Chapter 74
The LIFETEST Procedure

Contents

Overview: LIFETEST Procedure .................................................. 5566
Getting Started: LIFETEST Procedure ........................................... 5567
Syntax: LIFETEST Procedure .......................................................... 5576
   PROC LIFETEST Statement ....................................................... 5576
   BY Statement ........................................................................ 5588
   FREQ Statement .................................................................... 5588
   ID Statement .......................................................................... 5589
   STRATA Statement ................................................................. 5589
   TEST Statement ..................................................................... 5594
   TIME Statement ..................................................................... 5594
   WEIGHT Statement ................................................................. 5595
Details: LIFETEST Procedure ......................................................... 5596
   Missing Values ....................................................................... 5596
   Computational Formulas ........................................................... 5596
      Breslow, Fleming-Harrington, and Kaplan-Meier Methods .......... 5596
      Life-Table Method ............................................................... 5600
      Pointwise Confidence Limits in the OUTSURV= Data Set .......... 5601
      Simultaneous Confidence Intervals for Kaplan-Meier Curves .... 5603
      Kernel-Smoothed Hazard Estimate ......................................... 5605
      Comparison of Two or More Groups of Survival Data ............. 5607
      Rank Tests for the Association of Survival Time with Covariates . 5611
      Analysis of Competing-Risks Data ......................................... 5613
      Restricted Mean Analysis ...................................................... 5616
   Output Data Sets ..................................................................... 5618
      OUTCIF= Data Set ................................................................. 5618
      OUTSURV= Data Set ............................................................. 5619
      OUTTEST= Data Set .............................................................. 5621
   Displayed Output ..................................................................... 5621
   Plot Options Superseded by ODS Graphics ................................. 5631
   ODS Table Names .................................................................... 5635
   ODS Graphics ........................................................................ 5637
   Modifying the Survival Plots ...................................................... 5639
Examples: LIFETEST Procedure ...................................................... 5640
   Example 74.1: Product-Limit Estimates and Tests of Association .... 5640
   Example 74.2: Enhanced Survival Plot and Multiple-Comparison Adjustments . 5654
   Example 74.3: Life-Table Estimates for Males with Angina Pectoris ... 5659
Overview: LIFETEST Procedure

A common feature of lifetime or survival data is the presence of right-censored observations due either to withdrawal of experimental units or to termination of the experiment. For such observations, you know only that the lifetime exceeded a given value; the exact lifetime remains unknown. Such data cannot be analyzed by ignoring the censored observations because, among other considerations, the longer-lived units are generally more likely to be censored. The analysis methodology must correctly use the censored observations in addition to the uncensored observations.


Usually, a first step in the analysis of survival data is the estimation of the distribution of the survival times. Survival times are often called failure times, and event times are uncensored survival times. The survival distribution function (SDF), also known as the survivor function, is used to describe the lifetimes of the population of interest. The SDF evaluated at \( t \) is the probability that an experimental unit from the population will have a lifetime that exceeds \( t \)—that is,

\[
S(t) = \Pr(T > t)
\]

where \( S(t) \) denotes the survivor function and \( T \) is the lifetime of a randomly selected experimental unit. The LIFETEST procedure can be used to compute nonparametric estimates of the survivor function either by the product-limit method (also called the Kaplan-Meier method) or by the life-table method (also called the actuarial method). The life-table estimator is a grouped-data analog of the Kaplan-Meier estimator. The procedure can also compute the Breslow estimator or the Fleming-Harrington estimator, which are asymptotic equivalent alternatives to the Kaplan-Meier estimator.

Some functions closely related to the SDF are the cumulative distribution function (CDF), the probability density function (PDF), and the hazard function. The CDF, denoted \( F(t) \), is defined as \( 1 - S(t) \) and is the probability that a lifetime does not exceed \( t \). The PDF, denoted \( f(t) \), is defined as the derivative of \( F(t) \), and the hazard function, denoted \( h(t) \), is defined as \( f(t)/S(t) \). If the life-table method is chosen, the estimates of the probability density function can also be computed. Plots of these estimates can be produced with ODS Graphics.

An important task in the analysis of survival data is the comparison of survival curves. It is of interest to determine whether the underlying populations of \( k \) \((k \geq 2)\) samples have identical survivor functions. PROC LIFETEST provides nonparametric \( k \)-sample tests based on weighted comparisons of the estimated hazard rate of the individual population under the null and alternative hypotheses. Corresponding to various weight functions, a variety of tests can be specified, which include the log-rank test, Wilcoxon test, Tarone-Ware test, Peto-Peto test, modified Peto-Peto test, and Fleming-Harrington \( G_p \) family of tests. PROC LIFETEST also provides corresponding trend tests to detect ordered alternatives. Stratified tests can be specified to adjust for prognostic factors that affect the events rates in the various populations. A likelihood ratio test, based on an underlying exponential model, is also included to compare the survival curves of the samples.
There are other prognostic variables, called covariates, that are thought to be related to the failure time. These covariates can also be used to construct statistics to test for association between the covariates and the lifetime variable. PROC LIFETEST can compute two such test statistics: censored data linear rank statistics based on the exponential scores and the Wilcoxon scores. The corresponding tests are known as the log-rank test and the Wilcoxon test, respectively. These tests are computed by pooling over any defined strata, thus adjusting for the stratum variables.

One change in SAS 9.2 and later is that the calculation of confidence limits for the quartiles of survival time is based on the transformation specified by the CONFTYPE= option. Another change is that the SURVIVAL statement in SAS 9.1 is folded into the PROC LIFETEST statement; that is, options that were in the SURVIVAL statement can now be specified in the PROC LIFETEST statement. The SURVIVAL statement is no longer needed and it is not documented.

Starting in SAS/STAT 14.1, you can use PROC LIFETEST to carry out nonparametric analysis of competing-risks data. Competing risks arise in studies in which individuals are subject to a number of potential failure events and the occurrence of one event might impede the occurrence of other events. You can use PROC LIFETEST to estimate the cumulative incidence function (CIF), which is the probability subdistribution of failure of a specific cause. If you have more than one sample of competing-risks data, you can use PROC LIFETEST to perform Gray’s test (Gray 1988) to compare the CIFs of the samples.

---

**Getting Started: LIFETEST Procedure**

You can use the LIFETEST procedure to compute nonparametric estimates of the survivor functions, to compare survival curves, and to compute rank tests for association of the failure time variable with covariates.

For simple analyses, only the PROC LIFETEST and TIME statements are required. Consider a sample of survival data. Suppose that the time variable is $T$ and the censoring variable is $C$ with value 1 indicating censored observations. The following statements compute the product-limit estimate for the sample:

```sas
proc lifetest;
   time t*c(1);
   run;
```

You can use the STRATA statement to divide the data into various strata. A separate survivor function is then estimated for each stratum, and tests of the homogeneity of strata are performed. However, if the GROUP= option is also specified in the STRATA statement, the GROUP= variable is used to identify the samples whose survivor functions are to be compared, and the STRATA variables are used to define the strata for the stratified tests. You can specify covariates (prognostic variables) in the TEST statement, and PROC LIFETEST computes linear rank statistics to test the effects of these covariates on survival.

For example, consider the results of a small randomized trial on rats. Suppose you randomize 40 rats that have been exposed to a carcinogen into two treatment groups (Drug X and Placebo). The event of interest is death from cancer induced by the carcinogen. The response is the time from randomization to death. Four rats died of other causes; their survival times are regarded as censored observations. Interest lies in whether the survival distributions differ between the two treatments.

The following DATA step creates the data set `Exposed`, which contains four variables: `Days` (survival time in days from treatment to death), `Status` (censoring indicator variable: 0 if censored and 1 if not censored), `Treatment` (treatment indicator), and `Sex` (gender: F if female and M if male).
Chapter 74: The LIFETEST Procedure

```sas
proc format;
  value Rx 1='Drug X' 0='Placebo';
run;

data exposed;
  input Days Status Treatment Sex $ @@;
  format Treatment Rx.;
  datalines;
  179 1 1 F 378 0 1 M
  256 1 1 F 355 1 1 M
  262 1 1 M 319 1 1 M
  256 1 1 F 256 1 1 M
  255 1 1 M 171 1 1 F
  224 0 1 F 325 1 1 M
  225 1 1 F 325 1 1 M
  287 1 1 M 217 1 1 F
  319 1 1 M 255 1 1 F
  264 1 1 M 256 1 1 F
  237 0 0 F 291 1 0 M
  156 1 0 F 323 1 0 M
  270 1 0 M 253 1 0 M
  257 1 0 M 206 1 0 F
  242 1 0 M 206 1 0 F
  157 1 0 F 237 1 0 M
  249 1 0 M 211 1 0 F
  180 1 0 F 229 1 0 F
  226 1 0 F 234 1 0 F
  268 0 0 M 209 1 0 F
;
PROC LIFETEST is invoked as follows to compute the product-limit estimate of the survivor function for each treatment and to compare the survivor functions between the two treatments:

```sas
ods graphics on;
proc lifetest data=Exposed plots=(survival(atrisk) logsurv);
  time Days*Status(0);
  strata Treatment;
run;
ods graphics off;
```

In the TIME statement, the survival time variable, Days, is crossed with the censoring variable, Status, with the value 0 indicating censoring. That is, the values of Days are considered censored if the corresponding values of Status are 0; otherwise, they are considered as event times. In the STRATA statement, the variable Treatment is specified, which indicates that the data are to be divided into strata based on the values of Treatment. ODS Graphics must be enabled before producing graphs. Two plots are requested through the PLOTS= option—a plot of the survival curves with at risk numbers and a plot of the negative log of the survival curves.

The results of the analysis are displayed in the following figures.
Figure 74.1 displays the product-limit survival estimate for the Drug X group (Treatment=1). The figure lists, for each observed time, the survival estimate, failure rate, standard error of the estimate, cumulative number of failures, and number of subjects remaining in the study.

![Figure 74.1](image-url)

**Figure 74.1** Survivor Function Estimate for the Drug X-Treated Rats

**The LIFETEST Procedure**

**Stratum 1: Treatment = Drug X**

<table>
<thead>
<tr>
<th>Days</th>
<th>Survival</th>
<th>Failure</th>
<th>Survival Standard Error</th>
<th>Number Failed</th>
<th>Number Left</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>1.0000</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>20</td>
</tr>
<tr>
<td>171.000</td>
<td>0.9500</td>
<td>0.0500</td>
<td>0.0487</td>
<td>1</td>
<td>19</td>
</tr>
<tr>
<td>179.000</td>
<td>0.9000</td>
<td>0.1000</td>
<td>0.0671</td>
<td>2</td>
<td>18</td>
</tr>
<tr>
<td>217.000</td>
<td>0.8500</td>
<td>0.1500</td>
<td>0.0798</td>
<td>3</td>
<td>17</td>
</tr>
<tr>
<td>224.000</td>
<td>*</td>
<td>.</td>
<td>.</td>
<td>3</td>
<td>16</td>
</tr>
<tr>
<td>225.000</td>
<td>0.7969</td>
<td>0.2031</td>
<td>0.0908</td>
<td>4</td>
<td>15</td>
</tr>
<tr>
<td>255.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>5</td>
<td>14</td>
</tr>
<tr>
<td>255.000</td>
<td>0.6906</td>
<td>0.3094</td>
<td>0.1053</td>
<td>6</td>
<td>13</td>
</tr>
<tr>
<td>256.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>7</td>
<td>12</td>
</tr>
<tr>
<td>256.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>8</td>
<td>11</td>
</tr>
<tr>
<td>256.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>9</td>
<td>10</td>
</tr>
<tr>
<td>256.000</td>
<td>0.4781</td>
<td>0.5219</td>
<td>0.1146</td>
<td>10</td>
<td>9</td>
</tr>
<tr>
<td>262.000</td>
<td>0.4250</td>
<td>0.5750</td>
<td>0.1135</td>
<td>11</td>
<td>8</td>
</tr>
<tr>
<td>264.000</td>
<td>0.3719</td>
<td>0.6281</td>
<td>0.1111</td>
<td>12</td>
<td>7</td>
</tr>
<tr>
<td>287.000</td>
<td>0.3187</td>
<td>0.6813</td>
<td>0.1071</td>
<td>13</td>
<td>6</td>
</tr>
<tr>
<td>319.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>14</td>
<td>5</td>
</tr>
<tr>
<td>319.000</td>
<td>0.2125</td>
<td>0.7875</td>
<td>0.0942</td>
<td>15</td>
<td>4</td>
</tr>
<tr>
<td>325.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>16</td>
<td>3</td>
</tr>
<tr>
<td>325.000</td>
<td>0.1062</td>
<td>0.8938</td>
<td>0.0710</td>
<td>17</td>
<td>2</td>
</tr>
<tr>
<td>355.000</td>
<td>0.0531</td>
<td>0.9469</td>
<td>0.0517</td>
<td>18</td>
<td>1</td>
</tr>
<tr>
<td>378.000</td>
<td>*</td>
<td>.</td>
<td>.</td>
<td>18</td>
<td>0</td>
</tr>
</tbody>
</table>

*Note: The marked survival times are censored observations.*

Figure 74.2 displays summary statistics of survival times for the Drug X group. It contains estimates of the 25th, 50th, and 75th percentiles and the corresponding 95% confidence limits. The median survival time for rats in this treatment is 256 days. The mean and standard error are also displayed; however, these values are underestimated because the largest observed time is censored and the estimation is restricted to the largest event time.

![Figure 74.2](image-url)

**Figure 74.2** Summary Statistics of Survival Times for Drug X-Treated Rats

<table>
<thead>
<tr>
<th>Percent</th>
<th>Estimate</th>
<th>Transform</th>
<th>[Lower Upper]</th>
</tr>
</thead>
<tbody>
<tr>
<td>75</td>
<td>319.000</td>
<td>LOGLOG</td>
<td>256.000 355.000</td>
</tr>
<tr>
<td>50</td>
<td>256.000</td>
<td>LOGLOG</td>
<td>255.000 319.000</td>
</tr>
<tr>
<td>25</td>
<td>255.000</td>
<td>LOGLOG</td>
<td>171.000 256.000</td>
</tr>
</tbody>
</table>
Figure 74.2  continued

<table>
<thead>
<tr>
<th>Standard</th>
<th>Mean</th>
<th>Error</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>271.131</td>
<td>11.877</td>
</tr>
</tbody>
</table>

Note: The mean survival time and its standard error were underestimated because the largest observation was censored and the estimation was restricted to the largest event time.

Figure 74.3 and Figure 74.4 display the survival estimates and the summary statistics of the survival times for Placebo (Treatment=0). The median survival time for rats in this treatment is 235 days.

Figure 74.3  Survivor Function Estimate for Placebo-Treated Rats

The LIFETEST Procedure

Stratum 2: Treatment = Placebo

<table>
<thead>
<tr>
<th>Days</th>
<th>Survival</th>
<th>Failure</th>
<th>Standard Error</th>
<th>Number Failed</th>
<th>Number Left</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>1.0000</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>20</td>
</tr>
<tr>
<td>156.000</td>
<td>0.9500</td>
<td>0.0500</td>
<td>0.0487</td>
<td>1</td>
<td>19</td>
</tr>
<tr>
<td>157.000</td>
<td>0.9000</td>
<td>0.1000</td>
<td>0.0671</td>
<td>2</td>
<td>18</td>
</tr>
<tr>
<td>180.000</td>
<td>0.8500</td>
<td>0.1500</td>
<td>0.0798</td>
<td>3</td>
<td>17</td>
</tr>
<tr>
<td>206.000</td>
<td>....</td>
<td>....</td>
<td>....</td>
<td>4</td>
<td>16</td>
</tr>
<tr>
<td>206.000</td>
<td>0.7500</td>
<td>0.2500</td>
<td>0.0968</td>
<td>5</td>
<td>15</td>
</tr>
<tr>
<td>209.000</td>
<td>0.7000</td>
<td>0.3000</td>
<td>0.1025</td>
<td>6</td>
<td>14</td>
</tr>
<tr>
<td>211.000</td>
<td>0.6500</td>
<td>0.3500</td>
<td>0.1067</td>
<td>7</td>
<td>13</td>
</tr>
<tr>
<td>226.000</td>
<td>0.6000</td>
<td>0.4000</td>
<td>0.1095</td>
<td>8</td>
<td>12</td>
</tr>
<tr>
<td>229.000</td>
<td>0.5500</td>
<td>0.4500</td>
<td>0.1112</td>
<td>9</td>
<td>11</td>
</tr>
<tr>
<td>234.000</td>
<td>0.5000</td>
<td>0.5000</td>
<td>0.1118</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>237.000</td>
<td>0.4500</td>
<td>0.5500</td>
<td>0.1112</td>
<td>11</td>
<td>9</td>
</tr>
<tr>
<td>237.000*</td>
<td>....</td>
<td>....</td>
<td>....</td>
<td>11</td>
<td>8</td>
</tr>
<tr>
<td>242.000</td>
<td>0.3938</td>
<td>0.6063</td>
<td>0.1106</td>
<td>12</td>
<td>7</td>
</tr>
<tr>
<td>249.000</td>
<td>0.3375</td>
<td>0.6625</td>
<td>0.1082</td>
<td>13</td>
<td>6</td>
</tr>
<tr>
<td>253.000</td>
<td>0.2813</td>
<td>0.7188</td>
<td>0.1038</td>
<td>14</td>
<td>5</td>
</tr>
<tr>
<td>257.000</td>
<td>0.2250</td>
<td>0.7750</td>
<td>0.0971</td>
<td>15</td>
<td>4</td>
</tr>
<tr>
<td>268.000*</td>
<td>....</td>
<td>....</td>
<td>....</td>
<td>15</td>
<td>3</td>
</tr>
<tr>
<td>270.000</td>
<td>0.1500</td>
<td>0.8500</td>
<td>0.0891</td>
<td>16</td>
<td>2</td>
</tr>
<tr>
<td>291.000</td>
<td>0.0750</td>
<td>0.9250</td>
<td>0.0693</td>
<td>17</td>
<td>1</td>
</tr>
<tr>
<td>323.000</td>
<td>0</td>
<td>1.0000</td>
<td>.</td>
<td>18</td>
<td>0</td>
</tr>
</tbody>
</table>

Note: The marked survival times are censored observations.
**Figure 74.4** Summary Statistics of Survival Times for Placebo-Treated Rats

<table>
<thead>
<tr>
<th>Percent</th>
<th>Point Estimate</th>
<th>Transform</th>
<th>95% Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>75</td>
<td>257.000</td>
<td>LOGLOG</td>
<td>237.000 323.000</td>
</tr>
<tr>
<td>50</td>
<td>235.500</td>
<td>LOGLOG</td>
<td>206.000 253.000</td>
</tr>
<tr>
<td>25</td>
<td>207.500</td>
<td>LOGLOG</td>
<td>156.000 229.000</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>Mean</th>
<th>Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>235.156</td>
<td>10.211</td>
</tr>
</tbody>
</table>

A summary of the number of censored and event observations is shown in **Figure 74.5**. The figure lists, for each stratum, the number of event and censored observations, and the percentage of censored observations.

**Figure 74.5** Number of Event and Censored Observations

<table>
<thead>
<tr>
<th>Stratum</th>
<th>Treatment</th>
<th>Total</th>
<th>Failed</th>
<th>Censored</th>
<th>Percent Censored</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Drug X</td>
<td>20</td>
<td>18</td>
<td>2</td>
<td>10.00</td>
</tr>
<tr>
<td>2</td>
<td>Placebo</td>
<td>20</td>
<td>18</td>
<td>2</td>
<td>10.00</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>40</td>
<td>36</td>
<td>4</td>
<td>10.00</td>
</tr>
</tbody>
</table>

**Figure 74.6** displays the graph of the product-limit survivor function estimates versus survival time. The two treatments differ primarily at larger survival times. Note the number of subjects at risk in the plot. You can display the number of subjects at risk at specific time points by using the ATRISK= option.
Figure 74.6  Plot of Estimated Survivor Functions

Figure 74.7 displays the graph of the log survivor function estimates versus survival time. Neither curve approximates a straight line through the origin—the exponential model is not appropriate for the survival data.

Note that these graphical displays are generated through ODS. For general information about ODS Graphics, see Chapter 21, “Statistical Graphics Using ODS.”
Results of the comparison of survival curves between the two treatments are shown in Figure 74.8. The rank tests for homogeneity indicate a significant difference between the treatments ($p = 0.0175$ for the log-rank test and $p = 0.0249$ for the Wilcoxon test). Rats treated with Drug X live significantly longer than those treated with Placebo. Since the survival curves for the two treatments differ primarily at longer survival times, the Wilcoxon test, which places more weight on shorter survival times, becomes less significant than the log-rank test. As noted earlier, the exponential model is not appropriate for the given survival data; consequently, the result of the likelihood ratio test should be ignored.

**Figure 74.8** Results of the Two-Sample Tests

<table>
<thead>
<tr>
<th>Test of Equality over Strata</th>
<th>Chi-Square</th>
<th>DF</th>
<th>Pr &gt; Chi-Square</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log-Rank</td>
<td>5.6485</td>
<td>1</td>
<td>0.0175</td>
</tr>
<tr>
<td>Wilcoxon</td>
<td>5.0312</td>
<td>1</td>
<td>0.0249</td>
</tr>
<tr>
<td>-2Log(LR)</td>
<td>0.1983</td>
<td>1</td>
<td>0.6561</td>
</tr>
</tbody>
</table>
Next, suppose male rats and female rats are thought to have different survival rates, and you want to assess the treatment effect while adjusting for the gender differences. By specifying the variable Sex in the STRATA statement as a stratifying variable and by specifying the variable Treatment in the GROUP= option, you can carry out a stratified test to test Treatment while adjusting for Sex. The test statistics are computed by pooling over the strata defined by the values of Sex, thus controlling for the effect of Sex. The NOTABLE option is added to the PROC LIFETEST statement as follows to avoid estimating a survival curve for each gender:

```
proc lifetest data=Exposed notable;
  time Days*Status(0);
  strata Sex / group=Treatment;
run;
```

Results of the stratified tests are shown in Figure 74.9. The treatment effect is statistically significant for both the log-rank test ($p = 0.0071$) and the Wilcoxon test ($p = 0.0150$). As compared to the results of the unstratified tests in Figure 74.8, the significance of the treatment effect has been sharpened by controlling for the effect of the gender of the subjects.

![Figure 74.9 Results of the Stratified Two-Sample Tests](image)

The LIFETEST Procedure

<table>
<thead>
<tr>
<th>Stratified Test of Equality over Group</th>
<th>Pr &gt; Chi-Square</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test</td>
<td>Chi-Square</td>
</tr>
<tr>
<td>Log-Rank</td>
<td>7.2466</td>
</tr>
<tr>
<td>Wilcoxon</td>
<td>5.9179</td>
</tr>
</tbody>
</table>

Since Treatment is a binary variable, another way to study the effect of Treatment is to carry out a censored linear rank test with Treatment as an independent variable. This test is less popular than the two-sample test; nevertheless, in situations where the independent variables are continuous and are difficult to discretize, it might be infeasible to perform a $k$-sample test. To compute the censored linear rank statistics to test the Treatment effect, Treatment is specified in the TEST statement as follows:

```
proc lifetest data=Exposed notable;
  time Days*Status(0);
  test Treatment;
run;
```

Results of the linear rank tests are shown Figure 74.10. The $p$-values are very similar to those of the two-sample tests in Figure 74.8.
### Figure 74.10 Results of Linear Rank Tests of Treatment

**The LIFETEST Procedure**

<table>
<thead>
<tr>
<th>Variable</th>
<th>Test Statistic</th>
<th>Standard Error</th>
<th>Chi-Square</th>
<th>Pr &gt; Chi-Square</th>
</tr>
</thead>
<tbody>
<tr>
<td>Treatment</td>
<td>3.9525</td>
<td>1.7524</td>
<td>5.0875</td>
<td>0.0241</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Variable</th>
<th>Test Statistic</th>
<th>Standard Error</th>
<th>Chi-Square</th>
<th>Pr &gt; Chi-Square</th>
</tr>
</thead>
<tbody>
<tr>
<td>Treatment</td>
<td>6.2708</td>
<td>2.6793</td>
<td>5.4779</td>
<td>0.0193</td>
</tr>
</tbody>
</table>

With Sex as a prognostic factor that you want to control, you can compute a stratified linear rank statistic to test the effect of Treatment by specifying Sex in the STRATA statement and Treatment in the TEST statement as in the following program. The TEST=NONE option is specified in the STRATA statement to suppress the two-sample tests for Sex.

