a second-stage donor cell. The l_2th imputed value in the l_1th first-stage donor cell is $\mathbf{Y}_{i,\text{dcell}[l_2|l_1]} = (\mathbf{Y}_{i,\text{obs}}, \mathbf{Y}_{i,\text{miss}[l_2]}, Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$, where l_2 ranges from 1 to $M_{il_2|l_1}$, and the l_1th first-stage donor cell is defined by observation units that contain $Z_1 = \kappa_1, \ldots, Z_P = \kappa_P$.

The two-stage imputation-adjusted fractional weights are computed by multiplying the first-stage fractional weights by the second-stage fractional weights. The sampling weight for observation unit i is denoted by w_i. Let w_{il} be the first-stage fractional weight for donor cell l, and let $w_{il(t)}$ be the first-stage fractional weight for donor cell l at the tth EM iteration. Let $w_{il_2|l_1}$ be the second-stage fractional weight, and let $w_{il_1l_2}$ be the two-stage fractional weight for first-stage donor cell l_1 and second-stage donor cell l_2. Thus, the imputation-adjusted weight for observation unit i, first-stage donor cell l_1, and second-stage donor cell l_2 is $w_i w_{il_1l_2}$.

Replicate weights are adjusted for imputation by applying both the first-stage and the second-stage imputation in every replicate sample. Let $w_i^{(r)}$ be the unadjusted replicate weight for observation unit i in replicate sample r. The unadjusted replicate weights are created by using a replication method such as the bootstrap, BRR, or delete-1 jackknife. For more information about how the unadjusted replicate weights are created, see sections "Unadjusted Bootstrap Replicate Weights" on page 9640, "Unadjusted BRR Replicate Weights" on page 9640, and "Unadjusted Jackknife Replicate Weights" on page 9642. Let $w_{il}^{(r)}$ be the first-stage fractional replicate weight, $w_{il_2|l_1}^{(r)}$ be the second-stage fractional replicate weight, and $w_{il_1l_2}^{(r)}$ be the two-stage fractional replicate weight for replicate sample r, observation unit i, first-stage donor cell l_1, and second-stage donor cell l_2. Thus, the imputation-adjusted replicate weight for observation unit i, first-stage donor cell l_1, second-stage donor cell l_2, and replicate sample r is $w_i^{(r)} w_{il_1l_2}^{(r)}$.

The following assumptions are necessary:

- The conditional probability of observing an imputed value in the missing data is the same as the conditional probability of observing the value in the observed data in each imputation cell. For example, the conditional probability, $P(Z_{i1} = \kappa_1, Z_{i2} = \kappa_2 | Z_{i3} = \kappa_3, \ldots, Z_{iP} = \kappa_P)$, is the same for the observed data as it is for the data where Z_1 and Z_2 are missing.
- The conditional probability of observing a second-stage imputed value in the missing data is the same as the conditional probability of observing the value in the observed data in every first-stage donor cell. For example, the conditional probability in the first-stage donor cell $(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$, $P(Y_{i1} = \kappa_{21}, Y_{i2} = \kappa_{22} | Z_1 = \kappa_1, \ldots, Z_P = \kappa_p)$, is the same for the observed data as it is for the data in which (Y_1 and Y_2) are missing and $Z_1 = \kappa_1, \ldots, Z_P = \kappa_P$.
- For every observation unit that contains missing items, at least one realization for the missing items is available in the complete data; otherwise the observation is not imputed.
- For variance estimation, at least two realizations for the missing items from two different PSUs must be available in the complete data for every observation unit that contains missing items. If the condition is not satisfied, the variance due to imputing the missing items in that observation is ignored.

Fractional Hot-Deck Imputation Algorithm

The FHDI method first computes the fully efficient fractional weights by using an EM-by-weighting algorithm like that of Kim and Fuller (2013) to impute the missing values in $\mathbf{Z}_i$. The missing values in $\mathbf{Y}_i$ are imputed in the second-stage imputation. For the second-stage imputation, FEFI weights to impute $\mathbf{Y}_i$ are computed independently in every imputed level of $\mathbf{Z}_{i,\text{miss}[l]}$, where $l = 1, \ldots, M_{l_1}$ is the number of first-stage donor cells. If the number of second-stage donor cells is greater than m_2 (where m_2 is the value of the NDONORS= option in the PROC SURVEYIMPUTE statement), then m_2 second-stage donor cells are selected by using PPS sampling in which the second-stage fractional weights are used as the size measure.

The following steps describe the FHDI technique. If you do not use the CELL statement to specify imputation cells, PROC SURVEYIMPUTE uses the entire data set as one imputation cell. If you specify imputation cells, then all the probabilities are computed by using observations from the same imputation cell as the recipient unit. To simplify notation, subscripts are not used for imputation cells in the following description. Imputation cells are defined for the first-stage imputation. Steps 1 to 5 describe the two-stage FEFI. Step 6 describes donor selection for FHDI.

1. *Initialization*: For each observation that has missing items, determine the number of first-stage donor cells. The first-stage donor cells are determined by using the number of unique combinations of observed levels in $\mathbf{Z}_i$ for imputing the missing items in $\mathbf{Z}_i$. Only the responding units in the imputation cell are used to determine the number of first-stage donor cells. Compute the initial fractional weight from donor cell l to unit i, $w_{il(0)}$:

$$w_{il(0)} = \left\{ \sum_{k=1}^{M_{il_1}} \tilde{\pi}_{(0)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[k]}) \right\}^{-1} \tilde{\pi}_{(0)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[l]})$$

   where $l = 1, 2, \ldots, M_{l_1}$ is the number of first-stage donor cells and

$$\tilde{\pi}_{(0)}(\kappa_1, \ldots, \kappa_P) = \left\{ \sum_{i \in \mathcal{A}_c} w_i \right\}^{-1} \sum_{i \in \mathcal{A}_c} w_i I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

   The sum of the fractional weights over all the donor cells is 1 for every observation unit; that is, $\sum_l w_{il(0)} = 1$ for all i. The lth imputed row for unit i is created by keeping the observed items unchanged, replacing the missing items with the observed levels from the lth donor cell, and computing the fractional weight by $w_i w_{il(0)}$. Only the complete observations (observations that have no missing items) are used to compute the fractional weights in this step. If unit i has no missing items, then $w_{i1(0)} = 1$. The initial FEFI data set contains all the observed units, the imputed rows for observations that have missing items, and the corresponding fractional weights.

2. *M-step*: The tth maximization step (M-step) computes the joint probabilities by using the fractional weights from the (t–1)th expectation-step,

$$\tilde{\pi}_{(t)}(\kappa_1, \ldots, \kappa_P) = \left\{ \sum_i \sum_l w_i w_{il(t-1)} \right\}^{-1} \sum_i \sum_l w_i w_{il(t-1)} I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

   for all i, all l, and $t > 0$. Note that for $t > 0$, $\tilde{\pi}_{(t)}$ uses all observation units, including observations that have missing items and are imputed in the initialization step.

3. *E-step*: The tth expectation step (E-step) computes the fractional weights by using the joint probabilities $\tilde{\pi}_{(t)}(\kappa_1, \ldots, \kappa_P)$ from the tth M-step. The tth fractional weight for unit i and donor cell l is given by

$$w_{il(t)} = \left\{ \sum_{k=1}^{M_{il_1}} \tilde{\pi}_{(t)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[k]}) \right\}^{-1} \tilde{\pi}_{(t)}(\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{miss}[l]})$$

4. *Repetition*: The expectation maximization steps (EM-steps, step 2 and 3) are repeated for $t = 1, 2, \ldots,$ until the changes in fractional weights over all observation units between two successive EM-steps are negligible or the maximum number of EM repetitions is reached.

   The maximum absolute difference convergence criterion, ϵ_{AD}, at step t is defined as

$$\max_{i,l} |w_{il(t)} - w_{il(t-1)}| \leq \epsilon_{\text{AD}}$$

   The maximum absolute relative difference convergence criterion, ϵ_{RD}, at step t is defined as

$$\max_{i,l} |w_{il(t)} - w_{il(t-1)}| / w_{il(t-1)} \leq \epsilon_{\text{RD}}$$

   where $w_{il(t-1)} > 0$.

5. *Second-stage imputation*: The second-stage imputation replaces the missing values in the continuous variables by using the observed values within each selected first-stage donor cell. This step is similar to step 1 but is applied in order to impute the continuous variables.

   For a particular observation unit i, let $\mathbf{Z}_{i,\text{dcell}[l_1]} = (\mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{i,\text{mis}[l_1]})$ be the l_1th donor cell from the first-stage imputation, where l_1 ranges from 1 to M_{l_1}. For each observation unit, i, the possible number of second-stage donor cells is equal to the number of unique combinations of the observed levels for the missing items in $\mathbf{Y}_i$ from the responding units in the first-stage donor cell l_1.

   Let $\pi_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1} \cdots \kappa_{P_2|l_1})$ be the population proportion that falls in category $\kappa_{1|l_1}\kappa_{2|l_1} \cdots \kappa_{P_2|l_1}$. Assume that it is possible to estimate the population categories from the observed sample. For example, the conditional probability, $P(Y_{i1|l_1} = \kappa_{1|l_1}, Y_{i2|l_1} = \kappa_{2|l_1} | Y_{i3|l_1} = \kappa_{3|l_1}, \ldots, Y_{iP_2|l_1} = \kappa_{P_2|l_1})$, is the same for the observed data as it is for the data in which $(Y_{i1|l_1} = \kappa_{1|l_1}, Y_{i2|l_1} = \kappa_{2|l_1})$ are missing. The conditional probabilities are estimated by

$$\hat{P}(Y_{i1|l_1} = \kappa_{1|l_1}, Y_{i2|l_1} = \kappa_{2|l_1} | Y_{i3|l_1} = \kappa_{3|l_1}, \ldots, Y_{iP_2|l_1} = \kappa_{P_2|l_1}) = \left\{ \sum_{\kappa_{1|l_1}\kappa_{2|l_1}} \hat{\pi}_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1} \cdots \kappa_{P_2|l_1}) \right\}^{-1} \hat{\pi}_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1} \cdots \kappa_{P_2|l_1})$$

   where

$$\hat{\pi}_{2|l_1}(\kappa_{1|l_1}\kappa_{2|l_1} \cdots \kappa_{P_2|l_1}) = \left\{ \sum_{i \in \mathbf{Z}_{i,\text{dcell}[l_1]}} w_i \right\}^{-1} \sum_{i \in \mathbf{Z}_{i,\text{dcell}[l_1]}} w_i I(Y_{i1|l_1} = \kappa_{1|l_1}, \ldots, Y_{iP_2|l_1} = \kappa_{P_2|l_1})$$

   is the estimated joint probability, $I(.)$ is an indicator function, and w_i is the observation weight for unit i.

   Let $l = 1, 2, \ldots, M_{il_2|l_1}$ be all the observed combinations of $\mathbf{Y}_{k:k \in \mathbf{Z}_{i,\text{dcell}[l_1]}, k \neq i,\text{miss}}$ in the sample. Let $\mathbf{Y}_{i,\text{miss}[l]}$ be the lth realization of $\mathbf{Y}_{i,\text{miss}}$ in the sample. You must assume that at least one realization is available; otherwise, missing values in the continuous items for the observation are not imputed.

Compute the second-stage fractional weight from the second-stage donor cell l_2 conditional on the first-stage donor cell l_1 for unit i, $w_{il_2|l_1}$, by

$$w_{il_2|l_1} = \left\{ \sum_{k=1}^{M_{il_2|l_1}} \tilde{\pi}_{2|l_1}(\mathbf{Y}_{i,\text{obs}}, \mathbf{Y}_{i,\text{miss}[k]}) \right\}^{-1} \tilde{\pi}_{2|l_1}(\mathbf{Y}_{i,\text{obs}}, \mathbf{Y}_{i,\text{miss}[l_2]})$$

where $l = 1, 2, \ldots, M_{il_2|l_1}$ is the number of second-stage donor cells and

$$\tilde{\pi}_{2|l_1}(\kappa_1, \ldots, \kappa_{P_2}) = \left\{ \sum_{i \in \mathbf{Z}_{i,\text{dcell}[l_1]}} w_i \right\}^{-1} \sum_{i \in \mathbf{Z}_{i,\text{dcell}[l_1]}} w_i I(Y_{i1|l_1} = \kappa_1, \ldots, Y_{iP_2|l_1} = \kappa_{P_2})$$

The sum of the second-stage fractional weights over all second-stage donor cells is 1 for every observation unit; that is, $\sum_{l_2} w_{il_2|l_1} = 1$ for all l_1 and i. The l_2th second-stage imputed row in the l_1th first-stage imputed row for unit i is created by keeping the observed items unchanged, replacing the missing items in $\mathbf{Y}_i$ with the observed values from the l_2th second-stage donor cell, and computing the two-stage fractional weight by $w_{il_1l_2} = w_{il_1} w_{il_2|l_1}$, where w_{il_1} is the first-stage fractional weight for the first-stage donor cell l_1. The maximum number of donor cells for unit i is $M_{il_1} M_{il_2|l_1}$. Only the complete observations are used to compute the second-stage fractional weights.

6. *Second-stage selection*: Because all observed levels are used as the imputed values for missing items in the continuous variables in the previous step, the number of second-stage donor cells, $M_{il_2|l_1}$, is usually large. Suppose you want to use only m_2 second-stage donor cells (where m_2 is the value of the NDONORS= option in the PROC SURVEYIMPUTE statement). The second-stage selection chooses m_2 second-stage donor cells for every first-stage donor cell.

   The selection step selects a random sample of second-stage donor cells of size m_2 for every recipient unit and every first-stage donor cell in which the number of second-stage donor cells is greater than m_2. Consider the set of all observations in which the values of the observed items are the same and they all have the same missing items. The index set $p_i = \{j : j \in \mathcal{A}, \mathbf{Z}_{j,\text{obs}} = \mathbf{Z}_{i,\text{obs}}, \mathbf{Z}_{j,\text{miss}} = \mathbf{Z}_{i,\text{miss}}\}$ contains the indices for all units that have the same missing pattern and the same observed values in the nonmissing items. Let n_{pi} be the number of units in p_i. Note that the number of donor cells, $M_{il_2|l_1}$, and the fractional weights for all n_{pi} recipient units indexed by p_i are the same. If $M_{il_2|l_1} > m_2$, then select a PPS sample with replacement of $m_2 n_{pi}$ donor cells from $M_{il_2|l_1} n_{pi}$ donor cells by using the two-stage fractional weights of the donor cells as the size measure.

   The donor selection algorithm can be described as follows:

   a) Sort the second-stage donor cells by observed values of $\mathbf{Y}_i$ within each first-stage donor cell.
   b) Compute the cumulative sums of the fractional weights for the second-stage donor cells, and normalize the cumulative sums to 1.
   c) Select a random number between 0 and 1, and divide it by the sample size, $m_2 n_{pi}$.
   d) Select a PPS sample with replacement that starts from the scaled random number and uses $1/m_2 n_{pi}$ as the step length. For more information, see Särndal, Swensson, and Wretman (1992, p. 97).
   e) Use a random permutation to sort recipient units in a random order.

f) Distribute the selected donor cells to the recipient units in a cyclic manner, such that the first selected donor cell is allocated to the first recipient unit, the second selected donor cell is allocated to the second recipient unit, the $(n_{pi} + 1)$th selected donor cell is allocated to the first recipient unit, the $(n_{pi} + 2)$th selected donor cell is allocated to the second recipient unit, and so on. Because of the random sorting in the previous step, the first recipient unit after the sorting is not the same as the first recipient unit in the input data.

The second-stage fractional weights, $w_{il_2|l_1}$, are used as the size measure in the PPS sampling. Only one PPS sampling is performed for all recipient units in one first-stage donor cell.

Alternatively, if you specify METHOD=FHDI(SELECTION=PPSPEROBS), then independent selection is performed for every recipient unit and every first-stage donor cell in which the number of second-stage donor cells is greater than m_2. Thus the procedure selects n_{p_i} independent PPS samples with replacement of size m_2 for n_{pi} recipient units.

The imputation-adjusted weights for the second-stage donor cells are equal to w_{il_2} for observation units when no second-stage selection is performed and equal to $w_{il}h_{l_2}/m_2$ for observation units when the second-stage selection is performed, where h_{l_2} is the number of times the second-stage donor cell l_2 is selected. Combining the first-stage and the second-stage imputation, the total number of donor cells for an observation unit is greater than or equal to $M_{l_1}M_{l_2}$ and less than $M_{l_1}m_2$.

7. *Replicate weight adjustments*: The unadjusted replicate weights are created as if all rows of data were observed data by using a replication procedure such as the delete-1 jackknife, BRR, or bootstrap. The unadjusted replicate weights for rows that contain imputed data are then adjusted for two-stage FEFI by replicating all steps for two-stage FEFI for each replicate sample.

   Replication weights for FHDI rows are further adjusted to account for the selection of second-stage donor cells. Although every step in the two-stage FEFI procedure is applied in each replicate sample, the selection of second-stage donor cells is not repeated in FHDI. The fractional weights are adjusted instead.

   For available adjustments in the replicate weights, see the section "Replicate Weight Adjustments for FHDI" on page 9643.

Example of Two-Stage Fractional Hot-Deck Imputation

The small data set shown in Figure 116.15 is used to illustrate the FHDI technique. The data set contains 18 observation units, and each unit has four items (X, CX, Y, and CY). The variable Unit contains the observation identification. Variables CX and CY contains the imputation bins for variables X and Y, respectively. In this example, X and CX are missing for units 14 and 18, and Y and CY are missing for units 5 and 18.

Figure 116.15 Sample Data with Missing Items

Unit	X	CX	Y	CY
1	0.3	0	-0.54	0
2	0.2	0	-0.77	0
3	1.7	0	-0.59	0
4	1.7	0	-0.59	0
5	1.0	0	.	.
6	1.8	0	-0.03	1
7	2.0	0	0.95	1
8	1.9	0	0.78	1
9	6.7	1	-0.15	0
10	6.0	1	-1.01	0
11	3.3	1	-1.86	0
12	7.3	1	-0.21	0
13	6.7	1	0.80	1
14	.	.	1.23	1
15	2.9	1	0.65	1
16	9.6	1	0.95	1
17	10.0	1	0.13	1
18	.	.	.	.

The following statements request joint imputation of X and Y by using the FHDI method. The two CLEVVAR= options specify variables CX and CY to contain the imputation bins for variables X and Y, respectively. These statements also request imputation-adjusted replicate weights for the jackknife replication method. The OUTPUT statement stores the imputed values in the data set ImputedD3 and stores the jackknife coefficients in the data set OJKC. The FRACTIONALWEIGHTS= option in the OUTPUT statement saves the fractional weights in the ImputedD3 data set. The SEED= option specifies a seed for the random number generator, and the NDONORS=3 option requests three second-stage donor cells for each first-stage FEFI level.

```
proc surveyimpute data=Example method=fhdi seed=8943028 ndonors=3;
   var X (clevvar=CX) Y (clevvar=CY);
   output out=ImputedD3 fractionalweights=FracWt outjkcoefs=OJKC;
run;
```

The procedure first imputes the missing values in CX, CY, X, and Y by using the two-stage FEFI, as described in the section "Example of Two-Stage FEFI" on page 9617. The two-stage FEFI imputed values along with the imputation-adjusted weights and the imputation-adjusted replicate weights are shown in Figure 116.14.