```sas
proc lifetest data=Exposed notable;
  time Days*Status(0);
  strata Sex / test=none;
  test Treatment;
run;
```

Results of the stratified linear rank tests are shown in **Figure 74.11**. The p-values are very similar to those of the stratified tests in **Figure 74.9**.

### Figure 74.11 Results of Stratified Linear Rank Tests of Treatment

**The LIFETEST Procedure**

<table>
<thead>
<tr>
<th>Variable</th>
<th>Test Statistic</th>
<th>Standard Error</th>
<th>Chi-Square</th>
<th>Pr &gt; Chi-Square</th>
</tr>
</thead>
<tbody>
<tr>
<td>Treatment</td>
<td>4.2372</td>
<td>1.7371</td>
<td>5.9503</td>
<td>0.0147</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Variable</th>
<th>Test Statistic</th>
<th>Standard Error</th>
<th>Chi-Square</th>
<th>Pr &gt; Chi-Square</th>
</tr>
</thead>
<tbody>
<tr>
<td>Treatment</td>
<td>6.8021</td>
<td>2.5419</td>
<td>7.1609</td>
<td>0.0075</td>
</tr>
</tbody>
</table>
Chapter 74: The LIFETEST Procedure

Syntax: LIFETEST Procedure

The following statements are available in the LIFETEST procedure:

```
PROC LIFETEST <options> ;
   BY variables ;
   FREQ variable < / option > ;
   ID variables ;
   STRATA variable < (list) > < . . . variable < (list) > > < / options > ;
   TEST variables ;
   TIME variable < censor(list) > < / option > ;
   WEIGHT variable ;
```

The simplest use of PROC LIFETEST is to request the nonparametric estimates of the survivor function for a sample of survival times. In such a case, only the PROC LIFETEST statement and the TIME statement are required. You can use the STRATA statement to divide the data into various strata. A separate survivor function is then estimated for each stratum, and tests of the homogeneity of strata are performed. However, if the GROUP= option is also specified in the STRATA statement, stratified tests are carried out to test the k samples that are defined by the GROUP= variable while controlling for the effect of the STRATA variables. You can specify covariates in the TEST statement. PROC LIFETEST computes linear rank statistics to test the effects of these covariates on survival.

The PROC LIFETEST statement invokes the procedure. All statements except the TIME statement are optional, and there is no required order for the statements that follow the PROC LIFETEST statement. The TIME statement specifies the variables that define the survival time and censoring indicator. The STRATA statement specifies a variable or set of variables that define the strata for the analysis. The TEST statement specifies a list of numeric covariates to be tested for their association with the response survival time. Each variable is tested individually, and a joint test statistic is also computed. The ID statement provides a list of variables whose values identify observations in the product-limit, Breslow, or Fleming-Harrington estimates. When only the TIME statement appears, no strata are defined and no tests of homogeneity are performed.

PROC LIFETEST Statement

```
PROC LIFETEST < options > ;
```

The PROC LIFETEST statement invokes the LIFETEST procedure. Optionally, this statement identifies an input data set and an output data set, and specifies the computation details of the survivor function estimation. Table 74.1 summarizes the options available in the PROC LIFETEST statement. These options are described in alphabetic order.

ODS Graphics is the preferred method of creating graphs. Many new features have been added to the ODS Graphics plots. For example, you can display the number of subjects at risk in a survival plot. For information about ODS Graphics options, see the PLOTS= option.

If no plotting options are specified, PROC LIFETEST displays a table that shows the product-limit estimate of the survivor function. If ODS Graphics is enabled, PROC LIFETEST also displays a plot of the estimated survivor function. Other options for displaying the estimated survivor function are documented in the section “Plot Options Superseded by ODS Graphics” on page 5631.
Table 74.1 Options Available in the PROC LIFETEST Statement

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input and Output Data Sets</strong></td>
<td></td>
</tr>
<tr>
<td>DATA=</td>
<td>Specifies the input SAS data set</td>
</tr>
<tr>
<td>OUTCIF=</td>
<td>Names an output data set to contain cumulative incidence function (CIF) estimates</td>
</tr>
<tr>
<td>OUTSURV=</td>
<td>Names an output data set to contain survivor function estimates</td>
</tr>
<tr>
<td>OUTTEST=</td>
<td>Names an output data set to contain rank test statistics for association of survival time with covariates</td>
</tr>
<tr>
<td><strong>Nonparametric Estimation</strong></td>
<td></td>
</tr>
<tr>
<td>ERROR=</td>
<td>Specifies the variance method of the CIF estimator</td>
</tr>
<tr>
<td>INTERVALS=</td>
<td>Specifies interval endpoints for life-table estimates</td>
</tr>
<tr>
<td>NELSON</td>
<td>Adds the Nelson-Aalen estimates</td>
</tr>
<tr>
<td>METHOD=</td>
<td>Specifies the method to compute survivor function</td>
</tr>
<tr>
<td>NINTERVAL=</td>
<td>Specifies the number of intervals for life-table estimates</td>
</tr>
<tr>
<td>RMST</td>
<td>Performs the restricted mean survival time (RMST) analysis</td>
</tr>
<tr>
<td>RMTL</td>
<td>Performs the restricted mean time lost (RMTL) analysis</td>
</tr>
<tr>
<td>WIDTH=</td>
<td>Specifies the width of intervals for life-table estimates</td>
</tr>
<tr>
<td><strong>Confidence Limits for Survivorship</strong></td>
<td></td>
</tr>
<tr>
<td>ALPHA=</td>
<td>Sets the confidence level for interval estimation estimates</td>
</tr>
<tr>
<td>BANDMAXTIME=</td>
<td>Specifies the maximum time for confidence band</td>
</tr>
<tr>
<td>BANDMINTIME=</td>
<td>Specifies the minimum time for confidence band</td>
</tr>
<tr>
<td>CONFBAND=</td>
<td>Specifies the type of confidence band in the OUTSURV= data set</td>
</tr>
<tr>
<td>CONFTYPE=</td>
<td>Specifies the transformation applied to the survivor function to obtain confidence limits</td>
</tr>
<tr>
<td><strong>ODS Graphics</strong></td>
<td></td>
</tr>
<tr>
<td>MAXTIME=</td>
<td>Specifies the maximum time value for plotting</td>
</tr>
<tr>
<td>PLOTS=</td>
<td>Specifies plots to display</td>
</tr>
<tr>
<td><strong>Control Output</strong></td>
<td></td>
</tr>
<tr>
<td>ATRISK</td>
<td>Adds the number of subjects at risk to the survival estimate table</td>
</tr>
<tr>
<td>INTERVALS=</td>
<td>Displays only the estimate for the smallest time in each interval</td>
</tr>
<tr>
<td>NOLEFT</td>
<td>Suppresses the Number Left and Number Event columns in the survival estimate table</td>
</tr>
<tr>
<td>NOPRINT</td>
<td>Suppresses the display of printed output</td>
</tr>
<tr>
<td>NOTABLE</td>
<td>Suppresses the display of survival function estimates</td>
</tr>
<tr>
<td>REDUCEOUT=</td>
<td>Lists only INTERVALS= or TIMELIST= observations in the OUTSURV= data set</td>
</tr>
<tr>
<td>TIMELIST=</td>
<td>Lists the time points at which to display the survival estimate</td>
</tr>
<tr>
<td><strong>Miscellaneous</strong></td>
<td></td>
</tr>
<tr>
<td>ALPHAQT=</td>
<td>Sets the confidence level for survival time quartiles</td>
</tr>
<tr>
<td>CIFVAR</td>
<td>Displays the variance of the CIF estimator</td>
</tr>
<tr>
<td>MISSING</td>
<td>Allows missing values to be a stratum level</td>
</tr>
</tbody>
</table>
### Table 74.1 continued

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>SINGULAR=</td>
<td>Sets the tolerance for testing singularity of covariance matrix of rank statistics</td>
</tr>
<tr>
<td>STDERR</td>
<td>Outputs the standard error for the survival estimators to the OUTSURV= data set</td>
</tr>
<tr>
<td>TIMELIM=</td>
<td>Specifies the time limit used to estimate the mean survival time and its standard error</td>
</tr>
</tbody>
</table>

**ALPHA=**

specifies the level of significance $\alpha$ for the $100(1 - \alpha)$% confidence intervals for the survivor, hazard, and density functions. For example, the option ALPHA=0.05 requests the 95% confidence limits for the survivor function. The default value is 0.05.

**ALPHAQT=**

specifies the significance level $\alpha$ for the $100(1 - \alpha)$% confidence intervals for the quartiles of the survival time. For example, the option ALPHAQT=0.05 requests a 95% confidence interval for the quartiles of the survival time. The default value is 0.05.

**ATRISK**

adds a column that represents the number of subjects at risk to the survival estimate table. Also added is a column that represents the number of events at each observed time. This option has no effect for the life-table method.

**BANDMAXTIME=**

**BANDMAX=**

specifies the maximum time for the confidence bands. The default is the largest observed event time. If the specified BANDMAX= time exceeds the largest observed event time, it is truncated to the largest observed event time.

**BANDMINTIME=**

**BANDMIN=**

specifies the minimum time for the confidence bands. The default is the smallest observed event time. For the equal-precision band, if the BANDMIN= value is less than the smallest observed event time, it is defaulted to the smallest observed event time.

**CIFVAR**

displays the variance of the cumulative incidence function (CIF) estimator for competing-risks data. By default, PROC LIFETEST displays the standard error of the CIF estimator.

**CONFBAND=**

specifies the confidence bands to be output to the OUTSURV= data set. Confidence bands are available for METHOD=KM, METHOD=BRESLOW, or METHOD=FH. You can use the following *keywords*:

- **ALL** outputs both the Hall-Wellner and the equal-precision confidence bands.
- **EP** outputs the equal-precision confidence bands.
- **HW** outputs the Hall-Wellner confidence bands.
CONFTYPE=keyword
specifies the transformation applied to $S(t)$ to obtain the pointwise confidence intervals and the confidence bands for the survivor function in addition to the confidence intervals for the quartiles of the survival times. The following keywords can be used; the default is CONFTYPE=LOGLOG.

ASINSQRT the arcsine-square root transformation,
$$g(x) = \sin^{-1}(\sqrt{x})$$
LOGLOG the log-log transformation,
$$g(x) = \log(-\log(x))$$
This is also referred to as the log cumulative hazard transformation since it applies the logarithmic function to the cumulative hazard function. Collett (1994) and Lachin (2000) refer to it as the complementary log-log transformation.
LINEAR the identity transformation,
$$g(x) = x$$
LOG the logarithmic transformation,
$$g(x) = \log(x)$$
LOGIT the logit transformation,
$$g(x) = \log\left(\frac{x}{1-x}\right)$$

DATA=SAS-data-set
names the SAS data set used by PROC LIFETEST. By default, the most recently created SAS data set is used.

ERROR=AALEN | DELTA
specifies the method of calculating the variance of the CIF estimator. When ERROR=AALEN, the variance estimator is based on the theory of counting process (Aalen 1978). When ERROR=DELTA, the delta method is used to compute the variance. By default, ERROR=AALEN. For more information, see the section “Estimation of the CIF” on page 5614.

INTERVALS=values
specifies a list of interval endpoints for the life-table method. These endpoints must all be nonnegative numbers. The initial interval is assumed to start at zero whether or not zero is specified in the list. Each interval contains its lower endpoint but does not contain its upper endpoint. When this option is used with METHOD=KM, METHOD=BRESLOW, or METHOD=FH, it reduces the number of survival estimates displayed by showing only the estimates for the smallest time within each specified interval. The INTERVALS= option can be specified in any of the following ways:
- a list separated by blanks  INTERVALS=1 3 5 7
- a list separated by commas  INTERVALS=1, 3, 5, 7
- x to y  INTERVALS=1 to 7
- x to y BY z  INTERVALS=1 to 7 by 1
- a combination of the above  INTERVALS=1, 3 to 5, 7
For example, the specification
\[ \text{intervals}=5,10 \text{ to 30 by 10} \]

produces the set of intervals
\[ \{[0, 5), [5, 10), [10, 20), [20, 30), [30, \infty)\} \]

**MAXTIME=value**
specifies the maximum value of the time variable allowed on the plots so that outlying points do not determine the scale of the time axis of the plots. This option affects only the displayed plots and has no effect on any calculations.

**METHOD=type**
specifies the method to be used to compute the survival function estimates. Valid values for type are as follows:

- **BRESLOW**
  specifies that the Breslow estimates be computed. The Breslow estimator is the exponentiation of the negative Nelson-Aalen estimator of the cumulative hazard function.

- **FH**
  specifies that the Fleming-Harrington (FH) estimates be computed. The FH estimator is a tie-breaking modification of the Breslow estimator. If there are no tied event times, this estimator is the same as the Breslow estimator.

- **KM**
- **PL**
  specifies that Kaplan-Meier estimates (also known as the product-limit estimates) be computed.

- **ACT**
- **LIFE**
- **LT**
  specifies that life-table estimates (also known as actuarial estimates) be computed.

By default, METHOD=KM.

**MISSING**
treats missing values as valid values for the stratum variables. By default, PROC LIFETEST does not use observations that have a missing value in any stratum variables. For more information, see the section “Missing Values” on page 5596.

**NELSON**
**AALEN**
produces the Nelson-Aalen estimates of the cumulative hazards and the corresponding standard errors. This option is ignored if METHOD=LT is specified.

**NINTERVAL=value**
specifies the number of intervals used to compute the life-table estimates of the survivor function. This parameter is overridden by the WIDTH= option or the INTERVALS= option. When you specify the NINTERVAL= option, PROC LIFETEST tries to find an interval that results in round numbers for the endpoints. Consequently, the number of intervals can be different from the number requested. Use the INTERVALS= option to control the interval endpoints. The default is NINTERVAL=10.
NOLEFT
suppresses the Number Left and Number Event columns in the survival estimate table. This option has no effect for the life-table estimate.

NOPRINT
suppresses the display of output. This option is useful when only an output data set is needed. It temporarily disables the Output Delivery System (ODS); For more information about ODS, see Chapter 20, “Using the Output Delivery System.”

NOTABLE
suppresses the display of survival function estimates. Only the number of censored and event times, plots, and test results is displayed.

OUTCIF= SAS-data-set
creates an output SAS data set to contain the point and interval estimates for the cumulative incidence function (CIF). The data set also contains the number of subjects at risk, the number of events of interest, and the number of events of all types. For more information about the contents of the OUTCIF= data set, see the section “OUTCIF= Data Set” on page 5618.

OUTSURV= SAS-data-set
OUTS= SAS-data-set
creates an output SAS data set to contain the estimates of the survival function and corresponding confidence limits for all strata. For more information about the contents of the OUTSURV= data set, see the section “OUTSURV= Data Set” on page 5619.

OUTTEST= SAS-data-set
OUTT= SAS-data-set
creates an output SAS data set to contain the overall chi-square test statistic for association with failure time for the variables in the TEST statement, the values of the univariate rank test statistics for each variable in the TEST statement, and the estimated covariance matrix of the univariate rank test statistics. For more information about the contents of the OUTTEST= data set, see the section “OUTTEST= Data Set” on page 5621.

RMST< (options) >
performs the analysis of the restricted mean survival time (RMST). You can specify the following options:

BC
applies bias correction to standard error estimation.

TAU=value
specifies the upper time limit of the RMST. The value must be positive. The default is the largest observed time.

RMTL< (options) >
performs the analysis of the restricted mean time lost (RMTL). You can specify the following options:

BC
applies bias correction to standard error estimation.
**TAU=** value  
specifies the upper time limit of the RMTL. The value must be positive. The default is the largest observed time.

**PLOTS<** (global-plot-options) >= plot-request < (options) >  
**PLOTS<** (global-plot-options) >= (plot-request < (options) > < ... plot-request < (options) > >)  
controls the plots produced using ODS Graphics. When you specify only one plot-request, you can omit the parentheses around the plot-request. Here are some examples:

- `plots=none`
- `plots= (survival(atrisk=100 to 350 by 50) logsurv)`
- `plots(only)=hazard`

ODS Graphics must be enabled before plots can be requested. For example:

```
ods graphics on;

proc lifetest plots=survival(atrisk);
  time T*Status(0);
run;

ods graphics off;
```

For more information about enabling and disabling ODS Graphics, see the section “Enabling and Disabling ODS Graphics” on page 623 in Chapter 21, “Statistical Graphics Using ODS.”

If ODS Graphics is enabled but you do not specify the PLOTS= option, PROC LIFETEST produces a plot of the survivor function estimates, unless you use the FAILCODE option in the TIME statement to stipulate a competing-risks analysis. In such a case, PROC LIFETEST creates a plot of the cumulative incidence function (CIF) estimates.

You can specify the following `global-plot-option`:

**ONLY**  
specifies that only the specified plots in the list be produced; otherwise, the default survivor function plot is also displayed. This option has no effect if you use the FAILCODE option in the TIME statement to stipulate a competing-risks analysis.

The `plot-requests` and `plot-request options` include the following:

**ALL**  
produces all appropriate plots. For METHOD=KM, METHOD=BRESLOW, or METHOD=FH, specifying PLOTS=ALL is equivalent to specifying PLOTS=(SURVIVAL LOGSURV LOGLOGS); for the life-table method, specifying PLOTS=ALL is equivalent to specifying PLOTS=(SURVIVAL LOGSURV LOGLOGS DENSITY HAZARD). For a competing-risks analysis, specifying PLOTS=ALL is equivalent to specifying PLOTS=CIF.
PROC LIFETEST Statement  5583

CIF< (cif-options) >
plots the cumulative incidence function (CIF) estimates. If you specify a STRATA statement without the GROUP= option, PROC LIFETEST overlays the cumulative incidence curves of the strata in the same plot. If you specify a STRATA statement with the GROUP= option, PROC LIFETEST produces a panel plot, with one cell per stratum, and each cell contains the cumulative incidence curves for the groups within the given stratum.

You can specify the following cif-options:

CL

displays pointwise confidence limits for CIF.

TEST

displays the p-value of Gray’s test (Gray 1988) for testing the homogeneity of CIFs.

HAZARD < (hazard-options) >

H < hazard-options >
plots the estimated hazard functions. Kernel-smoothed estimates are produced for METHOD=KM, METHOD=BRESLOW, or METHOD=FH. You can specify the following hazard-options, but only the CL option can be used for the life-table method:

BANDWIDTH=bandwidth-option

BW=bandwidth-option

specifies what bandwidth is chosen for the kernel-smoothing and how it is chosen. You can specify one of the following bandwidth-options.

value

sets the bandwidth to the given value.

numeric-list

selects the bandwidth from the given numeric-list that minimizes the mean integrated squared error.

RANGE(lower,upper)

selects the bandwidth from the interval (lower, upper) that minimizes the mean integrated squared error. PROC LIFETEST uses the golden section search algorithm to find the minimum. If there is more than one local minimum in the interval, there is no guarantee that the local minimum found is also the global minimum.

See the section “Optimal Bandwidth” on page 5606 for details about the mean integrated squared error. If the BANDWIDTH= option is not specified, the default is BANDWIDTH= RANGE(0.2$b$, 20$b$), where $b = \frac{g_u - g_l}{8n^{1/3}}$, $g_l$ and $g_u$ are the values of the GRIDL= and GRIDU= options, respectively, and $n$ is the total number of noncensored observations.

CL

displays the pointwise confidence limits for the smoothed hazard.

GRIDL=number

specifies the lower grid limit for the kernel-smoothed estimate. The default value is the time origin.
**GRIDU=number**  
specifies the upper grid limit for the kernel-smoothed estimate. The default value equals the maximum event time.

**KERNEL=kernel-option**  
specifies the kernel used. You can specify the following kernel-options:

- **BIWEIGHT**
  - **BW**  
    \[ K_{BW}(x) = \frac{15}{16} (1 - x^2)^2, \quad -1 \leq x \leq 1 \]

- **EPANECHNIKOV**
  - **E**  
    \[ K_{E}(x) = \frac{3}{4} (1 - x^2), \quad -1 \leq x \leq 1 \]

- **UNIFORM**
  - **U**  
    \[ K_{U}(x) = \frac{1}{2}, \quad -1 \leq x \leq 1 \]

By default, **KERNEL=EPANECHNIKOV**.

**NGRID=number**  
specifies the number of grid points. By default, **NGRID=101**.

**NMINGRID=number**  
specifies the number of grid points that are used in determining the mean integrated square error (MISE). By default, **NMINGRID=51**.

**LOGLOGS**  
**LLS**  
plots the log of negative log of estimated survivor functions versus the log of time.

**LOGSURV**  
**LS**  
plots the negative log of estimated survivor functions versus time.

**NONE**  
suppresses all plots.

**PDF < (CL) >**  
**P < (CL) >**  
plots the estimated probability density functions (life-table method only). Pointwise confidence limits are displayed optionally by specifying the CL option.

**RMST< CL >**  
plots the restricted mean survival time (RMST) versus \( \tau \) values. If you specify a STRATA statement without the GROUP= option, **PROC LIFETEST** overlays the RMST curves of the strata in the same plot. If you specify a STRATA statement with the GROUP= option, the procedure produces a panel plot that has one cell per stratum, and each cell contains the RMST curves for the groups within the given stratum. The CL option displays pointwise confidence limits for the RMST.
RMTL< CL >
plots the restricted mean survival time (RMTL) versus τ values. If you specify a STRATA statement without the GROUP= option, PROC LIFETEST overlays the RMTL curves of the strata in the same plot. If you specify a STRATA statement with the GROUP= option, the procedure produces a panel plot that has one cell per stratum, and each cell contains the RMTL curves for the groups within the given stratum. The CL option displays pointwise confidence limits for the RMTL.

SURVIVAL < (survival-options) >
S < (survival-options) >
plots the estimated survivor functions. Censored times are plotted as a plus sign on the Kaplan-Meier, Breslow, or Fleming-Harrington survival curves unless the NOCENSOR option is specified. You can customize the display by using the following survival-options. If these options are not sufficient for your purposes, you can customize the survival plot by modifying its graph template. (For more information, see the section “Modifying the Survival Plots” on page 5639.)

ATRISK < (options) > <=number-list>
displays the numbers of subjects at risk at the given times. You can specify the following options:

ATRISKTICK
ATRISKLABEL
 guarantees that tick values are shown on the time axis for those times when the numbers of subjects at risk are displayed. If this option is not specified, you might not be able to tell at exactly which times the number of subjects at risk are displayed. If the ATRISKTICKONLY option is also specified, it takes precedence over the ATRISKTICK option.

ATRISKTICKONLY
 specifies that tick values on the time axis be shown only at the times that are given in the ATRISK= list. If the ATRISKTICK option is also specified, it is ignored; that is, ATRISKTICKONLY takes precedence over ATRISKTICK.

MAXLEN=n
 specifies the number of characters n that are allowed for displaying the stratum labels. If n is greater than or equal to the maximum length of the stratum labels, the stratum labels are used in the at-risk display; otherwise, the stratum numbers are used. The default is MAXLEN=12.

OUTSIDE< (p) >
specifies that the at-risk table be drawn outside the plot area. PROC LIFETEST uses a graph template that has a two-row lattice layout. The upper cell displays the survival plot, and the bottom cell displays the at-risk table. You can specify an optional number p that represents the fractional proportion of the at-risk table height relative to the overall grid height, but that specification is not necessary. By default, p is the preferred row weight in the GTL layout lattice statement that ensures that the plot displays well. If you specify a value of p too small for the table to be properly displayed, some of the rows might get cut off.
The number-list identifies the times when the numbers at risk are displayed. If the number-list is not specified, PROC LIFETEST displays the number of subjects at risk at each default tick value on the time axis of the survival plot.

CB <=keyword>

displays the confidence bands (that is, simultaneous confidence intervals) for the survivor functions. You can specify one of the following keywords. The default is CB=HW.

ALL

displays both the equal-precision and the Hall-Wellner bands.

EP

displays the equal-precision band.

HW

displays the Hall-Wellner confidence band.

CL

displays the pointwise confidence limits for the survivor functions.

FAILURE

F

changes all the displays for survivor functions to those for the failure functions. For example, if both the FAILURE and CL options are specified, the plot displays the failure curves in addition to the pointwise confidence limits for the failure functions.

NOCENSOR

suppresses the plotting of the censored times on a Kaplan-Meier, Breslow, or Fleming-Harrington survival curve.

STRATA=strata-option

specifies how to display the survival/failure curves for multiple strata. This option has no effect if there is only one stratum. You can choose one of the following strata options:

INDIVIDUAL

UNPACK

specifies that a separate plot be displayed for each stratum.

OVERLAY

specifies that the survival/failure curves for the strata be overlaid in one plot.

PANEL

specifies that separate plots for the strata be organized into panels of two or four plots, depending on the number of strata.

The default is STRATA=OVERLAY.

TEST

displays the p-value of a homogeneity test specified in the STRATA statement. If more than one test is produced, the test is chosen in the following order: LOGRANK, WILCOXON, TARONE, PETO, MODPETO, FLEMING, and LR.
**REDUCEOUT**

specifies that the OUTSURV= data set contain only those observations that are included in the INTERVALS= or TIMELIST= option. This option has no effect if the OUTSURV= option is not specified. It also has no effect if neither the INTERVALS= option nor the TIMELIST= option is specified.

**SINGULAR=value**

specifies the tolerance for testing singularity of the covariance matrix for the rank test statistics. The test requires that a pivot for sweeping a covariance matrix be at least this number times a norm of the matrix. The default value is 1E–12.

**STDERR**

specifies that the standard error of the survivor function (SDF_STDERR) be output to the OUTSURV= data set. If the life-table method is used, the standard error of the density function (PDF_STDERR) and the standard error of the hazard function (HAZ_STDERR) are also output.

**TIMELIM=time-limit**

specifies the time limit used in the estimation of the mean survival time and its standard error. The mean survival time can be shown to be the area under the Kaplan-Meier survival curve. However, if the largest observed time in the data is censored, the area under the survival curve is not a closed area. In such a situation, you can choose a time limit \( L \) and estimate the mean survival curve limited to a time \( L \) (Lee 1992, pp. 72–76). This option is ignored if the largest observed time is an event time. Valid time-limit values are as follows:

**EVENT**

**LET**

specifies that the time limit \( L \) be the largest event time in the data. TIMELIM=EVENT is the default.

**OBSERVED**

**LOT**

specifies that the time limit \( L \) be the largest observed time in the data.

**number**

specifies that the time limit \( L \) be the given number. The number must be positive and at least as large as the largest event time in the data.

**TIMELIST=number-list**

specifies a list of time points at which the Kaplan-Meier estimates are displayed. The time points are listed in the column labeled Timelist. Since the Kaplan-Meier survival curve is a decreasing step function, each given time point falls in an interval that has a constant survival estimate. The event time that corresponds to the beginning of the time interval is displayed along with its survival estimate.

**WIDTH=value**

sets the width of the intervals used in the life-table calculation of the survival function. This parameter is overridden by the INTERVALS= option.


**BY Statement**

\[
\text{BY variables ;}
\]

You can specify a BY statement in PROC LIFETEST to obtain separate analyses of observations in groups that are defined by the BY variables. When a BY statement appears, the procedure expects the input data set to be sorted in order of the BY variables. If you specify more than one BY statement, only the last one specified is used.

If your input data set is not sorted in ascending order, use one of the following alternatives:

- Sort the data by using the SORT procedure with a similar BY statement.
- Specify the NOTSORTED or DESCENDING option in the BY statement in the LIFETEST procedure. The NOTSORTED option does not mean that the data are unsorted but rather that the data are arranged in groups (according to values of the BY variables) and that these groups are not necessarily in alphabetical or increasing numeric order.
- Create an index on the BY variables by using the DATASETS procedure (in Base SAS software).

The BY statement is more efficient than the STRATA statement for defining strata in large data sets. However, if you use the BY statement to define strata, PROC LIFETEST does not pool over strata for testing the association of survival time with covariates, nor does it test for homogeneity across the BY groups.

When the life-table method is used to estimate survivor functions, each BY group might have a different set of intervals. To make intervals the same across BY groups, use the INTERVALS= or WIDTH= option in the PROC LIFETEST statement.

For more information about BY-group processing, see the discussion in *SAS Language Reference: Concepts*. For more information about the DATASETS procedure, see the discussion in the *Base SAS Procedures Guide*.

**FREQ Statement**

\[
\text{FREQ variable } / \text{option} ;
\]

The FREQ statement identifies a variable that contains the frequency of occurrence of each observation. PROC LIFETEST treats each observation as if it appeared \(n\) times, where \(n\) is the value of the FREQ variable for the observation. The FREQ statement is useful for producing life tables when the data are already in the form of a summary data set. If it is not an integer, it is truncated to an integer unless the NOTRUNCATE option is specified. If it is missing or less than or equal zero, the observation is not used.

The following option can be specified in the FREQ statement after a slash (/):

- **NOTRUNCATE**

  specifies that the frequency values are not truncated to integers. This option does not apply to the Fleming-Harrington estimator (METHOD=FH).
The ID statement identifies variables whose values are used to label the observations of the Kaplan-Meier, Breslow, or Fleming-Harrington survivor function estimates. SAS format statements can be used to format the values of the ID variables.

The STRATA statement identifies the variables that determine the strata levels. Strata are formed according to the nonmissing values of these variables. The MISSING option can be used to allow missing values as a valid stratum level. Other options enable you to specify various k-sample tests, stratified tests, or trend tests and to make multiple-comparison adjustments for paired differences.

In the preceding syntax, variable is a variable whose values determine the stratum levels, and list is a list of endpoints for a numeric variable. The values for variable can be formatted or unformatted. If variable is a character variable, or if variable is numeric and no list appears, then the strata are defined by the unique values of the STRATA variable. More than one variable can be specified in the STRATA statement, and each numeric variable can be followed by a list. Each interval contains its lower endpoint but not its upper endpoint. The corresponding strata are formed by the combination of levels. If a variable is numeric and is followed by a list, then the levels for that variable correspond to the intervals defined by the list. The initial interval is assumed to start at \(-\infty\), and the final interval is assumed to end at \(\infty\).

The specification of a STRATA variable can have any of the following forms:

- a list separated by blanks: \texttt{Age(5 10 20 30)}
- a list separated by commas: \texttt{Age(5,10,20,30)}
- \(x\) to \(y\): \texttt{Age(5 to 10)}
- \(x\) to \(y\) by \(z\): \texttt{Age(5 to 30 by 10)}
- a combination of the above: \texttt{Age(5,10 to 50 by 10)}

For example, the specification

\texttt{strata Age(5,20 to 50 by 10) Sex;}

indicates the following levels for the Age variable:

\(\{(-\infty, 5), [5, 20), [20, 30), [30, 40), [40, 50), [50, \infty]\}\)

This statement also specifies that the Age strata be further subdivided by values of the variable Sex. In this example, there are six age groups by two sex groups, forming a total of 12 strata.

The specification of several STRATA variables, such as
strata A B C;

is equivalent to the A*B*C syntax of the TABLES statement in the FREQ procedure. The number of strata levels usually grows very rapidly with the number of STRATA variables, so you must be cautious when specifying the list of STRATA variables.

When comparing more than two survival curves, a $k$-sample test tells you whether the curves are significantly different from each other, but it does not identify which pairs of curves are different. A multiple-comparison adjustment of the $p$-values for the paired comparisons retains the same overall false positives as the $k$-sample test. Two types of paired comparisons can be made: comparisons between all pairs of curves and comparisons between a control curve and all other curves. You use the DIFF= option to specify the comparison type, and you use the ADJUST= option to select a method of multiple-comparison adjustments.

Table 74.2 summarizes the options available in the STRATA statement.

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Homogeneity Tests</strong></td>
<td></td>
</tr>
<tr>
<td>GROUP=</td>
<td>Specifies the group variable for stratified tests</td>
</tr>
<tr>
<td>NODETAIL</td>
<td>Suppresses printing the test statistic and covariance matrix</td>
</tr>
<tr>
<td>NOTEST</td>
<td>Suppresses any tests</td>
</tr>
<tr>
<td>TEST=</td>
<td>Specifies tests corresponding to various weight functions</td>
</tr>
<tr>
<td>TREND</td>
<td>Requests a trend test</td>
</tr>
<tr>
<td><strong>Multiple Comparisons</strong></td>
<td></td>
</tr>
<tr>
<td>ADJUST=</td>
<td>Requests a multiple-comparison adjustment</td>
</tr>
<tr>
<td>DIFF=</td>
<td>Specifies the type of differences to consider</td>
</tr>
<tr>
<td><strong>Missing Strata Value</strong></td>
<td></td>
</tr>
<tr>
<td>MISSING</td>
<td>Allows missing values as valid stratum values</td>
</tr>
<tr>
<td><strong>Display Option</strong></td>
<td></td>
</tr>
<tr>
<td>NOLABEL</td>
<td>Uses the names of the STRATA variables in the display</td>
</tr>
</tbody>
</table>

You can specify the following options in the STRATA statement after a slash (“/”).

**ADJUST=method**

**ADJ=method**

specifies the multiple-comparison method for adjusting the $p$-values of the paired tests. See the section “Multiple-Comparison Adjustments” on page 5610 for mathematical details; also see Westfall et al. (1999). The adjustment methods include the following:

**BONFERRONI**

**BON**

applies the Bonferroni correction to the raw $p$-values.

**DUNNETT**

performs Dunnett’s two-tailed comparisons of the control group with all other groups. PROC LIFETEST uses the factor-analytic covariance approximation described in Hsu (1992) and
identifies the adjustment in the results as “Dunnett-Hsu.” Note that ADJUST=DUNNETT is incompatible with DIFF=ALL.

**SCHEFFE**
performs Scheffé’s multiple-comparison adjustment.

**SIDAK**
applies the Šidák correction to the raw \( p \)-values.

**SMM**
**GTE**
performs the paired comparisons based on the studentized maximum modulus test.

**TUKEY**
performs the paired comparisons based on Tukey’s studentized range test. PROC LIFETEST uses the approximation described in Kramer (1956) and identifies the adjustment as "Tukey-Kramer" in the results. Note that ADJUST=TUKEY is incompatible with DIFF=CONTROL.

**SIMULATE < (simulate-options) >**
computes the adjusted \( p \)-values from the simulated distribution of the maximum or maximum absolute value of a multivariate normal random vector. The simulation estimates \( q \), the true \( (1 - \alpha) \) quantile, where \( \alpha \) is the value of the ALPHA= simulate-option.

The number of samples for the SIMULATE adjustment is set so that the tail area for the simulated \( q \) is within a certain accuracy radius \( \gamma \) of \( 1 - \alpha \) with an accuracy confidence of \( 100(1 - \epsilon)\% \). In equation form,

\[
\Pr(|F(\hat{q}) - (1 - \alpha)| \leq \gamma) = 1 - \epsilon
\]

where \( \hat{q} \) is the simulated \( q \) and \( F \) is the true distribution function of the maximum; see Edwards and Berry (1987) for details. By default, \( \gamma = 0.005 \) and \( \epsilon = 0.01 \) so that the tail area of \( \hat{q} \) is within 0.005 of 0.95 with 99% confidence.

The **simulate-options** include the following:

**ACC=value**
specifies the target accuracy radius \( \gamma \) of a \( 100(1 - \epsilon)\% \) confidence interval for the true probability content of the estimated \( (1 - \alpha) \) quantile. The default value is ACC=0.005.

**ALPHA=value**
specifies the value \( \alpha \) for estimating the \( (1 - \alpha) \) quantile. The default value is the ALPHA= value in the PROC LIFETEST statement, or 0.05 if that option is not specified.

**EPS=value**
specifies the value \( \epsilon \) for a \( 100(1 - \epsilon)\% \) confidence interval for the true probability content of the estimated \( (1 - \alpha) \) quantile. The default value for the accuracy confidence is 99%, corresponding to EPS=0.01.

**NSAMP=n**
specifies the sample size for the simulation. By default, \( n \) is set based on the values of the target accuracy radius \( \gamma \) and accuracy confidence \( 100(1 - \epsilon)\% \) for an interval for the true probability content of the estimated \( (1 - \alpha) \) quantile. With the default values for \( \gamma \), \( \epsilon \), and \( \alpha \) (0.005, 0.01, and 0.05, respectively), NSAMP=12604 by default.
REPORT specifies that a report on the simulation should be displayed, including a listing of the parameters, such as $\gamma$, $\epsilon$, and $\alpha$, in addition to an analysis of various methods for estimating or approximating the quantile.

SEED=number specifies an integer used to start the pseudorandom number generator for the simulation. If you do not specify a seed, or if you specify a value less than or equal to zero, the seed is generated by default from reading the time of day from the computer’s clock.

DIFF=ALL | CONTROL<('string' < ... 'string'>)> specifies which pairs of survival curves are considered for the multiple comparisons.

DIFF=ALL requests all paired comparisons

DIFF=CONTROL<('string' < ... 'string'>)> requests comparisons of the control curve with all other curves. To specify the control curve, you specify the quotes strings of formatted values that represent the curve in parentheses. For example, if `Cell='large'` identifies the control group, you specify

DIFF=CONTROL('large')

If more than one variable is used to identify the curves (for example, if `Cell='large'` and `Sex='F'` represent the control), you specify

DIFF=CONTROL('large' 'F')

The order of the quoted strings should correspond to the order of the stratum variables. If no specific curve is specified as the control, the first stratum or group value is used.

By default, DIFF=ALL unless you specify ADJUST= DUNNETT, in which case DIFF=CONTROL.

GROUP=variable stipulates a stratified test. You specify the variable to identify the groups whose survivor functions or cumulative incidence functions you want to compare. Tests are stratified on the levels of the STRATA variables. For example, in a multicenter trial in which two forms of therapy are to be compared, you specify the variable that identifies therapies as the GROUP= variable and the variable that identifies centers as the STRATA variable:

```bash
proc lifetest;
  time T*Status(0);
  strata Center / group=Therapy;
run;
```

With this specification, PROC LIFETEST performs a stratified test to compare the therapies while controlling the effect of the centers.

The GROUP= option has a side effect on the estimation of the survivor function or the cumulative incidence function (CIF). Instead of estimating a survivor function (or CIF) for each stratum, PROC
LIFETEST estimates a survivor function (or CIF) for each group within a stratum. Suppose there are 10 centers and two therapies. The preceding PROC LIFETEST specification estimates 20 survivor functions: two for each center, and one for each therapy for each center.

If the GROUP= option is not specified, PROC LIFETEST performs a homogeneity test comparing the strata.

MISSING
allows missing values to be a stratum level or a valid value of the GROUP= variable.

NODETAIL
suppresses the display of the rank statistics and the corresponding covariance matrices for various strata. If you specified the TREND option, the display of the scores for computing the trend tests is suppressed.

NOLABEL
specifies that the names instead of the labels of the STRATA variables be used in the display of the survival estimate table and in the legend of the survival plot.

NOTEST
suppresses the $k$-sample tests, stratified tests, and trend tests.

ORDER=FORMATTED | INTERNAL
specifies the sorting order of the values of the STRATA variables. The strata are presented in the specified order in the analysis results. You can use this option, for example, to display the curve labels in your preferred order in the survival plot legend (see Example 74.2 for an illustration). The default is ORDER=FORMATTED, which sorts the strata according to their external formatted values, except for numeric variable with no explicit format, which are sorted by the unformatted (internal) values. ORDER=INTERNAL sorts the strata by their internal values. The ORDER= option has no effect on a stratum variable with cutpoints specified.

TREND
computes the trend tests for testing the null hypothesis that the $k$ population hazards rate are the same versus an ordered alternatives. If there is only one STRATA variable and the variable is numeric, the unformatted values of the variable are used as the scores; otherwise, the scores are 1, 2, ..., in the given order of the strata.

TEST=test-request | (test-request <... test-request>)
controls the tests produced. Each test corresponds to a different weight function (see the section “Nonparametric Tests” on page 5607 for the weight functions). The test-requests include the following:

ALL
specifies all the nonparametric tests with $\rho_1=1$ and $\rho_2=0$ for the Fleming and Harrington test—FLEMING(1,0).

FLEMING($\rho_1$, $\rho_2$)
specifies the family of tests in Harrington and Fleming (1982), where $\rho_1$ and $\rho_2$ are nonnegative numbers. FLEMING($\rho_1$, $\rho_2$) reduces to the Fleming-Harrington $G^\rho$ family (Fleming and Harrington 1981) when $\rho_2=0$, which you can specify as FLEMING($\rho$) with one argument. When $\rho=0$, the test becomes the log-rank test. When $\rho=1$, the test should be very close to the Peto-Peto test.

LOGRANK
specifies the log-rank test.
NONE suppresses all comparison tests. Specifying TEST=NONE is equivalent to specify NOTEST.

LR specifies the likelihood ratio test based on the exponential model.

MODPETO specifies the modified Peto-Peto test.

PETO specifies the Peto-Peto test. The test is also referred to as the Peto-Peto-Prentice test.

WILCOXON specifies the Wilcoxon test. The test is also referred to as the Gehan test or the Breslow test.

TARONE specifies the Tarone-Ware test.

By default, TEST=(LOGRANK WILCOXON LR) for the k-sample tests, and TEST=(LOGRANK WILCOXON) for stratified and trend tests.

TEST Statement

TEST variables ;

The TEST statement specifies a list of numeric covariates (prognostic variables) that you want tested for association with the failure time.

Two sets of rank statistics are computed. These rank statistics and their variances are pooled over all strata. Univariate (marginal) test statistics are displayed for each of the covariates. Additionally, a sequence of test statistics for joint effects of covariates is displayed. The first element of the sequence is the largest univariate test statistic. Other variables are then added on the basis of the largest increase in the joint test statistic. The process continues until all the variables have been added or until the remaining variables are linearly dependent on the previously added variables.

For more information, see the section “Rank Tests for the Association of Survival Time with Covariates” on page 5611.

TIME Statement

TIME variable < * censor(list) > < / option > ;

The TIME statement is required. It is used to indicate the failure time variable, where variable is the name of the failure time variable that can be optionally followed by an asterisk, the name of the censoring variable, and a parenthetical list of values that correspond to right-censoring. The censoring values should be numeric, nonmissing values. For example, the following statement identifies the variable T as containing the observed failure times (event or censored):

   time T*Status(0,2);

If the variable Status has the value 0 or 2, the corresponding value of T is a right-censored value.

You can specify the following option after a slash (/):
stipulates a competing-risks analysis, which consists of estimating cumulative incidence functions and computing Gray’s test (Gray 1988) for testing the homogeneity of two or more cumulative incidence functions. You specify a number that represents the event of interest after the equal sign. For example:

```plaintext
proc lifetest;
   time T*Status(0) / failcode=1;
run;
```

For this specification, PROC LIFETEST regards a Status value of 1 as the event of interest, a value of 0 as a censored observation indicator, and all other values as competing events.

You can specify a list of values after the equal sign. PROC LIFETEST performs a separate competing-risks analysis for each value, regarding it as representing the event of interest. For example:

```plaintext
proc lifetest;
   time T*Status(0) / failcode=1 2;
run;
```

This specification produces two analyses, one for FAILCODE=1 and the other for FAILCODE=2.

If you specify the FAILCODE option without the equal sign, PROC LIFETEST produces a separate analysis for each distinct event value. Consider a data set with an event indicator variable Status that assumes four distinct values, 0, 1, 2, and 3, where Status=0 represents observations that are censored and Status=1, Status=2, and Status=3 represent three different causes of failure. Consider the following statements:

```plaintext
proc lifetest;
   time T*Status(0) / failcode;
run;
```

PROC LIFETEST produces three separate competing-risks analyses: one uses Status=1 as the failure cause of interest, one uses Status=2 as the failure cause of interest, and one uses Status=3 as the failure cause of interest. This specification is convenient for an exploratory analysis when there is no predetermined failure cause of interest.

---

### WEIGHT Statement

**WEIGHT** variable;

The *variable* in the WEIGHT statement identifies the variable in the input data set that contains the weights of the subjects. Values of the WEIGHT variable can be nonintegral and are not truncated. Observations with negative, zero, or missing values for the WEIGHT variable are not used in the computation.
The implementation of weights in PROC LIFETEST is based on Xie and Liu (2005, 2011), who use inverse probability of treatment weights to reduce confounding effects. A weight is assigned to each subject as the inverse probability of being in a certain group. If a subject has a higher probability of being in a group, it is considered as overrepresented and is therefore assigned a lower weight; on the other hand, if the subject has a smaller probability of being in a group, it is considered as underrepresented and is assigned a higher weight.

You can use the WEIGHT statement only for the Kaplan-Meier curves. Other methods of estimating the survival curves using weights are not available.

### Details: LIFETEST Procedure

#### Missing Values

Observations with a missing value for either the failure time or the censoring variable are not used in the analysis. If a stratum variable value is missing, the observation is not used; however, the MISSING option can be used to request that missing values be treated as valid stratum values. If any variable specified in the TEST statement has a missing value, that observation is not used in the calculation of the rank statistics.

#### Computational Formulas

**Breslow, Fleming-Harrington, and Kaplan-Meier Methods**

Let \( t_1 < t_2 < \cdots < t_D \) represent the distinct event times. For each \( i = 1, \ldots, D \), let \( Y_i \) be the number of surviving units (the size of the risk set) just prior to \( t_i \) and let \( d_i \) be the number of units that fail at \( t_i \). If the NOTRUNCATE option is specified in the FREQ statement, \( Y_i \) and \( d_i \) can be nonintegers.

The Breslow estimate of the survivor function is

\[
\hat{S}(t_i) = \exp \left( - \sum_{j=1}^{i} \frac{d_j}{Y_j} \right)
\]

Note that the Breslow estimate is the exponentiation of the negative Nelson-Aalen estimate of the cumulative hazard function.

The Fleming-Harrington estimate (Fleming and Harrington 1984) of the survivor function is

\[
\hat{S}(t_i) = \exp \left( - \sum_{k=1}^{i} \sum_{j=0}^{d_k-1} \frac{1}{Y_k - j} \right)
\]

If the frequency values are not integers, the Fleming-Harrington estimate cannot be computed.

The Kaplan-Meier (product-limit) estimate of the survivor function at \( t_i \) is the cumulative product

\[
\hat{S}(t_i) = \prod_{j=1}^{i} \left( 1 - \frac{d_j}{Y_j} \right)
\]
Notice that all the estimators are defined to be right continuous; that is, the events at $t_i$ are included in the estimate of $S(t_i)$. The corresponding estimate of the standard error is computed using Greenwood's formula (Kalbfleisch and Prentice 1980) as

$$\hat{\sigma} \left( \hat{S}(t_i) \right) = \hat{S}(t_i) \sqrt{\sum_{j=1}^{i} \frac{d_j}{Y_j(Y_j - d_j)}}$$

The first quartile (or the 25th percentile) of the survival time is the time beyond which 75% of the subjects in the population under study are expected to survive. It is estimated by

$$q_{.25} = \min \{ t_j | \hat{S}(t_j) < 0.75 \}$$

If $\hat{S}(t)$ is exactly equal to 0.75 from $t_j$ to $t_{j+1}$, the first quartile is taken to be $(t_j + t_{j+1})/2$. If it happens that $\hat{S}(t)$ is greater than 0.75 for all values of $t$, the first quartile cannot be estimated and is represented by a missing value in the printed output.

The general formula for estimating the 100$p$th percentile point is

$$q_p = \min \{ t_j | \hat{S}(t_j) < 1 - p \}$$

The second quartile (the median) and the third quartile of survival times correspond to $p = 0.5$ and $p = 0.75$, respectively.

Brookmeyer and Crowley (1982) have constructed the confidence interval for the median survival time based on the confidence interval for $S(t)$. The methodology is generalized to construct the confidence interval for the 100$p$th percentile based on a $g$-transformed confidence interval for $S(t)$ (Klein and Moeschberger 1997). You can use the CONFTYPE= option to specify the $g$-transformation. The $100(1 - \alpha)%$ confidence interval for the first quartile survival time is the set of all points $t$ that satisfy

$$\left| \frac{g(\hat{S}(t)) - g(1 - 0.25)}{g'(\hat{S}(t))\hat{\sigma}(\hat{S}(t))} \right| \leq z_{1 - \frac{\alpha}{2}}$$

where $g'(x)$ is the first derivative of $g(x)$ and $z_{1 - \frac{\alpha}{2}}$ is the $(100(1 - \frac{\alpha}{2}))$th percentile of the standard normal distribution.

Consider the bone marrow transplant data described in Example 74.2. The following table illustrates the construction of the confidence limits for the first quartile in the ALL group. Values of $\frac{g(\hat{S}(t)) - g(1 - 0.25)}{g'(\hat{S}(t))\hat{\sigma}(\hat{S}(t))}$ that lie between $\pm z_{1 - 0.05} = \pm 1.965$ are highlighted.
Constructing 95% Confidence Limits for the 25th Percentile

<table>
<thead>
<tr>
<th>t</th>
<th>( \hat{S}(t) )</th>
<th>( \hat{\sigma}(\hat{S}(t)) )</th>
<th>LINEAR</th>
<th>LOGLOG</th>
<th>LOG</th>
<th>ASINSQRT</th>
<th>LOGIT</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.97368</td>
<td>0.025967</td>
<td>8.6141</td>
<td>2.37831</td>
<td>9.7871</td>
<td>4.44648</td>
<td>2.47903</td>
</tr>
<tr>
<td>55</td>
<td>0.94737</td>
<td>0.036224</td>
<td>5.4486</td>
<td>2.36375</td>
<td>6.1098</td>
<td>3.60151</td>
<td>2.46635</td>
</tr>
<tr>
<td>74</td>
<td>0.92105</td>
<td>0.043744</td>
<td>3.9103</td>
<td>2.16833</td>
<td>4.3257</td>
<td>2.94398</td>
<td>2.25757</td>
</tr>
<tr>
<td>86</td>
<td>0.89474</td>
<td>0.049784</td>
<td>2.9073</td>
<td>1.89961</td>
<td>3.1713</td>
<td>2.38164</td>
<td>1.97023</td>
</tr>
<tr>
<td>104</td>
<td>0.86842</td>
<td>0.054836</td>
<td>2.1595</td>
<td>1.59196</td>
<td>2.3217</td>
<td>1.87884</td>
<td>1.64297</td>
</tr>
<tr>
<td>107</td>
<td>0.84211</td>
<td>0.059153</td>
<td>1.5571</td>
<td>1.26050</td>
<td>1.6490</td>
<td>1.41733</td>
<td>1.29331</td>
</tr>
<tr>
<td>109</td>
<td>0.81579</td>
<td>0.062886</td>
<td>1.0462</td>
<td>0.91307</td>
<td>1.0908</td>
<td>0.98624</td>
<td>0.93069</td>
</tr>
<tr>
<td>110</td>
<td>0.78947</td>
<td>0.066135</td>
<td>0.5969</td>
<td>0.55415</td>
<td>0.6123</td>
<td>0.57846</td>
<td>0.56079</td>
</tr>
<tr>
<td>122</td>
<td>0.73684</td>
<td>0.071434</td>
<td>-0.1842</td>
<td>-0.18808</td>
<td>-0.1826</td>
<td>-0.18573</td>
<td>-0.18728</td>
</tr>
<tr>
<td>129</td>
<td>0.71053</td>
<td>0.073570</td>
<td>-0.5365</td>
<td>-0.56842</td>
<td>-0.5222</td>
<td>-0.54859</td>
<td>-0.56101</td>
</tr>
<tr>
<td>172</td>
<td>0.68421</td>
<td>0.075405</td>
<td>-0.8725</td>
<td>-0.95372</td>
<td>-0.8330</td>
<td>-0.90178</td>
<td>-0.93247</td>
</tr>
<tr>
<td>192</td>
<td>0.65789</td>
<td>0.076960</td>
<td>-1.1968</td>
<td>-1.34341</td>
<td>-1.1201</td>
<td>-1.24712</td>
<td>-1.30048</td>
</tr>
<tr>
<td>194</td>
<td>0.63158</td>
<td>0.078252</td>
<td>-1.5133</td>
<td>-1.73709</td>
<td>-1.3870</td>
<td>-1.58613</td>
<td>-1.66406</td>
</tr>
<tr>
<td>230</td>
<td>0.60412</td>
<td>0.079522</td>
<td>-1.8345</td>
<td>-2.14672</td>
<td>-1.6432</td>
<td>-1.92995</td>
<td>-2.03291</td>
</tr>
<tr>
<td>276</td>
<td>0.57666</td>
<td>0.080509</td>
<td>-2.1531</td>
<td>-2.55898</td>
<td>-1.8825</td>
<td>-2.26871</td>
<td>-2.39408</td>
</tr>
<tr>
<td>332</td>
<td>0.54920</td>
<td>0.081223</td>
<td>-2.4722</td>
<td>-2.97389</td>
<td>-2.1070</td>
<td>-2.60380</td>
<td>-2.74691</td>
</tr>
<tr>
<td>383</td>
<td>0.52174</td>
<td>0.081672</td>
<td>-2.7948</td>
<td>-3.39146</td>
<td>-2.3183</td>
<td>-2.93646</td>
<td>-3.09068</td>
</tr>
<tr>
<td>418</td>
<td>0.49428</td>
<td>0.081860</td>
<td>-3.1239</td>
<td>-3.81166</td>
<td>-2.5177</td>
<td>-3.26782</td>
<td>-3.42460</td>
</tr>
<tr>
<td>466</td>
<td>0.46682</td>
<td>0.081788</td>
<td>-3.4624</td>
<td>-4.23445</td>
<td>-2.7062</td>
<td>-3.59898</td>
<td>-3.74781</td>
</tr>
<tr>
<td>487</td>
<td>0.43936</td>
<td>0.081457</td>
<td>-3.8136</td>
<td>-4.65971</td>
<td>-2.8844</td>
<td>-3.93103</td>
<td>-4.05931</td>
</tr>
<tr>
<td>526</td>
<td>0.41190</td>
<td>0.080862</td>
<td>-4.1812</td>
<td>-5.08726</td>
<td>-3.0527</td>
<td>-4.26507</td>
<td>-4.35795</td>
</tr>
<tr>
<td>609</td>
<td>0.38248</td>
<td>0.080260</td>
<td>-4.5791</td>
<td>-5.52446</td>
<td>-3.2091</td>
<td>-4.60719</td>
<td>-4.64271</td>
</tr>
<tr>
<td>662</td>
<td>0.35306</td>
<td>0.079296</td>
<td>-5.0059</td>
<td>-5.96222</td>
<td>-3.3546</td>
<td>-4.95358</td>
<td>-4.90900</td>
</tr>
</tbody>
</table>

Consider the LINEAR transformation where \( g(x) = x \). The event times that satisfy \( \frac{g(\hat{S}(t)) - g(1-0.25)}{g'(\hat{S}(t))\sqrt{V(\hat{S}(t))}} \leq 1.9599 \) include 107, 109, 110, 122, 129, 172, 192, 194, and 230. The confidence of the interval \([107, 230]\) is less than 95%. Brookmeyer and Crowley (1982) suggest extending the confidence interval to but not including the next event time. As such the 95% confidence interval for the first quartile based on the linear transform is \([107, 276)\). The following table lists the confidence intervals for the various transforms.

<p>| 95% CI's for the 25th Percentile |</p>
<table>
<thead>
<tr>
<th>CONFTYPE</th>
<th>[Lower Upper]</th>
</tr>
</thead>
<tbody>
<tr>
<td>LINEAR</td>
<td>107 276</td>
</tr>
<tr>
<td>LOGLOG</td>
<td>86 230</td>
</tr>
<tr>
<td>LOG</td>
<td>107 332</td>
</tr>
<tr>
<td>ASINSQRT</td>
<td>104 276</td>
</tr>
<tr>
<td>LOGIT</td>
<td>104 230</td>
</tr>
</tbody>
</table>

Sometimes, the confidence limits for the quartiles cannot be estimated. For convenience of explanation, consider the linear transform \( g(x) = x \). If the curve that represents the upper confidence limits for the survivor function lies above 0.75, the upper confidence limit for first quartile cannot be estimated. On the other hand, if the curve that represents the lower confidence limits for the survivor function lies above 0.75, the lower confidence limit for the quartile cannot be estimated.
The estimated mean survival time is
\[
\hat{\mu} = \sum_{i=1}^{D} \hat{S}(t_{i-1})(t_i - t_{i-1})
\]
where \(t_0\) is defined to be zero. When the largest observed time is censored, this sum underestimates the mean. The standard error of \(\hat{\mu}\) is estimated as
\[
\hat{\sigma}(\hat{\mu}) = \sqrt{\frac{m}{m-1} \sum_{i=1}^{D-1} \frac{d_i A_i^2}{Y_i (Y_i - d_i)}}
\]
where
\[
A_i = \sum_{j=i}^{D-1} \hat{S}(t_j)(t_{j+1} - t_j)
\]
and
\[
m = \sum_{j=1}^{D} d_j
\]

If the largest observed time is not an event, you can use the TIMELIM= option to specify a time limit \(L\) and estimate the mean survival time limited to the time \(L\) and its standard error by replacing \(D\) by \(D + 1\) with \(t_{D+1} = L\).

**Nelson-Aalen Estimate of the Cumulative Hazard Function**

The Nelson-Aalen cumulative hazard estimator, defined up to the largest observed time on study, is
\[
\hat{H}(t) = \sum_{t_i \leq t} \frac{d_i}{Y_i}
\]
and its estimated variance is
\[
\hat{\sigma}^2(\hat{H}(t)) = \sum_{t_i \leq t} \frac{d_i}{Y_i^2}
\]

**Adjusted Kaplan-Meier Estimate**

PROC LIFETEST computes the adjusted Kaplan-Meier estimate (AKME) of the survivor function if you specify both METHOD=KM and the WEIGHT statement. Let \((T_i, \delta_i, w_i), i = 1, \ldots, n\), denote an independent sample of right-censored survival data, where \(T_i\) is the possibly right-censored time, \(\delta_i\) is the censoring indicator (\(\delta_i = 0\) if \(T_i\) is censored and \(\delta_i = 1\) if \(T_i\) is an event time), and \(w_i\) is the weight (from the WEIGHT statement). Let \(t_1 < t_2 < \cdots < t_D\) be the \(D\) distinct event times in the sample. At time \(t_j, j = 1, \ldots, D\), there are \(d_j = \sum \delta_i I(T_i = t_j)\) events out of \(Y_j = \sum I(T_i \geq t_j)\) subjects. The weighted number of events and the weighted number at risk are \(d_j^w = \sum w_i \delta_i I(T_i = t_j)\) and \(Y_j^w = \sum w_i I(T_i \geq t_j)\), respectively. The AKME (Xie and Liu 2005) is
\[
\hat{S}(t) = \begin{cases} 
1 & \text{if } t < t_1 \\
\prod_{t_j \leq t} \left[1 - \frac{d_j^w}{Y_j^w}\right] & \text{if } t \geq t_1
\end{cases}
\]
The estimated variance of \( \hat{S}(t) \) is
\[
\hat{\sigma}^2(\hat{S}(t)) = \left( \hat{S}(t) \right)^2 \sum_{j:t_j \leq t} \frac{d_j^w}{M_j (1 - d_j^w / Y_j^w)}
\]
where
\[
M_j = \frac{\left( \sum_{i:T_i \geq t_j} w_i \right)^2}{\sum_{i:T_i \geq t_j} w_i^2}
\]

**Life-Table Method**

The life-table estimates are computed by counting the numbers of censored and uncensored observations that fall into each of the time intervals \([t_{i-1}, t_i)\), \(i = 1, 2, \ldots, k + 1\), where \(t_0 = 0\) and \(t_{k+1} = \infty\). Let \(n_i\) be the number of units that enter the interval \([t_{i-1}, t_i)\), and let \(d_i\) be the number of events that occur in the interval. Let \(b_i = t_i - t_{i-1}\), and let \(n_i' = n_i - w_i / 2\), where \(w_i\) is the number of units censored in the interval. The effective sample size of the interval \([t_{i-1}, t_i)\) is denoted by \(n_i'\). Let \(t_{mi}\) denote the midpoint of \([t_{i-1}, t_i)\).

The conditional probability of an event in \([t_{i-1}, t_i)\) is estimated by
\[
\hat{q}_i = \frac{d_i}{n_i'}
\]
and its estimated standard error is
\[
\hat{\sigma}(\hat{q}_i) = \sqrt{\frac{\hat{q}_i \hat{p}_i}{n_i'}}
\]
where \(\hat{p}_i = 1 - \hat{q}_i\).

The estimate of the survival function at \(t_i\) is
\[
\hat{S}(t_i) = \begin{cases} 
1 & i = 0 \\
\hat{S}(t_{i-1}) p_{i-1} & i > 0 
\end{cases}
\]
and its estimated standard error is
\[
\hat{\sigma}(\hat{S}(t_i)) = \hat{S}(t_i) \sqrt{\sum_{j=1}^{i-1} \frac{\hat{q}_j}{n_j' \hat{p}_j}}
\]

The density function at \(t_{mi}\) is estimated by
\[
\hat{f}(t_{mi}) = \frac{\hat{S}(t_i) \hat{q}_i}{b_i}
\]
and its estimated standard error is
\[
\hat{\sigma}(\hat{f}(t_{mi})) = \hat{f}(t_{mi}) \left[ \sum_{j=1}^{i-1} \frac{\hat{q}_j}{n_j' \hat{p}_j} + \frac{\hat{p}_i}{n_i' \hat{q}_i} \right]
\]
The estimated hazard function at $t_{mi}$ is
\[
\hat{h}(t_{mi}) = \frac{2\hat{q}_i}{b_i(1 + \hat{p}_i)}
\]
and its estimated standard error is
\[
\hat{\sigma}(\hat{h}(t_{mi})) = \hat{h}(t_{mi})\sqrt{\frac{1 - (b_i\hat{h}(t_{mi})/2)^2}{n'_i\hat{q}_i}}
\]
Let $[t_{j-1}, t_j)$ be the interval in which $\hat{S}(t_{j-1}) \geq \hat{S}(t_i)/2 > \hat{S}(t_j)$. The median residual lifetime at $t_i$ is estimated by
\[
\hat{M}_i = t_{j-1} - t_i + b_j \frac{\hat{S}(t_{j-1}) - \hat{S}(t_i)/2}{\hat{S}(t_{j-1}) - \hat{S}(t_j)}
\]
and the corresponding standard error is estimated by
\[
\hat{\sigma}(\hat{M}_i) = \frac{\hat{S}(t_i)}{2\hat{f}(t_{mi})\sqrt{n'_i}}
\]

**Interval Determination**
If you want to determine the intervals exactly, use the INTERVALS= option in the PROC LIFETEST statement to specify the interval endpoints. Use the WIDTH= option to specify the width of the intervals, thus indirectly determining the number of intervals. If neither the INTERVALS= option nor the WIDTH= option is specified in the life-table estimation, the number of intervals is determined by the NINTERVAL= option. The width of the time intervals is 2, 5, or 10 times an integer (possibly a negative integer) power of 10. Let $c = \log_{10}(\text{maximum observed time/number of intervals})$, and let $b$ be the largest integer not exceeding $c$. Let $d = 10^{c-b}$ and let
\[
a = 2 \times I(d \leq 2) + 5 \times I(2 < d \leq 5) + 10 \times I(d > 5)
\]
with $I$ being the indicator function. The width is then given by
\[
\text{width} = a \times 10^b
\]
By default, NINTERVAL=10.

**Pointwise Confidence Limits in the OUTSURV= Data Set**
Pointwise confidence limits are computed for the survivor function, and for the density function and hazard function when the life-table method is used. Let $\alpha$ be specified by the ALPHA= option. Let $z_{\alpha/2}$ be the critical value for the standard normal distribution. That is, $\Phi(-z_{\alpha/2}) = \alpha/2$, where $\Phi$ is the cumulative distribution function of the standard normal random variable.
Survivor Function

When the computation of confidence limits for the survivor function \( S(t) \) is based on the asymptotic normality of the survival estimator \( \hat{S}(t) \), the approximate confidence interval might include impossible values outside the range \([0,1]\) at extreme values of \( t \). This problem can be avoided by applying the asymptotic normality to a transformation of \( S(t) \) for which the range is unrestricted. In addition, certain transformed confidence intervals for \( S(t) \) perform better than the usual linear confidence intervals (Borgan and Liestøl 1990). The CONFTYPE= option enables you to pick one of the following transformations: the log-log function (Kalbfleisch and Prentice 1980), the arcsine-square root function (Nair 1984), the logit function (Meeker and Escobar 1998), the log function, and the linear function.

Let \( g \) be the transformation that is being applied to the survivor function \( S(t) \). By the delta method, the standard error of \( g(\hat{S}(t)) \) is estimated by

\[
\tau(t) = \hat{\sigma} \left[ g(\hat{S}(t)) \right] = g'\left(\hat{S}(t)\right) \hat{\sigma}\left[\hat{S}(t)\right]
\]

where \( g' \) is the first derivative of the function \( g \). The 100(1–\( \alpha \))% confidence interval for \( S(t) \) is given by

\[
g^{-1}\left\{g[\hat{S}(t)] \pm z_{\alpha/2} g'([\hat{S}(t)]\hat{\sigma}([\hat{S}(t)])\right\}
\]

where \( g^{-1} \) is the inverse function of \( g \). That choices of the transformation \( g \) are as follows:

- **arcsine-square root transformation**: The estimated variance of \( \sin^{-1}\left(\sqrt{\hat{S}(t)}\right) \) is \( \hat{\sigma}^2(t) = \frac{\hat{\sigma}^2(\hat{S}(t))}{4\hat{S}(t)(1-\hat{S}(t))} \). The 100(1–\( \alpha \))% confidence interval for \( S(t) \) is given by

\[
\sin^2\left\{\max\left[0,\sin^{-1}\left(\sqrt{\hat{S}(t)} - z_{\alpha/2} \hat{\tau}(t)\right)\right]\right\} \leq S(t) \leq \sin^2\left\{\min\left[\frac{\pi}{2},\sin^{-1}\left(\sqrt{\hat{S}(t)} + z_{\alpha/2} \hat{\tau}(t)\right)\right]\right\}
\]

- **linear transformation**: This is the same as having no transformation in which \( g \) is the identity. The 100(1–\( \alpha \))% confidence interval for \( S(t) \) is given by

\[
\hat{S}(t) - z_{\alpha/2} \hat{\sigma} \left[\hat{S}(t)\right] \leq S(t) \leq \hat{S}(t) + z_{\alpha/2} \hat{\sigma} \left[\hat{S}(t)\right]
\]

- **log transformation**: The estimated variance of \( \log(\hat{S}(t)) \) is \( \hat{\tau}^2(t) = \frac{\hat{\sigma}^2(\hat{S}(t))}{\hat{S}(t)} \). The 100(1–\( \alpha \))% confidence interval for \( S(t) \) is given by

\[
\hat{S}(t) \exp\left(-z_{\alpha/2} \hat{\tau}(t)\right) \leq S(t) \leq \hat{S}(t) \exp\left(z_{\alpha/2} \hat{\tau}(t)\right)
\]

- **log-log transformation**: The estimated variance of \( \log(-\log(\hat{S}(t)) \) is \( \hat{\tau}^2(t) = \frac{\hat{\sigma}^2(\hat{S}(t))}{[S(t)\log(\hat{S}(t))]^2} \). The 100(1–\( \alpha \))% confidence interval for \( S(t) \) is given by

\[
\left[\hat{S}(t)\right]^{\exp\left(-z_{\alpha/2} \hat{\tau}(t)\right)} \leq S(t) \leq \left[\hat{S}(t)\right]^{\exp\left(z_{\alpha/2} \hat{\tau}(t)\right)}
\]
logit transformation: The estimated variance of \( \log \left( \frac{\hat{S}(t)}{1-\hat{S}(t)} \right) \) is
\[
\hat{\tau}^2(t) = \frac{\hat{\sigma}^2(\hat{S}(t))}{\hat{S}^2(t)[1-\hat{S}(t)]^2}.
\]

The 100(1–\( \alpha \))% confidence limits for \( S(t) \) are given by
\[
\frac{\hat{S}(t)}{\hat{S}(t) + \left[ 1 - \hat{S}(t) \right] \exp \left( z_{\frac{\alpha}{2}} \hat{\tau}(t) \right)} \leq S(t) \leq \frac{\hat{S}(t)}{\hat{S}(t) + \left[ 1 - \hat{S}(t) \right] \exp \left( -z_{\frac{\alpha}{2}} \hat{\tau}(t) \right)}
\]

**Density and Hazard Functions**

For the life-table method, a 100(1–\( \alpha \))% confidence interval for hazard function or density function at time \( t \) is computed as
\[
\hat{g}(t) \pm z_{\frac{\alpha}{2}} \hat{\sigma}[\hat{g}(t)]
\]
where \( \hat{g}(t) \) is the estimate of either the hazard function or the density function at time \( t \), and \( \hat{\sigma}[\hat{g}(t)] \) is the corresponding standard error estimate.

**Simultaneous Confidence Intervals for Kaplan-Meier Curves**

The pointwise confidence interval for the survivor function \( S(t) \) is valid for a single fixed time at which the inference is to be made. In some applications, it is of interest to find the upper and lower confidence bands that guarantee, with a given confidence level, that the survivor function falls within the band for all \( t \) in some interval. Hall and Wellner (1980) and Nair (1984) provide two different approaches for deriving the confidence bands. An excellent review can be found in Klein and Moeschberger (1997). You can use the CONFBAND= option in the PROC LIFETEST statement to select the confidence bands. The EP confidence band provides confidence bounds that are proportional to the pointwise confidence interval, while those of the HW band are not proportional to the pointwise confidence bounds. The maximum time, \( t_U \), for the bands can be specified by the BANDMAX= option; the minimum time, \( t_L \), can be specified by the BANDMIN= option. Transformations that are used to improve the pointwise confidence intervals can be applied to improve the confidence bands. It might turn out that the upper and lower bounds of the confidence bands are not decreasing in \( t_L < t < t_U \), which is contrary to the nonincreasing characteristic of survivor function. Meeker and Escobar (1998) suggest making an adjustment so that the bounds do not increase: if the upper bound is increasing on the right, it is made flat from the minimum to \( t_U \); if the lower bound is increasing from the right, it is made flat from \( t_L \) to the maximum. PROC LIFETEST does not make any adjustment for the nondecreasing behavior of the confidence bands in the OUTSURV= data set. However, the adjustment was made in the display of the confidence bands by using ODS Graphics.

For Kaplan-Meier estimation, let \( t_1 < t_2 < \cdots < t_D \) be the \( D \) distinct events times, and at time \( t_i \), there are \( d_i \) events. Let \( Y_i \) be the number of individuals who are at risk at time \( t_i \). The variance of \( \hat{S}(t) \), given by the Greenwood formula, is \( \hat{\sigma}^2[\hat{S}(t)] = \sigma^2_S(t)\hat{S}(t) \), where
\[
\sigma^2_S(t) = \sum_{i \leq t} \frac{d_i}{Y_i(Y_i - d_i)}
\]
Let \( t_L < t_U \) be the time range for the confidence band so that \( t_U \) is less than or equal to the largest event time. For the Hall-Wellner band, \( t_L \) can be zero, but for the equal-precision band, \( t_L \) is greater than or equal to the smallest event time. Let

\[
\alpha_L = \frac{n \sigma^2_S(t_L)}{1 + n \sigma^2_S(t_L)} \quad \text{and} \quad \alpha_U = \frac{n \sigma^2_S(t_U)}{1 + n \sigma^2_S(t_U)}
\]

Let \( \{W^0(u), 0 \leq u \leq 1\} \) be a Brownian bridge.

**Hall-Wellner Band**

The 100(1–\( \alpha \))% HW band of Hall and Wellner (1980) is

\[
\hat{S}(t) - h_\alpha(\alpha_L, \alpha_U) n^{-1/2} [1 + n \sigma^2_S(t)] \hat{S}(t) \leq S(t) \leq \hat{S}(t) + h_\alpha(\alpha_L, \alpha_U) n^{-1/2} [1 + n \sigma^2_S(t)] \hat{S}(t)
\]

for all \( t_L \leq t \leq t_U \), where the critical value \( h_\alpha(\alpha_L, \alpha_U) \) is given by

\[
\alpha = \Pr\{ \sup_{\alpha_L \leq u \leq \alpha_U} |W^0(u)| > h_\alpha(\alpha_L, \alpha_U) \}
\]

The critical values are computed from the results in Chung (1986).

Note that the given confidence band has a formula similar to that of the (linear) pointwise confidence interval, where \( h_\alpha(\alpha_L, \alpha_U) \) and \( n^{-1/2} [1 + n \sigma^2_S(t)] \hat{S}(t) \) in the former correspond to \( z_\alpha \) and \( \hat{S}(t) \) in the latter, respectively. You can obtain the other transformations (arcsine-square root, log-log, log, and logit) for the confidence bands by replacing \( z_\alpha \) and \( \hat{S}(t) \) in the corresponding pointwise confidence interval formula by \( h_\alpha(\alpha_L, \alpha_U) \) and the following \( \hat{s}(t) \), respectively:

- **arcsine-square root transformation**:
  \[
  \hat{s}(t) = \frac{1 + n \sigma^2_S(t)}{\sqrt{n}} \sqrt{\frac{S(t)}{2n[1 - S(t)]}}
  \]

- **log transformation**:
  \[
  \hat{s}(t) = \frac{1 + n \sigma^2_S(t)}{\sqrt{n}} \sqrt[n]{S(t)}
  \]

- **log-log transformation**:
  \[
  \hat{s}(t) = \frac{1 + n \sigma^2_S(t)}{\sqrt[n]{\log[\hat{S}(t)]}}
  \]

- **logit transformation**:
  \[
  \hat{s}(t) = \frac{1 + n \sigma^2_S(t)}{\sqrt[n]{\log[1 - \hat{S}(t)]}}
  \]
Equal-Precision Band

The 100(1−α)% EP band of Nair (1984) is

\[ \hat{S}(t) - e_\alpha(a_L, a_U)\hat{S}(t)\sigma_S(t) \leq S(t) \leq \hat{S}(t) + e_\alpha(a_L, a_U)\hat{S}(t)\sigma_S(t) \]

for all \( t_L \leq t \leq t_U \), where \( e_\alpha(a_L, a_U) \) is given by

\[ \alpha = \Pr\{ \sup_{a_L \leq u \leq a_U} \left| W^0(u) \right| > e_\alpha(a_L, a_U) \} \]

PROC LIFETEST uses the approximation of Miller and Siegmund (1982, Equation 8) to approximate the tail probability in which \( e_\alpha(a_L, a_U) \) is obtained by solving \( x \) in

\[ \frac{4x\phi(x)}{x} + \phi(x) \left( x - \frac{1}{x} \right) \log \left[ \frac{a_U(1-a_L)}{a_L(1-a_U)} \right] = \alpha \]

where \( \phi(x) \) is the standard normal density function evaluated at \( x \). Note that the confidence bounds given are proportional to the pointwise confidence intervals. As a matter of fact, this confidence band and the (linear) pointwise confidence interval have the same formula except for the critical values (\( z_{\alpha/2} \) for the pointwise confidence interval and \( e_\alpha(a_L, a_U) \) for the band). You can obtain the other transformations (arcsine-square root, log-log, log, and logit) for the confidence bands by replacing \( z_{\alpha/2} \) by \( e_\alpha(a_L, a_U) \) in the formula of the pointwise confidence intervals.

Kernel-Smoothed Hazard Estimate

Kernel-smoothed estimators of the hazard function \( h(t) \) are based on the Nelson-Aalen estimator \( \hat{H}(t) \) and its variance \( \hat{V}(\hat{H}(t)) \). Consider the jumps of \( \hat{H}(t_i) \) and \( \hat{V}(\hat{H}(t_i)) \) at the event times \( t_1 < t_2 < \cdots < t_D \) as follows:

\[ \Delta \hat{H}(t_i) = \hat{H}(t_i) - \hat{H}(t_{i-1}) \]
\[ \hat{V}(\hat{H}(t_i)) = \mathcal{V}(\hat{H}(t_i)) - \mathcal{V}(\hat{H}(t_{i-1})) \]

where \( t_0=0 \).

The kernel-smoothed estimator of \( h(t) \) is a weighted average of \( \Delta \hat{H}(t) \) over event times that are within a bandwidth distance \( b \) of \( t \). The weights are controlled by the choice of kernel function, \( K() \), defined on the interval \([-1,1]\). The choices are as follows:

- uniform kernel:
  \[ K_U(x) = \frac{1}{2}, \quad -1 \leq x \leq 1 \]

- Epanechnikov kernel:
  \[ K_E(x) = \frac{3}{4}(1-x^2), \quad -1 \leq x \leq 1 \]

- biweight kernel:
  \[ K_{BW}(x) = \frac{15}{16}(1-x^2)^2, \quad -1 \leq x \leq 1 \]
The kernel-smoothed hazard rate estimator is defined for all time points on (0, \(t_D\)). For time points \(t\) for which \(b \leq t \leq t_D - b\), the kernel-smoothed estimated of \(h(t)\) based on the kernel \(K()\) is given by

\[
\hat{h}(t) = \frac{1}{b} \sum_{i=1}^{D} K\left(\frac{t - t_i}{b}\right) \Delta \hat{H}(t_i)
\]

The variance of \(\hat{h}(t)\) is estimated by

\[
\hat{\sigma}^2(\hat{h}(t)) = \frac{1}{b^2} \sum_{i=1}^{D} K\left(\frac{t - t_i}{b}\right)^2 \Delta \hat{V}(\hat{H}(t_i))
\]

For \(t < b\), the symmetric kernels \(K()\) are replaced by the corresponding asymmetric kernels of Gasser and Müller (1979). Let \(q = \frac{t}{b}\). The modified kernels are as follows:

- Uniform kernel:
  \[
  K_{U,q}(x) = \frac{4(1 + q^3)}{(1 + q)^4} + \frac{6(1 - q)}{(1 + q)^3} x, \quad -1 \leq x \leq q
  \]

- Epanechnikov kernel:
  \[
  K_{E,q}(x) = K_E(x) \frac{64(2 - 4q + 6q^2 - 3q^3) + 240(1 - q)^2 x}{(1 + q)^4(19 - 18q + 3q^2)}, \quad -1 \leq x \leq q
  \]

- Biweight kernel:
  \[
  K_{BW,q}(x) = K_{BW}(x) \frac{64(8 - 24q + 48q^2 - 45q^3 + 15q^4) + 1120(1 - q)^3 x}{(1 + q)^5(81 - 168q + 126q^2 - 40q^3 + 5q^4)}, \quad -1 \leq x \leq q
  \]

For \(t_D - b \leq t \leq t_D\), let \(q = \frac{t_D - t}{b}\). The asymmetric kernels for \(t < b\) are used with \(x\) replaced by \(-x\).

Using the log transform on the smoothed hazard rate, the 100(1-\(\alpha\))% pointwise confidence interval for the smoothed hazard rate \(\hat{h}(t)\) is given by

\[
\hat{h}(t) = \hat{h}(t) \exp\left[\pm \frac{z_{1-\alpha/2} \hat{\sigma}(\hat{h}(t))}{\hat{h}(t)}\right]