The FHDI selects three second-stage donor cells in each first-stage FEFI cell. The imputed data set after the FHDI is displayed in Figure 116.16.

Figure 116.16 Fractional Hot-Deck Imputation Using Three Donors

Unit	ImpIndex	ImpWt	FracWt	X	CX	Y	CY
1	0	1.0000	1.0000	0.3	0	-0.54	0
2	0	1.0000	1.0000	0.2	0	-0.77	0
3	0	1.0000	1.0000	1.7	0	-0.59	0
4	0	1.0000	1.0000	1.7	0	-0.59	0
5	1	0.1340	0.1340	1.0	0	-0.77	0
5	2	0.1340	0.1340	1.0	0	-0.54	0
5	3	0.2680	0.2680	1.0	0	-0.59	0
5	4	0.1547	0.1547	1.0	0	-0.03	1
5	5	0.1547	0.1547	1.0	0	0.78	1
5	6	0.1547	0.1547	1.0	0	0.95	1
6	0	1.0000	1.0000	1.8	0	-0.03	1
7	0	1.0000	1.0000	2.0	0	0.95	1
8	0	1.0000	1.0000	1.9	0	0.78	1
9	0	1.0000	1.0000	6.7	1	-0.15	0
10	0	1.0000	1.0000	6.0	1	-1.01	0
11	0	1.0000	1.0000	3.3	1	-1.86	0
12	0	1.0000	1.0000	7.3	1	-0.21	0
13	0	1.0000	1.0000	6.7	1	0.80	1
14	1	0.1547	0.1547	1.8	0	1.23	1
14	2	0.1547	0.1547	1.9	0	1.23	1
14	3	0.1547	0.1547	2.0	0	1.23	1
14	4	0.1787	0.1787	2.9	1	1.23	1
14	5	0.1787	0.1787	6.7	1	1.23	1
14	6	0.1787	0.1787	10.0	1	1.23	1
15	0	1.0000	1.0000	2.9	1	0.65	1
16	0	1.0000	1.0000	9.6	1	0.95	1
17	0	1.0000	1.0000	10.0	1	0.13	1
18	1	0.0667	0.0667	0.2	0	-0.77	0
18	2	0.0667	0.0667	0.3	0	-0.54	0
18	3	0.1334	0.1334	1.7	0	-0.59	0
18	4	0.0770	0.0770	1.8	0	-0.03	1
18	5	0.0770	0.0770	1.9	0	0.78	1
18	6	0.0770	0.0770	2.0	0	0.95	1
18	7	0.0784	0.0784	3.3	1	-1.86	0
18	8	0.0784	0.0784	6.7	1	-0.15	0
18	9	0.0784	0.0784	7.3	1	-0.21	0
18	10	0.0889	0.0889	6.7	1	0.80	1
18	11	0.0889	0.0889	9.6	1	0.95	1
18	12	0.0889	0.0889	10.0	1	0.13	1

The FHDI is described as follows:

- Observation unit 1 has no missing value. Therefore, the ImpIndex value is 0; the FracWt value is 1; and the values of X, CX, Y, and CY are the same as the observed values for observation unit 1 in Figure 116.16. Because all observation units have a weight of 1, the fractional weights (FracWt) and the imputation-adjusted weights (ImpWt) are the same for all rows.

- Observation unit 5 has missing values in Y and CY. The variable CY has two imputed levels (0 and 1) from the first-stage imputation. The observed level of CX for observation unit 5 is 0.

  There are six rows for observation unit 5 after two-stage FEFI (Figure 116.14). ImpIndex values 1 to 3 contain imputed values when CY=0, and ImpIndex values 4 to 6 contain imputed values when CY=1. Because there are only three rows for each imputed level of CY and NDONORS=3 is specified in the PROC SURVEYIMPUTE statement, no selection is performed for FHDI for observation unit 5. Thus, all six imputed rows from FHDI (Figure 116.16) are the same as the six imputed rows from two-stage FEFI for observation unit 5 (Figure 116.14).

- Observation unit 14 has missing values in X and CX. The variable CX has two imputed levels (0 and 1) from the first-stage imputation. The observed level of CY for observation unit 14 is 1. There are seven rows for observation unit 14 after two-stage FEFI (Figure 116.14).

  ImpIndex values 1 to 3 for observation unit 14 contain imputed values for X when CX=0. Because there are only three rows for CX=0 and NDONORS=3 is specified in the PROC SURVEYIMPUTE statement, no selection is performed for FHDI for observation unit 14 and CX=0.

  ImpIndex values 4 to 7 for observation unit 14 contain imputed values for X when CX=1. Because the number of imputed rows for observation unit 14 and CX=1 is greater than 3, the procedure selects three donor cells by using a PPS sample with replacement. Donor cells that have imputed X values of 2.9, 6.7, and 10.0 are selected. Each row is assigned a second-stage fractional weight of 1/3. The second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.54) for observation unit 14 when CX=1 to obtain the FHDI weight.

  Although three donor cells are selected for observation unit 14 when CX=0, the procedure selects six donor cells from four donor cells for observation units 14 and 18 together by using one PPS sample with replacement. Note that observation unit 14 for ImpIndex values 4 to 7 and observation unit 18 for ImpIndex values 11 to 14 have the same levels for the first-stage imputation variables CX (=1) and CY (=1).

Thus, there are six rows for observation unit 14 after FHDI in Figure 116.16.

- Observation unit 18 has missing values in all four variables, X, CX, Y, and CY. The variable CX has two imputed levels (0 and 1) and the variable CY has two imputed levels (0 and 1) from the first-stage imputation. There are 14 rows for observation unit 18 after two-stage FEFI (Figure 116.14).

  ImpIndex values 1 to 3 for observation unit 18 after two-stage FEFI contain three imputed values for X and Y when CX=0 and CY=0 (Figure 116.14). Because there are only three imputed rows for CX=0 and CY=0 and NDONORS=3 is specified in the PROC SURVEYIMPUTE statement, no selection is performed for FHDI for observation unit 18 when CX=0 and CY=0. Similarly, no selection is performed for FHDI for observation unit 18 when CX=0 and CY=1. Thus, all rows for observation unit 18 and ImpIndex values 1 to 6 from FHDI (Figure 116.16) are the same as the rows for observation unit 18 and ImpIndex values 1 to 6 from two-stage FEFI (Figure 116.14).

  Three donor cells are selected from four donor cells for observation unit 18 and ImpIndex values 7 to 10, where CX=1 and CY=0. A PPS sample with replacement is used, where the fractional weights of the donor cells are used as the size measure. The selected donor cells are (3.3, –1.86), (6.7, –0.15), and (7.3, –0.21) for (X, Y). Each row is assigned a second-stage fractional weight of 1/3. The second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.24) for the observation unit 18 in which CX=1 and CY=0 in order to obtain the FHDI weight.

  Similarly, donor cells (6.7, 0.80), (9.6, 0.95), and (10.0, 0.13) are selected for (X, Y) for the observation unit 18 in which CX=1 and CX=1. Each row is assigned a second-stage fractional weight of 1/3. The second-stage fractional weight is then multiplied by the first-stage FEFI weight (0.27) for the observation unit 18 in which CX=1 and CY=1 in order to obtain the FHDI weight.

  Thus, there are 12 imputed rows after FHDI for observation unit 18.

The resulting data set has 39 rows: 15 rows for fully observed units (ImpIndex=0), six rows for unit 5, six rows for unit 14, and 12 rows for unit 18. The sum of the fractional weights is 1 for all observation units.

The imputation-adjusted replicate weights are computed by applying the first-stage imputation, second-stage imputation, and neighbor adjustment (as discussed in section "Replicate Weight Adjustments for FHDI" on page 9643) independently in each replicate sample. The imputed data set along with first four imputation-adjusted replicate weights is displayed in Figure 116.17.

Figure 116.17 Fractional Hot-Deck Imputation with Imputation-Adjusted Replicate Weights

Unit	ImpIndex	ImpWt	FracWt	X	CX	Y	CY	ImpRepWt_1	ImpRepWt_2	ImpRepWt_3	ImpRepWt_4
1	0	1.0000	1.0000	0.3	0	-0.54	0	0	1.0588	1.0588	1.0588
2	0	1.0000	1.0000	0.2	0	-0.77	0	1.0588	0	1.0588	1.0588
3	0	1.0000	1.0000	1.7	0	-0.59	0	1.0588	1.0588	0	1.0588
4	0	1.0000	1.0000	1.7	0	-0.59	0	1.0588	1.0588	1.0588	0
5	1	0.1340	0.1340	1.0	0	-0.77	0	0.1637	0	0.1637	0.1637
5	2	0.1340	0.1340	1.0	0	-0.54	0	0	0.1637	0.1637	0.1637
5	3	0.2680	0.2680	1.0	0	-0.59	0	0.3274	0.3274	0.1637	0.1637
5	4	0.1547	0.1547	1.0	0	-0.03	1	0.1893	0.1893	0.1893	0.1893
5	5	0.1547	0.1547	1.0	0	0.78	1	0.1893	0.1893	0.1893	0.1893
5	6	0.1547	0.1547	1.0	0	0.95	1	0.1893	0.1893	0.1893	0.1893
6	0	1.0000	1.0000	1.8	0	-0.03	1	1.0588	1.0588	1.0588	1.0588
7	0	1.0000	1.0000	2.0	0	0.95	1	1.0588	1.0588	1.0588	1.0588
8	0	1.0000	1.0000	1.9	0	0.78	1	1.0588	1.0588	1.0588	1.0588
9	0	1.0000	1.0000	6.7	1	-0.15	0	1.0588	1.0588	1.0588	1.0588
10	0	1.0000	1.0000	6.0	1	-1.01	0	1.0588	1.0588	1.0588	1.0588
11	0	1.0000	1.0000	3.3	1	-1.86	0	1.0588	1.0588	1.0588	1.0588
12	0	1.0000	1.0000	7.3	1	-0.21	0	1.0588	1.0588	1.0588	1.0588
13	0	1.0000	1.0000	6.7	1	0.80	1	1.0588	1.0588	1.0588	1.0588
14	1	0.1547	0.1547	1.8	0	1.23	1	0.1656	0.1656	0.1656	0.1656
14	2	0.1547	0.1547	1.9	0	1.23	1	0.1656	0.1656	0.1656	0.1656
14	3	0.1547	0.1547	2.0	0	1.23	1	0.1656	0.1656	0.1656	0.1656
14	4	0.1787	0.1787	2.9	1	1.23	1	0.1873	0.1873	0.1873	0.1873
14	5	0.1787	0.1787	6.7	1	1.23	1	0.1873	0.1873	0.1873	0.1873
14	6	0.1787	0.1787	10.0	1	1.23	1	0.1873	0.1873	0.1873	0.1873
15	0	1.0000	1.0000	2.9	1	0.65	1	1.0588	1.0588	1.0588	1.0588
16	0	1.0000	1.0000	9.6	1	0.95	1	1.0588	1.0588	1.0588	1.0588
17	0	1.0000	1.0000	10.0	1	0.13	1	1.0588	1.0588	1.0588	1.0588
18	1	0.0667	0.0667	0.2	0	-0.77	0	0.0764	0	0.0764	0.0764
18	2	0.0667	0.0667	0.3	0	-0.54	0	0	0.0764	0.0764	0.0764
18	3	0.1334	0.1334	1.7	0	-0.59	0	0.1528	0.1528	0.0764	0.0764
18	4	0.0770	0.0770	1.8	0	-0.03	1	0.0884	0.0884	0.0884	0.0884
18	5	0.0770	0.0770	1.9	0	0.78	1	0.0884	0.0884	0.0884	0.0884
18	6	0.0770	0.0770	2.0	0	0.95	1	0.0884	0.0884	0.0884	0.0884
18	7	0.0784	0.0784	3.3	1	-1.86	0	0.0882	0.0882	0.0882	0.0882
18	8	0.0784	0.0784	6.7	1	-0.15	0	0.0882	0.0882	0.0882	0.0882
18	9	0.0784	0.0784	7.3	1	-0.21	0	0.0882	0.0882	0.0882	0.0882
18	10	0.0889	0.0889	6.7	1	0.80	1	0.0999	0.0999	0.0999	0.0999
18	11	0.0889	0.0889	9.6	1	0.95	1	0.0999	0.0999	0.0999	0.0999
18	12	0.0889	0.0889	10.0	1	0.13	1	0.0999	0.0999	0.0999	0.0999

Hot-Deck Imputation

Imputation techniques that use observed values from the sample to impute (fill in) missing values are known as hot-deck imputation. For more information, see Fellegi and Holt (1976), Lohr (2010, Section 8.6.3), Andridge and Little (2010), Fuller (2009, Section 5.2.1), Särndal and Lundström (2005), and Bethlehem

(2009, Section 8.3). The observation unit that contains the missing values is known as the recipient unit, and the observation unit that provides the value for imputation is known as the donor unit. It is common to group similar observation units in one imputation cell and then select the donor units from the same imputation cell as the recipient unit. This imputation technique is also known as hot-deck imputation within classes (Särndal, Swensson, and Wretman 1992, p. 593). If the donor unit is selected randomly for a recipient unit, then the imputation technique is called random hot-deck imputation.

PROC SURVEYIMPUTE implements cell-based random hot-deck imputation methods. You identify imputation cells by using the CELLS statement and specify a random selection method by using the SELECTION= suboption for METHOD=HOTDECK in the PROC SURVEYIMPUTE statement. If an observation unit does not contain any missing values in the analysis variables, then the observation unit is considered as a donor unit. If an observation unit contains at least one missing value in the analysis variables, then the observation unit is treated as a recipient unit. You specify the analysis variables in the VAR statement. If no donors are found for an observation unit in the imputation cell, then the missing items are not imputed for that observation unit.

To illustrate the technique, consider the data set in Figure 116.18. Assume these six units are in the same imputation cell and you want to use the hot-deck imputation to impute the missing values in units 3, 4, and 6.

Figure 116.18 Units in an Imputation Cell

Unit	Age	Gender	Pregnancy
1	48	Male	0
2	22	Female	1
3	31		2
4	.	Male	0
5	22	Female	0
6	35		.

The following SAS statements use units 1, 2, and 5, which contain no missing values as the donor units for all recipient units 3, 4, and 6. For every recipient unit, PROC SURVEYIMPUTE selects a donor unit at random from all available donor units and replaces the missing values in the recipient unit with the observed values from the selected donor unit.

Both Age and Pregnancy are missing for unit 6, and PROC SURVEYIMPUTE uses the same donor to impute both items. Using the same donor unit to impute multiple items helps preserve the observed multivariate relationship.

However, it is possible to generate impossible responses. For example, if observation unit 1 is randomly selected as the donor unit for observation unit 3, then observation unit 3 will have Gender=Male but Pregnancy=2—a biological impossibility! To deal with such situations, consider filling the deterministic values before using imputation. For example, unit 3 is reported to be pregnant twice, and thus must be a female respondent. So you assign Gender=Female for unit 3 before using PROC SURVEYIMPUTE.

```
proc surveyimpute method=hotdeck(selection=srswr);
   var Age Gender Pregnancy;
   output out=JointHotDeck;
run;
```

If you do not want to preserve the multivariate relationship among the items, then you can impute the items marginally. The following SAS statements impute Age marginally. The recipient unit is 4, and the possible donor units are 1, 2, 3, 5, and 6.

```
proc surveyimpute method=hotdeck(selection=srswr);
   var Age;
   output out=MarginalHotDeck;
run;
```

The random selection of donors preserves the expectations within the imputation cells, but the random selection process increases the variance (Fuller 2009, p. 289). The variance estimator must include both the sampling variability and the imputation variability (Särndal and Lundström 2005).

PROC SURVEYIMPUTE implements the random selection methods that are described in the following subsections.

Approximate Bayesian Bootstrap

Suppose there are m recipient units and r donor units in an imputation cell. The approximate Bayesian bootstrap technique uses the following two steps for donor selection:

1. Select a sample of size r from the r donor units by using a simple random sample with replacement. The selected set is called the donor set for this imputation cell.
2. Select m donor units from the donor set by using a simple random sample with replacement.

To account for the imputation variance, you must select multiple donor units for every recipient unit. You can use the NDONORS= option in the PROC SURVEYIMPUTE statement to select multiple donor units. The procedure repeats the preceding two steps independently to select multiple donor units for every recipient unit. If you have a stratified design, Little and Rubin (2002, p. 89) suggest defining the imputation cells that are nested within strata. By default, the procedure does not assume that the cells are nested within the strata. You must specify the STRATA variables in the CELLS statement to define the imputation cells that are nested within the strata. For more information about the approximate Bayesian bootstrap method, see Rubin and Schenker (1986), Little and Rubin (2002, p. 89), and Kim (2002).

Simple Random Samples without Replacement

Suppose there are m recipient units and r donor units in an imputation cell. PROC SURVEYIMPUTE selects a simple random sample without replacement of size m from the r donors. One requirement for this selection method is that the number of donor units must be greater than or equal to the number of the recipient units. PROC SURVEYIMPUTE uses the selection-rejection method described in Tillé (2006, p. 48). If you select multiple (d) donor units for each recipient unit (by using the NDONORS= option in the PROC SURVEYIMPUTE statement), then the procedure selects d simple random samples independently.

Simple Random Samples with Replacement

Suppose there are m recipient units and r donor units in an imputation cell. PROC SURVEYIMPUTE selects a simple random sample with replacement of size m from the r donors. If you select multiple (d) donor units for each recipient unit (by using the NDONORS= option in the PROC SURVEYIMPUTE statement), then the procedure selects d simple random samples independently.

Weighted Selection

Suppose there are m recipient units and r donor units in an imputation cell. Let w_i be the weight of the donor unit i. PROC SURVEYIMPUTE selects a probability proportional to donor weight, w_i, with replacement sample of size m from the r donors. The procedure uses the probability proportional to size sampling algorithm described in Särndal, Swensson, and Wretman (1992, p. 97). For more information about the weighted hot-deck method, see Shao and Tu (1995, p. 271), and Rao and Shao (1992).

Replication Variance Estimation

Replication methods are useful for estimating variances that account for both the sampling variability and the imputation variability. If you specify the METHOD=FEFI or the METHOD=FHDI option in the PROC SURVEYIMPUTE statement, then, by default, the procedure creates imputation-adjusted jackknife replicate weights unless you also specify the VARMETHOD=NONE option in the same statement. If you specify your own replicate weights by using the REPWEIGHTS statement and if you specify the METHOD=FEFI or the METHOD=FHDI option in the PROC SURVEYIMPUTE statement, then the procedure creates new replicate weights by adjusting the replicate weights that you provide for imputation. It does not create imputation-adjusted replicate weights when you specify the METHOD=HOTDECK option in the PROC SURVEYIMPUTE statement.

The SURVEYIMPUTE procedure does not compute any variances. The replicate weights that are created can be used in any SAS/STAT survey procedure for variance computation. For an example, see the section "Getting Started: SURVEYIMPUTE Procedure" on page 9581.

Replication methods draw multiple replicates (also called subsamples) from a full sample according to a specific resampling scheme. The most commonly used resampling schemes are the balanced repeated replication (BRR) method, the jackknife method, and the bootstrap method. For each replicate, the original weights are modified for the primary sampling units (PSUs) in the replicates to create replicate weights. The parameters of interest are estimated by using the replicate weights for each replicate. These estimates are also known as replicate estimates. Then the variances of parameters of interest are estimated by estimating variability among the replicate estimates. The SURVEYIMPUTE procedure automatically creates replicate weights based on the replication method that you specify; alternatively you can use the REPWEIGHTS statement to provide your own replicate weights.

The following subsections provide details about how the replication weights are created for each variance estimation method.

Bootstrap Method

The naive bootstrap variance estimator that is suitable for infinite population is not consistent when applied to complex surveys. Bootstrap replicate samples for complex surveys are created by using a simple random sample with replacement of primary sampling units (PSUs) within each stratum. PSUs in different strata are sampled independently. The original sampling weights are then adjusted in each replicate to reflect the full sample. These adjusted weights are also called bootstrap replicate weights. McCarthy and Snowden (1985), Rao and Wu (1988), Sitter (1992b), and Sitter (1992a) provide several adjusted bootstrap variance estimators that are consistent for complex surveys. For more information about bootstrap variance estimation for complex surveys, see Mashreghi, Haziza, and Léger (2016), Beaumont and Patak (2012), Lohr (2010, Section 9.3.3), Fuller (2009, Section 4.5), Wolter (2007, Chapter 5), and Shao and Tu (1995, Section 6.2.4).

If you do not provide replicate weights by using the REPWEIGHTS statement, then the BOOTSTRAP option in the PROC SURVEYIMPUTE statement creates bootstrap replicate weights for you. This bootstrap method is similar to the method of Rao, Wu, and Yue (1992) and is also known as bootstrap weights method (Mashreghi, Haziza, and Léger 2016).

If you use the FEFI or the FHDI method, then the unadjusted bootstrap weights are adjusted for the imputation to create the *imputation-adjusted replicate weights*. The section "Unadjusted Bootstrap Replicate Weights" on page 9640 describes how the unadjusted replicate weights are created, and sections "Imputation-Adjusted Replicate Weights" on page 9643 and "Replicate Weight Adjustments for FHDI" on page 9643 describe how the imputation-adjusted replicate weights are created.

Unadjusted Bootstrap Replicate Weights

Each replicate is obtained by selecting a simple random sample with replacement of m_h PSUs from stratum h. The rth bootstrap replicate weight for observation unit j in PSU i and stratum h is given by

$$w_{hij}^{(r)} = w_{hij}\left\{1 - \sqrt{(1-f_h)m_h/(n_h-1)} + \sqrt{(1-f_h)m_h/(n_h-1)}(n_h/m_h)k_{hi}^{(r)}\right\}$$

where $k_{hi}^{(r)}$ is the number of times PSU i in stratum h is selected in replicate sample r, and f_h is the sampling fraction in stratum h.

If you use the hot-deck imputation method, then you can use the OUTPUT statement to store the unadjusted replicate weights. The unadjusted replicate weights are not saved when you use the FEFI or FHDI method. You should use the imputation-adjusted replicate weights for variance estimation from a fractionally imputed data set.

For more information about how the bootstrap variance estimators are computed for related statistics, see the section "Bootstrap Method" in each of the following chapters: Chapter 115, "The SURVEYFREQ Procedure," Chapter 117, "The SURVEYLOGISTIC Procedure," Chapter 118, "The SURVEYMEANS Procedure," Chapter 119, "The SURVEYPHREG Procedure," and Chapter 120, "The SURVEYREG Procedure."

Balanced Repeated Replication (BRR) Method

The balanced repeated replication (BRR) method requires that the full sample be drawn by using a stratified sample design with two primary sampling units (PSUs) per stratum. The BRR method constructs half-sample replicates by deleting one PSU per stratum according to a Hadamard matrix and doubling the original weight of the other PSU in that stratum. If you use the FEFI or the FHDI method, then the unadjusted BRR weights are adjusted for the imputation to create the *imputation-adjusted replicate weights*. The sections "Unadjusted BRR Replicate Weights" on page 9640 and "Unadjusted Fay's BRR Replicate Weights" on page 9641 describe how the unadjusted replicate weights are created, and the section "Imputation-Adjusted Replicate Weights" on page 9643 describes how the imputation-adjusted replicate weights are created.

Unadjusted BRR Replicate Weights

Let H be the total number of strata. The total number of replicates, R, is the smallest multiple of 4 that is greater than H. However, if you prefer a larger number of replicates, you can specify the REPS=*n* *method-option*. If an $n \times n$ Hadamard matrix cannot be constructed, the number of replicates is increased until a Hadamard matrix becomes available.

Each replicate is obtained by deleting one PSU per stratum according to a corresponding Hadamard matrix and adjusting the original weights for the remaining PSUs. The new weights are called replicate weights.

Replicates are constructed by using the first H columns of the $R \times R$ Hadamard matrix. The rth ($r = 1, 2, \ldots, R$) replicate is drawn from the full sample according to the rth row of the Hadamard matrix as follows:

- If the (r, h) element of the Hadamard matrix is 1, then the first PSU of stratum h is included in the rth replicate and the second PSU of stratum h is excluded.
- If the (r, h) element of the Hadamard matrix is –1, then the second PSU of stratum h is included in the rth replicate and the first PSU of stratum h is excluded.

The replicate weights of the remaining PSUs in each half sample are then doubled to their original weights. For more information about the BRR method, see Wolter (2007) and Lohr (2010).

By default, PROC SURVEYIMPUTE generates an appropriate Hadamard matrix automatically to create the replicates. You can display the Hadamard matrix by specifying the VARMETHOD=BRR(PRINTH) *method-option*. If you provide a Hadamard matrix by specifying the VARMETHOD=BRR(HADAMARD=) *method-option*, then the replicates are generated according to the provided Hadamard matrix.

For more information about how the BRR variance estimators are computed for related statistics, see the section "Balanced Repeated Replication (BRR) Method" in each of the following chapters: Chapter 115, "The SURVEYFREQ Procedure," Chapter 117, "The SURVEYLOGISTIC Procedure," Chapter 118, "The SURVEYMEANS Procedure," Chapter 119, "The SURVEYPHREG Procedure," and Chapter 120, "The SURVEYREG Procedure."

Unadjusted Fay's BRR Replicate Weights

The traditional BRR method constructs half-sample replicates by deleting one PSU per stratum according to a Hadamard matrix and doubling the original weight of the other PSU. Fay's BRR method uses the Fay coefficient, ϵ ($0 \leq \epsilon < 1$), and instead of deleting one PSU per stratum, it multiplies the original weight by the coefficient ϵ. The original weight of the remaining PSU in that stratum is multiplied by $2 - \epsilon$. PROC SURVEYIMPUTE uses $\epsilon = 0.5$ as the default value; alternatively, you can specify a value for ϵ by using the FAY= *method-option*. When $\epsilon = 0$, Fay's method becomes the traditional BRR method. For more information, see Dippo, Fay, and Morganstein (1984); Fay (1984, 1989); Judkins (1990). Because the traditional BRR method uses only half of the total sample in every replicate, some observed levels of the analysis variables might not be available in the replicate samples. Fay's BRR method is especially useful in this situation because it uses all the sampled units in every replicate.

For more information about how Fay's BRR variance estimators are computed for related statistics, see the section "Balanced Repeated Replication (BRR) Method" in each of the following chapters: Chapter 115, "The SURVEYFREQ Procedure," Chapter 117, "The SURVEYLOGISTIC Procedure," Chapter 118, "The SURVEYMEANS Procedure," Chapter 119, "The SURVEYPHREG Procedure," and Chapter 120, "The SURVEYREG Procedure."

Hadamard Matrix

PROC SURVEYIMPUTE uses a Hadamard matrix to construct replicates for BRR variance estimation. You can provide a Hadamard matrix for replicate construction by using the HADAMARD= *method-option* for VARMETHOD=BRR. Otherwise, PROC SURVEYIMPUTE generates an appropriate Hadamard matrix. You can display the Hadamard matrix by specifying the PRINTH *method-option*.

A Hadamard matrix $\mathbf{A}$ of dimension R is a square matrix that has all elements equal to 1 or –1 such that $\mathbf{A}'\mathbf{A} = R\mathbf{I}$, where $\mathbf{I}$ is an identity matrix of appropriate order. The dimension of a Hadamard matrix must equal 1, 2, or a multiple of 4.

For example, the following matrix is a Hadamard matrix of dimension $k = 8$:

$$\begin{array}{rrrrrrrr}
1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
1 & -1 & 1 & -1 & 1 & -1 & 1 & -1 \\
1 & 1 & -1 & -1 & 1 & 1 & -1 & -1 \\
1 & -1 & -1 & 1 & 1 & -1 & -1 & 1 \\
1 & 1 & 1 & 1 & -1 & -1 & -1 & -1 \\
1 & -1 & 1 & -1 & -1 & 1 & -1 & 1 \\
1 & 1 & -1 & -1 & -1 & -1 & 1 & 1 \\
1 & -1 & -1 & 1 & -1 & 1 & 1 & -1
\end{array}$$

For BRR replicate construction, the dimension of the Hadamard matrix must be at least H, where H denotes the number of first-stage strata in your design. If a Hadamard matrix of a particular dimension exists, it is not necessarily unique. Therefore, if you want to use a specific Hadamard matrix, you must provide the matrix as a SAS data set in the HADAMARD= *method-option*. You must ensure that the matrix that you provide is actually a Hadamard matrix; PROC SURVEYIMPUTE does not check the validity of your Hadamard matrix.

For more information about how the Hadamard matrix is used to construct replicates for BRR variance estimation, see the section "Unadjusted BRR Replicate Weights" on page 9640.

Jackknife Method

The jackknife method of variance estimation deletes one PSU at a time from the full sample to create replicates. This method is also known as the delete-1 jackknife method because it deletes exactly one PSU in every replicate. The total number of replicates R is the same as the total number of PSUs. In each replicate, the sampling weights of the remaining PSUs are modified by the jackknife coefficient α_r. The modified weights are called *replicate weights*. If you use the FEFI or the FHDI method, then the unadjusted replicate weights are adjusted for the imputation to create the *imputation-adjusted replicate weights*. The section "Unadjusted Jackknife Replicate Weights" on page 9642 describes how the unadjusted replicate weights are created, and the section "Imputation-Adjusted Replicate Weights" on page 9643 describes how the imputation-adjusted replicate weights are created.

Unadjusted Jackknife Replicate Weights

Let PSU i in stratum h_r be omitted for the rth replicate. Then the jackknife coefficient, α_r, and replicate weights, $w_{hij}^{(r)}$, are computed as

$$\alpha_r = \begin{cases} \frac{n_{h_r}-1}{n_{h_r}} & \text{for a stratified design} \\ \frac{R-1}{R} & \text{for designs without stratification} \end{cases}$$

$$w_{hij}^{(r)} = \begin{cases} w_{hij} & \text{if observation unit } j \text{ is not in donor stratum } h_r \\ 0 & \text{if observation unit } j \text{ is in PSU } i \text{ of donor stratum } h_r \\ w_{hij}/\alpha_r & \text{if observation unit } j \text{ is not in PSU } i \text{ but is in donor stratum } h_r \end{cases}$$

If you use the hot-deck imputation method, then you can use the OUTPUT statement in PROC SURVEYIMPUTE to store the unadjusted replicate weights. The unadjusted replicate weights are not saved for the FEFI or the FHDI method. You should use the imputation-adjusted replicate weights for variance estimation

from a fractionally imputed data set. Use the OUTJKCOEFS= option in the OUTPUT statement to store the jackknife coefficients in a SAS data set.

For more information about how the jackknife variance estimators are computed for related statistics, see the section "Jackknife Method" in each of the following chapters: Chapter 115, "The SURVEYFREQ Procedure," Chapter 117, "The SURVEYLOGISTIC Procedure," Chapter 118, "The SURVEYMEANS Procedure," Chapter 119, "The SURVEYPHREG Procedure," and Chapter 120, "The SURVEYREG Procedure."

Imputation-Adjusted Replicate Weights

If you use the hot-deck imputation technique by specifying the METHOD=HOTDECK option in the PROC SURVEYIMPUTE statement, the procedure does not create imputation-adjusted replicate weights. Naive variance estimators that do not use imputation-adjusted replicate weights and assume the imputed data as the observed data might underestimate the true variance. For more information, see Haziza (2009); Särndal and Lundström (2005); Rao and Shao (1992).

If specify the METHOD=FEFI or the METHOD=FHDI option in the PROC SURVEYIMPUTE statement, the procedure adjusts the replicate weights for imputation. The imputation-adjusted replicate weights should be used with other SAS/STAT survey procedures to estimate the variance of an estimator that uses the imputed data. For more information, see Fuller (2009, Section 5.2.2) and Kim and Shao (2014, Section 4.6).

Let $w_i^{(r)}$ be the unadjusted replicate weight for observation unit i. To facilitate discussion, separate subscripts for strata, clusters, and imputation cells are omitted. The unadjusted replicate weights can come from a jackknife method as described in the section "Unadjusted Jackknife Replicate Weights" on page 9642, from a BRR method as described in the section "Unadjusted BRR Replicate Weights" on page 9640, or from a bootstrap method as described in the section "Unadjusted Bootstrap Replicate Weights" on page 9640, or they can be specified by using the REPWEIGHTS statement. The adjustment follows the similar EM-by-weighting algorithm that is described in the section "Fully Efficient Fractional Imputation" on page 9608 but uses the replicate weights, $w_i^{(r)}$, instead of the full sample weight, w_i.

In particular, the joint probabilities for the tth M-step and the rth replicate weight are computed by

$$\tilde{\pi}_{(t)}^{(r)}(\kappa_1 \cdots \kappa_P) = \left\{ \sum_i \sum_l w_i^{(r)} w_{il(t-1)}^{(r)} \right\}^{-1} \sum_i \sum_l w_i^{(r)} w_{il(t-1)}^{(r)} I(Z_{i1} = \kappa_1, \ldots, Z_{iP} = \kappa_P)$$

for all i, l, and $t > 0$.

The rth replicate fractional weights for the tth E-step is computed by

$$w_{il(t)}^{(r)} = \left\{ \sum_{k=1}^{M_l} \tilde{\pi}_{(t)}^{(r)}(\mathbf{Z}_{i,\mathrm{obs}}, \mathbf{Z}_{i,\mathrm{miss}[k]}) \right\}^{-1} \tilde{\pi}_{(t)}^{(r)}(\mathbf{Z}_{i,\mathrm{obs}}, \mathbf{Z}_{i,\mathrm{miss}[l]})$$

where M_l is the number of donor cells.

Replicate Weight Adjustments for FHDI

If you use the FHDI method (by specifying the METHOD=FHDI option in the PROC SURVEYIMPUTE statement), the procedure adjusts the replicate weights for imputation. You must use the imputation-adjusted replicate weights with other SAS/STAT survey procedures to estimate the variance of an estimator that uses the imputed data.

Let m_2 be the number of second-stage donor cells that are requested for FHDI (the value of the NDONORS= option in the PROC SURVEYIMPUTE statement), and let $m_{2u,i}$ be the unique number of selected second-stage donor cells for observation unit i. Further assume that $h_{l_2|l_1}$ is the number of times the second-stage donor cell l_2 is selected for first-stage donor cell l_1.

Let $w_i^{(r)}$ be the unadjusted replicate weight, $w_{il_1}^{(r)}$ be the first-stage fractional replicate weight, and $w_{il_2|l_1}^{(r)}$ be the second-stage replicate weight from two-stage FEFI for observation unit i, first-stage donor cell l_1, second-stage donor cell l_2, and replicate sample r. Let $M_{il_2|l_1}$ be the total number of second-stage donor cells conditional on the first-stage donor cell l_1 for observation unit i.

The following weight adjustments are available:

- *No adjustment*: If you specify the REPWTADJ=NONE option, then PROC SURVEYIMPUTE does not adjust the replicate weights for FHDI.

  The two-stage imputation-adjusted fractional replicate weight for the rth replicate sample for the second-stage donor cell l_2 in the first-stage donor cell l_1 for observation unit i is

  $$w_{il_1l_2}^{(r)} = \begin{cases} w_{il_1}^{(r)} w_{il_2|l_1}^{(r)} & , \quad M_{il_2|l_1} \le m_2 \\ w_{il_1}^{(r)} h_{l_2|l_1}/m_2 & , \quad M_{il_2|l_1} > m_2 \end{cases}$$

  where $l_2 = 1, 2, \ldots, \min(M_{il_2|l_1}, m_{2u,i})$.

  The two-stage imputation-adjusted replicate weight for observation unit i, first-stage donor cell l_1, and second-stage donor cell l_2 in the rth replicate sample is $w_i^{(r)} w_{il_1l_2}^{(r)}$.

- *Ratio adjustment*: If you specify the REPWTADJ=RATIO option, then PROC SURVEYIMPUTE adjusts the replicate weights for FHDI by using ratio adjustment.

  The two-stage imputation-adjusted fractional replicate weight for the rth replicate sample for the second-stage donor cell l_2 in the first-stage donor cell l_1 for observation unit i is

  $$w_{il_1l_2}^{(r)} = \begin{cases} w_{il_1}^{(r)} w_{il_2|l_1}^{(r)} & , \quad M_{il_2|l_1} \le m_2 \\ w_{il_1}^{(r)} \left[s_i^{(r)}\right]^{-1} h_{l_2|l_1} \left[w_{il_2|l_1}^{(r)}/w_{il_2|l_1}\right] & , \quad M_{il_2|l_1} > m_2 \end{cases}$$

  where $l_2 = 1, 2, \ldots, \min(M_{il_2|l_1}, m_{2u,i})$ and $s_i^{(r)} = \sum_{l_2=1}^{m_{2u,i}} \left[w_{il_2|l_1}^{(r)}/w_{il_2|l_1}\right] h_{l_2|l_1}$ is the sum of the ratios of the second-stage replicate fractional weight to the second-stage full sample fractional weight for observation unit i.