\]

where \(z_{1-\alpha/2}\) is the \((100(1-\alpha/2))\)th percentile of the standard normal distribution.

### Optimal Bandwidth

The following mean integrated squared error (MISE) over the range \(\tau_L\) and \(\tau_U\) is used as a measure of the global performance of the kernel function estimator:

\[
MISE(b) = E \int_{\tau_L}^{\tau_U} (\hat{h}(i) - h(u))^2 du = E \int_{\tau_L}^{\tau_U} \hat{h}^2(u) du - 2E \int_{\tau_L}^{\tau_U} \hat{h}(u)h(u) du + E \int_{\tau_L}^{\tau_U} h^2(u) du
\]
The last term is independent of the choice of the kernel and bandwidth and can be ignored when you are looking for the best value of $b$. The first integral can be approximated by using the trapezoid rule by evaluating $O_h(t_i)$ at a grid of points $u_1 < \cdots < u_M = \tau_U$. You can specify $\tau_L$, $\tau_R$, and $M$ by using the options GRIDL=, GRIDU=, and NMINGRID=, respectively, of the HAZARD plot. The second integral can be estimated by the Ramlau-Hansen (1983a, b) cross-validation estimate:

$$\frac{1}{b} \sum_{i \neq j} K\left(\frac{t_i - t_j}{b}\right) \Delta \hat{H}(t_i) \Delta \hat{H}(t_j)$$

Therefore, for a fixed kernel, the optimal bandwidth is the quantity $b$ that minimizes

$$g(b) = \sum_{i=1}^{M-1} \left[ \frac{u_{i+1} - u_k}{2} \left( \hat{h}^2(u_i) + \hat{h}^2(u_{i+1}) \right) \right] - \frac{2}{b} \sum_{i \neq j} K\left(\frac{t_i - t_j}{b}\right) \Delta \hat{H}(t_i) \Delta \hat{H}(t_j)$$

The minimization is carried out by the golden section search algorithm.

**Comparison of Two or More Groups of Survival Data**

Let $K$ be the number of groups. Let $S_k(t)$ be the underlying survivor function of the $k$th group, $k = 1, \ldots, K$. The null and alternative hypotheses to be tested are

$$H_0 : S_1(t) = S_2(t) = \cdots = S_K(t) \text{ for all } t \leq \tau$$

versus

$$H_1 : \text{at least one of the } S_k(t) \text{'s is different for some } t \leq \tau$$

respectively, where $\tau$ is the largest observed time.

**Likelihood Ratio Test**

The likelihood ratio test statistic (Lawless 1982) for test $H_0$ versus $H_1$ assumes that the data in the various samples are exponentially distributed and tests that the scale parameters are equal. The test statistic is computed as

$$\chi^2 = 2N \log \left( \frac{T}{N} \right) - 2 \sum_{k=1}^{K} N_k \log \left( \frac{T_k}{N_k} \right)$$

where $N_k$ is the total number of events in the $k$th group, $N = \sum_{k=1}^{K} N_k$, $T_k$ is the total time on test in the $k$th stratum, and $T = \sum_{k=1}^{K} T_k$. The approximate probability value is computed by treating $\chi^2$ as having a chi-square distribution with $K - 1$ degrees of freedom.

**Nonparametric Tests**

Let $(T_i, \delta_i, X_i), i = 1, \ldots, n$, denote an independent sample of right-censored survival data, where $T_i$ is the possibly right-censored time, $\delta_i$ is the censoring indicator ($\delta_i=0$ if $T_i$ is censored and $\delta_i=1$ if $T_i$ is an event time), and $X_i = 1, \ldots, K$ for $K$ different groups. Let $t_1 < t_2 < \cdots < t_D$ be the distinct event times in the sample. At time $t_j, j = 1, \ldots, D$, let $W(t_j)$ be a positive weight function, and let $Y_{jk} = \sum_{i:T_i=t_j} I(X_i = k)$ and $d_{jk} = \sum_{i:T_i=t_j} \delta_i I(X_i = k)$ be the size of the risk set and the number of events in the $k$th group, respectively. Let $Y_j = \sum_{k=1}^{K} Y_{jk}, d_j = \sum_{k=1}^{K} d_{jk}$.

The choices of the weight function $W(t_j)$ are given in Table 74.3.
Table 74.3  Weight Functions for Various Tests

<table>
<thead>
<tr>
<th>Test</th>
<th>(W(t_i))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log-rank</td>
<td>1.0</td>
</tr>
<tr>
<td>Wilcoxon</td>
<td>(Y_j)</td>
</tr>
<tr>
<td>Tarone-Ware</td>
<td>(\sqrt{Y_j})</td>
</tr>
<tr>
<td>Peto-Peto</td>
<td>(\hat{S}(t_j))</td>
</tr>
<tr>
<td>Modified Peto-Peto</td>
<td>(\hat{S}(t_j)) (Y_j^{1/2})</td>
</tr>
<tr>
<td>Harrington-Fleming ((p,q))</td>
<td>([\hat{S}(t_{j-1})]^p[1 - \hat{S}(t_{j-1})]^q), (p \geq 0, q \geq 0)</td>
</tr>
</tbody>
</table>

In Table 74.3, \(\hat{S}(t)\) is the product-limit estimate at \(t\) for the pooled sample, and \(\hat{S}(t)\) is a survivor function estimate close to \(\hat{S}(t)\) given by

\[
\hat{S}(t) = \prod_{t_j \leq t} \left(1 - \frac{d_j}{Y_j + 1}\right)
\]

**Unstratified Tests**  The rank statistics (Klein and Moeschberger 1997, Section 7.3) for testing \(H_0\) versus \(H_1\) have the form of a \(K\)-vector \(v = (v_1, v_2, \ldots, v_K)^\prime\) with

\[
v_k = \sum_{j=1}^{D} \left[W(t_j) \left(d_{jk} - Y_{jk} \frac{d_j}{Y_j}\right)\right]
\]

and the variance of \(v_k\) and the covariance of \(v_k\) and \(v_h\) are, respectively,

\[
V_{kk} = \sum_{j=1}^{D} \left[W^2(t_j) \frac{d_j(Y_j - d_j)Y_{jk}(Y_j - Y_{jk})}{Y_j^2(Y_j - 1)}\right], \quad 1 \leq k \leq K
\]
\[
V_{kh} = -\sum_{j=1}^{D} \left[W^2(t_j) \frac{d_j(Y_j - d_j)Y_{jk}Y_{jk}}{Y_j^2(Y_j - 1)}\right], \quad 1 \leq k \neq h \leq K
\]

The statistic \(v_k\) can be interpreted as a weighted sum of observed minus expected numbers of failure for the \(k\)th group under the null hypothesis of identical survival curves. Let \(V = (V_{kh})\). The overall test statistic for homogeneity is \(v'V^-v\), where \(V^-\) denotes a generalized inverse of \(V\). This statistic is treated as having a chi-square distribution with degrees of freedom equal to the rank of \(V\) for the purposes of computing an approximate probability level.

**Adjusted Log-Rank Test**  PROC LIFETEST computes the weighted log-rank test (Xie and Liu 2005, 2011) if you specify the WEIGHT statement. Let \((T_i, \delta_i, X_i, w_i), i = 1, \ldots, n\), denote an independent sample of right-censored survival data, where \(T_i\) is the possibly right-censored time, \(\delta_i\) is the censoring indicator (\(\delta_i=0\) if \(T_i\) is censored and \(\delta_i=1\) if \(T_i\) is an event time), \(X_i = 1, \ldots, K\) for \(K\) different groups, and \(w_i\) is the weight from the WEIGHT statement. Let \(t_1 < t_2 < \cdots < t_D\) be the distinct event times in the sample. At each
Let \( t_j, j = 1, \ldots, D \), and for each \( 1 \leq k \leq K \), let
\[
d_{jk} = \sum_{i: T_i = t_j} I(X_i = k) \quad d_{jk}^w = \sum_{i: T_i = t_j} w_i I(X_i = k)
\]
\[
Y_{jk} = \sum_{i: T_i \geq t_j} I(X_i = k) \quad Y_{jk}^w = \sum_{i: T_i \geq t_j} w_i I(X_i = k)
\]

Let \( d_j = \sum_{k=1}^K d_{jk} \) and \( Y_j = \sum_{k=1}^K Y_{jk} \) denote the number of events and the number at risk, respectively, in the combined sample at time \( t_j \). Similarly, let \( d_{jk}^w = \sum_{k=1}^K d_{jk}^w \) and \( Y_{jk}^w = \sum_{k=1}^K Y_{jk}^w \) denote the weighted number of events and the weighted number at risk, respectively, in the combined sample at time \( t_j \).

The test statistic is
\[
v_k = \sum_{j=1}^D \left( d_{jk}^w - Y_{jk}^w \frac{d_{jk}}{Y_j} \right), \quad k = 1, \ldots, K
\]
and the variance of \( v_k \) and the covariance of \( v_k \) and \( v_h \) are, respectively,
\[
V_{kk} = \sum_{j=1}^D \left\{ \frac{d_j}{Y_j(Y_j - 1)} \sum_{i=1}^{Y_j} \left[ \left( \frac{Y_{jk}}{Y_j} \right)^2 w_i^2 I\{X_i \neq k\} + \left( \frac{Y_{jk}^w}{Y_j^w} \right)^2 w_i^2 I\{X_i = k\} \right] \right\}, \quad 1 \leq k \leq K
\]
\[
V_{kh} = \sum_{j=1}^D \left\{ \frac{d_j}{Y_j(Y_j - 1)} \sum_{i=1}^{Y_j} \left[ \frac{Y_{jk}^w Y_{jh}^w}{(Y_j^w)^2} w_i^2 I\{X_i \neq k, h\} - \frac{(Y_{jk}^w - Y_{jh}^w) Y_{jh}^w}{(Y_j^w)^2} w_i^2 I\{X_i = k\} \right] \right\}, \quad 1 \leq k \neq h \leq K
\]

Let \( V = (V_{kh}) \). Under \( H_0 \), the weighted \( K \)-sample test has a \( \chi^2 \) statistic given by
\[
\chi^2 = (v_1, \ldots, v_K)^T V^{-1} (v_1, \ldots, v_K)
\]
with \( K - 1 \) degrees of freedom.

**Stratified Tests** Suppose the test is to be stratified on \( M \) levels of a set of STRATA variables. Based only on the data of the \( s \)th stratum \((s = 1, \ldots, M)\), let \( v_s \) be the test statistic (Klein and Moeschberger 1997, Section 7.5) for the \( s \)th stratum, and let \( V_s \) be its covariance matrix. Let
\[
v = \sum_{s=1}^M v_s
\]
\[
V = \sum_{s=1}^M V_s
\]

A global test statistic is constructed as
\[
\chi^2 = v^T V^{-1} v
\]
Under the null hypothesis, the test statistic has a \( \chi^2 \) distribution with the same degrees of freedom as the individual test for each stratum.
Multiple-Comparison Adjustments  Let $\chi^2_r$ denote a chi-square random variable with $r$ degrees of freedom. Denote $\phi$ and $\Phi$ as the density function and the cumulative distribution function of a standard normal distribution, respectively. Let $m$ be the number of comparisons; that is,

$$m = \begin{cases} \frac{k(k-1)}{2} & \text{DIFF = ALL} \\ k - 1 & \text{DIFF = CONTROL} \end{cases}$$

For a two-sided test that compares the survival of the $j$th group with that of $l$th group, $1 \leq j \neq l \leq r$, the test statistic is

$$z_{jl}^2 = \frac{(v_j - v_l)^2}{V_{jj} + V_{ll} - 2V_{jl}}$$

and the raw $p$-value is

$$p = \Pr(\chi^2_1 > z_{jl}^2)$$

Adjusted $p$-values for various multiple-comparison adjustments are computed as follows:

- Bonferroni adjustment:
  
  $$p = \min\{1, m \Pr(\chi^2_1 > z_{jl}^2)\}$$

- Dunnett-Hsu adjustment: With the first group being the control, let $C = (c_{ij})$ be the $(r - 1) \times r$ matrix of contrasts; that is,

  $$c_{ij} = \begin{cases} 1 & i = 1, \ldots, r - 1, j = 2, \ldots, r \\ -1 & j = i + 1, i = 2, \ldots, r \\ 0 & \text{otherwise} \end{cases}$$

Let $\Sigma = (\sigma_{ij})$ and $R = (r_{ij})$ be covariance and correlation matrices of $Cv$, respectively; that is,

$$\Sigma = CVC'$$

and

$$r_{ij} = \frac{\sigma_{ij}}{\sqrt{\sigma_{ii}\sigma_{jj}}}$$

The factor-analytic covariance approximation of Hsu (1992) is to find $\lambda_1, \ldots, \lambda_{r-1}$ such that

$$R = D + \lambda \lambda'$$

where $D$ is a diagonal matrix with the $j$th diagonal element being $1 - \lambda_j$ and $\lambda = (\lambda_1, \ldots, \lambda_{r-1})'$. The adjusted $p$-value is

$$p = 1 - \int_{-\infty}^{\infty} \phi(y) \prod_{i=1}^{r-1} \left[ \Phi\left( \frac{\lambda_i y + z_{jl}}{\sqrt{1 - \lambda_i^2}} \right) - \Phi\left( \frac{\lambda_i y - z_{jl}}{\sqrt{1 - \lambda_i^2}} \right) \right] dy$$

which can be obtained in a DATA step as

$$p = \text{PROBMC("DUNNETT2",}\ z_{ij}, \ldots, r - 1, \lambda_1, \ldots, \lambda_{r-1}).$$
Computational Formulas

- Scheffé adjustment:
  \[ p = \Pr \left( \chi^2_{r-1} > z_{jl}^2 \right) \]

- Šidák adjustment:
  \[ p = 1 - \left( 1 - \Pr \left( \chi^2_{1} > z_{jl}^2 \right) \right)^m \]

- SMM adjustment:
  \[ p = 1 - [2 \Phi(z_{jl}) - 1]^m \]

which can also be evaluated in a DATA step as
\[ p = 1 - \text{PROBMC}("\text{MAXMOD}^n, z_{jl}, \ldots, m). \]

- Tukey adjustment:
  \[ p = 1 - \int_{-\infty}^{\infty} r \phi(y) [\Phi(y) - \Phi(y - \sqrt{2z_{jl}})] r^{-1} dy \]

which can also be evaluated in a DATA step as
\[ p = 1 - \text{PROBMC}("\text{RANGE}^n, \sqrt{2z_{jl}}, \ldots, r). \]

### Trend Tests

Trend tests (Klein and Moeschberger 1997, Section 7.4) have more power to detect ordered alternatives as

\[ H_2 : S_1(t) \geq S_2(t) \geq \cdots \geq S_k(t), t \leq \tau, \text{ with at least one inequality} \]

or

\[ H_2 : S_1(t) \leq S_2(t) \leq \cdots \leq S_k(t), t \leq \tau, \text{ with at least one inequality} \]

Let \( a_1 < a_2 < \cdots < a_k \) be a sequence of scores associated with the \( k \) samples. The test statistic and its standard error are given by \( \sum_{j=1}^{k} a_j v_j \) and \( \sum_{j=1}^{k} \sum_{l=1}^{k} a_j a_l V_{jl} \), respectively. Under \( H_0 \), the \( z \)-score

\[ Z = \frac{\sum_{j=1}^{k} a_j v_j}{\sqrt{\sum_{j=1}^{k} \sum_{l=1}^{k} a_j a_l V_{jl}}} \]

has, asymptotically, a standard normal distribution. PROC LIFETEST provides both one-tail and two-tail \( p \)-values for the test.

### Rank Tests for the Association of Survival Time with Covariates

The rank tests for the association of covariates (Kalbfleisch and Prentice 1980, Chapter 6) are more general cases of the rank tests for homogeneity. In this section, the index \( \alpha \) is used to label all observations, \( \alpha = 1, 2, \ldots, n \), and the indices \( i, j \) range only over the observations that correspond to events, \( i, j = 1, 2, \ldots, k \). The ordered event times are denoted as \( t_{(i)} \), the corresponding vectors of covariates are denoted as \( \mathbf{z}_{(i)} \), and the ordered times, both censored and event times, are denoted as \( t_{(\alpha)} \).
The rank test statistics have the form
\[ v = \sum_{\alpha = 1}^{n} c_{\alpha, \delta_{\alpha}} z_{\alpha} \]
where \( n \) is the total number of observations, \( c_{\alpha, \delta_{\alpha}} \) are rank scores, which can be either log-rank or Wilcoxon rank scores, \( \delta_{\alpha} \) is 1 if the observation is an event and 0 if the observation is censored, and \( z_{\alpha} \) is the vector of covariates in the TEST statement for the \( \alpha \)th observation. Notice that the scores, \( c_{\alpha, \delta_{\alpha}} \), depend on the censoring pattern and that the terms are summed up over all observations.

The log-rank scores are
\[ c_{\alpha, \delta_{\alpha}} = \sum_{(j: t_{ij} \leq t_{\alpha})} \left( \frac{1}{n_j} - \delta_{\alpha} \right) \]
and the Wilcoxon scores are
\[ c_{\alpha, \delta_{\alpha}} = 1 - (1 + \delta_{\alpha}) \prod_{(j: t_{ij} \leq t_{\alpha})} \frac{n_j}{n_j + 1} \]
where \( n_j \) is the number at risk just prior to \( t_{ij} \).

The estimates used for the covariance matrix of the log-rank statistics are
\[ V = \sum_{i=1}^{k} \frac{V_i}{n_i} \]
where \( V_i \) is the corrected sum of squares and crossproducts matrix for the risk set at time \( t_{(i)} \); that is,
\[ V_i = \sum_{(\alpha: t_{\alpha} \geq t_{(i)})} (z_{\alpha} - \bar{z}_i)'(z_{\alpha} - \bar{z}_i) \]
where
\[ \bar{z}_i = \sum_{(\alpha: t_{\alpha} \geq t_{(i)})} \frac{z_{\alpha}}{n_i} \]

The estimate used for the covariance matrix of the Wilcoxon statistics is
\[ V = \sum_{i=1}^{k} \left[ a_i (1 - a_i^*) (2z_{(i)}z_{(i)}' + S_i) - (a_i^* - a_i) \left( a_i x_i x_i' + \sum_{j=i+1}^{k} a_j (x_i x_j' + x_j x_j') \right) \right] \]
where
In the case of tied failure times, the statistics $v$ are averaged over the possible orderings of the tied failure times. The covariance matrices are also averaged over the tied failure times. Averaging the covariance matrices over the tied orderings produces functions with appropriate symmetries for the tied observations; however, the actual variances of the $v$ statistics would be smaller than the preceding estimates. Unless the proportion of ties is large, it is unlikely that this will be a problem.

The univariate tests for each covariate are formed from each component of $v$ and the corresponding diagonal element of $V$ as $v_i^2 / V_{ii}$. These statistics are treated as coming from a chi-square distribution for calculation of probability values.

The statistic $v'V^{-1}v$ is computed by sweeping each pivot of the $V$ matrix in the order of greatest increase to the statistic. The corresponding sequence of partial statistics is tabulated. Sequential increments for including a given covariate and the corresponding probabilities are also included in the same table. These probabilities are calculated as the tail probabilities of a chi-square distribution with one degree of freedom. Because of the selection process, these probabilities should not be interpreted as $p$-values.

If desired for data screening purposes, the output data set requested by the OUTTEST= option can be treated as a sum of squares and crossproducts matrix and processed by the REG procedure by using the option METHOD=RSQUARE. Then the sets of variables of a given size can be found that give the largest test statistics. Output 74.1 illustrates this process.

**Analysis of Competing-Risks Data**

Competing risks arise in studies in which individuals are exposed to two or more mutually exclusive failure events, denoted by $\delta \in \{1, \ldots, J\}$. When a failure occurs, you observe the time $T$ and the cause of failure $\delta$. The cumulative incidence function (CIF), also known as the subdistribution function, for failures of cause $j$ is the probability

$$F_j(t) = \Pr(T \leq t, \delta = j)$$

The nonparametric analysis of competing-risks data consists of estimating the CIF and comparing the CIFs of two or more groups.
Estimation of the CIF
For a set of competing-risks data with \( J \geq 2 \) causes of failure, let \( t_1 < t_2 < \cdots < t_L \) be the distinct uncensored times. For each \( l = 1, \ldots, L \), let \( Y_l \) be the number of subjects at risk at \( t_l \), and let \( d_{jl} \) be the number of failures of cause \( j \) at \( t_l \). Let \( \hat{S}(t) \) be the Kaplan-Meier estimator that would have been obtained by assuming that all failure causes are of the same type. Denote \( t_0 = 0 \).

The nonparametric maximum likelihood estimator of the CIF of cause \( j \) is
\[
\hat{F}_j(t) = \sum_{t_l \leq t} \frac{d_{jl}}{Y_l} \hat{S}(t_{l-1})
\]

PROC LIFETEST provides two standard error estimators of the CIF estimator: one is based on the theory of counting processes (Aalen 1978), and the other is based on the delta method (Marubini and Valsecchi 1995). You use the ERROR= option in the PROC LIFETEST statement to choose the standard error estimator. The default is the Aalen estimator (ERROR=AALLEN). Denote \( d_j = \sum_{j=1}^J d_{jl} \).

Aalen Estimator
\[
\hat{\sigma}^2_A(\hat{F}_j(t)) = \sum_{t_l \leq t} \left[ \hat{F}_j(t) - \hat{F}_j(t_l) \right]^2 \frac{d_l}{Y_l(Y_l - d_j)} + \sum_{t_l \leq t} \hat{S}^2(t_{l-1}) \frac{d_{kj}(Y_l - d_{jl})}{Y_l^2(Y_l - 1)} - 2 \sum_{t_l \leq t} \left[ \hat{F}_j(t) - \hat{F}_j(t_l) \right] \hat{S}(t_{l-1}) \frac{d_{jl}(Y_l - d_{jl})}{Y_l(Y_l - d_j)(Y_l - 1)}
\]

Delta Estimator
\[
\hat{\sigma}^2_D(\hat{F}_j(t)) = \sum_{t_l \leq t} \left[ \hat{F}_j(t) - \hat{F}_j(t_l) \right]^2 \frac{d_l}{Y_l(Y_l - d_j)} + \sum_{t_l \leq t} \hat{S}^2(t_{l-1}) \frac{d_{jl}(Y_l - d_{jl})}{Y_l^3} - 2 \sum_{t_l \leq t} \left[ \hat{F}_j(t) - \hat{F}_j(t_l) \right] \hat{S}(t_{l-1}) \frac{d_{jl}}{Y_l^2}
\]

Comparison of the CIF of a Competing Risk for Two or More Groups
Let \( K \) be the number of groups. Consider failure of type 1 to be the failure type of interest. Let \( F_{1k} \) be the cumulative incidence function of type 1 in group \( k \). The null hypothesis to be tested is
\[
H_0 : F_{11} = F_{12} = \cdots = F_{1K} = F_1^0
\]

Gray (1988, Section 2) gives the following \( K \)-sample test procedure for testing \( H_0 \). Let \( (T_{ik}, \delta_{ik}), i = 1, \ldots, n_k \) be the observed data in the \( k \)th group. Without loss of generality, assume that there are only two types of failure (\( J = 2 \)). The number of failures of type \( j \) by \( i \) is
\[ N_{jk}(t) = \sum_{i=1}^{n_k} I(T_{ik} \leq t, \delta_{ik} = j), \quad j = 1, 2 \]

and the number of subjects at risk just before \( t \) in group \( k \) is

\[ Y_k(t) = \sum_{i=1}^{n_k} I(T_{ik} \geq t) \]

For group \( k \), let \( \hat{S}_k(t) \) be the Kaplan-Meier estimator of the survivor function that you obtain by assuming that all failure causes are of the same type. The cumulative incidence function \( \hat{F}_{jk}(t) \) of type \( j \) in the \( k \)th group is estimated by

\[ \hat{F}_{jk}(t) = \int_0^t \hat{S}_k(u-)Y_k^{-1}(u)dN_{jk}(u) \]

Let \( \tau_k \) be the largest uncensored time in group \( k \). Define

\[ \hat{G}_{jk}(t) = 1 - \hat{F}_{jk}(t) \]

\[ R_k(t) = I(\tau_k \geq t)Y_k(t)\frac{\hat{G}_{1k}(t-)}{\hat{S}_k(t-)} \]

The cumulative hazard of the subdistribution for group \( k \), \( \Gamma_{1k} \), is estimated by

\[ \hat{\Gamma}_{1k}(t) = \int_0^t \frac{d\hat{F}_{1k}(u)}{G_{1k}(u-)} = \int_0^t \frac{dN_{1k}(u)}{R_k(u-)}, \quad t \leq \tau_k \]

Under the null hypothesis \( H_0 \), you can estimate the null value of \( \Gamma_{1k}(t) \), denoted by \( \Gamma_{1}^0(t) \), by

\[ \hat{\Gamma}_{1}^0(t) = \int_0^t \frac{dN_{1}(u)}{R_1(u)} \]

The \( K \)-sample test is based on \( z = (z_1, \ldots, z_K)' \), where

\[ z_k = \int_0^{\tau_k} R_k(t) \left[ d\hat{\Gamma}_{1k}(t) - d\hat{\Gamma}_{1}^0(t) \right] \]

You can estimate the asymptotic covariance matrix \( \Sigma = (\sigma_{kk'}) \) as

\[ \hat{\sigma}_{kk'}^2 = \sum_{r=1}^{K} \int_0^{\tau_k \wedge \tau_{k'}} \frac{a_{kr}(t)a_{k'r}(t)}{\hat{h}_r(t)}d\hat{F}_{1}^0(t) + \sum_{r=1}^{K} \int_0^{\tau_k \wedge \tau_{k'}} \frac{b_{2kr}(t)b_{2k'r}(t)}{\hat{h}_r(t)}d\hat{F}_{2r}(t) \]
where

\[
\hat{h}_r(t) = \frac{I(t \leq \tau_r)Y_r(t)}{\hat{S}_r(t)}
\]

\[
\hat{F}^0_1(t) = \int_0^t \frac{dN_1(u)}{\hat{h}(u)}
\]

\[
\hat{G}^0_1(t) = 1 - \hat{F}^0_1(t)
\]

\[
d_{kr}(t) = d_{1kr}(t) + b_{1kr}(t)
\]

\[
b_{jkr}(t) = \left[ I(j = 1) - \frac{\hat{G}^0_1(t)}{\hat{S}_r(t)} \right] [c_{kr}(t) - b_{jkr}(t)]
\]

\[
c_{kr}(t) = \int_0^t d_{1kr}(u)d\hat{F}^0_1(u)
\]

\[
d_{jkr}(t) = I(j = 1)R_k(t)\frac{I(k = r) - \hat{h}_r(t)}{\hat{S}_r(t)}
\]

Because \(\sum_{k=1}^K z_k = 0\), only \(K - 1\) scores are linearly independent. The \(K\)-sample test statistic is formed as a quadratic form of the first \(K - 1\) components of \(z\) and the inverse of the estimated covariance matrix. Under the null hypothesis \(H_0\), this \(K\)-sample test statistic has approximately a chi-square distribution with \(K - 1\) degrees of freedom.

If you specify the GROUP= option in the STRATA statement, you can obtain a stratified version of the test by computing the contributions to \(z_k\) and \(\hat{z}_{kk}\) for each stratum, summing the contributions over the strata, and proceeding as before.

**Restricted Mean Analysis**

Let \(T\) be a nonnegative random variable that represents the failure time of an individual from a homogeneous population. The survivor function (also known as the survival function) of \(T\) is defined as

\[
S(t) = \Pr(T > t)
\]

Assume that \(\tau\) is a prespecified time point of interest. Let \(R\) be the minimum of \(T\) and \(\tau\),

\[
R = T \land \tau = \min(T, \tau)
\]

The restricted mean survival time (RMST) is defined as the expected value of \(R\):

\[
\text{RMST}(\tau) = E(R) = E[\min(T, \tau)]
\]

It can be evaluated by the area under the survivor function over \([0, \tau]\) as

\[
\text{RMST}(\tau) = \int_0^\tau S(u)du
\]

The restricted mean time lost (RMTL) is defined as the expected value of \(\tau - R\):

\[
\text{RMTL}(\tau) = E(\tau - R) = \tau - E[\min(T, \tau)] = \int_0^\tau [1 - S(u)]du
\]
Let $t_1 < t_2 < \cdots < t_D$ represent the distinct event times. For each $i = 1, \ldots, D$, let $Y_i$ be the number of surviving units (the size of the risk set) just prior to $t_i$, and let $d_i$ be the number of units that fail at $t_i$.

The Kaplan-Meier (product-limit) estimate of the survivor function at $t_i$ is the cumulative product

$$\hat{S}(t_i) = \prod_{j=1}^{i} \left(1 - \frac{d_j}{Y_j}\right)$$

If the largest observed time is uncensored, the estimated mean survival time is

$$\hat{\mu} = \sum_{i=1}^{D} \hat{S}(t_{i-1})(t_i - t_{i-1})$$

where $t_0$ is defined to be zero.

RMST(\tau) is estimated by

$$\overline{\text{RMST}}(\tau) = \int_{0}^{\tau} \hat{S}(t) dt = \sum_{i=1}^{N^*} \hat{S}(t_{i-1})(t_i - t_{i-1}) + \hat{S}(t_{N^*})(\tau - t_{N^*})$$

where $N^*$ is the number of $t_i$ values that are less than $\tau$.

RMTL(\tau) is estimated by $\overline{\text{RMTL}}(\tau) = \tau - \text{RMST}(\tau)$.

The standard error of $\overline{\text{RMST}}(\tau)$ or $\overline{\text{RMTL}}(\tau)$ is estimated as

$$\hat{\sigma} = \sqrt{\frac{m}{m-1} \sum_{i=1}^{N^*} d_i A_i^2} \sqrt{\frac{\sum_{i=1}^{N^*} d_i Y_i(Y_i - d_i)}{m - 1}}$$

where

$$A_i = \int_{t_i}^{\tau} \hat{S}(t) dt = \sum_{j=i}^{N^*} \hat{S}(t_j)(t_{j+1} - t_j) + \hat{S}(t_{N^*})(\tau - t_{N^*})$$

$$m = \sum_{j=1}^{N^*} d_j$$

You can use the TAU= suboption in the RMST or RMTL option in the PROC LIFETEST statement to specify a $\tau$ value in the calculation. Note that the term $\frac{m}{m-1}$ is omitted unless you specify the BC suboption in the RMST or RMTL option in the PROC LIFETEST statement. The WEIGHT statement is not supported for the restricted mean analysis.
Comparing the Restricted Means of Two or More Groups
Let $K$ be the number of groups. Let $S_k(t)$ be the underlying survivor function of the $k$th group, $k = 1, \ldots, K$.

Assume that $\tau$ is a prespecified time point of interest and $S_k(\tau) > 0$. The following methods are presented in terms of $\text{RMST}(\tau)$, but they also extend to the analysis of $\text{RMTL}(\tau)$.

The null and alternative hypotheses to be tested are

$$H_0 : \text{RMST}_1(\tau) = \text{RMST}_2(\tau) = \cdots = \text{RMST}_K(\tau)$$

versus

$$H_1 : \text{at least one of the } \text{RMST}_k(\tau) \text{'s is different.}$$

Let $\hat{\text{RMST}}(\tau) = [\hat{\text{RMST}}_1(\tau), \hat{\text{RMST}}_2(\tau), \ldots, \hat{\text{RMST}}_K(\tau)]^T$ be the vector of estimated RMSTs for the $K$ groups.

Let $\hat{\Sigma}$ be the estimated covariance matrix for $\hat{\text{RMST}}(\tau)$. It is a diagonal matrix, and the $j$th diagonal element is $\hat{\sigma}_j^2$, which is the estimated variance of $\hat{\text{RMST}}_j(\tau)$.

Let $D$ be a $(K - 1) \times K$ matrix whose $j$th row is $e_j - e_{j+1}$, where $e_j$ is a $K$-dimensional vector whose $j$th element is 1 and whose other elements are 0. The test statistic is computed as

$$(\hat{\text{RMST}}(\tau))^T D^T (D \hat{\Sigma} D^T)^{-1} D \hat{\text{RMST}}(\tau)$$

Under the null hypothesis $H_0$, this $K$-sample test statistic has approximately a chi-square distribution with degrees of freedom equal to the rank of $D \hat{\Sigma} D^T$.

If you specify the GROUP= option in the STRATA statement, you can obtain a stratified version of the test by computing $\hat{\text{RMST}}(\tau)$ and $\hat{\Sigma}$ for each stratum, summing them over the strata, and performing the chi-square test as before.

If you specify the DIFF= option in the STRATA statement, you can make inference with regard to paired differences of the RMST. If you also specify the GROUP= option, the RMST for a given group under comparison is computed as the sample mean of the stratum-specific RMSTs of the corresponding group, and the variance is obtained as the variance of the sample mean. You can use the ADJUST= option in the STRATA statement to make multiple-comparison adjustments to the $p$-values.

Output Data Sets
OUTCIF Data Set
You can specify the OUTCIF= option in the PROC LIFETEST statement to create an output data set that contains the cumulative incidence estimates. The data set contains the following columns:

- any specified BY variables
- the censoring variable as given in the TIME statement to indicate the failure of interest
- a numeric variable named STRATUM that numbers the strata, if you specify the STRATA statement
Output Data Sets

- any specified STRATA variables, whose values come from either their original values or the midpoints of the stratum intervals if you use cutpoints to define strata (semi-infinite intervals are labeled by their finite endpoint)
- the GROUP= variable, if you specify the GROUP= option in the STRATA statement
- the Timelist variable, if you specify the TIMELIST= option and the REDUCEOUT option in the PROC LIFETEST statement
- the time variable as specified in the TIME statement
- AtRisk, a variable that contains the number of subjects at risk just before the specified time. This variable is omitted if you specify the REDUCEOUT option in the PROC LIFETEST statement.
- Event, a variable that contains the number of subjects that fail at the specified time from the cause of interest. This variable is omitted if you specify the REDUCEOUT option in the PROC LIFETEST statement.
- AllEventTypes, a variable that contains the number of subjects that fail at the specified time from any cause. This variable is omitted if you specify the REDUCEOUT option in the PROC LIFETEST statement.
- CIF, a variable that contains the point estimates of the cumulative incidence function
- CIF_STDERR, a variable that contains the standard errors of the CIF estimator
- ALPHA, a variable that contains the $\alpha$-level of the confidence intervals
- CONFTYPE, a variable that contains the name of the transformation that is applied to the CIF to compute the confidence intervals for the CIF
- CIF_LCL, a variable that contains the lower confidence limits of the CIF
- CIF_UCL, a variable that contains the upper confidence limits of the CIF

Each estimated CIF contains an initial observation whose value is 1 for the CIF and 0 for the time. The output data set contains an observation for each distinct failure time when an event occurs or an observation is censored.

OUTSURV= Data Set

You can specify the OUTSURV= option in the PROC LIFETEST statement to create an output data set that contains the survival estimates. The data set contains the following columns:

- any specified BY variables
- a numeric variable STRATUM that numbers the strata, if you specify the STRATA statement