  If $w_{il_2|l_1}^{(r)} = 0$ for all selected second-stage donor cells in the rth replicate sample, then each selected second-stage donor cell is assigned a second-stage fractional weight of $h_{l_2|l_1}/m_2$.

  The two-stage imputation-adjusted replicate weight for observation unit i, first-stage donor cell l_1, and second-stage donor cell l_2 in the rth replicate sample is $w_i^{(r)} w_{il_1l_2}^{(r)}$.

- *Neighbor adjustment*: If you specify the REPWTADJ=NEIGHBOR option or if you do not specify the REPWTADJ= option, then PROC SURVEYIMPUTE adjusts the replicate weights for FHDI by using neighbor adjustment.

  Neighbor adjustment first computes the proportion of the full-sample fractional weights that fall in each of m_2 equally spaced intervals and then adjusts the replicate sample fractional weights by using the proportions from the full sample. Let $S_k = \sum_{j_2=1}^{k} w_{ij_2|l_1}$ be the cumulative sum of the second-stage

full-sample fractional weights for the first k second-stage donor cells. S_k depends on both i and l_1 but, for simplicity, subscripts i and l_1 are not used in S_k. By construction, $S_{k-1} \leq S_k$. Define factors α_{dk} according to how the interval $[S_{k-1}, S_k]$ for the kth second-stage donor cell overlaps with the dth equally spaced interval $[(d-1)/m_2, d/m_2]$:

$$\alpha_{dk} = \begin{cases} \frac{\min(S_k, \frac{d}{m_2}) - \max(S_{k-1}, \frac{d-1}{m_2})}{S_k - S_{k-1}} & , \quad \min(S_k, \frac{d}{m_2}) > \max(S_{k-1}, \frac{d-1}{m_2}) \\ 0 & , \quad \text{otherwise} \end{cases}$$

for $d = 1, 2, \ldots, m_2$ and $k = 1, 2, \ldots, M_{il_2|l_1}$. The replicate fraction for the second-stage donor cell l_2 is computed as

$$w^{*(r)}_{il_2|l_1} = \sum_{k=1}^{M_{il_2|l_1}} w^{(r)}_{ik|l_1} \alpha_{l_2 k}$$

for all $r = 1, 2, \ldots, R$, and $l_2 = 1, 2, \ldots, m_2$. Let $s^{*(r)}_i = \sum_{l_2=1}^{m_2} w^{*(r)}_{il_2|l_1}$.

The two-stage imputation-adjusted fractional replicate weight for the rth replicate sample for the second-stage donor cell l_2 in the first-stage donor cell l_1 for observation unit i is

$$w^{(r)}_{il_1l_2} = \begin{cases} w^{(r)}_{il_1} w^{(r)}_{il_2|l_1} & , \quad M_{il_2|l_1} \leq m_2 \\ w^{(r)}_{il_1} \left[s^{*(r)}_i \right]^{-1} w^{*(r)}_{il_2|l_1} & , \quad M_{il_2|l_1} > m_2 \end{cases}$$

where $l_2 = 1, 2, \ldots, \min(M_{il_2|l_1}, m_{2u,i})$.

If $w^{(r)}_{il_2|l_1} = 0$ for all selected second-stage donor cells in the rth replicate sample, then each selected second-stage donor cell is assigned a second-stage fractional weight of $h_{l_2|l_1}/m_2$, where $h_{l_2|l_1}$ is the number of times the second-stage donor cell l_2 is selected.

The two-stage imputation-adjusted replicate weight for observation unit i, first-stage donor cell l_1, and second-stage donor cell l_2 in the rth replicate sample is $w^{(r)}_i w^{(r)}_{il_1l_2}$.

Output Data Sets

PROC SURVEYIMPUTE creates an output data set to store the imputed data and the replicate weights, and an output data set to store the jackknife coefficients for jackknife variance estimation. You can use the Output Delivery System (ODS) to create a SAS data set from any piece of PROC SURVEYIMPUTE output. For more information, see the section "Displayed Output" on page 9646.

OUT= Output Data Set

You can use the OUTPUT statement to create a data set to store the imputed data. The OUTPUT OUT= data set contains all the variables from the input data set, imputed values for missing values for the variables in the VAR statement, and some observation-level quantities. These quantities can include the fractionally adjusted weights, replicate weights, recipient numbers, and donor identifications.

Jackknife Coefficients Output Data Set

If you specify the OUTJKCOEFS= option in the OUTPUT statement, PROC SURVEYIMPUTE stores the jackknife coefficients in an output data set. The OUTJKCOEFS= output data set contains one observation for each replicate. The OUTJKCOEFS= data set contains the following variables:

- Replicate: the replicate number for the jackknife coefficient
- JKCoefficient: the jackknife coefficient for the replicate
- DonorStratum: the stratum of the PSU that was deleted to construct the replicate, if you use a STRATA statement

You can use the JKCOEFS= option in the REPWEIGHTS statement in any SAS/STAT survey procedure to provide jackknife coefficients for that procedure. If the jackknife coefficients are different from $(R-1)/R$, where R is the total number of replicates, then you must provide the jackknife coefficients to correctly estimate the variance.

Displayed Output

If you use the NOPRINT option in the PROC SURVEYIMPUTE statement, the procedure does not display any output. Otherwise, PROC SURVEYIMPUTE displays results of the imputation in a collection of tables, which are described in the following subsections.

Class Level Information

If you use a CLASS statement, PROC SURVEYIMPUTE displays a “Class Level Information” table, which lists the categories of every CLASS variable that is used in the imputation. The ODS name of the “Class Level Information” table is ClassLevelInfo.

Convergence Status

If you specify METHOD=FEFI or METHOD=FHDI, PROC SURVEYIMPUTE displays a “Convergence Status” table, which shows the convergence status of the EM optimization routine. If the optimization routine converges, then the Status is set to 0; otherwise, the Status is set to 1. The ODS name of the “Convergence Status” table is ConvergenceStatus.

Design Summary

If you use a STRATA or CLUSTER statement, PROC SURVEYIMPUTE displays a “Design Summary” table, which provides information about the sample design. The table displays the total number of strata that are read and used, and the total number of clusters that are read and used. The ODS name of the “Design Summary” table is DesignSummary.

Donor Count

If you specify METHOD=FEFI or METHOD=FHDI, PROC SURVEYIMPUTE displays a “Donor Count” table, which shows the number of donor cells in the first-stage FEFI and the number of recipient units that use those donor cells. The ODS name of the “Donor Count” table is DonorCount.

Hadamard Matrix

If you specify the PRINTH *method-option* for VARMETHOD=BRR, PROC SURVEYIMPUTE displays the Hadamard matrix that is used to construct replicates for BRR variance estimation. If you provide a Hadamard matrix by using the HADAMARD= *method-option* for VARMETHOD=BRR but the procedure does not use the entire matrix, the procedure displays only the rows and columns that are actually used to construct replicates. The ODS name of the "Hadamard Matrix" table is HadamardMatrix.

Imputation Information

By default, PROC SURVEYIMPUTE displays an "Imputation Information" table, which provides information about the imputation method. The table displays the two-level name of the input data set, the name and label of the WEIGHT variable, the name and label of each STRATA variable, the name and label of each CLUSTER variable, the name of the imputation method used, the random number generator seed, the name of the replication method, and the number of replicates. The ODS name of the "Imputation Information" table is ImputationInfo.

Imputation Summary

By default, PROC SURVEYIMPUTE displays an "Imputation Summary" table, which provides summary information about the imputation. The table displays the number of observations and the sum of weights for the following:

- Nonmissing observations – all variables specified in the VAR statement have nonmissing values
- Missing – at least one variable specified in the VAR statement has a missing value
- Missing, Imputed – all missing values have been imputed
- Missing, Not Imputed – no missing values are imputed
- Missing, Partially Imputed – missing values in some variables are imputed, but missing values in some other variables are not imputed

The ODS name of the "Imputation Summary" table is ImputationSummary.

Iteration History

If you specify METHOD=FEFI or METHOD=FHDI, PROC SURVEYIMPUTE displays an "Iteration History" table, which provides information about the iteration history for the EM algorithm. The table displays iteration numbers, maximum absolute differences, and maximum relative absolute differences for the fractional weights over all the observations. The ODS name of the "Iteration History" table is IterationHistory.

Missing Data Patterns

By default, PROC SURVEYIMPUTE displays a "Missing Data Patterns" table, which provides information about the missing data patterns. The table displays the missing data pattern groups, "X" if the variable is observed in the group, and "." if the variable is missing in that group. In addition, it displays observation frequencies, the sum of weights, unweighted percentages, and weighted percentages for each group. The ODS name of the "Missing Data Patterns" table is MissPattern.

Number of Observations

By default, PROC SURVEYIMPUTE displays a "Number of Observations" table, which shows the number of observations that are read and used, and the sum of weights that are read and used in the imputation. The ODS name of the "Number of Observations" table is NObs.

Stratum Information

If you specify the LIST option in the STRATA statement, PROC SURVEYIMPUTE displays a "Stratum Information" table. This table provides the following information for each stratum:

- Stratum Index, which is a sequential stratum identification number
- STRATA variables, which list the levels of STRATA variables for the stratum
- Number of Observations, which is the number of observations used in the stratum
- Number of Clusters, which is the number of clusters in the stratum, if you specify a CLUSTER statement
- Sum of Weights, which is the sum of the weights for observations in the stratum
- Sampling Rate for the stratum, if you specify the TOTAL= or RATE= option

The ODS name of the "Stratum Information" table is StrataInfo.

Weighted Moments

If you specify METHOD=FHDI(DISP=MEAN) or METHOD=FHDI(DISP=SSCP), PROC SURVEYIMPUTE displays a "Weighted Moments" table, which shows the weighted means and weighted mean-squared deviations from both two-stage FEFI and FHDI for the variables that are specified in the VAR statement but not in the CLASS statement. The weighted moments for two-stage FEFI are computed by using imputation-adjusted weights from two-stage FEFI, and the weighted moments for FHDI are computed by using imputation-adjusted weights from FHDI. The ODS name of the "Weighted Moments" table is ContMean.

Weighted Mean SSCP for FEFI

If you specify METHOD=FHDI(DISP=SSCP), PROC SURVEYIMPUTE displays a "Weighted Mean SSCP for FEFI" table, which shows the weighted mean SSCP from two-stage FEFI for the variables that are specified in the VAR statement but not in the CLASS statement. The weighted mean SSCP matrix is computed by using imputation-adjusted weights from two-stage FEFI. The ODS name of the "Weighted Mean SSCP for FEFI" table is ContMSFEFI.

Weighted Mean SSCP for FHDI

If you specify METHOD=FHDI(DISP=SSCP), PROC SURVEYIMPUTE displays a "Weighted Mean SSCP for FHDI" table, which shows the weighted mean SSCP from FHDI for the variables that are specified in the VAR statement but not in the CLASS statement. The weighted mean SSCP matrix is computed by using imputation-adjusted weights from FHDI. The ODS name of the "Weighted Mean SSCP for FHDI" table is ContMSFHDI.

ODS Table Names

PROC SURVEYIMPUTE assigns a name to each table that it creates. You can use this name to refer to the table when you use the Output Delivery System (ODS) to select tables and create output data sets. For more information about ODS, see Chapter 20, "Using the Output Delivery System." Table 116.5 lists the table names.

Table 116.5 ODS Tables Produced by PROC SURVEYIMPUTE

ODS Table Name	Description	Statement	Option
ClassLevelInfo	CLASS variable levels	CLASS	
ContMean	Weighted moments	PROC	METHOD=FHDI(DISP=MEAN | SSCP)
ContMSFEFI	Weighted mean SSCP for FEFI	PROC	METHOD=FHDI(DISP=SSCP)
ContMSFHDI	Weighted mean SSCP for FHDI	PROC	METHOD=FHDI(DISP=SSCP)
ConvergenceStatus	Convergence status	PROC	METHOD=FEFI | FHDI
DesignSummary	Design summary	STRATA or CLUSTER	
DonorCount	Donor count	PROC	METHOD=FEFI | FHDI
HadamardMatrix	Hadamard matrix	PROC	VARMETHOD=BRR (PRINTH)
ImputationInfo	Imputation information	PROC	
ImputationSummary	Imputation summary	PROC	
IterationHistory	Iteration history	PROC	METHOD= FEFI | FHDI
MissPattern	Missing data patterns	PROC	
NObs	Number of observations	PROC	
StrataInfo	Stratum information	STRATA / LIST	

Examples: SURVEYIMPUTE Procedure

Example 116.1: Approximate Bayesian Bootstrap Imputation

This example illustrates the approximate Bayesian bootstrap hot-deck imputation method by using a simulated data set from a fictitious survey of drug abusers. A stratified clustered sample of drug abuse treatment centers is taken from a list of available treatment centers. The list is first stratified based on geographic locations. From each strata, two or three treatment centers are sampled as the primary sampling units (PSU). Data are collected from individual patients within the selected treatment centers. The survey collects information about the substances that the patients used (such as drugs, alcohol, and marijuana) along with insurance information and treatment information.

The data set contains 736 observation units in 35 PSUs and 10 strata. The sum of the weights is 19,600. Therefore, the survey data represent a population of 19,600 patients from the study area. Some participants did not respond to all questions. The data set contains missing values in many variables.

To impute the missing items, you first need to decide whether to impute within imputation cells. Imputation cells divide the data into groups of similar units such that the recipient units share similar characteristics with the donor units in the same group. For example, it is reasonable to believe that different age groups, races, and income categories might have different responses to the drug abuse survey. You can use these characteristics to create imputation cells. Characteristics for imputation cells might come from the same survey or might come from other sources such as census data or previous surveys. In this example, assume that the imputation cells are available as a variable called ImputationCell in the data set.

The data set DrugAbuse contains the following items:

- Strata: stratum identification
- PSU: PSU identification (treatment centers)
- ObsWeight: observation weight for patients
- ImputationCell: imputation cell identification
- Age: age, in years
- Sex: 1 for female and 2 for male
- Race: 1 for white, 2 for black, and 3 for others
- Insurance: 1 if the patient has any insurance, and 2 otherwise
- Drug: 1 if the patient used any drugs in the past three months, and 2 otherwise
- Alcohol: 1 if the patient consumed any alcohol in the past month, and 2 otherwise
- Treatment: 1 if the patient is being treated for the first time, and 2 otherwise

```
data DrugAbuse;
   input Strata PSU ObsWeight ImputationCell Age Sex Race Insurance
         Drug Alcohol Treatment;
   datalines;
 1    1     5        1      74  1    1      3       2      2        1
 1    1     5        1      20  0    3      1       2      2        1
 1    1     5        3      42  1    2      1       1      2        1
 1    1     5        3      65  1    3      2       1      2        1
 1    1     5        2      53  1    1      1       1      1        1
 1    1     5        3      49  1    1      1       1      2        1
 1    1     5        3      51  0    2      1       2      1        1
 1    1     5        2      77  0    3      1       1      1        1
 1    1     5        2      26  1    1      1       1      2        1
 1    1     5        3      28  0    3      1       1      1        1
 1    1     5        1      71  1    1      1       2      2        1
 1    1     5        2      72  1    1      3       2      2        1
 1    1     5        3      24  1    1      1       1      1        1
 1    1     5        2      65  1    1      2       1      1        2
 1    1     5        3      47  1    1      1       1      1        1
 1    1     5        2      37  1    1      2       1      2        1
```

```
 1    1     5        2      46  1    1      3       1      1        1
 1    1     5        2      52  1    1      1       1      2        2
 1    1     5        3      60  0    3      1       1      2        1
 1    1     5        1      31  0    1      1       1      2        1
 1    2     5        1      23  0    3      3       1      1        1
 1    2     5        2      78  1    1      .       .      .        .
 1    2     5        2      29  1    1      1       1      1        1
 1    2     5        2      21  .    .      .       .      .        .

   ... more lines ...

10    4  55.5556      1      40  0    3      2       1      1        2
10    4  55.5556      1      32  1    3      1       2      2        1
10    4  55.5556      3      68  0    1      2       2      1        2
10    4  55.5556      3      35  1    1      2       1      2        2
;
```

The following statements request that the missing items be imputed by using the approximate Bayesian bootstrap hot-deck imputation method:

```
proc surveyimpute data=DrugAbuse method=hotdeck(selection=abb)
                  ndonors=5 seed=773269;
   var Sex Race Insurance Drug Alcohol Treatment;
   cells ImputationCell;
   output out=DrugAbuseABB;
run;
```

The PROC SURVEYIMPUTE statement invokes the procedure, the DATA= option specifies the input data set DrugAbuse, the METHOD= option requests the hot-deck imputation method, the METHOD=HOTDECK(SELECTION=ABB) option requests the approximate Bayesian bootstrap method, the NDONORS= option requests five donor units for every recipient unit, and the SEED= option specifies the random number generator seed. The VAR statement specifies the variables that are to be imputed, the CELLS statement identifies the imputation cell variable ImputationCell, and the OUT= option in the OUTPUT statement names the output data set DrugAbuseABB.

You do not need to use WEIGHTS, STRATA, and CLUSTER statements for the approximate Bayesian bootstrap method unless you want to create the jackknife replication weights by including the VARMETHOD=JACKKNIFE option in the PROC SURVEYIMPUTE statement. The selection of donors does not use the design information. However, if you want to select donors from the same strata or the same group of clusters, then you must include that information in the imputation cell.

Summary information about the imputation method, number of observations, and missing data patterns is shown in Output 116.1.1. The "Imputation Information" table summarizes the imputation method. The "Number of Observations" table shows that PROC SURVEYIMPUTE read and used all 736 observations. The "Missing Data Pattern" table displays the missing patterns in the data set. There are four different missing data pattern groups: all items observed, one item missing, four items missing, and all items missing. Of the observation units, 92.53% have all items observed; 4.64% have missing values in Treatment; 1.77% have missing values in Insurance, Drug, Alcohol, and Treatment; and 1.09% have missing values in all variables. Because the WEIGHT statement is not specified, these percentages represent the percentages of missing units in the input data.

Output 116.1.1 Imputation Summary

The SURVEYIMPUTE Procedure

Imputation Information	
Data Set	WORK.DRUGABUSE
Imputation Method	HOTDECK
Selection Method	ABB
Random Number Seed	773269
Replication Method	NONE

Number of Observations Read	736
Number of Observations Used	736

Missing Data Patterns

Group	Sex	Race	Insurance	Drug	Alcohol	Treatment	Freq	Sum of Weights	Unweighted Percent	Weighted Percent
1	X	X	X	X	X	X	681	681	92.53	92.53
2	X	X	X	X	X	.	34	34	4.62	4.62
3	X	X	.	.	.	.	13	13	1.77	1.77
4	.	.	.	.	.	.	8	8	1.09	1.09

Missing Data Patterns

Group Means

Group	Sex	Race	Insurance	Drug	Alcohol	Treatment
1	0.566814	1.491924	1.718062	1.292217	1.716593	1.201175
2	0.500000	1.441176	1.588235	1.294118	1.588235	.
3	0.692308	1.230769	.	.	.	.
4	.	.	.	.	.	.