- any specified STRATA variables, their values coming from either their original values or the midpoints of the stratum intervals if endpoints are used to define strata (semi-infinite intervals are labeled by their finite endpoint)
- the GROUP= variables, if you specify the GROUP= option in the STRATA statement
the time variable as specified in the TIME statement. For METHOD=KM, METHOD=BRESLOW, or METHOD=FH, it contains the observed failure or censored times. For the life-table estimates, it contains the lower endpoints of the time intervals.

- SURVIVAL, a variable that contains the survivor function estimates
- CONFTYPE, a variable that contains the name of the transformation applied to the survival time in the computation of confidence intervals
- SDF_LCL, a variable that contains the lower limits of the pointwise confidence intervals for the survivor function
- SDF_UCL, a variable that contains the upper limits of the pointwise confidence intervals for the survivor function

If the estimation uses the product-limit, Breslow, or Fleming-Harrington method, then the data set also contains the following:

- _CENSOR_, an indicator variable that has a value 1 for a censored observation and a value 0 for an event observation
- SDF_STDERR, a variable that contains the standard error of the survivor function estimator
- HW_LCL, a variable that contains the lower limits of the Hall-Wellner confidence bands (if you specify the CONFBAND=HW option or the CONFBAND=ALL option in the PROC LIFETEST statement)
- HW_UCL, a variable that contains the upper limits of the Hall-Wellner confidence bands (if you specify the CONFBAND=HW option or the CONFBAND=ALL option in the PROC LIFETEST statement)
- EP_LCL, a variable that contains the lower limits of the equal-precision confidence bands (if you specify the CONFBAND=EP option or the CONFBAND=ALL option in the PROC LIFETEST statement)
- EP_UCL, a variable that contains the upper limits of the equal-precision confidence bands (if you specify the CONFBAND=EP option or the CONFBAND=ALL option in the PROC LIFETEST statement)

If the estimation uses the life-table method, then the data set also contains the following:

- MIDPOINT, a variable that contains the value of the midpoint of the time interval
- PDF, a variable that contains the density function estimates
- PDF_LCL, a variable that contains the lower endpoints of the PDF confidence intervals
- PDF_UCL, a variable that contains the upper endpoints of the PDF confidence intervals
- HAZARD, a variable that contains the hazard estimates
- HAZ_LCL, a variable that contains the lower endpoints of the hazard confidence intervals
- HAZ_UCL, a variable that contains the upper endpoints of the hazard confidence intervals
Each survival function contains an initial observation with the value 1 for the SDF and the value 0 for the time. The output data set contains an observation for each distinct failure time if the product-limit, Breslow, or Fleming-Harrington method is used, or it contains an observation for each time interval if the life-table method is used. The product-limit, Breslow, or Fleming-Harrington survival estimates are defined to be right continuous; that is, the estimates at a given time include the factor for the failure events that occur at that time.

**OUTTEST= Data Set**

The OUTTEST= option in the LIFETEST statement creates an output data set that contains the rank statistics for testing the association of failure time with covariates. It contains the following:

- any specified BY variables
- _TYPE_, a character variable of length 8 that labels the type of rank test, either “LOG-RANK” or “WILCOXON”
- _NAME_, a character variable of length 8 that labels the rows of the covariance matrix and the test statistics
- the TIME variable, containing the overall test statistic in the observation that has _NAME_ equal to the name of the time variable and the univariate test statistics under their respective covariates.
- all variables listed in the TEST statement

The output is in the form of a symmetric matrix formed by the covariance matrix of the rank statistics bordered by the rank statistics and the overall chi-square statistic. If the value of _NAME_ is the name of a variable in the TEST statement, the observation contains a row of the covariance matrix and the value of the rank statistic in the time variable. If the value of _NAME_ is the name of the TIME variable, the observation contains the values of the rank statistics in the variables from the TEST list and the value of the overall chi-square test statistic in the TIME variable.

Two complete sets of statistics labeled by the _TYPE_ variable are produced, one for the log-rank test and one for the Wilcoxon test.

**Displayed Output**

The following sections describe the output that PROC LIFETEST produces by default. The output is organized into various tables, which are discussed in their order of appearance. The set of tables that PROC LIFETEST produces for a survival analysis, specifically with one type of failure, is different from the set of tables that it produces for an analysis of competing-risks data, which have multiple types of failure.

**Tables for Survival Analysis**

*Product-Limit Survival Estimates*

The “Product-Limit Survival Estimates” table is displayed if you request the product-limit method of estimation. The table displays the following:
the observed (event or censored) time
• the number of units at risk (if you specify the ATRISK option in the PROC LIFETEST statement)
• the number of events (if you specify the ATRISK option in the PROC LIFETEST statement)
• the product-limit estimate of the survivor function
• the corresponding estimate of the cumulative distribution function of the failure time
• the standard error estimate of the survivor function estimator
• the Nelson-Aalen cumulative hazard function estimate (if you specify the NELSON option in the PROC LIFETEST statement)
• the standard error of the Nelson-Aalen estimator (if you specify the NELSON option in the PROC LIFETEST statement)
• the number of event times that have been observed
• the number of event or censored times that remain to be observed
• the frequency of the observed times (if you specify the FREQ statement)
• values of the ID variables (if you specify the ID statement)

The ODS name of this table is ProductLimitEstimates.

**Breslow Survival Estimates**

The “Breslow Survival Estimates” table is displayed if you request the Breslow method of estimation. The table displays the following:

• the observed (event or censored) time
• the number of units at risk (if you specify the ATRISK option in the PROC LIFETEST statement)
• the number of events (if you specify the ATRISK option in the PROC LIFETEST statement)
• the Breslow estimate of the survivor function
• the corresponding estimate of the cumulative distribution function of the failure time
• the standard error estimate of the survivor function estimator
• the Nelson-Aalen cumulative hazard function estimate (if you specify the NELSON option in the PROC LIFETEST statement)
• the standard error of the Nelson-Aalen estimator (if you specify the NELSON option in the PROC LIFETEST statement)
• the number of event times that have been observed
• the number of event or censored times that remain to be observed
• the frequency of the observed times (if you specify the FREQ statement)
values of the ID variables (if you specify the ID statement)

The ODS name of this table is BreslowEstimates.

**Fleming-Harrington Survival Estimates**

The “Fleming-Harrington Survival Estimates” table is displayed if you request the Fleming-Harrington method of estimation. The table displays the following:

- the observed (event or censored) time
- the number of units at risk (if you specify the ATRISK option in the PROC LIFETEST statement)
- the number of events (if you specify the ATRISK option in the PROC LIFETEST statement)
- the Fleming-Harrington estimate of the survivor function
- the corresponding estimate of the cumulative distribution function of the failure time
- the standard error estimate of the survivor function estimator
- the Nelson-Aalen cumulative hazard function estimate (if you specify the NELSON option in the PROC LIFETEST statement)
- the standard error of the Nelson-Aalen estimator (if you specify the NELSON option in the PROC LIFETEST statement)
- the number of event times that have been observed
- the number of event or censored times that remain to be observed
- the frequency of the observed times (if you specify the FREQ statement)
- values of the ID variables (if you specify the ID statement)

The ODS name of this table is FlemingEstimates.

**Quartile Estimates**

The “Quartiles Estimates” table is displayed if you request the product-limit, Breslow, or Fleming-Harrington method of estimation. The table displays the following:

- point estimates of the quartiles of the survival times
- the lower and upper confidence limits for the quartiles

The ODS name of this table is Quartiles.
**Mean Estimate**

The “Mean Estimate” table is displayed if you request the product-limit, Breslow, or Fleming-Harrington method of estimation. The table displays the following:

- the estimated mean survival time
- the estimated standard error of the mean estimator

The ODS name of this table is Means.

**Life-Table Survival Estimates**

The “Life-Table Survival Estimates” table is displayed if you request the life-table method of estimation. The table displays the following:

- the time intervals into which the failure and censored times are distributed. Each interval is from the lower limit, up to but not including the upper limit; if the upper limit is infinity, the missing value is printed.
- the number of events that occur in the interval
- the number of censored observations that fall into the interval
- the effective sample size for the interval
- the estimate of conditional probability of events (failures) in the interval
- the standard error of the conditional probability estimator
- the estimate of the survival function at the beginning of the interval
- the estimate of the cumulative distribution function of the failure time at the beginning of the interval
- the standard error estimate of the survivor function estimator
- the estimate of the median residual lifetime, which is the amount of time elapsed before reducing the number of at-risk units to one-half. This is also known as the *median future lifetime* in Elandt-Johnson and Johnson (1980)).
- the estimated standard error of the median residual lifetime estimator
- the density function estimated at the midpoint of the interval
- the standard error estimate of the density estimator
- the hazard rate estimated at the midpoint of the interval
- the standard error estimate of the hazard estimator

The ODS name of this table is LifetableEstimates.
Summary of the Number of Censored and Uncensored Values
The “Summary of the Number of Censored and Uncensored Values” table displays following:

- the stratum identification (if you specify the STRATA statement)
- the total number of observations
- the number of event observations
- the number of censored observations
- the percentage of censored observations

The ODS name of this table is CensoredSummary.

Rank Statistics
The “Rank Statistics” table contains the test statistics of the nonparametric $k$-sample tests. The ODS name of this table is HomStats.

Covariance Matrix for the Log-Rank Statistics
The “Covariance Matrix for the Log-Rank Statistics” table is displayed if the log-rank $k$-sample test is requested. The ODS name of this table is LogrankHomCov.

Covariance Matrix for the Wilcoxon Statistics
The “Covariance Matrix for the Wilcoxon Statistics” table is displayed if the Wilcoxon $k$-sample test is requested. The ODS name of this table is WilHomCov.

Covariance Matrix for the Tarone Statistics
The “Covariance Matrix for the Tarone Statistics” table is displayed if the Tarone-Ware $k$-sample test is requested. The ODS name of this table is TaroneHomCov.

Covariance Matrix for the Peto Statistics
The “Covariance Matrix for the Peto Statistics” table is displayed if the Peto-Peto $k$-sample test is requested. The ODS name of this table is PetoHomCov.

Covariance Matrix for the ModPeto Statistics
The “Covariance Matrix for the ModPeto Statistics” table is displayed if the modified Peto-Peto $k$-sample test is requested. The ODS name of this table is ModPetoHomCov.

Covariance Matrix for the Fleming Statistics
The “Covariance Matrix for the Fleming Statistics” table is displayed if the Fleming-Harrington $k$-sample test is requested. The ODS name of this table is FlemingHomCov.

Legend for Strata
The “Legend for Strata” table is displayed if two or more variables are specified in the STRATA statement. The ODS name of this table is Legend.
Test of Equality over Strata
The “Test of Equality over Strata” table is displayed if an unstratified \( k \)-sample test is carried out. The table contains the chi-square statistics, degrees of freedom, and \( p \)-values of the nonparametric tests and the likelihood ratio test (which is based on the exponential distribution). The ODS name of this table is HomTests.

Stratified Test of Equality over Group
The “Stratified Test of Equality over Group” table is displayed if a stratified test is carried out. The tables contains the chi-square statistics, degrees of freedom, and \( p \)-values of the stratified tests. The ODS name of this table is HomTests.

Scores for Trend Test
The “Scores for Trend Test” table is displayed if you specify the TREND option in the STRATA statement. The table contains the set of scores used to construct the trend tests. The ODS name of this table is TrendScores.

Trend Tests
The “Trend Tests” table is displayed if you specify the TREND option in the STRATA statement. The table contains the results of the trend tests. The ODS name of this table is TrendTests.

Adjustment for Multiple Comparisons for the Log-Rank Test
The “Adjustment for Multiple Comparisons for the Log-Rank Test” table is displayed if the log-rank test and a multiple-comparison adjustment method are specified. The table contains the chi-square statistics and the raw and adjusted \( p \)-values of the paired comparisons. The ODS name of this table is SurvDiff.

Adjustment for Multiple Comparisons for the Wilcoxon Test
The “Adjustment for Multiple Comparisons for the Wilcoxon Test” table is displayed if the Wilcoxon test and a multiple-comparison method are specified. The table contains the chi-square statistics and the raw and adjusted \( p \)-values of the paired comparisons. The ODS name of this table is SurvDiff.

Adjustment for Multiple Comparisons for the Tarone Test
The “Adjustment for Multiple Comparisons for the Tarone Test” table is displayed if the Tarone-Ware test and a multiple-comparison method are specified. The table contains the chi-square statistics and the raw and adjusted \( p \)-values of the paired comparisons. The ODS name of this table is SurvDiff.

Adjustment for Multiple Comparisons for the Peto Test
The “Adjustment for Multiple Comparisons for the Peto Test” table is displayed if the Peto-Peto test and a multiple-comparison method are specified. The table contains the chi-square statistics and the raw and adjusted \( p \)-values of the paired comparisons. The ODS name of this table is SurvDiff.

Adjustment for Multiple Comparisons for the ModPeto Test
The “Adjustment for Multiple Comparisons for the ModPeto Test” table is displayed if the modified Peto-Peto test and a multiple-comparison method are specified. The table contains the chi-square statistics and the raw and adjusted \( p \)-values of the paired comparisons. The ODS name of this table is SurvDiff.
Adjustment for Multiple Comparisons for the Fleming Test
The “Adjustment for Multiple Comparisons for the Fleming Test” table is displayed if the Fleming-Harrington test and a multiple-comparison method are specified. The table contains the chi-square statistics and the raw and adjusted $p$-values of the paired comparisons. The ODS name of this table is SurvDiff.

Univariate Chi-Squares for the Log-Rank Test
The “Univariate Chi-Squares for the Log-Rank Test” table is displayed if you specify the TEST statement. The table displays the log-rank test results for individual variables in the TEST statement. The ODS name of this table is LogUniChiSq.

Covariance Matrix of the Log-Rank Statistics
The “Covariance Matrix of the Log-Rank Statistics” table is displayed if you specify the TEST statement. The table displays the estimated covariance matrix of the log-rank statistics for association. The ODS name of this table is LogTestCov.

Forward Stepwise Sequence of Chi-Squares for the Log-Rank Test
The “Forward Stepwise Sequence of Chi-Squares for the Log-Rank Test” table is displayed if you specify the TEST statement. The table contains the sequence of partial chi-square statistics for the log-rank test in the order of the greatest increase to the overall test statistic, the degrees of freedom of the partial chi-square statistics, the approximate probability values of the partial chi-square statistics, the chi-square increments for including the given variables, and the probability values of the chi-square increments. The ODS name of this table is LogForStepSeq.

Univariate Chi-Squares for the Wilcoxon Test
The “Univariate Chi-Squares for the Wilcoxon Test” table displays the Wilcoxon test results for individual variables in the TEST statement. The ODS name of this table is WilUniChiSq.

Covariance Matrix of the Wilcoxon Statistics
The “Covariance Matrix of the Wilcoxon Statistics” table is displayed if you specify the TEST statement. The table displays the estimated covariance matrix of the Wilcoxon statistics for association. The ODS name of this table is WilTestCov.

Forward Stepwise Sequence of Chi-Squares for the Wilcoxon Test
The “Forward Stepwise Sequence of Chi-Squares for the Wilcoxon Test” table is displayed if you specify the TEST statement. The table contains the sequence of partial chi-square statistics for the Wilcoxon test in the order of the greatest increase to the overall test statistic, the degrees of freedom of the partial chi-square statistics, the approximate probability values of the partial chi-square statistics, the chi-square increments for including the given variables, and the probability values of the chi-square increments. The ODS name of this table is WilForStepSeq.

Tables for Competing-Risks Analysis
Summary of Failure Outcomes
The “Summary of Failure Outcomes” table displays the following:

- the stratum identification, if you specify the STRATA statement
- the group identification, if you specify the GROUP= option in the STRATA statement
Chapter 74: The LIFETEST Procedure

- the number of failure events of interest
- the number of competing events
- the number of censored observations

The ODS name of this table is FailureSummary.

**Cumulative Incidence Function Estimates**
The “Cumulative Incidence Function Estimates” table is displayed if you use the FAILCODE= option in the TIME statement to stipulate a competing-risk analysis. The table displays the following:

- the group identification, if you specify the GROUP= option in the STRATA statement
- the failure time of the event of interest
- the estimated cumulative incidence function
- the standard error estimate of the cumulative incidence estimator
- the lower and upper confidence limits of the cumulative incidence function

The ODS name of this table is CIF.

**Gray’s Test for Equality of Cumulative Incidence Functions**
The “Gray’s Test for Equality of Cumulative Incidence Functions” table is displayed if you specify the STRATA statement. The table displays the following:

- the failure code, if you specify more than one FAILCODE= option value
- the chi-square statistic of Gray’s test (Gray 1988)
- the degrees of freedom
- the p-value

The ODS name of this table is GrayTest.

**Tables for Restricted Mean Analysis**

**RMST Analysis Information**
The “RMST Analysis Information” table is displayed if you specify the RMST option in the PROC LIFETEST statement to perform an RMST analysis. The table displays the following:

- the \( \tau \) value that is used in computing the RMST

The ODS name of this table is RMSTInfo.
**RMST Estimates**
The “RMST Estimates” table is displayed if you specify the RMST option in the PROC LIFETEST statement to perform an RMST analysis. The table displays the following:

- the stratum identification, if you specify the STRATA statement
- the group identification, if you specify the GROUP= option in the STRATA statement
- the estimated RMST
- the standard error estimate of the RMST

The ODS name of this table is RMST.

**RMST Test for Equality**
The “RMST Test for Equality” table is displayed if you specify the STRATA statement and the RMST option in the PROC LIFETEST statement. The table displays the following:

- the source of the groups under comparison
- the chi-square statistic of the test
- the degrees of freedom
- the p-value

The ODS name of this table is RMSTTest.

**Stratified RMST Test for Equality**
The “Stratified RMST Test for Equality” table is displayed if you specify the GROUP= option in the STRATA statement and the RMST option in the PROC LIFETEST statement. The table displays the following:

- the source of the groups under comparison
- the chi-square statistic of the test
- the degrees of freedom
- the p-value

The ODS name of this table is RMSTStratifiedTest.

**Restricted Mean Survival Time Comparisons**
The “Restricted Mean Survival Time Comparisons” table is displayed if you specify the DIFF= option in the STRATA statement and the RMST option in the PROC LIFETEST statement. The table contains the chi-square statistics and the unadjusted and adjusted p-values of the paired comparisons. The ODS name of this table is RMSTDiff.
**RMTL Analysis Information**
The “RMTL Analysis Information” table if you specify the RMTL option in the PROC LIFETEST statement to perform an RMST analysis. The table displays the following:

- the $\tau$ value that is used in computing the RMTL

The ODS name of this table is RMTLInfo.

**RMTL Estimates**
The “RMTL Estimates” table is displayed if you specify the RMTL option in the PROC LIFETEST statement to perform an RMTL analysis. The table displays the following:

- the stratum identification, if you specify the STRATA statement
- the group identification, if you specify the GROUP= option in the STRATA statement
- the estimated RMTL
- the standard error estimate of the RMTL

The ODS name of this table is RMTL.

**RMTL Test for Equality**
The “RMTL Test for Equality” table is displayed if you specify the STRATA statement and the RMTL option in the PROC LIFETEST statement. The table displays the following:

- the source of the groups under comparison
- the chi-square statistic of the test
- the degrees of freedom
- the $p$-value

The ODS name of this table is RMTLTest.

**Stratified RMTL Test for Equality**
The “Stratified RMTL Test for Equality” table is displayed if you specify the GROUP= option in the STRATA statement and the RMTL option in the PROC LIFETEST statement. The table displays the following:

- the source of the groups under comparison
- the chi-square statistic of the test
- the degrees of freedom
- the $p$-value

The ODS name of this table is RMTLStratifiedTest.
**Restricted Mean Time Lost Comparisons**

The “Restricted Mean Time Lost Comparisons” table is displayed if you specify the DIFF= option in the STRATA statement and the RMTL option in the PROC LIFETEST statement. The table contains the chi-square statistics and the unadjusted and adjusted $p$-values of the paired comparisons. The ODS name of this table is RMTLDiff.

---

**Plot Options Superseded by ODS Graphics**

You can select one of the following three types of graphics in PROC LIFETEST: ODS, traditional, and line printer. ODS Graphics is the preferred method of creating graphs, superseding the other two.

When ODS Graphics is enabled, you can use the PLOTS= option in the PROC LIFETEST statement to create plots by using ODS Graphics. For more information about ODS Graphics options, see the PLOTS= option in the section “PROC LIFETEST Statement” on page 5576.

If ODS Graphics is not enabled and you specify the LINEPRINTER option, line printer plots are produced; otherwise traditional graphics are produced.

Table 74.4 summarizes the ways in which you can request graphics.

<table>
<thead>
<tr>
<th>Graphics Result</th>
<th>ODS Graphics</th>
<th>PLOTS= Option Specified?</th>
<th>LINEPRINTER Option Specified?</th>
</tr>
</thead>
<tbody>
<tr>
<td>ODS Graphics</td>
<td>Enabled</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>ODS Graphics survival plot</td>
<td>Enabled</td>
<td>No</td>
<td>No</td>
</tr>
<tr>
<td>Traditional graphics</td>
<td>Disabled</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Line printer plot</td>
<td>Enabled</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>No graphics</td>
<td>Disabled</td>
<td>No</td>
<td>No</td>
</tr>
<tr>
<td>No graphics</td>
<td>Disabled</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>No graphics</td>
<td>Enabled</td>
<td>No</td>
<td>Yes</td>
</tr>
</tbody>
</table>

Table 74.5 summarizes the options available in the PROC LIFETEST statement for line printer and traditional graphics.

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Line Printer Plots</td>
<td></td>
</tr>
<tr>
<td>FORMCHAR(1,2,7,9)=</td>
<td>Defines the characters to be used for line printer plot axes</td>
</tr>
<tr>
<td>LINEPRINTER</td>
<td>Specifies that plots be produced by a line printer</td>
</tr>
<tr>
<td>MAXTIME=</td>
<td>Specifies the maximum time value for plotting</td>
</tr>
<tr>
<td>NOCENSPLOT</td>
<td>Suppresses the plot of censored observations</td>
</tr>
<tr>
<td>PLOTS=</td>
<td>Specifies the plots to display</td>
</tr>
</tbody>
</table>
The following options are used to produce line printer and traditional graphics:

**ANNOTATE=SAS-data-set**

specifies an input data set that contains appropriate variables for annotation of the traditional graphics. The ANNOTATE= option enables you to add features (for example, labels that explain extreme observations) to plots produced on graphics devices. The ANNOTATE= option cannot be used if you specify LINEPRINTER option or if ODS Graphics is enabled. The data set specified must be an ANNOTATE= type data set, as described in **SAS/GRAPH: Reference**.

The data set specified with the ANNOTATE= option in the PROC LIFETEST statement is “global” in the sense that the information in this data set is displayed in every plot produced by a single invocation of PROC LIFETEST.

**CENSOREDSYMBOL=name | 'string'**

specifies the symbol value for the censored observations in traditional graphics. The value, name or 'string', is the symbol value specification allowed in SAS/GRAPH software. The default is CS=CIRCLE. If you want to omit plotting the censored observations, specify CS=NONE. The CENSOREDSYMBOL= option cannot be used if you specify LINEPRINTER option or if you enable ODS Graphics.

**DESCRIPTION='string'**

specifies a descriptive string of up to 256 characters that appears in the “Description” field of the traditional graphics catalog. The description does not appear in the plots. By default, PROC LIFETEST assigns a description of the form PLOT OF vname versus hname, where vname and hname are the names of the y variable and the x variable, respectively. The DESCRIPTION= option cannot be used if you specify the LINEPRINTER option or if you enable ODS Graphics.
**EVENTSYMBOL=** *name | 'string'*

**ES=** *name | 'string'*

specifies the symbol value for the event observations in traditional graphics. The value, *name* or 'string', is the symbol value specification allowed in SAS/GRAPH software. The default is ES=NONE. The EVENTSYMBOL= option cannot be used if you specify the LINEPRINTER option or if you enable ODS Graphics.

**FORMCHAR(1,2,7,9)=** *string*

defines the characters to be used for constructing the vertical and horizontal axes of the line printer plots. The string should be four characters. The first and second characters define the vertical and horizontal bars, respectively, which are also used in drawing the steps of the Kaplan-Meier, Breslow, or Fleming-Harrington survival curve. The third character defines the tick mark for the axes, and the fourth character defines the lower left corner of the plot. The default is FORMCHAR(1,2,7,9)='|-+-'. Any character or hexadecimal string can be used to customize the plot appearance. If you use hexadecimals, you must put an x after the closing quote. For example, to send the plot output to a printer with the IBM graphics character set (1 or 2), specify the following:

```
formchar(1,2,7,9)='B3C4C5C0'x
```

See the chapter titled “The PLOT Procedure” in the *Base SAS Procedures Guide* for further information.

**GOUT=** *graphics-catalog*

specifies the graphics catalog for saving traditional graphics output from PROC LIFETEST. The default is Work.Gseg. The GOUT= option cannot be used if you specify the LINEPRINTER option or if you enable ODS Graphics. For more information, see the chapter titled “The GREPLAY Procedure” in *SAS/GRAPH: Reference*.

**LANNOTATE=** *SAS-data-set*

specifies an input data set that contains variables for local annotation of traditional graphics. You can use the LANNOTATE= option to specify a different annotation for each BY group, in which case the BY variables must be included in the LANNOTATE= data set. The LANNOTATE= option cannot be used if you specify the LINEPRINTER option or if you enable ODS Graphics. The data set specified must be an ANNOTATE= type data set, as described in *SAS/GRAPH: Reference*.

If there is no BY-group processing, the ANNOTATE= and LANNOTATE= options have the same effects.

**LINEPRINTER**

**LS**

specifies that plots are produced by a line printer instead of by a graphical device.

**MAXTIME=** *value*

specifies the maximum value of the time variable allowed on the plots so that outlying points do not determine the scale of the time axis of the plots. This option affects only the displayed plots and has no effect on any calculations.
NOCENSPLOT requests that the plot of censored observations be suppressed when the LINEPRINTER and PLOTS= options are specified. This option is not needed when the life-table method is used to compute the survival estimates, because the plot of censored observations is not produced.

**Line Printer PLOTS= Option**

\[
\text{PLOTS=plot-request} \\
\text{PLOTS=(plot-requests)}
\]

controls the line printer plots produced. You must also specify the LINEPRINTER option to obtain line printer plots. When you specify only one plot-request, you can omit the parentheses around the plot-request. Here are some examples:

\[
\text{plots=s} \\
\text{plots=(s ls lls)}
\]

The plot-requests include the following:

**CENSTED**

C specifies a plot of censored observations. This option is available for METHOD=KM, METHOD=BRESLOW, or METHOD=FH only.

**SURVIVAL**

S specifies a plot of the estimated SDF versus time.

**LOGSURV**

LS specifies a plot of the negative log of the estimated SDF versus time.

**LOGLOGS**

LLS specifies a plot of the log of the negative log of the estimated SDF versus the log of time.

**HAZARD**

H specifies a plot of the estimated hazard function versus time (life-table method only).

**PDF**

P specifies a plot of the estimated probability density function versus time (life-table method only).
**Traditional Graphics PLOTS= Option**

\[
\text{PLOTS=plot-request < (NAME=name | 'string') >}
\]

\[
\text{PLOTS=(plot-request < (NAME=name | 'string') >, \ldots, plot-request < (NAME=name | 'string') >)}
\]

controls plots produced in traditional graphics. To obtain traditional graphics, you must neither enable ODS Graphics nor specify the LINEPRINTER option. For each plot-request, you can use the NAME= option to specify a name to identify the plot. The name can be specified as a SAS name or as a quoted string of up to 256 characters. Only the first eight characters are used as the entry name in the GOUT= catalog. The plot-requests include the following:

**SURVIVAL**

* S plots the estimated survivor functions versus time.

**LOGSURV**

* LS plots the negative log of estimated survivor functions versus time.

**LOGLOGS**

* LLS plots the log of negative log of estimated survivor functions versus the log of time.

**HAZARD**

* H plots estimated hazard function versus time (life-table method only).

**PDF**

* P plots the estimated probability density function versus time (life-table method only).

When you specify only one plot-request, you can omit the parentheses around the plot-request. Here are some examples:

\[
\begin{align*}
\text{plots=s} \\
\text{plots=(s(name=Surv2), h(name=Haz2))}
\end{align*}
\]

The latter requests a plot of the estimated survivor function versus time and a plot of the estimated hazard function versus time, with Surv2 and Haz2 as their names in the GOUT= catalog, respectively.

---

**ODS Table Names**

PROC LIFETEST assigns a name to each table it creates. You can use these names to reference the table when using the Output Delivery System (ODS) to select tables and create output data sets. These names are listed in Table 74.6. For more information about ODS, see Chapter 20, “Using the Output Delivery System.”
<table>
<thead>
<tr>
<th>ODS Table Name</th>
<th>Description</th>
<th>Statement</th>
<th>Option</th>
</tr>
</thead>
<tbody>
<tr>
<td>BreslowEstimates</td>
<td>Breslow estimates</td>
<td>PROC</td>
<td>METHOD=BRESLOW</td>
</tr>
<tr>
<td>CensoredSummary</td>
<td>Number of event and censored observations</td>
<td>PROC</td>
<td>METHOD=BRESLOW</td>
</tr>
<tr>
<td>CIF</td>
<td>Cumulative incidence function estimates</td>
<td>TIME</td>
<td>EVENTCODE</td>
</tr>
<tr>
<td>FailureSummary</td>
<td>Summary of failure outcomes for competing-risks data</td>
<td>TIME</td>
<td>EVENTCODE</td>
</tr>
<tr>
<td>FlemingEstimates</td>
<td>Fleming-Harrington estimates</td>
<td>PROC</td>
<td>METHOD=FH</td>
</tr>
<tr>
<td>FlemingHomCov</td>
<td>Covariance matrix for k-sample FLEMING statistics</td>
<td>STRATA</td>
<td>TEST=FLEMING</td>
</tr>
<tr>
<td>GrayTest</td>
<td>Results of k-sample test of Gray (1988) comparing CIFs</td>
<td>TIME, STRATA</td>
<td>EVENTCODE</td>
</tr>
<tr>
<td>HomStats</td>
<td>Test statistics for k-sample tests</td>
<td>STRATA</td>
<td>Default</td>
</tr>
<tr>
<td>HomTests</td>
<td>Results of k-sample tests</td>
<td>STRATA</td>
<td>Default</td>
</tr>
<tr>
<td>Legend</td>
<td>Strata legend for two or more strata variables</td>
<td>STRATA</td>
<td></td>
</tr>
<tr>
<td>LifetableEstimates</td>
<td>Life-table survival estimates</td>
<td>PROC</td>
<td>METHOD=LT</td>
</tr>
<tr>
<td>LogForStepSeq</td>
<td>Forward stepwise sequence for the log-rank statistics for association</td>
<td>TEST</td>
<td>Default</td>
</tr>
<tr>
<td>LogrankHomCov</td>
<td>Covariance matrix for k-sample log-rank statistics</td>
<td>STRATA</td>
<td>TEST=LOGRANK</td>
</tr>
<tr>
<td>LogTestCov</td>
<td>Covariance matrix for log-rank statistics for association</td>
<td>TEST</td>
<td>Default</td>
</tr>
<tr>
<td>LogUniChisq</td>
<td>Univariate chi-squares for log-rank statistics for association</td>
<td>TEST</td>
<td>Default</td>
</tr>
<tr>
<td>Means</td>
<td>Mean and standard error of survival times</td>
<td>PROC</td>
<td>METHOD=PL</td>
</tr>
<tr>
<td>ModPetoHomCov</td>
<td>Covariance matrix for k-sample MODPETO statistics</td>
<td>STRATA</td>
<td>TEST=MODPETO</td>
</tr>
<tr>
<td>PetoHomCov</td>
<td>Covariance matrix for k-sample PETO statistics</td>
<td>STRATA</td>
<td>TEST=PETO</td>
</tr>
<tr>
<td>ProductLimitEstimates</td>
<td>Product-limit survival estimates</td>
<td>PROC</td>
<td>METHOD=PL</td>
</tr>
<tr>
<td>Quartiles</td>
<td>Quartiles of the survival times</td>
<td>PROC</td>
<td>METHOD=BRESLOW</td>
</tr>
<tr>
<td>RMST</td>
<td>Restricted mean survival time estimates</td>
<td>PROC</td>
<td>RMST</td>
</tr>
<tr>
<td>RMSTDiff</td>
<td>Adjustments for multiple comparisons</td>
<td>STRATA</td>
<td>ADJUST=</td>
</tr>
<tr>
<td>RMSTInfo</td>
<td>RMST analysis information</td>
<td>PROC</td>
<td>RMST</td>
</tr>
<tr>
<td>RMSTStratifiedTest</td>
<td>Results of stratified k-sample RMST test</td>
<td>PROC, STRATA</td>
<td>RMST, GROUP=</td>
</tr>
<tr>
<td>RMSTTest</td>
<td>Results of k-sample RMST test</td>
<td>PROC, STRATA</td>
<td>RMST</td>
</tr>
</tbody>
</table>
### Table 74.6 continued

<table>
<thead>
<tr>
<th>ODS Table Name</th>
<th>Description</th>
<th>Statement</th>
<th>Option</th>
</tr>
</thead>
<tbody>
<tr>
<td>RMTL</td>
<td>Restricted mean time lost estimates</td>
<td>PROC</td>
<td>RMTL</td>
</tr>
<tr>
<td>RMTLDiff</td>
<td>Adjustments for multiple comparisons</td>
<td>STRATA</td>
<td>ADJUST=</td>
</tr>
<tr>
<td>RMTLInfo</td>
<td>RMTL analysis information</td>
<td>PROC</td>
<td>RMTL</td>
</tr>
<tr>
<td>RMTLStratifiedTest</td>
<td>Results of stratified $k$-sample RMTL test</td>
<td>PROC, STRATA</td>
<td>RMTL, GROUP=</td>
</tr>
<tr>
<td>RMTLTest</td>
<td>Results of $k$-sample RMTL test</td>
<td>PROC, STRATA</td>
<td>RMTL</td>
</tr>
<tr>
<td>SimDetails</td>
<td>Details of quantile simulations</td>
<td>STRATA</td>
<td>ADJUST=SIMULATE(REPORT)</td>
</tr>
<tr>
<td>SimResults</td>
<td>Quantile simulation results</td>
<td>STRATA</td>
<td>ADJUST=SIMULATE(REPORT)</td>
</tr>
<tr>
<td>SurvDiff</td>
<td>Adjustments for multiple comparisons</td>
<td>STRATA</td>
<td>ADJUST=</td>
</tr>
<tr>
<td>TaroneHomCov</td>
<td>Covariance matrix for $k$-sample TARONE statistics</td>
<td>STRATA</td>
<td>TEST=TARONE</td>
</tr>
<tr>
<td>TrendScores</td>
<td>Scores used to construct trend tests</td>
<td>STRATA</td>
<td>TREND</td>
</tr>
<tr>
<td>TrendTests</td>
<td>Results of trend tests</td>
<td>STRATA</td>
<td>TREND</td>
</tr>
<tr>
<td>WilcoxonHomCov</td>
<td>Covariance matrix for $k$-sample WILCOXON statistics</td>
<td>STRATA</td>
<td>TEST=WILCOXON</td>
</tr>
<tr>
<td>WilForStepSeq</td>
<td>Forward stepwise sequence for the log-rank statistics for association</td>
<td>TEST</td>
<td>Default</td>
</tr>
<tr>
<td>WilTestCov</td>
<td>Covariance matrix for log-rank statistics for association</td>
<td>TEST</td>
<td>Default</td>
</tr>
<tr>
<td>WilUniChiSq</td>
<td>Univariate chi-squares for Wilcoxon statistics for association</td>
<td>TEST</td>
<td>Default</td>
</tr>
</tbody>
</table>

## ODS Graphics

Statistical procedures use ODS Graphics to create graphs as part of their output. ODS Graphics is described in detail in Chapter 21, “Statistical Graphics Using ODS.”

Before you create graphs, ODS Graphics must be enabled (for example, by specifying the ODS GRAPHICS ON statement). For more information about enabling and disabling ODS Graphics, see the section “Enabling and Disabling ODS Graphics” on page 623 in Chapter 21, “Statistical Graphics Using ODS.”

The overall appearance of graphs is controlled by ODS styles. Styles and other aspects of using ODS Graphics are discussed in the section “A Primer on ODS Statistical Graphics” on page 622 in Chapter 21, “Statistical Graphics Using ODS.”

The survival plot is produced by default; other graphs are produced by using the PLOTS= option in the PROC LIFETEST statement. You can reference every graph produced through ODS Graphics with a name.
The names of the graphs that PROC LIFETEST generates are listed in Table 74.7, along with the required keywords for the PLOTS= option.

### Table 74.7  Graphs Produced by PROC LIFETEST

<table>
<thead>
<tr>
<th>ODS Graph Name</th>
<th>Plot Description</th>
<th>PLOTS= Option</th>
</tr>
</thead>
<tbody>
<tr>
<td>cifPlot</td>
<td>Cumulative incidence function</td>
<td>CIF</td>
</tr>
<tr>
<td>cifPlot</td>
<td>Cumulative incidence function with pointwise confidence limits</td>
<td>CIF(CL)</td>
</tr>
<tr>
<td>cifPlot</td>
<td>Cumulative incidence function with Gray’s test</td>
<td>CIF(TEST)</td>
</tr>
<tr>
<td>DensityPlot</td>
<td>Density function for life-table method</td>
<td>PDF</td>
</tr>
<tr>
<td>FailurePlot</td>
<td>Cumulative distribution function</td>
<td>survival(FAILURE)</td>
</tr>
<tr>
<td>HazardPlot</td>
<td>Hazard function for life-table method or smoothed hazard for product-limit, Breslow, or Fleming-Harrington method</td>
<td>HAZARD</td>
</tr>
<tr>
<td>LogNegLogSurvivalPlot</td>
<td>Log(–log(survivor function))</td>
<td>LOGLOGS</td>
</tr>
<tr>
<td>NegLogSurvivalPlot</td>
<td>Log(survivor function)</td>
<td>LOGSURV</td>
</tr>
<tr>
<td>RMSTPlot</td>
<td>Restricted mean survival time curve</td>
<td>RMST</td>
</tr>
<tr>
<td>RMSTPlot</td>
<td>Restricted mean survival time curve with pointwise confidence limits</td>
<td>RMST(CL)</td>
</tr>
<tr>
<td>RMTLPlot</td>
<td>Restricted mean time lost curve</td>
<td>RMTL</td>
</tr>
<tr>
<td>RMTLPlot</td>
<td>Restricted mean time lost curve with pointwise confidence limits</td>
<td>RMTL(CL)</td>
</tr>
<tr>
<td>SurvivalPlot</td>
<td>Survivor function</td>
<td>SURVIVAL</td>
</tr>
<tr>
<td>SurvivalPlot</td>
<td>Survivor function with number of subjects at risk</td>
<td>SURVIVAL(ATRISK)</td>
</tr>
<tr>
<td>SurvivalPlot</td>
<td>Survivor function with pointwise confidence limits</td>
<td>SURVIVAL(CL)</td>
</tr>
<tr>
<td>SurvivalPlot</td>
<td>Survivor function with equal-precision band</td>
<td>SURVIVAL(CB=EP)</td>
</tr>
<tr>
<td>SurvivalPlot</td>
<td>Survivor function with Hall-Wellner band</td>
<td>SURVIVAL(CB=HW)</td>
</tr>
<tr>
<td>SurvivalPlot</td>
<td>Survivor function with homogeneity test</td>
<td>SURVIVAL(TEST)</td>
</tr>
</tbody>
</table>

### Additional Dynamic Variables for Survival Plots Using ODS Graphics

PROC LIFETEST passes a number of summary statistics as dynamic variables to the ODS Graphics for survival plots. Table 74.8 and Table 74.9 list these additional dynamic variables for the Kaplan-Meier curves and the life-table curves, respectively. These dynamic variables are not declared in the templates for the survival curves, but you can declare them and use them to enhance the default plots. The names of the dynamic variables depend on the STRATA= suboption of the PLOTS=SURVIVAL option: STRATA=INDIVIDUAL produces a separate plot for each stratum, and STRATA=OVERALL produces one plot with overlaid curves.
Table 74.8  Additional Dynamic Variables for

<table>
<thead>
<tr>
<th>STRATA=</th>
<th>Dynamic</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>OVERLAY</td>
<td>StrValj</td>
<td>Label for the jth stratum</td>
</tr>
<tr>
<td></td>
<td>NObsj</td>
<td>Number of observations in the jth stratum</td>
</tr>
<tr>
<td></td>
<td>NEventj</td>
<td>Number of events in the jth stratum</td>
</tr>
<tr>
<td></td>
<td>Medianj</td>
<td>Median survival time of the jth stratum</td>
</tr>
<tr>
<td></td>
<td>LowerMedianj</td>
<td>Lower median survival time of the jth stratum</td>
</tr>
<tr>
<td></td>
<td>UpperMedianj</td>
<td>Upper median survival time of the jth stratum</td>
</tr>
<tr>
<td></td>
<td>PctMedianConfid</td>
<td>Confidence of the median intervals in percent</td>
</tr>
<tr>
<td>INDIVIDUAL</td>
<td>NObs</td>
<td>Number of observations</td>
</tr>
<tr>
<td></td>
<td>NEvent</td>
<td>Number of events</td>
</tr>
<tr>
<td></td>
<td>Median</td>
<td>Median survival time</td>
</tr>
<tr>
<td></td>
<td>LowerMedian</td>
<td>Lower median survival time</td>
</tr>
<tr>
<td></td>
<td>UpperMedian</td>
<td>Upper median survival time</td>
</tr>
<tr>
<td></td>
<td>PctMedianConfid</td>
<td>Confidence of the median interval in percent</td>
</tr>
</tbody>
</table>

Table 74.9  Additional Dynamic Variables for

<table>
<thead>
<tr>
<th>STRATA=</th>
<th>Dynamic</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>OVERLAY</td>
<td>StrValj</td>
<td>Label for the jth stratum</td>
</tr>
<tr>
<td></td>
<td>NObsj</td>
<td>Number of observations in the jth stratum</td>
</tr>
<tr>
<td></td>
<td>NEventj</td>
<td>Number of events in the jth stratum</td>
</tr>
<tr>
<td>INDIVIDUAL</td>
<td>NObs</td>
<td>Number of observations</td>
</tr>
<tr>
<td></td>
<td>NEvent</td>
<td>Number of events</td>
</tr>
</tbody>
</table>

For information about all of the dynamic variables that are available for use in the ODS Graphics survival plot, see the section “Dynamic Variables” on page 936 in Chapter 23, “Customizing the Kaplan-Meier Survival Plot.” For the use of the particular dynamic variables shown in this section, see the sections “Adding a Small Inset Table with Event Information” on page 915 and “Adding an External Table with Event Information” on page 917 in Chapter 23, “Customizing the Kaplan-Meier Survival Plot.”

Modifying the Survival Plots

PROC LIFETEST, like other statistical procedures, provides a PLOTS= option and other options for modifying its graphical output without requiring template changes. Those options are sufficient for most purposes, and the following subsections of the section “Controlling the Survival Plot by Specifying Procedure Options” on page 873 in Chapter 23, “Customizing the Kaplan-Meier Survival Plot,” provide examples:

- “Enabling ODS Graphics and the Default Kaplan-Meier Plot” on page 873
- “Individual Survival Plots” on page 875
When those options are not sufficient, you can use a set of macros and macro variables to modify the graph templates. Using these macros and macro variables is easier than directly modifying the graph templates. The following subsections of the section “Controlling the Survival Plot by Modifying Graph Templates” on page 894 in Chapter 23, “Customizing the Kaplan-Meier Survival Plot,” provide examples:

- “Changing the Plot Title” on page 897
- “Modifying the Y Axis” on page 899
- “Changing the Line Thickness” on page 901
- “Changing the Group Color” on page 902
- “Changing the Line Pattern” on page 903
- “Changing the Font” on page 904
- “Changing the Legend and Inset Position” on page 906
- “Changing How the Censored Points Are Displayed” on page 907
- “Adding a Y-Axis Reference Line” on page 908
- “Changing the Homogeneity Test Inset” on page 910
- “Changing the Second Title and Adding a Footnote” on page 912
- “Adding a Small Inset Table with Event Information” on page 915
- “Adding an External Table with Event Information” on page 917
- “Suppressing the Legend” on page 919
- “Kaplan-Meier Plot with Event Table and Other Customizations” on page 920

Example 74.1: Product-Limit Estimates and Tests of Association

The data presented in Appendix I of Kalbfleisch and Prentice (1980) are coded in the following DATA step. The response variable, SurvTime, is the survival time in days of a lung cancer patient. Negative values of SurvTime are censored values. The covariates are Cell (type of cancer cell), Therapy (type of therapy: standard or test), Prior (prior therapy: 0=no, 10=yes), Age (age in years), DiagTime (time in months from diagnosis to entry into the trial), and Kps (performance status). A censoring indicator variable Censor is created from the data, with the value 1 indicating a censored time and the value 0 indicating an event time. Since there are only two types of therapy, an indicator variable, Treatment, is constructed for therapy type, with value 0 for standard therapy and value 1 for test therapy.
data VALung;
drop check m;
retain Therapy Cell;
infile cards column=column;
length Check $ 1;
label SurvTime='Failure or Censoring Time'
  Kps='Karnofsky Index'
  DiagTime='Months till Randomization'
  Age='Age in Years'
  Prior='Prior Treatment?'
  Cell='Cell Type'
  Therapy='Type of Treatment'
  Treatment='Treatment Indicator';
M=Column;
input Check $ @@;
if M>Column then M=1;
if Check='s' then input @M Therapy $ Cell $ ;
else input @M SurvTime Kps DiagTime Age Prior @@;
if SurvTime > .;
censor=(SurvTime<0);
SurvTime=abs(SurvTime);
Treatment=(Therapy='test');
datalines;
standard squamous
  72 60 7 69 0 411 70 5 64 10 228 60 3 38 0 126 60 9 63 10
  118 70 11 65 10 10 20 5 49 0 82 40 10 69 10 110 80 29 68 0
  314 50 18 43 0 -100 70 6 70 0 42 60 4 81 0 8 40 58 63 10
  144 30 4 63 0 -25 80 9 52 10 11 70 11 48 10
standard small
  30 60 3 61 0 384 60 9 42 0 4 40 2 35 0 54 80 4 63 10
  13 60 4 56 0 -123 40 3 55 0 -97 60 5 67 0 153 60 14 63 10
  59 30 2 65 0 117 80 3 46 0 16 30 4 53 10 151 50 12 69 0
  22 60 4 68 0 56 80 12 43 10 21 40 2 55 10 18 20 15 42 0
  139 80 2 64 0 20 30 5 65 0 31 75 3 65 0 52 70 2 55 0
  287 60 25 66 10 18 30 4 60 0 51 60 1 67 0 122 80 28 53 0
  27 60 8 62 0 54 70 1 67 0 7 50 7 72 0 63 50 11 48 0
  392 40 4 68 0 10 40 23 67 10
standard adeno
  8 20 19 61 10 92 70 10 60 0 35 40 6 62 0 117 80 2 38 0
  132 80 5 50 0 12 50 4 63 10 162 80 5 64 0 3 30 3 43 0
  95 80 4 34 0
standard large
  177 50 16 66 10 162 80 5 62 0 216 50 15 52 0 553 70 2 47 0
  278 60 12 63 0 12 40 12 68 10 260 80 5 45 0 200 80 12 41 10
  156 70 2 66 0 -182 90 2 62 0 143 90 8 60 0 105 80 11 66 0
  103 80 5 38 0 250 70 8 53 10 100 60 13 37 10
test squamous
  999 90 12 54 10 112 80 6 60 0 -87 80 3 48 0 -231 50 8 52 10
  242 50 1 70 0 991 70 7 50 10 111 70 3 62 0 1 20 21 65 10
  587 60 3 58 0 389 90 2 62 0 33 30 6 64 0 25 20 36 63 0
  357 70 13 58 0 467 90 2 64 0 201 80 28 52 10 1 50 7 35 0
  30 70 11 63 0 44 60 13 70 10 283 90 2 51 0 15 50 13 40 10
test small
In the following statements, PROC LIFETEST is invoked to compute the product-limit estimate of the survivor function for each type of cancer cell and to analyze the effects of the variables Age, Prior, DiagTime, Kps, and Treatment on the survival of the patients. These prognostic factors are specified in the TEST statement, and the variable Cell is specified in the STRATA statement. ODS Graphics must be enabled before producing graphs. Graphical displays of the product-limit estimates (S), the negative log estimates (LS), and the log of negative log estimates (LLS) are requested through the PLOTS= option in the PROC LIFETEST statement. Because of a few large survival times, a MAXTIME of 600 is used to set the scale of the time axis; that is, the time scale extends from 0 to a maximum of 600 days in the plots. The variable Therapy is specified in the ID statement to identify the type of therapy for each observation in the product-limit estimates. The OUTTEST option specifies the creation of an output data set named Test to contain the rank test matrices for the covariates.

ods graphics on;
proc lifetest data=VALung plots=(s,ls,lls) outtest=Test maxtime=600;
   time SurvTime*Censor(1);
   id Therapy;
   strata Cell;
   test Age Prior DiagTime Kps Treatment;
run;
ods graphics off;

Output 74.1.1 through Output 74.1.4 display the product-limit estimates of the survivor functions for the four cell types. Summary statistics of the survival times are also shown. The median survival times are 51 days, 156 days, 51 days, and 118 days for patients with adeno cells, large cells, small cells, and squamous cells, respectively.
Output 74.1.1 Estimation Results for Adeno Cells

The LIFETEST Procedure

Stratum 1: Cell Type = adeno

<table>
<thead>
<tr>
<th>SurvTime</th>
<th>Survival</th>
<th>Failure</th>
<th>Standard Error</th>
<th>Number Failed</th>
<th>Number Left</th>
<th>Therapy</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>1.0000</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>27</td>
<td></td>
</tr>
<tr>
<td>3.000</td>
<td>0.9630</td>
<td>0.0370</td>
<td>0.0363</td>
<td>1</td>
<td>26</td>
<td>standard</td>
</tr>
<tr>
<td>7.000</td>
<td>0.9259</td>
<td>0.0741</td>
<td>0.0504</td>
<td>2</td>
<td>25</td>
<td>test</td>
</tr>
<tr>
<td>8.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>3</td>
<td>24</td>
<td>standard</td>
</tr>
<tr>
<td>8.000</td>
<td>0.8519</td>
<td>0.1481</td>
<td>0.0684</td>
<td>4</td>
<td>23</td>
<td>test</td>
</tr>
<tr>
<td>12.000</td>
<td>0.8148</td>
<td>0.1852</td>
<td>0.0748</td>
<td>5</td>
<td>22</td>
<td>standard</td>
</tr>
<tr>
<td>18.000</td>
<td>0.7778</td>
<td>0.2222</td>
<td>0.0800</td>
<td>6</td>
<td>21</td>
<td>test</td>
</tr>
<tr>
<td>19.000</td>
<td>0.7407</td>
<td>0.2593</td>
<td>0.0843</td>
<td>7</td>
<td>20</td>
<td>test</td>
</tr>
<tr>
<td>24.000</td>
<td>0.7037</td>
<td>0.2963</td>
<td>0.0879</td>
<td>8</td>
<td>19</td>
<td>test</td>
</tr>
<tr>
<td>31.000</td>
<td>0.6667</td>
<td>0.3333</td>
<td>0.0907</td>