Imputation Summary

Observation Status	Number of Observations	Sum of Weights
Nonmissing	681	681
Missing	55	55
Missing, Imputed	55	55
Missing, Not Imputed	0	0

Some selected observations from the output data set are displayed in Output 116.1.2. The output data set DrugAbuseABB contains the unit identification, the recipient index, and all the variables from the input data set DrugAbuse. Units that are complete respondents have one row, but units that are incomplete respondents have five rows in the output data set. For example, unit 21 is a complete respondent, so it has only one row in the output data set and its ImpIndex value is 0. Unit 22 is an incomplete respondent, so it has five rows in the output data set and its ImpIndex values range from 1 to 5.

Output 116.1.2 Observations for Some Selected Units

UnitID	ImpIndex	Strata	PSU	ObsWeight	ImputationCell	Age	Sex	Race	Insurance	Drug	Alcohol	Treatment
20	0	1	1	5	1	31	0	1	1	1	2	1
21	0	1	2	5	1	23	0	3	3	1	1	1
22	1	1	2	5	2	78	1	1	1	1	1	1
22	2	1	2	5	2	78	1	1	1	1	1	1
22	3	1	2	5	2	78	1	1	2	1	2	1
22	4	1	2	5	2	78	1	1	3	1	2	1
22	5	1	2	5	2	78	1	1	1	1	2	2
23	0	1	2	5	2	29	1	1	1	1	1	1
24	1	1	2	5	2	21	1	2	2	1	2	2
24	2	1	2	5	2	21	1	3	1	1	1	1
24	3	1	2	5	2	21	1	2	2	1	2	1
24	4	1	2	5	2	21	1	1	2	1	2	1
24	5	1	2	5	2	21	1	2	2	2	1	1
25	0	1	2	5	3	85	0	1	3	1	2	1

Suppose you want to perform a logistic regression analysis by using the imputed data set. If you want to use the multiple imputation variance estimator that is available in the MIANALYZE procedure with the imputed data set, then you need to create one complete data set for every imputation. The following SAS statements create five complete data sets and then merge the five data sets into one. Each complete data set contains the complete respondents and only one donor unit for the incomplete respondents. Each data set also contains the imputation number (_Imputation_).

```
data DAIMP;
   set DrugAbuseABB;
   if (ImpIndex = 0) then do;  /* Include complete respondents */
      do _Imputation_=1 to 5;   /* in all imputations.          */
         output;
      end;
   end;
   else do;                     /* Put incomplete respondents   */
      _Imputation_ = ImpIndex; /* in separate imputations.     */
      output;
   end;
proc sort data=DAIMP;
   by _Imputation_ UnitID;
run;
```

The following SAS statements first use the SURVEYLOGISTIC procedure (see Chapter 117, "The SURVEYLOGISTIC Procedure") to perform separate logistic regression analyses within the imputed data sets and use the MIANALYZE procedure (Chapter 80, "The MIANALYZE Procedure") to combine the logistic regression results from five imputed data sets:

```
ods select none;
proc surveylogistic data=DAIMP;
   by _imputation_;
   class Treatment Insurance Sex Race;
   strata Strata;
   cluster PSU;
   weight ObsWeight;
   model Drug=Treatment Insurance Age Sex Race / covb;
   ods output parameterestimates=Estimates covb=Covariances;
run;
ods select all;

proc mianalyze parms(classvar=classval)=Estimates
               covb(effectvar=stacking)=Covariances
               edf=25;
   class Treatment Insurance Sex Race;
   modeleffects Intercept Treatment Insurance Age Sex Race;
   ods output parameterestimates=ABBLogisticAnalysis;
run;
```

Although the survey design information was not directly used in the imputation, you must use the complete design information, including strata, clusters, and weights, to estimate the design variance within each imputed data set. The STRATA, CLUSTER, and WEIGHT statements in PROC SURVEYLOGISTIC specify the design information. However, separate logistic regression results from any single imputed data set should not be used for inference.

Degrees of freedom values for survey data are often much less than the number of observation units. In this example, there are 736 observation units, but there are 35 PSUs in 10 strata. The degrees of freedom for the Taylor series linearized variance estimator is 25 (35 – 10). You should specify the reduced degrees of freedom by using the EDF= option in PROC MIANALYZE. For more information, see the section "EDF=*number*" on page 6483 in Chapter 80, "The MIANALYZE Procedure"; also see Barnard and Rubin (1999).

The estimated regression parameters and their standard errors from a multiply imputed data set are shown in Output 116.1.3.

Output 116.1.3 Logistic Regression Analysis Using a Multiply Imputed Data Set

The MIANALYZE Procedure

Parameter Estimates (5 Imputations)											
Parameter	**Treatment**	**Insurance**	**Sex**	**Race**	**Estimate**	**Std Error**	**95% Confidence Limits**		**DF**	**Minimum**	**Maximum**
Intercept					0.527080	0.232094	0.04656	1.007603	22.658	0.492600	0.574832
Treatment	1				0.094937	0.153297	-0.22225	0.412121	22.916	0.078459	0.114233
Insurance		1			-0.128475	0.144781	-0.42822	0.171268	22.671	-0.157661	-0.108998
Insurance		2			-0.038353	0.119353	-0.28536	0.208658	22.816	-0.059264	-0.024690
Age					0.001926	0.004635	-0.00767	0.011524	22.577	0.000858	0.002539
Sex			0		-0.088823	0.088702	-0.27265	0.095000	22.279	-0.101860	-0.063631
Race				1	0.436564	0.156414	0.11307	0.760060	23.092	0.418673	0.443484
Race				2	-0.111091	0.195368	-0.51509	0.292904	23.16	-0.118899	-0.096429

Parameter Estimates (5 Imputations)							
Parameter	**Treatment**	**Insurance**	**Sex**	**Race**	**Theta0**	**t for H0: Parameter=Theta0**	**Pr > |t|**
Intercept					0	2.27	0.0330
Treatment	1				0	0.62	0.5418
Insurance		1			0	-0.89	0.3842
Insurance		2			0	-0.32	0.7509
Age					0	0.42	0.6817
Sex			0		0	-1.00	0.3274
Race				1	0	2.79	0.0104
Race				2	0	-0.57	0.5751

Example 116.2: Fully Efficient Fractional Imputation

This example illustrates the fully efficient fractional imputation (FEFI) method by using the data set DrugAbuse from a fictitious survey of drug abusers from Example 116.1. The survey collects information about substance that are used (such as drugs, alcohol, and marijuana) along with insurance information and treatment information. Some participants did not respond to all questions. The data set contains 736 observation units in 35 PSUs and 10 strata. The sum of the weights is 19,600. The data set contains missing values for many variables.

As in Example 116.1, to impute the missing items, you first need to decide whether to impute within imputation cells. Imputation cells divide the data into groups of similar units such that the recipient units share similar characteristics with the donor units in the same group. For example, it is reasonable to believe that different age groups, races, and income categories might have different responses to the drug abuse survey. You can use these characteristics to create imputation cells. Characteristics for imputation cells might come from the same survey or from other sources such as census data or previous surveys. In this example, assume that the imputation cells are available as a variable called ImputationCell in the data set.

The following statements request that the missing items be imputed by using the FEFI method:

```
proc surveyimpute data=DrugAbuse method=FEFI varmethod=Jackknife;
   class Sex Race Insurance Drug Alcohol Treatment;
   var   Sex Race Insurance Drug Alcohol Treatment;
   cells ImputationCell;
   strata Strata;
   cluster PSU;
   weight ObsWeight;
   output out=DrugAbuseFEFI outjkcoefs=DrugAbuseJKCOEFS;
run;
```

The PROC SURVEYIMPUTE statement invokes the procedure, the DATA= option specifies the input data set DrugAbuse, the METHOD= option requests the FEFI method, and the VARMETHOD= option requests that imputation-adjusted jackknife replicate weights be created. The VAR statement specifies the variables that are to be imputed, and the CELLS statement identifies the imputation cell variable ImputationCell. Because no IMPJOINT statements are specified, all the variables in the VAR statement are to be imputed by using their joint categories. For more information, see the section "IMPJOINT Statement" on page 9598. The STRATA, CLUSTER, and WEIGHT statements specify the strata, cluster, and weight variables. The OUT= option in the OUTPUT statement names the output data set DrugAbuseFEFI to store the imputed values, and the OUTJKCOEFS= option in the OUTPUT statement names the output data set DrugAbuseJKCOEFS to store the jackknife coefficients.

Summary information about the imputation method, number of observations, and survey design is shown in Output 116.2.1. The "Imputation Information" table summarizes the imputation method. The "Number of Observations" table displays the number of observations that are read and used (736) and the weighted number of observation that are read and used (19,600) by PROC SURVEYIMPUTE. The "Design Information" table shows that there are 35 PSUs and 10 strata.

Output 116.2.1 Imputation Information

The SURVEYIMPUTE Procedure

Imputation Information	
Data Set	WORK.DRUGABUSE
Weight Variable	ObsWeight
Stratum Variable	Strata
Cluster Variable	PSU
Imputation Method	FEFI
Replication Method	JACKKNIFE
Number of Replicates	35

Number of Observations Read	736
Number of Observations Used	736
Sum of Weights Read	19599.9937
Sum of Weights Used	19599.9937

Design Summary	
Number of Strata	10
Number of Clusters	35

Selected observations for some variables from the output data set are displayed in Output 116.2.2. The output data set, DrugAbuseFEFI, contains unit identification, the recipient index, imputation-adjusted full-sample weights, imputation-adjusted jackknife weights, and all the variables from the input data set DrugAbuse. The output data set contains 35 sets of replicate weights, but only the first three sets of replicate weights are shown in Output 116.2.2. Units that are complete respondents have one row, but units that are incomplete respondents have multiple rows in the output data set. For example, unit 21 is a complete respondent, so it has only one row in the output data set and its ImpIndex value is 0. Unit 22 is an incomplete respondent; it has 20 rows in the output data set, its ImpIndex values range from 1 to 20, and its imputation-adjusted full-sample weights (ImpWt) range from 0.02 to 1.02. The sum of ImpWt for all rows (donor cells) for observation unit 22 is 5, which is the full sample weight for unit 22.

Output 116.2.2 Observations for Selected Units

UnitID	ImpIndex	ImpWt	Strata	PSU	ObsWeight	ImputationCell	Sex	Race	Insurance	Drug
20	0	5.00000	1	1	5	1	0	1	1	1
21	0	5.00000	1	2	5	1	0	3	3	1
22	1	0.49238	1	2	5	2	1	1	1	1
22	2	1.01597	1	2	5	2	1	1	1	1
22	3	0.14661	1	2	5	2	1	1	1	1
22	4	0.11496	1	2	5	2	1	1	1	2
22	5	0.03894	1	2	5	2	1	1	1	2
22	6	0.32730	1	2	5	2	1	1	1	2
22	7	0.21661	1	2	5	2	1	1	1	2
22	8	0.24024	1	2	5	2	1	1	2	1
22	9	0.10453	1	2	5	2	1	1	2	1
22	10	0.46726	1	2	5	2	1	1	2	1
22	11	0.19382	1	2	5	2	1	1	2	1
22	12	0.37531	1	2	5	2	1	1	2	2
22	13	0.03697	1	2	5	2	1	1	2	2
22	14	0.15533	1	2	5	2	1	1	3	1
22	15	0.08672	1	2	5	2	1	1	3	1
22	16	0.69416	1	2	5	2	1	1	3	1
22	17	0.03688	1	2	5	2	1	1	3	1
22	18	0.02106	1	2	5	2	1	1	3	2
22	19	0.18442	1	2	5	2	1	1	3	2
22	20	0.05053	1	2	5	2	1	1	3	2
23	0	5.00000	1	2	5	2	1	1	1	1

Alcohol	Treatment	ImpRepWt_1	ImpRepWt_2	ImpRepWt_3
2	1	0.00000	6.66667	6.66667
1	1	6.66667	0.00000	6.66667
1	1	0.65757	0.00000	0.66513
2	1	1.36836	0.00000	1.33813
2	2	0.18561	0.00000	0.19845
1	1	0.15441	0.00000	0.15268
1	2	0.05231	0.00000	0.05172
2	1	0.44358	0.00000	0.43861
2	2	0.29074	0.00000	0.28749
1	1	0.32268	0.00000	0.31907
1	2	0.12908	0.00000	0.14255
2	1	0.61595	0.00000	0.62442
2	2	0.26067	0.00000	0.25730
2	1	0.50409	0.00000	0.49845
2	2	0.04966	0.00000	0.04911
1	1	0.19731	0.00000	0.21002
1	2	0.11647	0.00000	0.11517
2	1	0.93613	0.00000	0.92566
2	2	0.04953	0.00000	0.04897
1	1	0.02828	0.00000	0.02796
2	1	0.23638	0.00000	0.24865
2	2	0.06788	0.00000	0.06712
1	1	6.66667	0.00000	6.66667

You can use the imputed data set and the imputation-adjusted replicate weights to compute any estimators from your imputed data. You can use the REPWEIGHTS statement in any SAS/STAT survey analysis procedures to specify the imputation-adjusted replicate weights. For example, the following statements use PROC SURVEYLOGISTIC to perform logistic regression analysis of the imputed data:

```
proc surveylogistic data=DrugAbuseFEFI varmethod=Jackknife;
   class Treatment Insurance Sex Race;
   model Drug=Treatment Insurance Age Sex Race;
   weight ImpWt;
   repweights ImpRepWt_: / jkcoefs=DrugAbuseJKCOEFS;
   ods output parameterestimates=FEFILogisticAnalysis;
run;
```

The WEIGHT statement specifies the imputation-adjusted full-sample weight (ImpWt), and the REPWEIGHTS statement specifies the imputation-adjusted replicate weights (ImpRepWt_1, . . . , ImpRepWt_35). The JKCOEFS= option in the REPWEIGHTS statement specifies the jackknife coefficients.

The parameter estimates and their standard errors are displayed in Output 116.2.3. The variance estimators correctly account for both the design variability and the imputation variability.

Output 116.2.3 Logistic Regression Analysis of the Fractionally Imputed Data Set

The SURVEYLOGISTIC Procedure

Analysis of Maximum Likelihood Estimates

Parameter		Estimate	Standard Error	t Value	Pr > |t|
Intercept		0.5105	0.2281	2.24	0.0317
Treatment	1	0.1048	0.1600	0.65	0.5168
Insurance	1	-0.1152	0.1454	-0.79	0.4337
Insurance	2	-0.0461	0.1183	-0.39	0.6988
Age		0.00195	0.00459	0.42	0.6736
Sex	0	-0.0719	0.0931	-0.77	0.4452
Race	1	0.4463	0.1574	2.84	0.0075
Race	2	-0.1212	0.2110	-0.57	0.5695

NOTE:
The degrees of freedom for the t tests is 35.

Example 116.3: Fully Efficient Fractional Imputation, Fay's Balanced Repeated Replication, and Domain Analysis

This example demonstrates the FEFI method by using data from the third National Health and Nutrition Examination Survey (NHANES III). The data set contains a set of BRR replicate weights. The REPWEIGHTS statement in PROC SURVEYIMPUTE is used to create imputation-adjusted replicate weights. The imputed data set and the imputation-adjusted replicate weights are then used in PROC SURVEYFREQ to create crosstabulation tables and to perform domain analysis.

The objective of NHANES is to study the health and nutritional status of the US population. NHANES uses a multistage stratified area sample with typically two PSUs per stratum. Strata are created based on geographic location, Metropolitan Statistical Areas (MSAs), and other demographics. An MSA or a group of counties are selected as PSUs from each stratum. Sampling weights are unequal because of different selection

probabilities among different subgroups and for reasons such as nonresponse and undercoverage. For more information about NHANES, see http://www.cdc.gov/nchs/nhanes/about_nhanes.htm.

NHANES III data contain missing values in many items. Multiple imputation was used to impute some of the missing items. Five multiply imputed data sets are available for public use. Because FEFI will be used in this example to impute the missing values, you need the observed data, the missing (or imputation) flag for every item, and only one imputed data set. The data sets Core and IMP1 have been downloaded from the Centers for Disease Control and Prevention's website (https://www.cdc.gov/). The Core data set contains the demographic variables, full sample weights, replicate weights, and imputation flags. The replicate weights are created by using Fay's BRR method with a Fay coefficient of 0.3. The IMP1 data set contains the first version of the five multiply imputed data sets.

For this example, a new data set, Smoke, is created by merging the Core and IMP1 data sets by the observation sequence number, SEQN. The Smoke data set contains the following items:

- SEQN: observation sequence number
- WTPFQX6: observation weight
- WTPQRP1 to WTPQRP52: 52 replicate weights from the BRR method
- DMARETHN: race-ethnicity; 1 for white, 2 for black, 3 for Mexican American, and 4 for other
- HSSEX: gender; 1 for male and 2 for female
- HFF1IF: imputation flag for HFF1MI; 1 for observed and 2 for imputed
- HAN6SRIF: imputation flag for HAN6SRMI; 0 for not applicable, 1 for observed, and 2 for imputed
- HAR3RIF: imputation flag for HAR3RMI; 0 for not applicable, 1 for observed, and 2 for imputed
- HAT28IF: imputation flag for HAT28MI; 0 for not applicable, 1 for observed, and 2 for imputed
- HFF1MI: anyone smokes cigarettes in the home; 1 for yes, and 2 for no
- HAN6SRMI: beer, wine, or liquor per month; –9 for not applicable, 1 for 0 time in the past month, 2 for 1 to 10 times in the past month, and 3 for more than 10 times in the past month
- HAR3RMI: smoke cigarettes now; –9 for not applicable, 1 for yes, and 2 for no
- HAT28MI: activity level compared to others; –9 for not applicable, 1 for more active, 2 for less active, and 3 for about the same
- Education: highest education attained; levels are elementary, high school, college, and unknown

For donor-based imputation methods, auxiliary information is used to create imputation cells. Imputation cells divide the data into groups of similar units such that the recipient units share similar characteristics with the donor units in the same group. Characteristics for imputation cells might come from the same survey or from other auxiliary sources such as census data or previous surveys. The cell identification is known for every unit in the sample. Categorical levels of auxiliary variables are often used to create imputation cells. For a helpful review, see Brick and Kalton (1996). For the purpose of this example, seven imputation cells were created by using only two demographic variables: race-ethnicity status (DMARETHN) and gender

(HSSEX). Both variables are available in the Core data set, and both have no missing values. The imputation cells are identified by the variable ImputationCells in the Smoke data set.

The following DATA step creates the imputation cells and the variable Education, and replaces the multiply imputed values with missing values:

```
*---Create education levels and imputation cells, ---;
*---and assign . to missing items                 ---;
data Smoke; set Smoke;
   if HFA7 <=8                 then Education='Elementary ';
   if HFA7 > 8  and HFA7 <= 12 then Education='High School';
   if HFA7 > 12 and HFA7 <= 17 then Education='College    ';
   if HFA7 > 17                then Education='Unknown    ';
   if DMARETHN = 1 & HSSEX = 1 then ImputationCells=1;
   if DMARETHN = 1 & HSSEX = 2 then ImputationCells=2;
   if DMARETHN = 2 & HSSEX = 1 then ImputationCells=3;
   if DMARETHN = 2 & HSSEX = 2 then ImputationCells=4;
   if DMARETHN = 3 & HSSEX = 1 then ImputationCells=5;
   if DMARETHN = 3 & HSSEX = 2 then ImputationCells=6;
   if DMARETHN = 4             then ImputationCells=7;
   if HFF1IF   = 2 then HFF1MI   = .;
   if HAN6SRIF = 2 then HAN6SRMI = .;
   if HAR3RIF  = 2 then HAR3RMI  = .;
   if HAT28IF  = 2 then HAT28MI  = .;
run;
```

The following statements request that the missing values be imputed by using the FEFI method:

```
proc surveyimpute data=Smoke method=FEFI varmethod=BRR;
   weight wtpfqx6;
   repweights wtpqrp:;
   id seqn;
   class hff1mi han6srmi har3rmi hat28mi;
   var   hff1mi han6srmi har3rmi hat28mi;
   cells ImputationCells;
   output out=SmokeImputed;
run;
```

The PROC SURVEYIMPUTE statement invokes the procedure, the DATA= option specifies the input data set Smoke, the METHOD= option requests the FEFI method, and the VARMETHOD= option requests the imputation-adjusted BRR replication weights. The WEIGHT statement specifies the weight variable, and the REPWEIGHTS statement specifies the unadjusted BRR replicate weights. Because you specify replicate weights by using the REPWEIGHTS statement, you do not need to specify the Fay coefficient in PROC SURVEYIMPUTE. The variable SEQN in the ID statement identifies the observation units. The VAR statement specifies the variables to be imputed, the CELLS statement identifies the imputation cell variable ImputationCells, and the OUT= option in the OUTPUT statement names the output data set SmokeImputed. You request that all four variables be imputed jointly and that the imputed data be saved in the SmokeImputed data set.

Note that this example creates imputation-adjusted BRR replicate weights from the unadjusted BRR replicate weights that are available for these data. If the unadjusted BRR replicate weights are not available to you, then PROC SURVEYIMPUTE first creates the unadjusted BRR replicate weights and then updates the unadjusted weights for imputation to create the imputation-adjusted BRR replicate weights. For more information, see the section "Balanced Repeated Replication (BRR) Method" on page 9640.

Summary information about the number of observations and class level information are shown in Output 116.3.1. The "Number of Observations" table displays the number of observations (33,994) that are read and used. The weighted number of observations that are read shows that the 33,994 observation units in the sample represent over 251,000,000 observation units in the population. The "Class Level Information" table displays the observed levels for the analysis variables. The "Missing Data Patterns" table shows an arbitrary missing pattern. There are 12 different missing pattern groups. An "X" denotes that the variable is observed in that group, and a "." denotes that the variable is missing. Almost 94% of the observation units have no missing values (Group 1), 4.5% of the observation units have missing values for the variable HAN6SRMI (Group 4), and 1% of the observation units have missing values for the variable HAT28MI (Group 2).

Output 116.3.1 Imputation Information

The SURVEYIMPUTE Procedure

Number of Observations Read	33994
Number of Observations Used	33994
Sum of Weights Read	251097002
Sum of Weights Used	251097002

Class Level Information

Class	Levels	Values
HFF1MI	2	1 2
HAN6SRMI	4	-9 1 2 3
HAR3RMI	3	-9 1 2
HAT28MI	4	-9 1 2 3

Output 116.3.2 Missing Data Patterns

Missing Data Patterns									Group Means		
Group	HFF1MI	HAN6SRMI	HAR3RMI	HAT28MI	Freq	Sum of Weights	Unweighted Percent	Weighted Percent	HFF1MI 1	HFF1MI 2	HAN6SRMI -9
1	X	X	X	X	31916	229183908	93.89	91.27	0.370883	0.629117	0.275976
2	X	X	X	.	383	3584032.5	1.13	1.43	0.312278	0.687722	0
3	X	X	.	X	2	6696.18	0.01	0.00	0	1.000000	0
4	X	.	X	X	1536	17201675.8	4.52	6.85	0.417227	0.582773	.
5	X	.	X	.	25	255366.75	0.07	0.10	0.512251	0.487749	.
6	X	.	.	.	1	1137.27	0.00	0.00	0	1.000000	.
7	.	X	X	X	106	723161.98	0.31	0.29	.	.	0.277402
8	.	X	X	.	5	21175.81	0.01	0.01	.	.	0
9	.	X	.	.	2	43867.66	0.01	0.02	.	.	0
10	.	.	X	X	4	11751.6	0.01	0.00	.	.	.
11	.	.	X	.	1	4483.45	0.00	0.00	.	.	.
12	.	.	.	.	13	59745.61	0.04	0.02	.	.	.

Missing Data Patterns					Group Means					
Group	HAN6SRMI 1	HAN6SRMI 2	HAN6SRMI 3	HAR3RMI -9	HAR3RMI 1	HAR3RMI 2	HAT28MI -9	HAT28MI 1	HAT28MI 2	HAT28MI 3
1	0.365368	0.219609	0.139048	0.275976	0.199395	0.524629	0.275976	0.239253	0.160019	0.324752
2	0.533112	0.322946	0.143942	0	0.231400	0.768600	.	.	.	.
3	0	0.695886	0.304114	.	.	.	0	0.695886	0	0.304114
4	.	.	.	0	0.362741	0.637259	0	0.339890	0.222725	0.437384
5	.	.	.	0	0.371613	0.628387	.	.	.	.
6	.	.	.	.	.	.	.	.	.	.
7	0.570801	0.099198	0.052599	0.277402	0.156784	0.565813	0.277402	0.185712	0.192402	0.344483
8	0.414365	0.585635	0	0	0.078044	0.921956	.	.	.	.
9	0.262239	0.737761	0	.	.	.	.	.	.	.
10	.	.	.	0	0	1.000000	0	0.664584	0	0.335416
11	.	.	.	0	0	1.000000	.	.	.	.
12	.	.	.	.	.	.	.	.	.	.

The "Iteration History" table shown in Output 116.3.3 displays the maximum absolute and relative differences of the fractional weights for the EM algorithm for the full sample. The algorithm converged after four iterations. The "Imputation Summary" table shown in Output 116.3.4 displays the number of observed units (31,961), the number of missing units (2,078), and the number of imputed units. All units that have missing values have been imputed.

Output 116.3.3 Iteration History for the EM

Iteration History		
Iteration Number	Maximum Absolute Difference	Maximum Relative Difference
1	830.4733	0.18278
2	93.33655	0.00904
3	16.14668	0.00237
4	4.138731	0.00061

Output 116.3.4 Imputation Summary

Imputation Summary		
Observation Status	Number of Observations	Sum of Weights
Nonmissing	31916	229183908
Missing	2078	21913094.6
Missing, Imputed	2078	21913094.6
Missing, Not Imputed	0	0

The imputed data set SmokeImputed contains the imputation-adjusted weight (ImpWt) and 52 imputation-adjusted replicate weights (ImpRepWt_1 to ImpRepWt_52). The SmokeImputed data set has 38,701 data lines. The number of imputed values for an observation unit ranges from two to six, but around 80% of the units are imputed by using two or three imputed values.

You can use the imputed data set, the imputation-adjusted replicate weights, and the appropriate Fay coefficient to compute any estimators from your imputed data. You should use the REPWEIGHTS statement in SAS/STAT survey analysis procedures to specify the imputation-adjusted replicate weights. This example uses PROC SURVEYFREQ to perform the following analyses:

- estimate the percentage of smokers and nonsmokers in the population
- describe the smoking habits of an individual and of anyone who smokes in the home
- perform a domain analysis of activity levels for different levels of education

The PROC SURVEYFREQ statement invokes the procedure, the DATA= option names the imputed data set SmokeImputed, and the VARMETHOD=option requests the BRR variance estimation. The FAY= option for VARMETHOD=BRR specifies the Fay coefficient 0.3. Because your replicate weights come from Fay's BRR method, you must specify the FAY= option in the SAS/STAT survey analysis procedures to appropriately estimate the variance. The VARHEADER=LABEL option in the PROC SURVEYFREQ statement requests that the labels of the variables be displayed in the output. The WEIGHT statement specifies the imputation-adjusted full sample weights, and the REPWEIGHTS statement specifies the imputation-adjusted replicate weights. Note that the imputation-adjusted full sample and replicate weights are created by

PROC SURVEYIMPUTE, and they are different from the unadjusted weights available in the Smoke data set. The first TABLE statement requests a two-way frequency analysis for HFF1MI and HAR3RMI. The second TABLE statement requests a domain analysis for HAT28MI, where the variable Education is used as the domain variable. The ROW option in the TABLE statement is required in order to compute the distribution of HAT28MI for different levels of Education. The NOTOTAL, NOFREQ, and NOWT options suppress some output columns.

```
proc surveyfreq data=SmokeImputed varmethod=brr(fay=0.3) varheader=label;
   weight ImpWt;
   repweights ImpRepWt_:;
   table HFF1MI*HAR3RMI;
   table Education*HAT28MI / row nototal nofreq nowt;
run;
```

The data summary and the variance estimation information are displayed in Output 116.3.5. There are 38,701 data lines in the SmokeImputed data set. These 38,701 data lines represent the 33,994 observation units in the Smoke data set. The observation units are identified by the variable SEQN. The sum of weights is over 251,000,000, which is the same as the sum of weights in the Smoke data set. The sum of weights is an estimate of the population size. The "Variance Estimation" table shows that 52 replicate weights from Fay's BRR method are used for variance estimation with the Fay coefficient 0.3.

Output 116.3.5 Summary Information

The SURVEYFREQ Procedure

Data Summary	
Number of Observations	38701
Sum of Weights	251097002

Variance Estimation	
Method	BRR
Replicate Weights	SMOKEIMPUTED
Number of Replicates	52
Fay Coefficient	0.300

A two-way table for the smoking habit of the observation unit and smoking in the home is shown in Output 116.3.6. There are 21% smokers and 54% nonsmokers in the population. Nearly 19% of the individuals are smokers and live in a home where at least one person smokes in the home, but only 2% of the individuals are smokers and live in a home where no other household member smokes in the home. However, almost 9% of the individuals are nonsmokers but live in a home where at least one household member smokes in the home. The standard errors that are reported in the table properly account for the imputation.

Output 116.3.6 Two-Way Table for Smoking Status

Table of Anyone living here smoke cigs in home by Smoke cigarettes now (recode)						
Anyone living here smoke cigs in home	Smoke cigarettes now (recode)	Frequency	Weighted Frequency	Std Err of Wgt Freq	Percent	Std Err of Percent
1	-9	5431	24762830	717089	9.8619	0.2856
	1	5788	47166758	1361381	18.7843	0.5422
	2	3341	21790932	614088	8.6783	0.2446
	Total	14560	93720520	2180565	37.3244	0.8684
2	-9	8582	38702422	701855	15.4133	0.2795
	1	881	5837874	397358	2.3249	0.1582
	2	14678	112836186	1602093	44.9373	0.6380
	Total	24141	157376482	2180565	62.6756	0.8684
Total	-9	14013	63465252	260068	25.2752	0.1036
	1	6669	53004633	1276926	21.1092	0.5085
	2	18019	134627118	1328833	53.6156	0.5292
	Total	38701	251097002	2.25270	100.0000	

Suppose you want to perform a domain analysis by using the imputed data. If a list of domain variables is available before the imputation, then sometimes it is desirable to use the domain variables to create the imputation cells. However, requests for domain analyses often come after the imputation. In addition, data users might use domain variables that are different from what are used to create the imputation cells. In this example, the domain variable Education was not used to create the imputation cells. Although education level is not used in the imputation, it is reasonable to use the imputed data to perform domain analysis for every level of education. Domain analysis for activity levels for different education levels is shown in Output 116.3.7. If the highest education level is college, then 38% are reported as more active and 21% are reported as less active than their peers. If the highest education level is high school, then 28% are reported as more active and 20% are reported as less active than their peers. The standard errors that are reported in the table properly account for the imputation.

Output 116.3.7 Domain Analysis for Activity Levels by Education

Table of Education by Compare own activity level to others					
Education	**Compare own activity level to others**	**Percent**	**Std Err of Percent**	**Row Percent**	**Std Err of Row Percent**
College	**-9**	0.0017	0.0016	0.0055	0.0052
	1	11.9908	0.4117	38.3446	0.9792
	2	6.5292	0.3253	20.8795	0.8461
	3	12.7494	0.4641	40.7704	0.9978
Elementary	**-9**	21.8961	0.1269	74.2986	0.9154
	1	1.8571	0.1193	6.3015	0.3596
	2	2.0051	0.1500	6.8039	0.4513
	3	3.7121	0.1970	12.5961	0.5420
High School	**-9**	3.2191	0.1238	8.3653	0.3251
	1	10.6977	0.2990	27.7997	0.6634
	2	7.8486	0.2782	20.3959	0.6333
	3	16.7160	0.4958	43.4391	0.7062
Unknown	**-9**	0.1583	0.0289	20.3674	3.2674
	1	0.1981	0.0463	25.4966	3.7217
	2	0.1502	0.0346	19.3311	3.3973
	3	0.2704	0.0426	34.8049	3.2211

Example 116.4: Fractional Hot-Deck Imputation for Mixed Variables

This example imputes missing values in both categorical and continuous variables by applying the fractional hot-deck imputation (FHDI) method to a data set from the third National Health and Nutrition Examination Survey (NHANES III). The data set contains a set of balanced repeated replication (BRR) replicate weights. The REPWEIGHTS statement in PROC SURVEYIMPUTE accepts the BRR weights and creates imputation-adjusted replicate weights. The imputed data set and the imputation-adjusted replicate weights are then used in PROC SURVEYMEANS and PROC SURVEYREG to perform domain analysis and regression analysis, respectively.

The objective of NHANES is to study the health and nutritional status of the US population. NHANES uses a multistage stratified area sample that typically has two PSUs per stratum. Strata are created on the basis of geographic location, metropolitan statistical area (MSA), and other demographic information. MSAs or a group of counties are selected as PSUs from each stratum. Sampling weights are unequal because of different selection probabilities among different subgroups and for reasons such as nonresponse and undercoverage. For more information about NHANES, see `http://www.cdc.gov/nchs/nhanes/about_nhanes.htm`.

NHANES III data contain missing values in many items. Multiple imputation was used to impute some of the missing items. Five multiply imputed data sets are available for public use. Because FHDI is used in this example to impute the missing values, you need the observed data, the missing (or imputation) flag for every item, and only one imputed data set. The data sets Core and IMP1 have been downloaded from the Centers for Disease Control and Prevention's website (`https://www.cdc.gov/`). The Core data set contains the demographic variables, full sample weights, replicate weights, and imputation flags. The replicate weights are created by using Fay's BRR method, with a Fay coefficient of 0.3. The IMP1 data set contains the first version of the five multiply imputed data sets.

The data set HealthMiss is obtained by merging the Core and IMP1 data sets by using the observation sequence number SEQN. The HealthMiss data set contains observation units that are between 17 and 60

years of age. Missing values are added according to the imputation flag in the Core data set. The following items are available in the HealthMiss data set for each observation unit:

- SEQN: observation sequence number
- WTPFQX6: observation weight, ranging from 220.18 to 140916.28
- WTPQRP1 to WTPQRP52: 52 replicate weights from the BRR method
- HSSEX: gender; 1 for male and 2 for female
- HFF1MI: whether anyone smokes cigarettes in the home; 1 for yes and 2 for no
- HAT28MI: activity level compared to others; –9 for not applicable, 1 for more active, 2 for less active, and 3 for about the same
- BMPHTMI: standing height (cm), ranging from 130.6 to 206.5
- BMPWTMI: body weight (kg), ranging from 26.75 to 241.80
- PEP6G3MI: K5 diastolic blood pressure (mmHg), ranging from 0 to 136
- HSAGEIR: age in years, ranging from 17 to 60
- HSHSIZER: household size; categories from 1 to 10
- Married: marital status; 1 for married and 0 for not married

There are no missing values in the variables SEQN, HSAGEIR, HSHSIZER, Married, and WTPFQX6 or in the replicate weight variables. The variables HFF1MI, HAT28MI, BMPHTMI, BMPWTMI, and PEP6G3MI contain missing values, which are imputed in this example. Although HFF1MI and HAT28MI have two and four observed levels, respectively, BMPHTMI, BMPWTMI, and PEP6G3MI have many observed levels. Because these last three variables have many observed levels, FHDI is applied to impute missing values jointly in all five variables.

Before you apply the FHDI method to a data set, you should (1) incorporate auxiliary information in the imputation by creating imputation cells and (2) create bins for variables that have many levels.

Imputation cells divide the data into groups of similar units such that the recipient units have characteristics similar to those of the donor units in the same group. Characteristics of imputation cells might come from the same survey or from other sources, such as census data or previous surveys. The cell identification is known for every unit in the sample. For a helpful review of handling missing data, see Brick and Kalton (1996). For the purpose of this example, a cluster variable is created by using two demographic variables, HSAGEIR and HSHSIZER, and by using the FASTCLUS procedure in SAS/STAT. Both variables are available in the Core data set, and they do not contain missing values. These clusters are identified by the variable Cluster in the HealthMiss data set. Levels of the variables Cluster and Married are used to create imputation cells.

If you request FHDI, then the variables that have many levels (these are identified by the variables that you specify in the VAR statement but not in the CLASS statement) are first levelized to create bins. You can use the CLEVVAR= option to specify the variable that contains the bins for a numeric variable. Alternatively, you use the CLEVELS=*k* option to divide the observed range of the numeric variable into *k* equally spaced bins. First-stage FEFI is applied to the CLEVVAR= variables and to the variables that you specify in the CLASS statement. In this example, the bins are created for a numeric variable by using the observed 33rd

and 66th percentiles for that variable. The CLEVVAR= variable should contain a missing value for every observation unit in which the corresponding numeric variable has a missing value. The following statements create the CLEVVAR= variables:

```
*---Create bins for continuous variables---;
data HealthMiss; set HealthMiss;
   if bmphtmi       = .     then bmphtlev=.;
   else if bmphtmi <= 162.6 then bmphtlev=1;
   else if bmphtmi <= 171.5 then bmphtlev=2;
   else                          bmphtlev=3;
   if bmpwtmi       = .    then bmpwtlev=.;
   else if bmpwtmi <= 65.7 then bmpwtlev=1;
   else if bmpwtmi <= 80.2 then bmpwtlev=2;
   else                         bmpwtlev=3;
   if pep6g3mi       = .    then pep6g3lev=.;
   else if pep6g3mi <= 65.3 then pep6g3lev=1;
   else if pep6g3mi <= 75.8 then pep6g3lev=2;
   else                          pep6g3lev=4;
   label bmphtlev  = "Bin values for BMPHTMI"
         bmpwtlev  = "Bin values for BMPWTMI"
         pep6g3lev = "Bin values for PEP6G3MI";
run;
```

The following statements use the FHDI method to impute the missing values:

```
proc surveyimpute data=HealthMiss method=fhdi varmethod=brr
                      ndonors=5 seed=9388401;
   id seqn;
   class hff1mi hat28mi;
   weight wtpfqx6;
   repweights wtpqrp:;
   cells cluster married;
   var hff1mi hat28mi bmphtmi (clevvar=bmphtlev)
                      bmpwtmi (clevvar=bmpwtlev)
                      pep6g3mi(clevvar=pep6g3lev);
   output out=HealthFHDI;
run;
```

The PROC SURVEYIMPUTE statement invokes the procedure, the DATA= option specifies the input data set HealthMiss, the METHOD= option requests the FHDI method, the VARMETHOD= option requests the imputation-adjusted BRR replication weights, the NDONORS= option specifies the maximum number of second-stage donors, and the SEED= option specifies the random number generator seed. The variable SEQN in the ID statement identifies the observation units. The WEIGHT statement identifies the weight variable, and the REPWEIGHTS statement identifies the variables that contain the unadjusted BRR replicate weights. The CELLS statement identifies the imputation cell variables Cluster and Married, and the OUT= option in the OUTPUT statement names the output data set HealthFHDI.

The VAR statement specifies the variables in which the missing values are to be imputed. The CLASS statement identifies the categorical variables. Only first-stage FEFI will be applied to the CLASS variables. Second-stage FEFI and FHDI will be applied to the variables that are specified in the VAR statement but not in the CLASS statement. The CLEVVAR= option for these variables identifies the corresponding bin variables in which first-stage FEFI will be performed. In this example, you requested first-stage FEFI for the variables HFF1MI, HAT28MI, BMPHTLEV, BMPWTLEV, and PEP6G3LEV; and second-stage FEFI and FHDI for the variables BMPHTMI, BMPWTMI, and PEP6G3MI.

You request that all five variables be imputed jointly and that the imputed data be saved in the HealthFHDI data set.

The number of observations and the CLASS level information are shown in Output 116.4.1. The Sum of Weights Read row shows that the 13,721 observation units in the sample represent over 149 million observation units in the population. The "Class Level Information" table displays the observed levels for the CLASS variables.

Output 116.4.1 Imputation Information

The SURVEYIMPUTE Procedure

Number of Observations Read	13721
Number of Observations Used	13721
Sum of Weights Read	149546400
Sum of Weights Used	149546400

Class Level Information

Class	Levels	Values
HFF1MI	2	1 2
HAT28MI	3	1 2 3

The "Missing Data Patterns" table shows an arbitrary missing pattern. There are 13 different missing pattern groups. An "X" denotes that the variable is observed in that group, and a "." denotes that the variable is missing. Almost 87.42% of the observation units have no missing values (Group 1); 7.17% of the observation units have missing values for the variables BMPHTMI, BMPWTMI, and PEP6G3MI (Group 6); and 0.03% of the observation units have missing values in all five variables (Group 13).

Output 116.4.2 Missing Data Patterns

Missing Data Patterns

Group	HFF1MI	HAT28MI	BMPHTMI	BMPWTMI	PEP6G3MI	Freq	Sum of Weights	Unweighted Percent	Weighted Percent
1	X	X	X	X	X	11995	129773812	87.42	86.78
2	X	X	X	X	.	475	3493749.6	3.46	2.34
3	X	X	X	.	X	10	16064.94	0.07	0.01
4	X	X	X	.	.	1	12796.75	0.01	0.01
5	X	X	.	.	X	6	49022.69	0.04	0.03
6	X	X	.	.	.	984	13080725.9	7.17	8.75
7	X	.	X	X	X	167	2193493.99	1.22	1.47
8	X	.	X	X	.	11	138241.25	0.08	0.09
9	X	.	.	X	X	1	2742.56	0.01	0.00
10	X	.	.	.	.	20	307483.94	0.15	0.21
11	.	X	X	X	X	15	42007.38	0.11	0.03
12	.	X	.	.	.	32	390724.57	0.23	0.26
13	.	.	.	.	.	4	45534.74	0.03	0.03

Missing Data Patterns

Group Means

Group	BMPHTMI	BMPWTMI	PEP6G3MI	HFF1MI 1	HFF1MI 2	HAT28MI 1	HAT28MI 2	HAT28MI 3
1	169.387674	75.258624	71.746316	0.403270	0.596730	0.310384	0.231793	0.457823
2	168.189385	79.263271	.	0.464648	0.535352	0.301674	0.252490	0.445836
3	154.554452	.	53.348310	0.370184	0.629816	0	0.164085	0.835915
4	156.500000	.	.	0	1.000000	0	0	1.000000
5	.	.	87.096205	0.870574	0.129426	0	0.468602	0.531398
6	.	.	.	0.402061	0.597939	0.336804	0.214523	0.448674
7	168.361303	76.971926	72.511286	0.322006	0.677994	.	.	.
8	168.749387	79.516017	.	0.470061	0.529939	.	.	.
9	.	70.450000	84.000000	0	1.000000	.	.	.
10	.	.	.	0.483659	0.516341	.	.	.
11	166.962303	84.023762	75.389658	.	.	0.158780	0.312686	0.528534
12	.	.	.	.	.	0.255939	0.237827	0.506235
13	.	.	.	.	.	.	.	.

The "Imputation Summary" table in Output 116.4.3 displays the number of observation units that contain no missing items (11,995), the number of observation units that contain at least one missing item (1,726), and the number of units in which the missing values are imputed. Missing values in all 1,726 units are imputed.

Output 116.4.3 Imputation Summary

Imputation Summary

Observation Status	Number of Observations	Sum of Weights
Nonmissing	11995	129773812
Missing	1726	19772588.3
Missing, Imputed	1726	19772588.3
Missing, Not Imputed	0	0

Because fractional imputation replaces one observed unit with several observation rows that contain imputed values, the 13,721 observed units in the input data set HealthMiss generate 127,002 observation rows in the imputed data set HealthFHDI. The following note displays the number of observation rows (127,007) in this imputed data set:

```
NOTE: The data set WORK.HEALTHFHDI has 127007 observations and 134 variables.
```

You can use the imputed data set, the imputation-adjusted replicate weights, and the appropriate Fay coefficient to compute any estimators from your imputed data. However, you must use the REPWEIGHTS statement in SAS/STAT survey analysis procedures to specify the imputation-adjusted replicate weights. The following two examples describe a domain analysis and a regression analysis that use the imputed data.

The following PROC SURVEYMEANS statements estimate the mean diastolic blood pressure in the year 2000 population and in the subpopulation of smokers and nonsmokers:

```
ods graphics on;
proc surveymeans data=HealthFHDI varmethod=brr(Fay=0.3) plots=domain;
   weight ImpWt;
   repweights ImpRepWt_:;
   var pep6g3mi;
   domain hff1mi;
run;
```

The "Data Summary" table in Output 116.4.4 displays the number of observation rows (127,007) and the sum of weights (149,546,400). Because fractional imputation is used, the number of observation rows is not equal to the number of observation units (13,721). However, the sum of weights from the observation rows, which is an estimate of the population size, is the same as the sum of weights from the observation units. The "Variance Estimation" table in Output 116.4.4 shows that Fay's BRR with 52 replicate weights and a Fay coefficient of 0.3 are used for variance estimation.

Output 116.4.4 Data Summary

The SURVEYMEANS Procedure

Data Summary	
Number of Observations	127007
Sum of Weights	149546400

Variance Estimation	
Method	BRR
Replicate Weights	HEALTHFHDI
Number of Replicates	52
Fay Coefficient	0.3

The first table in Output 116.4.5 displays the mean diastolic blood pressure for the overall population as 71.78, with a standard error of 1.34. The second table shows data for smokers and nonsmokers. For smokers, the mean diastolic blood pressure is 70.67, with a standard error of 1.63. For nonsmokers, it is 72.55, with a standard error of 1.45. The N column in both tables displays the number of observation rows, not the number of observation units.

Output 116.4.5 Mean Diastolic Blood Pressure

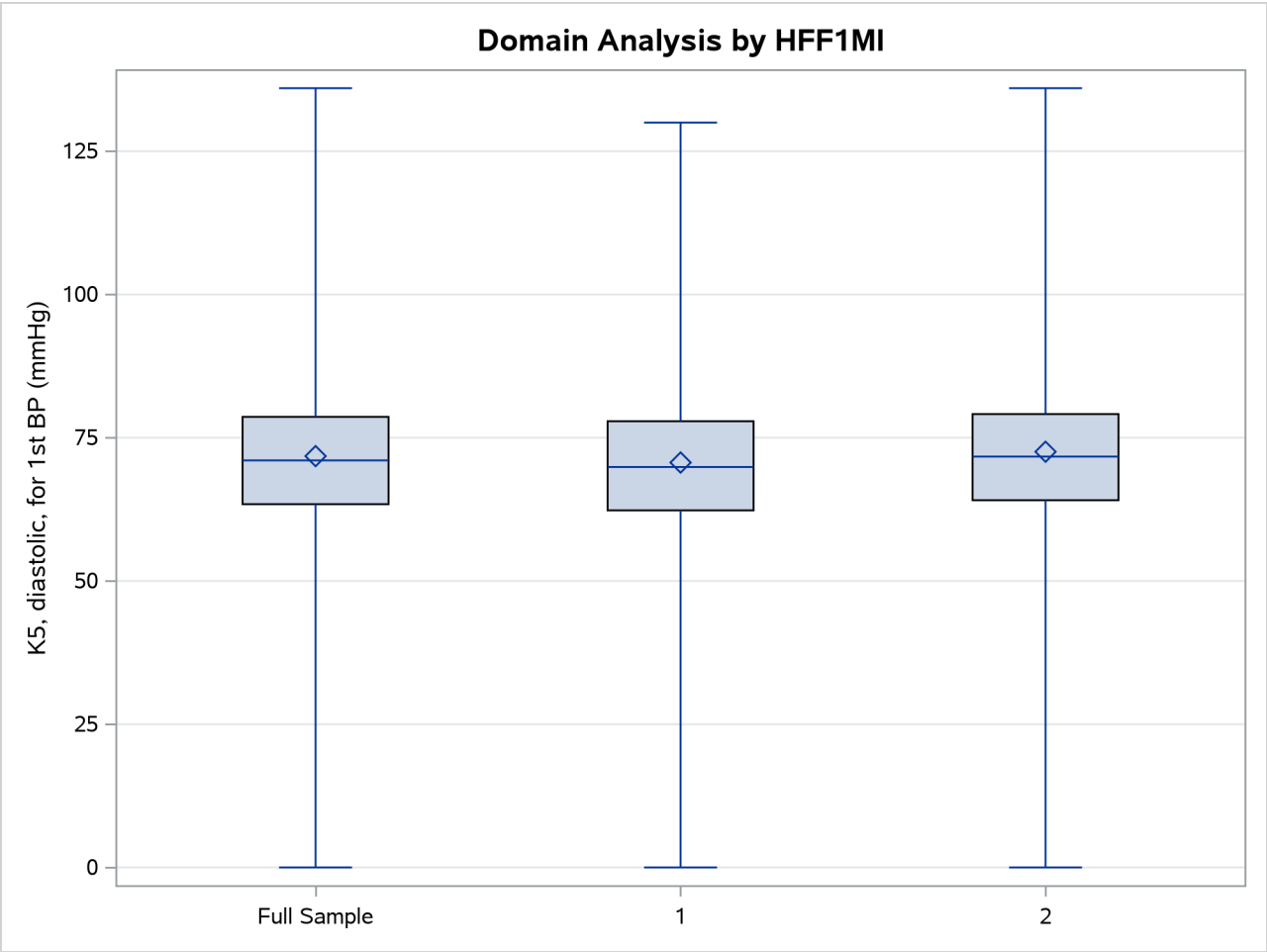
Statistics						
Variable	Label	N	Mean	Std Error of Mean	95% CL for Mean	
PEP6G3MI	K5, diastolic, for 1st BP (mmHg)	127007	71.788404	0.268699	71.2492203	72.3275871

The SURVEYMEANS Procedure

Statistics for HFF1MI Domains							
HFF1MI	Variable	Label	N	Mean	Std Error of Mean	95% CL for Mean	
1	**PEP6G3MI**	K5, diastolic, for 1st BP (mmHg)	49876	70.665325	0.326577	70.0100015	71.3206493
2	**PEP6G3MI**	K5, diastolic, for 1st BP (mmHg)	77131	72.548913	0.289446	71.9680973	73.1297289

A box plot of the weighted distribution of diastolic blood pressure is displayed in Output 116.4.6. The first box is for the overall population, and the other two boxes are for the two domains defined by smoking habits.

Output 116.4.6 Diastolic Blood Pressure



The following PROC SURVEYREG statements estimate the regression coefficients for regressing diastolic blood pressure on smoking status, gender, height, weight, and age. Imputation-adjusted weights and

imputation-adjusted replicate weights are used for point estimation and variance estimation, respectively. The SOLUTION option in the MODEL statement displays the parameter estimates. Estimated values of the regression parameters, along with their standard errors, are shown in Output 116.4.7. The OUT= option in the OUTPUT statement saves the residuals and the fitted values in the SAS data set Resid.

```
proc surveyreg data=HealthFHDI varmethod=brr(Fay=0.3);
   weight ImpWt;
   repweights ImpRepWt_:;
   class hff1mi hssex;
   model pep6g3mi = hff1mi hssex bmphtmi bmpwtmi hsageir / solution;
   output out=Resid residual=Residuals predicted=Fitted;
run;
```

Estimated regression parameters and their standard errors are displayed in Output 116.4.7. All covariates except height (BMPHTMI) have small standard errors compared to their estimated values. Thus, they are all important in describing the regression relationship in the NHANES III population between 17 and 60 years of age. The degrees of freedom for the *t* tests is 52, which is equal to the number of BRR replicates.

Output 116.4.7 Parameter Estimates

The SURVEYREG Procedure

Regression Analysis for Dependent Variable PEP6G3MI

Estimated Regression Coefficients

Parameter	Estimate	Standard Error	t Value	Pr > |t|
Intercept	45.6902005	4.00157249	11.42	<.0001
HFF1MI 1	-1.3855994	0.33509056	-4.13	0.0001
HFF1MI 2	0.0000000	0.00000000	.	.
HSSEX 1	3.2312257	0.28893940	11.18	<.0001
HSSEX 2	0.0000000	0.00000000	.	.
BMPHTMI	0.0038192	0.02220508	0.17	0.8641
BMPWTMI	0.1792811	0.00940559	19.06	<.0001
HSAGEIR	0.3021222	0.02373061	12.73	<.0001

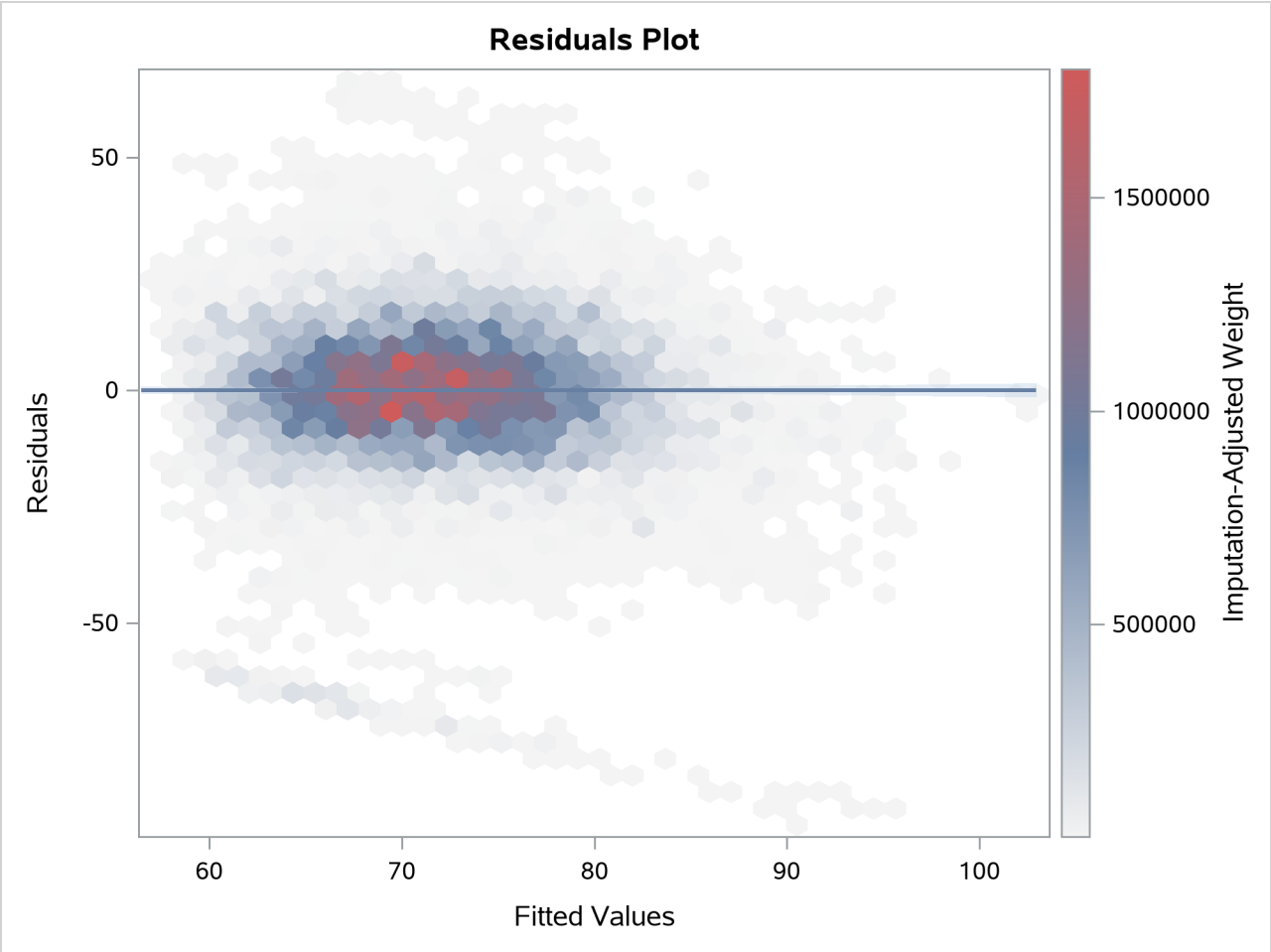
Note: The degrees of freedom for the t tests is 52.
Matrix X'WX is singular and a generalized inverse was used to solve the normal equations. Estimates are not unique.

The following PROC SURVEYREG statements request a residual plot by using the residuals and fitted values from the Resid data set. Imputation-adjusted weights are displayed by using a heat map, as shown in Output 116.4.8. The SHAPE=HEXAGONAL option requests hexagonal bins, and the NBINS=60 option specifies that 60 bins be used. For more information about how to create customized graphs by using ODS graphs, see Kuhfeld (2016). The weighted residual plot does not reveal any major violations of the model assumptions—namely, linearity and equal variance.

Because fractional imputation increases the number of observation rows, you must use imputation-adjusted weights in all analyses that involve fractionally imputed data sets.

```
ods graphics on;
proc surveyreg data=resid plots(nbins=60)=fit(shape=hexagonal);
   model Residuals=Fitted;
   weight impwt;
run;
```

Output 116.4.8 Plot of Residuals versus Fitted Values



References

Andridge, R. R., and Little, R. J. A. (2010). "A Review of Hot Deck Imputation for Survey Non-response." *International Statistical Review* 78:40–64.

Barnard, J., and Rubin, D. B. (1999). "Small-Sample Degrees of Freedom with Multiple Imputation." *Biometrika* 86:948–955.

Beaumont, J.-F., and Patak, Z. (2012). "On the Generalized Bootstrap for Sample Surveys with Special Attention to Poisson Sampling." *International Statistical Review* 80:127–148.

Bethlehem, J. (2009). *Applied Survey Methods: A Statistical Perspective*. Hoboken, NJ: John Wiley & Sons.

Brick, J. M., and Kalton, G. (1996). "Handling Missing Data in Survey Research." *Statistical Methods in Medical Research* 5:215–238.

Cochran, W. G. (1977). *Sampling Techniques*. 3rd ed. New York: John Wiley & Sons.

Dippo, C. S., Fay, R. E., and Morganstein, D. H. (1984). "Computing Variances from Complex Samples with Replicate Weights." In *Proceedings of the Survey Research Methods Section*, 489–494. Alexandria, VA: American Statistical Association.

Fay, R. E. (1984). "Some Properties of Estimates of Variance Based on Replication Methods." In *Proceedings of the Survey Research Methods Section*, 495–500. Alexandria, VA: American Statistical Association.

Fay, R. E. (1989). "Theory and Application of Replicate Weighting for Variance Calculations." In *Proceedings of the Survey Research Methods Section*, 212–217. Alexandria, VA: American Statistical Association.

Fay, R. E. (1993). "Valid Inferences from Imputed Survey Data." In *Proceedings of the Survey Research Methods Section*, 41–48. Alexandria, VA: American Statistical Association.

Fay, R. E. (1996). "Alternative Paradigms for the Analysis of Imputed Survey Data." *Journal of the American Statistical Association* 91:490–498.

Fellegi, I. P., and Holt, D. (1976). "A Systematic Approach to Automatic Edit and Imputation." *Journal of the American Statistical Association* 71:17–35.

Fuller, W. A. (2009). *Sampling Statistics*. Hoboken, NJ: John Wiley & Sons.

Fuller, W. A., and Kim, J. K. (2005). "Hot Deck Imputation for the Response Model." *Survey Methodology* 31:139–149.

Haziza, D. (2009). "Imputation and Inference in the Presence of Missing Data." In *Sample Surveys: Design, Methods, and Applications*, edited by D. Pfeffermann and C. R. Rao, 215–246. Vol. 29A of Handbook of Statistics. Amsterdam: North-Holland.

Ibrahim, J. G. (1990). "Incomplete Data in Generalized Linear Models." *Journal of the American Statistical Association* 85:765–769.

Im, J., Kim, J. K., and Fuller, W. A. (2015). "Two-Phase Sampling Approach to Fractional Hot Deck Imputation." In *Proceedings of the Survey Research Methods Section*, 1030–1043. Alexandria, VA: American Statistical Association.

Judkins, D. R. (1990). "Fay's Method for Variance Estimation." *Journal of Official Statistics* 6:223–239.

Kalton, G., and Kasprzyk, D. (1986). "The Treatment of Missing Survey Data." *Survey Methodology* 12:1–16.

Kalton, G., and Kish, L. (1984). "Some Efficient Random Imputation Methods." *Communications in Statistics—Theory and Methods* 13:1919–1939.

Kim, J. K. (2002). "A Note on Approximate Bayesian Bootstrap Imputation." *Biometrika* 89:470–477.

Kim, J. K., and Fuller, W. A. (2004). "Fractional Hot Deck Imputation." *Biometrika* 91:559–578.

Kim, J. K., and Fuller, W. A. (2013). "Hot Deck Imputation for Multivariate Missing Data." In *Proceedings of the Fifty-Ninth ISI World Statistics Congress*, 924–929. The Hague: International Statistics Institute.

Kim, J. K., and Shao, J. (2014). *Statistical Methods for Handling Incomplete Data*. Boca Raton, FL: CRC Press.

Kish, L. (1965). *Survey Sampling*. New York: John Wiley & Sons.

Kuhfeld, W. F. (2016). "Highly Customized Graphs Using ODS Graphics." In *Proceedings of the SAS Global Forum 2016 Conference*. Cary, NC: SAS Institute Inc. http://support.sas.com/resources/papers/proceedings16/SAS1800-2016.pdf.

Little, R. J. A., and Rubin, D. B. (2002). *Statistical Analysis with Missing Data*. 2nd ed. Hoboken, NJ: John Wiley & Sons.

Lohr, S. L. (2010). *Sampling: Design and Analysis*. 2nd ed. Boston: Brooks/Cole.

Mashreghi, Z., Haziza, D., and Léger, C. (2016). "A Survey of Bootstrap Methods in Finite Population Sampling." *Statistics Surveys* 10:1–52.

Matsumoto, M., and Nishimura, T. (1998). "Mersenne Twister: A 623-Dimensionally Equidistributed Uniform Pseudo-random Number Generator." *ACM Transactions on Modeling and Computer Simulation* 8:3–30.

McCarthy, P. J., and Snowden, C. B. (1985). *The Bootstrap and Finite Population Sampling*. Vital and Health Statistics, Series 2, no. 95. DHHS Publication Number 85–1369. Washington, DC: US Government Printing Office. https://www.cdc.gov/nchs/data/series/sr_02/sr02_095.pdf.

Myers, T. A. (2011). "Goodbye, Listwise Deletion: Presenting Hot Deck Imputation as an Easy and Effective Tool for Handling Missing Data." *Communication Methods and Measures* 5:297–310.

Rao, J. N. K., and Shao, J. (1992). "Jackknife Variance Estimation with Survey Data under Hot Deck Imputation." *Biometrika* 79:811–822.

Rao, J. N. K., and Wu, C. F. J. (1988). "Resampling Inference with Complex Survey Data." *Journal of the American Statistical Association* 83:231–241.

Rao, J. N. K., Wu, C. F. J., and Yue, K. (1992). "Some Recent Work on Resampling Methods for Complex Surveys." *Survey Methodology* 18:209–217.

Rubin, D. B., and Schenker, N. (1986). "Multiple Imputation for Interval Estimation from Simple Random Samples with Ignorable Nonresponse." *Journal of the American Statistical Association* 81:366–374.

Särndal, C.-E., and Lundström, S. (2005). *Estimation in Surveys with Nonresponse*. Chichester, UK: John Wiley & Sons.

Särndal, C.-E., Swensson, B., and Wretman, J. (1992). *Model Assisted Survey Sampling*. New York: Springer-Verlag.

Shao, J., and Tu, D. (1995). *The Jackknife and Bootstrap*. New York: Springer-Verlag.

Sitter, R. R. (1992a). "Comparing Three Bootstrap Methods for Survey Data." *Canadian Journal of Statistics* 20:135–154.

Sitter, R. R. (1992b). "A Resampling Procedure for Complex Survey Data." *Journal of the American Statistical Association* 87:755–765.

Tillé, Y. (2006). *Sampling Algorithms*. New York: Springer.

Wolter, K. M. (2007). *Introduction to Variance Estimation*. 2nd ed. New York: Springer.

Subject Index

analysis variable
SURVEYIMPUTE procedure, 9602
approximate Bayesian bootstrap
SURVEYIMPUTE procedure, 9638

balanced repeated replication
SURVEYIMPUTE procedure, 9640
bootstrap
SURVEYIMPUTE procedure, 9639
variance estimation (SURVEYIMPUTE), 9639
bootstrap variance estimation
SURVEYIMPUTE procedure, 9639
BRR method
SURVEYIMPUTE procedure, 9640
BRR variance estimation
SURVEYIMPUTE procedure, 9640

class level information
SURVEYIMPUTE procedure, 9646
clustering
SURVEYIMPUTE procedure, 9598, 9604
convergence status
SURVEYIMPUTE procedure, 9646

definitions
SURVEYIMPUTE procedure, 9603
design summary
SURVEYIMPUTE procedure, 9646
donor count
SURVEYIMPUTE procedure, 9646

Fay coefficient
SURVEYIMPUTE procedure, 9641
Fay's BRR method
replication methods (SURVEYIMPUTE), 9641
finite population correction
SURVEYIMPUTE procedure, 9592
fractional hot-deck imputation
SURVEYIMPUTE procedure, 9625
fully efficient fractional imputation
SURVEYIMPUTE procedure, 9608

Hadamard matrix
BRR replicate weights (SURVEYIMPUTE), 9641
hot-deck imputation
SURVEYIMPUTE procedure, 9636

imputation
SURVEYIMPUTE procedure, 9608, 9613, 9625, 9636, 9638
imputation index
SURVEYIMPUTE procedure, 9600
imputation information
SURVEYIMPUTE procedure, 9647
imputation summary
SURVEYIMPUTE procedure, 9647
imputation-adjusted weights
SURVEYIMPUTE procedure, 9600
iteration history
SURVEYIMPUTE procedure, 9647

jackknife coefficients
SURVEYIMPUTE procedure, 9642
jackknife method
SURVEYIMPUTE procedure, 9642
jackknife variance estimation
SURVEYIMPUTE procedure, 9642

missing data patterns
SURVEYIMPUTE procedure, 9647
missing values
SURVEYIMPUTE procedure, 9606

number of observations
SURVEYIMPUTE procedure, 9648
number of replicates
SURVEYIMPUTE procedure, 9639–9642

primary sampling units (PSUs)
SURVEYIMPUTE procedure, 9598

random number generation
SURVEYIMPUTE procedure, 9608
replicate weights
SURVEYIMPUTE procedure, 9601

sample design
SURVEYIMPUTE procedure, 9604
sampling rates
SURVEYIMPUTE procedure, 9592, 9605
sampling weights
SURVEYIMPUTE procedure, 9602, 9605
stratification
SURVEYIMPUTE procedure, 9601, 9604
survey data analysis
SURVEYIMPUTE procedure, 9579
survey sampling
imputation (SURVEYIMPUTE), 9579
SURVEYIMPUTE procedure, 9579

analysis variable, 9602
approximate Bayesian bootstrap, 9638
balanced repeated replication, 9640
bootstrap, 9639
bootstrap variance estimation, 9639
BRR method, 9640
BRR variance estimation, 9640
clustering, 9598, 9604
definitions, 9603
displayed output, 9646
Fay coefficient, 9641
Fay's BRR method, 9641
finite population correction, 9592
fractional hot-deck imputation, 9625
fully efficient fractional imputation, 9608
Hadamard matrix (BRR replicate weights), 9641
hot-deck imputation, 9636
imputation, 9608, 9613, 9625, 9636, 9638
imputation index, 9600
imputation-adjusted weights, 9600
jackknife coefficients, 9642
jackknife method, 9642
jackknife variance estimation, 9642
missing values, 9606
number of replicates, 9639–9642
ODS table names, 9649
ordering of effects, 9591
output data sets, 9645
OUTPUT statistics, 9599
population totals, 9592, 9605
primary sampling units (PSUs), 9598
random number generation, 9608
random number generator seed, 9592
replicate weights, 9601
sample design, 9604
sampling rates, 9592, 9605
sampling weights, 9602, 9605
stratification, 9601, 9604
two-stage fully efficient fractional imputation, 9613
weighting, 9602, 9605

two-stage fully efficient fractional imputation
SURVEYIMPUTE procedure, 9613

variance estimation
bootstrap (SURVEYIMPUTE), 9639
BRR (SURVEYIMPUTE), 9640
jackknife (SURVEYIMPUTE), 9642

weighted mean sscp
SURVEYIMPUTE procedure, 9648
weighted moments
SURVEYIMPUTE procedure, 9648
weighting
SURVEYIMPUTE procedure, 9602, 9605

Syntax Index

ABSEMWTCONV= option
METHOD=FEFI (PROC SURVEYIMPUTE statement), 9588
METHOD=FHDI (PROC SURVEYIMPUTE statement), 9589

BY statement
SURVEYIMPUTE procedure, 9596

CELLS statement
SURVEYIMPUTE procedure, 9596
CLASS statement
SURVEYIMPUTE procedure, 9597
CLUSTER statement
SURVEYIMPUTE procedure, 9598

DATA= option
PROC SURVEYIMPUTE statement, 9588
DESCENDING option
CLASS statement (SURVEYIMPUTE), 9597
DISP= option
METHOD=FHDI (PROC SURVEYIMPUTE statement), 9589
DONORID
OUTPUT statement (SURVEYIMPUTE), 9599

FAY= option
VARMETHOD=BRR (PROC SURVEYIMPUTE statement), 9594
FRACTIONALWEIGHTS= option
OUTPUT statement (SURVEYIMPUTE), 9600

HADAMARD= option
VARMETHOD=BRR (PROC SURVEYIMPUTE statement), 9594

ID statement
SURVEYIMPUTE procedure, 9598
IMPADJWEIGHTS= option
OUTPUT statement (SURVEYIMPUTE), 9600
IMPINDEX= option
OUTPUT statement (SURVEYIMPUTE), 9600
IMPJOINT statement
SURVEYIMPUTE procedure, 9598
IMPSTATUS= option
OUTPUT statement (SURVEYIMPUTE), 9600

LIST option
STRATA statement (SURVEYIMPUTE), 9601

MAXDONORCELLS= option
METHOD=FEFI (PROC SURVEYIMPUTE statement), 9589
METHOD=FHDI (PROC SURVEYIMPUTE statement), 9589
MAXEMITER= option
METHOD=FEFI (PROC SURVEYIMPUTE statement), 9589
METHOD=FHDI (PROC SURVEYIMPUTE statement), 9590
METHOD= option
PROC SURVEYIMPUTE statement, 9588
MH= method-option
PROC SURVEYIMPUTE statement, 9593

NDONORS= option
PROC SURVEYIMPUTE statement, 9591
NOPRINT option
PROC SURVEYIMPUTE statement, 9591

OBSID= option
OUTPUT statement (SURVEYIMPUTE), 9600
ORDER= option
CLASS statement (SURVEYIMPUTE), 9597
PROC SURVEYIMPUTE statement, 9591
OUT= option
OUTPUT statement (SURVEYIMPUTE), 9599
OUTCONTLEVELS= option
OUTPUT statement (SURVEYIMPUTE), 9600
OUTJKCOEFS= option
OUTPUT statement (SURVEYIMPUTE), 9599
OUTPUT statement
SURVEYIMPUTE procedure, 9599
OUTPUT statement (SURVEYIMPUTE)
DONORID, 9599
FRACTIONALWEIGHTS= option, 9600
IMPADJWEIGHTS= option, 9600
IMPINDEX= option, 9600
IMPSTATUS= option, 9600
OBSID= option, 9600
OUTCONTLEVELS= option, 9600

PRINTH option
VARMETHOD=BRR (PROC SURVEYIMPUTE statement), 9595
PROC SURVEYIMPUTE statement, *see* SURVEYIMPUTE procedure

RATE= option

PROC SURVEYIMPUTE statement, 9592
RELEMWTCONV= option
METHOD=FEFI (PROC SURVEYIMPUTE statement), 9589
METHOD=FHDI (PROC SURVEYIMPUTE statement), 9590
REPS= option
VARMETHOD=BOOTSTRAP (PROC SURVEYIMPUTE statement), 9594
VARMETHOD=BRR (PROC SURVEYIMPUTE statement), 9595
REPWEIGHTS statement
SURVEYIMPUTE procedure, 9601
REPWTADJ= option
METHOD=FHDI (PROC SURVEYIMPUTE statement), 9590

SEED= option
PROC SURVEYIMPUTE statement, 9592
SELECTION= option
METHOD=FHDI (PROC SURVEYIMPUTE statement), 9590
METHOD=HOTDECK (PROC SURVEYIMPUTE statement), 9590
STRATA statement
SURVEYIMPUTE procedure, 9601
SURVEYIMPUTE procedure, BY statement, 9596
SURVEYIMPUTE procedure, CELLS statement, 9596
SURVEYIMPUTE procedure, CLASS statement, 9597
DESCENDING option, 9597
ORDER= option, 9597
TRUNCATE option, 9597
SURVEYIMPUTE procedure, CLUSTER statement, 9598
SURVEYIMPUTE procedure, ID statement, 9598
SURVEYIMPUTE procedure, IMPJOINT statement, 9598
SURVEYIMPUTE procedure, OUTPUT statement, 9599
OUT= option, 9599
OUTJKCOEFS= option, 9599
SURVEYIMPUTE procedure, PROC SURVEYIMPUTE statement, 9587
ABSEMWTCONV= option, 9588, 9589
DATA= option, 9588
DISP= option, 9589
FAY= option (VARMETHOD=BRR), 9594
HADAMARD= option (VARMETHOD=BRR), 9594
MAXDONORCELLS= option, 9589
MAXEMITER= option, 9589, 9590
METHOD= option, 9588
MH= method-option, 9593
NDONORS= option, 9591
NOPRINT option, 9591
ORDER= option, 9591
PRINTH option (VARMETHOD=BRR), 9595
RATE= option, 9592
RELEMWTCONV= option, 9589, 9590
REPS= option (VARMETHOD=BOOTSTRAP), 9594
REPS= option (VARMETHOD=BRR), 9595
REPWTADJ= option, 9590
SEED= option, 9592
SELECTION= option, 9590
TOTAL= option, 9592
VARMETHOD= option, 9593
SURVEYIMPUTE procedure, REPWEIGHTS statement, 9601
SURVEYIMPUTE procedure, STRATA statement, 9601
LIST option, 9601
SURVEYIMPUTE procedure, VAR statement, 9602
SURVEYIMPUTE procedure, WEIGHT statement, 9602

TOTAL= option
PROC SURVEYIMPUTE statement, 9592
TRUNCATE option
CLASS statement (SURVEYIMPUTE), 9597

VAR statement
SURVEYIMPUTE procedure, 9602
VARMETHOD= option
PROC SURVEYIMPUTE statement, 9593

WEIGHT statement
SURVEYIMPUTE procedure, 9602