<td>9</td>
<td>18</td>
<td>test</td>
</tr>
<tr>
<td>35.000</td>
<td>0.6296</td>
<td>0.3704</td>
<td>0.0929</td>
<td>10</td>
<td>17</td>
<td>standard</td>
</tr>
<tr>
<td>36.000</td>
<td>0.5926</td>
<td>0.4074</td>
<td>0.0946</td>
<td>11</td>
<td>16</td>
<td>test</td>
</tr>
<tr>
<td>45.000</td>
<td>0.5556</td>
<td>0.4444</td>
<td>0.0956</td>
<td>12</td>
<td>15</td>
<td>test</td>
</tr>
<tr>
<td>48.000</td>
<td>0.5185</td>
<td>0.4815</td>
<td>0.0962</td>
<td>13</td>
<td>14</td>
<td>test</td>
</tr>
<tr>
<td>51.000</td>
<td>0.4815</td>
<td>0.5185</td>
<td>0.0962</td>
<td>14</td>
<td>13</td>
<td>test</td>
</tr>
<tr>
<td>52.000</td>
<td>0.4444</td>
<td>0.5556</td>
<td>0.0956</td>
<td>15</td>
<td>12</td>
<td>test</td>
</tr>
<tr>
<td>73.000</td>
<td>0.4074</td>
<td>0.5926</td>
<td>0.0946</td>
<td>16</td>
<td>11</td>
<td>test</td>
</tr>
<tr>
<td>80.000</td>
<td>0.3704</td>
<td>0.6296</td>
<td>0.0929</td>
<td>17</td>
<td>10</td>
<td>test</td>
</tr>
<tr>
<td>83.000</td>
<td>*</td>
<td>.</td>
<td>.</td>
<td>17</td>
<td>9</td>
<td>test</td>
</tr>
<tr>
<td>84.000</td>
<td>0.3292</td>
<td>0.6708</td>
<td>0.0913</td>
<td>18</td>
<td>8</td>
<td>test</td>
</tr>
<tr>
<td>90.000</td>
<td>0.2881</td>
<td>0.7119</td>
<td>0.0887</td>
<td>19</td>
<td>7</td>
<td>test</td>
</tr>
<tr>
<td>92.000</td>
<td>0.2469</td>
<td>0.7531</td>
<td>0.0850</td>
<td>20</td>
<td>6</td>
<td>standard</td>
</tr>
<tr>
<td>95.000</td>
<td>0.2058</td>
<td>0.7942</td>
<td>0.0802</td>
<td>21</td>
<td>5</td>
<td>standard</td>
</tr>
<tr>
<td>117.000</td>
<td>0.1646</td>
<td>0.8354</td>
<td>0.0740</td>
<td>22</td>
<td>4</td>
<td>standard</td>
</tr>
<tr>
<td>132.000</td>
<td>0.1235</td>
<td>0.8765</td>
<td>0.0659</td>
<td>23</td>
<td>3</td>
<td>standard</td>
</tr>
<tr>
<td>140.000</td>
<td>0.0823</td>
<td>0.9177</td>
<td>0.0553</td>
<td>24</td>
<td>2</td>
<td>test</td>
</tr>
<tr>
<td>162.000</td>
<td>0.0412</td>
<td>0.9588</td>
<td>0.0401</td>
<td>25</td>
<td>1</td>
<td>standard</td>
</tr>
<tr>
<td>186.000</td>
<td>0</td>
<td>1.0000</td>
<td></td>
<td>26</td>
<td>0</td>
<td>test</td>
</tr>
</tbody>
</table>

Note: The marked survival times are censored observations.
Output 74.1.2  Estimation Results for Large Cells

The LIFETEST Procedure

Stratum 2: Cell Type = large

<table>
<thead>
<tr>
<th>SurvTime</th>
<th>Survival</th>
<th>Failure</th>
<th>Standard Error</th>
<th>Number Failed</th>
<th>Number Left</th>
<th>Therapy</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>1.0000</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>27</td>
<td></td>
</tr>
<tr>
<td>12.000</td>
<td>0.9630</td>
<td>0.0370</td>
<td>0.0363</td>
<td>1</td>
<td>26</td>
<td>standard</td>
</tr>
<tr>
<td>15.000</td>
<td>0.9259</td>
<td>0.0741</td>
<td>0.0504</td>
<td>2</td>
<td>25</td>
<td>test</td>
</tr>
<tr>
<td>19.000</td>
<td>0.8889</td>
<td>0.1111</td>
<td>0.0605</td>
<td>3</td>
<td>24</td>
<td>test</td>
</tr>
<tr>
<td>43.000</td>
<td>0.8519</td>
<td>0.1481</td>
<td>0.0684</td>
<td>4</td>
<td>23</td>
<td>test</td>
</tr>
<tr>
<td>49.000</td>
<td>0.8148</td>
<td>0.1852</td>
<td>0.0748</td>
<td>5</td>
<td>22</td>
<td>test</td>
</tr>
<tr>
<td>52.000</td>
<td>0.7778</td>
<td>0.2222</td>
<td>0.0800</td>
<td>6</td>
<td>21</td>
<td>test</td>
</tr>
<tr>
<td>53.000</td>
<td>0.7407</td>
<td>0.2593</td>
<td>0.0843</td>
<td>7</td>
<td>20</td>
<td>test</td>
</tr>
<tr>
<td>100.000</td>
<td>0.7037</td>
<td>0.2963</td>
<td>0.0879</td>
<td>8</td>
<td>19</td>
<td>standard</td>
</tr>
<tr>
<td>103.000</td>
<td>0.6667</td>
<td>0.3333</td>
<td>0.0907</td>
<td>9</td>
<td>18</td>
<td>standard</td>
</tr>
<tr>
<td>105.000</td>
<td>0.6296</td>
<td>0.3704</td>
<td>0.0929</td>
<td>10</td>
<td>17</td>
<td>standard</td>
</tr>
<tr>
<td>111.000</td>
<td>0.5926</td>
<td>0.4074</td>
<td>0.0946</td>
<td>11</td>
<td>16</td>
<td>test</td>
</tr>
<tr>
<td>133.000</td>
<td>0.5556</td>
<td>0.4444</td>
<td>0.0956</td>
<td>12</td>
<td>15</td>
<td>test</td>
</tr>
<tr>
<td>143.000</td>
<td>0.5185</td>
<td>0.4815</td>
<td>0.0962</td>
<td>13</td>
<td>14</td>
<td>standard</td>
</tr>
<tr>
<td>156.000</td>
<td>0.4815</td>
<td>0.5185</td>
<td>0.0962</td>
<td>14</td>
<td>13</td>
<td>standard</td>
</tr>
<tr>
<td>162.000</td>
<td>0.4444</td>
<td>0.5556</td>
<td>0.0956</td>
<td>15</td>
<td>12</td>
<td>standard</td>
</tr>
<tr>
<td>164.000</td>
<td>0.4074</td>
<td>0.5926</td>
<td>0.0946</td>
<td>16</td>
<td>11</td>
<td>test</td>
</tr>
<tr>
<td>177.000</td>
<td>0.3704</td>
<td>0.6296</td>
<td>0.0929</td>
<td>17</td>
<td>10</td>
<td>standard</td>
</tr>
<tr>
<td>182.000</td>
<td>*</td>
<td>.</td>
<td>.</td>
<td>17</td>
<td>9</td>
<td>standard</td>
</tr>
<tr>
<td>200.000</td>
<td>0.3292</td>
<td>0.6708</td>
<td>0.0913</td>
<td>18</td>
<td>8</td>
<td>standard</td>
</tr>
<tr>
<td>216.000</td>
<td>0.2881</td>
<td>0.7119</td>
<td>0.0887</td>
<td>19</td>
<td>7</td>
<td>standard</td>
</tr>
<tr>
<td>231.000</td>
<td>0.2469</td>
<td>0.7531</td>
<td>0.0850</td>
<td>20</td>
<td>6</td>
<td>test</td>
</tr>
<tr>
<td>250.000</td>
<td>0.2058</td>
<td>0.7942</td>
<td>0.0802</td>
<td>21</td>
<td>5</td>
<td>standard</td>
</tr>
<tr>
<td>260.000</td>
<td>0.1646</td>
<td>0.8354</td>
<td>0.0740</td>
<td>22</td>
<td>4</td>
<td>standard</td>
</tr>
<tr>
<td>278.000</td>
<td>0.1235</td>
<td>0.8765</td>
<td>0.0659</td>
<td>23</td>
<td>3</td>
<td>standard</td>
</tr>
<tr>
<td>340.000</td>
<td>0.0823</td>
<td>0.9177</td>
<td>0.0553</td>
<td>24</td>
<td>2</td>
<td>test</td>
</tr>
<tr>
<td>378.000</td>
<td>0.0412</td>
<td>0.9588</td>
<td>0.0401</td>
<td>25</td>
<td>1</td>
<td>test</td>
</tr>
<tr>
<td>553.000</td>
<td>0</td>
<td>1.0000</td>
<td>.</td>
<td>26</td>
<td>0</td>
<td>standard</td>
</tr>
</tbody>
</table>

Note: The marked survival times are censored observations.
Output 74.1.3 Estimation Results for Small Cells

The LIFETEST Procedure

Stratum 3: Cell Type = small

<table>
<thead>
<tr>
<th>SurvTime</th>
<th>Survival</th>
<th>Failure</th>
<th>Standard Error</th>
<th>Number Failed</th>
<th>Number Left</th>
<th>Therapy</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>1.0000</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>48</td>
<td></td>
</tr>
<tr>
<td>2.000</td>
<td>0.9792</td>
<td>0.0208</td>
<td>0.0206</td>
<td>1</td>
<td>47</td>
<td>test</td>
</tr>
<tr>
<td>4.000</td>
<td>0.9583</td>
<td>0.0417</td>
<td>0.0288</td>
<td>2</td>
<td>46</td>
<td>standard</td>
</tr>
<tr>
<td>7.000</td>
<td>0.9167</td>
<td>0.0833</td>
<td>0.0399</td>
<td>4</td>
<td>44</td>
<td>test</td>
</tr>
<tr>
<td>8.000</td>
<td>0.8958</td>
<td>0.1042</td>
<td>0.0441</td>
<td>5</td>
<td>43</td>
<td>test</td>
</tr>
<tr>
<td>10.000</td>
<td>0.8750</td>
<td>0.1250</td>
<td>0.0477</td>
<td>6</td>
<td>42</td>
<td>standard</td>
</tr>
<tr>
<td>13.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>7</td>
<td>41</td>
<td>standard</td>
</tr>
<tr>
<td>16.000</td>
<td>0.8125</td>
<td>0.1875</td>
<td>0.0563</td>
<td>9</td>
<td>39</td>
<td>standard</td>
</tr>
<tr>
<td>18.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>10</td>
<td>38</td>
<td>standard</td>
</tr>
<tr>
<td>18.000</td>
<td>0.7708</td>
<td>0.2292</td>
<td>0.0607</td>
<td>11</td>
<td>37</td>
<td>standard</td>
</tr>
<tr>
<td>20.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>12</td>
<td>36</td>
<td>standard</td>
</tr>
<tr>
<td>20.000</td>
<td>0.7292</td>
<td>0.2708</td>
<td>0.0641</td>
<td>13</td>
<td>35</td>
<td>test</td>
</tr>
<tr>
<td>21.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>14</td>
<td>34</td>
<td>standard</td>
</tr>
<tr>
<td>21.000</td>
<td>0.6875</td>
<td>0.3125</td>
<td>0.0669</td>
<td>15</td>
<td>33</td>
<td>test</td>
</tr>
<tr>
<td>22.000</td>
<td>0.6667</td>
<td>0.3333</td>
<td>0.0680</td>
<td>16</td>
<td>32</td>
<td>standard</td>
</tr>
<tr>
<td>24.000</td>
<td>0.6458</td>
<td>0.3542</td>
<td>0.0690</td>
<td>17</td>
<td>31</td>
<td>test</td>
</tr>
<tr>
<td>25.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>18</td>
<td>30</td>
<td>test</td>
</tr>
<tr>
<td>25.000</td>
<td>0.6042</td>
<td>0.3958</td>
<td>0.0706</td>
<td>19</td>
<td>29</td>
<td>test</td>
</tr>
<tr>
<td>27.000</td>
<td>0.5833</td>
<td>0.4167</td>
<td>0.0712</td>
<td>20</td>
<td>28</td>
<td>standard</td>
</tr>
<tr>
<td>29.000</td>
<td>0.5625</td>
<td>0.4375</td>
<td>0.0716</td>
<td>21</td>
<td>27</td>
<td>test</td>
</tr>
<tr>
<td>30.000</td>
<td>0.5417</td>
<td>0.4583</td>
<td>0.0719</td>
<td>22</td>
<td>26</td>
<td>standard</td>
</tr>
<tr>
<td>31.000</td>
<td>0.5208</td>
<td>0.4792</td>
<td>0.0721</td>
<td>23</td>
<td>25</td>
<td>standard</td>
</tr>
<tr>
<td>51.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>24</td>
<td>24</td>
<td>standard</td>
</tr>
<tr>
<td>51.000</td>
<td>0.4792</td>
<td>0.5208</td>
<td>0.0721</td>
<td>25</td>
<td>23</td>
<td>test</td>
</tr>
<tr>
<td>52.000</td>
<td>0.4583</td>
<td>0.5417</td>
<td>0.0719</td>
<td>26</td>
<td>22</td>
<td>standard</td>
</tr>
<tr>
<td>54.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>27</td>
<td>21</td>
<td>standard</td>
</tr>
<tr>
<td>54.000</td>
<td>0.4167</td>
<td>0.5833</td>
<td>0.0712</td>
<td>28</td>
<td>20</td>
<td>standard</td>
</tr>
<tr>
<td>56.000</td>
<td>0.3958</td>
<td>0.6042</td>
<td>0.0706</td>
<td>29</td>
<td>19</td>
<td>standard</td>
</tr>
<tr>
<td>59.000</td>
<td>0.3750</td>
<td>0.6250</td>
<td>0.0712</td>
<td>30</td>
<td>18</td>
<td>standard</td>
</tr>
<tr>
<td>61.000</td>
<td>0.3542</td>
<td>0.6458</td>
<td>0.0690</td>
<td>31</td>
<td>17</td>
<td>test</td>
</tr>
<tr>
<td>63.000</td>
<td>0.3333</td>
<td>0.6667</td>
<td>0.0680</td>
<td>32</td>
<td>16</td>
<td>standard</td>
</tr>
<tr>
<td>80.000</td>
<td>0.3125</td>
<td>0.6875</td>
<td>0.0669</td>
<td>33</td>
<td>15</td>
<td>test</td>
</tr>
<tr>
<td>87.000</td>
<td>0.2917</td>
<td>0.7083</td>
<td>0.0656</td>
<td>34</td>
<td>14</td>
<td>test</td>
</tr>
<tr>
<td>95.000</td>
<td>0.2708</td>
<td>0.7292</td>
<td>0.0641</td>
<td>35</td>
<td>13</td>
<td>test</td>
</tr>
<tr>
<td>97.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>35</td>
<td>12</td>
<td>standard</td>
</tr>
<tr>
<td>99.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>36</td>
<td>11</td>
<td>test</td>
</tr>
<tr>
<td>99.000</td>
<td>0.2257</td>
<td>0.7743</td>
<td>0.0609</td>
<td>37</td>
<td>10</td>
<td>test</td>
</tr>
<tr>
<td>103.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>37</td>
<td>9</td>
<td>test</td>
</tr>
<tr>
<td>117.000</td>
<td>0.2006</td>
<td>0.7994</td>
<td>0.0591</td>
<td>38</td>
<td>8</td>
<td>standard</td>
</tr>
<tr>
<td>122.000</td>
<td>0.1755</td>
<td>0.8245</td>
<td>0.0567</td>
<td>39</td>
<td>7</td>
<td>standard</td>
</tr>
<tr>
<td>123.000</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>39</td>
<td>6</td>
<td>standard</td>
</tr>
</tbody>
</table>
Output 74.1.3  continued

The LIFETEST Procedure

Stratum 3: Cell Type = small

<table>
<thead>
<tr>
<th>SurvTime</th>
<th>Survival</th>
<th>Failure</th>
<th>Standard Error</th>
<th>Number Failed</th>
<th>Number Left</th>
<th>Therapy</th>
</tr>
</thead>
<tbody>
<tr>
<td>139.000</td>
<td>0.1463</td>
<td>0.8537</td>
<td>0.0543</td>
<td>40</td>
<td>5</td>
<td>standard</td>
</tr>
<tr>
<td>151.000</td>
<td>0.1170</td>
<td>0.8830</td>
<td>0.0507</td>
<td>41</td>
<td>4</td>
<td>standard</td>
</tr>
<tr>
<td>153.000</td>
<td>0.0878</td>
<td>0.9122</td>
<td>0.0457</td>
<td>42</td>
<td>3</td>
<td>standard</td>
</tr>
<tr>
<td>287.000</td>
<td>0.0585</td>
<td>0.9415</td>
<td>0.0387</td>
<td>43</td>
<td>2</td>
<td>standard</td>
</tr>
<tr>
<td>384.000</td>
<td>0.0293</td>
<td>0.9707</td>
<td>0.0283</td>
<td>44</td>
<td>1</td>
<td>standard</td>
</tr>
<tr>
<td>392.000</td>
<td>0</td>
<td>1.0000</td>
<td>.</td>
<td>45</td>
<td>0</td>
<td>standard</td>
</tr>
</tbody>
</table>

Note: The marked survival times are censored observations.
### Output 74.1.4  Estimation Results for Squamous Cells

#### The LIFETEST Procedure

**Stratum 4: Cell Type = squamous**

<table>
<thead>
<tr>
<th>SurvTime</th>
<th>Survival</th>
<th>Failure</th>
<th>Standard Error</th>
<th>Number Failed</th>
<th>Number Left</th>
<th>Therapy</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>1.0000</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>35</td>
<td></td>
</tr>
<tr>
<td>1.000</td>
<td></td>
<td></td>
<td>0.0392</td>
<td>2</td>
<td>34</td>
<td>test</td>
</tr>
<tr>
<td>8.000</td>
<td>0.9429</td>
<td>0.0571</td>
<td>0.0473</td>
<td>3</td>
<td>32</td>
<td>standard</td>
</tr>
<tr>
<td>10.000</td>
<td>0.8857</td>
<td>0.1143</td>
<td>0.0538</td>
<td>4</td>
<td>31</td>
<td>standard</td>
</tr>
<tr>
<td>11.000</td>
<td>0.8571</td>
<td>0.1429</td>
<td>0.0591</td>
<td>5</td>
<td>30</td>
<td>standard</td>
</tr>
<tr>
<td>15.000</td>
<td>0.8286</td>
<td>0.1714</td>
<td>0.0637</td>
<td>6</td>
<td>29</td>
<td>test</td>
</tr>
<tr>
<td>25.000</td>
<td>0.8000</td>
<td>0.2000</td>
<td>0.0676</td>
<td>7</td>
<td>28</td>
<td>test</td>
</tr>
<tr>
<td>25.000 *</td>
<td></td>
<td></td>
<td></td>
<td>7</td>
<td>27</td>
<td>standard</td>
</tr>
<tr>
<td>30.000</td>
<td>0.7704</td>
<td>0.2296</td>
<td>0.0713</td>
<td>8</td>
<td>26</td>
<td>test</td>
</tr>
<tr>
<td>33.000</td>
<td>0.7407</td>
<td>0.2593</td>
<td>0.0745</td>
<td>9</td>
<td>25</td>
<td>test</td>
</tr>
<tr>
<td>42.000</td>
<td>0.7111</td>
<td>0.2889</td>
<td>0.0772</td>
<td>10</td>
<td>24</td>
<td>standard</td>
</tr>
<tr>
<td>44.000</td>
<td>0.6815</td>
<td>0.3185</td>
<td>0.0794</td>
<td>11</td>
<td>23</td>
<td>test</td>
</tr>
<tr>
<td>72.000</td>
<td>0.6519</td>
<td>0.3481</td>
<td>0.0813</td>
<td>12</td>
<td>22</td>
<td>standard</td>
</tr>
<tr>
<td>82.000</td>
<td>0.6222</td>
<td>0.3778</td>
<td>0.0828</td>
<td>13</td>
<td>21</td>
<td>standard</td>
</tr>
<tr>
<td>87.000 *</td>
<td></td>
<td></td>
<td></td>
<td>13</td>
<td>20</td>
<td>test</td>
</tr>
<tr>
<td>100.000 *</td>
<td></td>
<td></td>
<td></td>
<td>13</td>
<td>19</td>
<td>standard</td>
</tr>
<tr>
<td>110.000</td>
<td>0.5895</td>
<td>0.4105</td>
<td>0.0847</td>
<td>14</td>
<td>18</td>
<td>standard</td>
</tr>
<tr>
<td>111.000</td>
<td>0.5567</td>
<td>0.4433</td>
<td>0.0861</td>
<td>15</td>
<td>17</td>
<td>test</td>
</tr>
<tr>
<td>112.000</td>
<td>0.5240</td>
<td>0.4760</td>
<td>0.0870</td>
<td>16</td>
<td>16</td>
<td>test</td>
</tr>
<tr>
<td>118.000</td>
<td>0.4912</td>
<td>0.5088</td>
<td>0.0875</td>
<td>17</td>
<td>15</td>
<td>standard</td>
</tr>
<tr>
<td>126.000</td>
<td>0.4585</td>
<td>0.5415</td>
<td>0.0876</td>
<td>18</td>
<td>14</td>
<td>standard</td>
</tr>
<tr>
<td>144.000</td>
<td>0.4257</td>
<td>0.5743</td>
<td>0.0873</td>
<td>19</td>
<td>13</td>
<td>standard</td>
</tr>
<tr>
<td>201.000</td>
<td>0.3930</td>
<td>0.6070</td>
<td>0.0865</td>
<td>20</td>
<td>12</td>
<td>test</td>
</tr>
<tr>
<td>228.000</td>
<td>0.3602</td>
<td>0.6398</td>
<td>0.0852</td>
<td>21</td>
<td>11</td>
<td>standard</td>
</tr>
<tr>
<td>231.000 *</td>
<td></td>
<td></td>
<td></td>
<td>21</td>
<td>10</td>
<td>test</td>
</tr>
<tr>
<td>242.000</td>
<td>0.3242</td>
<td>0.6758</td>
<td>0.0840</td>
<td>22</td>
<td>9</td>
<td>test</td>
</tr>
<tr>
<td>283.000</td>
<td>0.2882</td>
<td>0.7118</td>
<td>0.0820</td>
<td>23</td>
<td>8</td>
<td>test</td>
</tr>
<tr>
<td>314.000</td>
<td>0.2522</td>
<td>0.7478</td>
<td>0.0793</td>
<td>24</td>
<td>7</td>
<td>standard</td>
</tr>
<tr>
<td>357.000</td>
<td>0.2161</td>
<td>0.7839</td>
<td>0.0757</td>
<td>25</td>
<td>6</td>
<td>test</td>
</tr>
<tr>
<td>389.000</td>
<td>0.1801</td>
<td>0.8199</td>
<td>0.0711</td>
<td>26</td>
<td>5</td>
<td>test</td>
</tr>
<tr>
<td>411.000</td>
<td>0.1441</td>
<td>0.8559</td>
<td>0.0654</td>
<td>27</td>
<td>4</td>
<td>standard</td>
</tr>
<tr>
<td>467.000</td>
<td>0.1081</td>
<td>0.8919</td>
<td>0.0581</td>
<td>28</td>
<td>3</td>
<td>test</td>
</tr>
<tr>
<td>587.000</td>
<td>0.0720</td>
<td>0.9280</td>
<td>0.0487</td>
<td>29</td>
<td>2</td>
<td>test</td>
</tr>
<tr>
<td>991.000</td>
<td>0.0360</td>
<td>0.9640</td>
<td>0.0352</td>
<td>30</td>
<td>1</td>
<td>test</td>
</tr>
<tr>
<td>999.000</td>
<td>0</td>
<td>1.0000</td>
<td>0</td>
<td>31</td>
<td>0</td>
<td>test</td>
</tr>
</tbody>
</table>

**Note:** The marked survival times are censored observations.
The distribution of event and censored observations among the four cell types is summarized in Output 74.1.5.

Output 74.1.5  Summary of Censored and Uncensored Values

<table>
<thead>
<tr>
<th>Stratum</th>
<th>Cell</th>
<th>Total</th>
<th>Failed</th>
<th>Censored</th>
<th>Percent Censored</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>adeno</td>
<td>27</td>
<td>26</td>
<td>1</td>
<td>3.70</td>
</tr>
<tr>
<td>2</td>
<td>large</td>
<td>27</td>
<td>26</td>
<td>1</td>
<td>3.70</td>
</tr>
<tr>
<td>3</td>
<td>small</td>
<td>48</td>
<td>45</td>
<td>3</td>
<td>6.25</td>
</tr>
<tr>
<td>4</td>
<td>squamous</td>
<td>35</td>
<td>31</td>
<td>4</td>
<td>11.43</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>137</td>
<td>128</td>
<td>9</td>
<td>6.57</td>
</tr>
</tbody>
</table>

The graph of the estimated survivor functions is shown in Output 74.1.6. The adeno cell curve and the small cell curve are much closer to each other than they are to the large cell curve or the squamous cell curve. The survival rates of the adeno cell patients and the small cell patients decrease rapidly to approximately 29% in 90 days. Shapes of the large cell curve and the squamous cell curve are quite different, although both decrease less rapidly than those of the adeno and small cells. The squamous cell curve decreases more rapidly initially than the large cell curve, but the role is reversed in the later period.

Output 74.1.6  Graph of the Estimated Survivor Functions
The graph of the negative log of the estimated survivor functions is displayed in Output 74.1.7. Output 74.1.8 displays the log of the negative log of the estimated survivor functions against the log of time.

Output 74.1.7  Graph of Negative Log of the Estimated Survivor Functions
Results of the homogeneity tests across cell types are given in Output 74.1.9. The log-rank and Wilcoxon statistics and their corresponding covariance matrices are displayed. Also given is a table that consists of the approximate chi-square statistics, degrees of freedom, and $p$-values for the log-rank, Wilcoxon, and likelihood ratio tests. All three tests indicate strong evidence of a significant difference among the survival curves for the four types of cancer cells ($p < 0.0001$).

### Output 74.1.9 Homogeneity Tests across Cell Types

<table>
<thead>
<tr>
<th>Cell</th>
<th>Log-Rank</th>
<th>Wilcoxon</th>
</tr>
</thead>
<tbody>
<tr>
<td>adeno</td>
<td>10.306</td>
<td>697.0</td>
</tr>
<tr>
<td>large</td>
<td>-8.549</td>
<td>-1085.0</td>
</tr>
<tr>
<td>small</td>
<td>14.898</td>
<td>1278.0</td>
</tr>
<tr>
<td>squamous</td>
<td>-16.655</td>
<td>-890.0</td>
</tr>
</tbody>
</table>
### Output 74.1.9 continued

<table>
<thead>
<tr>
<th>Covariance Matrix for the Log-Rank Statistics</th>
<th>Cell</th>
<th>adeno</th>
<th>large</th>
<th>small</th>
<th>squamous</th>
</tr>
</thead>
<tbody>
<tr>
<td>adeno</td>
<td>12.9662</td>
<td>-4.0701</td>
<td>-4.4087</td>
<td>-4.4873</td>
<td></td>
</tr>
<tr>
<td>large</td>
<td>-4.0701</td>
<td>24.1990</td>
<td>-7.8117</td>
<td>-12.3172</td>
<td></td>
</tr>
<tr>
<td>small</td>
<td>-4.4087</td>
<td>-7.8117</td>
<td>21.7543</td>
<td>-9.5339</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Covariance Matrix for the Wilcoxon Statistics</th>
<th>Cell</th>
<th>adeno</th>
<th>large</th>
<th>small</th>
<th>squamous</th>
</tr>
</thead>
<tbody>
<tr>
<td>adeno</td>
<td>121188</td>
<td>-34718</td>
<td>-46639</td>
<td>-39831</td>
<td></td>
</tr>
<tr>
<td>large</td>
<td>-34718</td>
<td>151241</td>
<td>-59948</td>
<td>-56576</td>
<td></td>
</tr>
<tr>
<td>small</td>
<td>-46639</td>
<td>-59948</td>
<td>175590</td>
<td>-69002</td>
<td></td>
</tr>
<tr>
<td>squamous</td>
<td>-39831</td>
<td>-56576</td>
<td>-69002</td>
<td>165410</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Test of Equality over Strata</th>
<th>Test</th>
<th>Chi-Square</th>
<th>DF</th>
<th>Pr &gt; Chi-Square</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log-Rank</td>
<td>25.4037</td>
<td>3</td>
<td>&lt;.0001</td>
<td></td>
</tr>
<tr>
<td>Wilcoxon</td>
<td>19.4331</td>
<td>3</td>
<td>0.0002</td>
<td></td>
</tr>
<tr>
<td>-2Log(LR)</td>
<td>33.9343</td>
<td>3</td>
<td>&lt;.0001</td>
<td></td>
</tr>
</tbody>
</table>

Results of the log-rank test of the prognostic variables are shown in Output 74.1.10. The univariate test results correspond to testing each prognostic factor marginally. The joint covariance matrix of these univariate test statistics is also displayed. In computing the overall chi-square statistic, the partial chi-square statistics following a forward stepwise entry approach are tabulated.

Consider the log-rank test in Output 74.1.10. Since the univariate test for Kps has the largest chi-square (43.4747) among all the covariates, Kps is entered first. At this stage, the partial chi-square and the chi-square increment for Kps are the same as the univariate chi-square. Among all the covariates not in the model (Age, Prior, DiagTime, Treatment), Treatment has the largest approximate chi-square increment (1.7261) and is entered next. The approximate chi-square for the model that contains Kps and Treatment is 43.4747+1.7261=45.2008 with 2 degrees of freedom. The third covariate entered is Age. The fourth is Prior, and the fifth is DiagTime. The overall chi-square statistic in the last line of the output is the partial chi-square for including all the covariates. It has a value of 46.4200 with 5 degrees of freedom, which is highly significant ($p < 0.0001$).

### Output 74.1.10 Log-Rank Test of the Prognostic Factors

<table>
<thead>
<tr>
<th>Variable</th>
<th>Univariate Chi-Squares for the Log-Rank Test</th>
<th>Pr &gt; Chi-Square</th>
<th>Label</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Test</strong></td>
<td><strong>Standard Error</strong></td>
<td><strong>Chi-Square</strong></td>
<td><strong>Label</strong></td>
</tr>
<tr>
<td>Age</td>
<td>-40.7383</td>
<td>105.7</td>
<td>0.1485</td>
</tr>
<tr>
<td>Prior</td>
<td>-19.9435</td>
<td>46.9836</td>
<td>0.1802</td>
</tr>
<tr>
<td>DiagTime</td>
<td>-115.9</td>
<td>97.8708</td>
<td>1.4013</td>
</tr>
<tr>
<td>Kps</td>
<td>1123.1</td>
<td>170.3</td>
<td>43.4747</td>
</tr>
<tr>
<td>Treatment</td>
<td>-4.2076</td>
<td>5.0407</td>
<td>0.6967</td>
</tr>
</tbody>
</table>
Output 74.1.10 continued

<table>
<thead>
<tr>
<th>Variable</th>
<th>Age</th>
<th>Prior</th>
<th>DiagTime</th>
<th>Kps</th>
<th>Treatment</th>
</tr>
</thead>
<tbody>
<tr>
<td>Age</td>
<td>11175.4</td>
<td>-301.2</td>
<td>-892.2</td>
<td>-2948.4</td>
<td>119.3</td>
</tr>
<tr>
<td>Prior</td>
<td>-301.2</td>
<td>2207.5</td>
<td>2010.9</td>
<td>78.6</td>
<td>13.9</td>
</tr>
<tr>
<td>DiagTime</td>
<td>-892.2</td>
<td>2010.9</td>
<td>9578.7</td>
<td>-2295.3</td>
<td>21.9</td>
</tr>
<tr>
<td>Kps</td>
<td>-2948.4</td>
<td>78.6</td>
<td>-2295.3</td>
<td>29015.6</td>
<td>61.9</td>
</tr>
<tr>
<td>Treatment</td>
<td>119.3</td>
<td>13.9</td>
<td>21.9</td>
<td>61.9</td>
<td>25.4</td>
</tr>
</tbody>
</table>

Forward Stepwise Sequence of Chi-Squares for the Log-Rank Test

<table>
<thead>
<tr>
<th>Variable</th>
<th>DF</th>
<th>Chi-Square</th>
<th>Pr &gt; Chi-Square</th>
<th>Chi-Square Increment</th>
<th>Pr &gt; Increment</th>
<th>Label</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kps</td>
<td>1</td>
<td>43.4747</td>
<td>&lt;.0001</td>
<td>43.4747</td>
<td>&lt;.0001</td>
<td>Karnofsky Index</td>
</tr>
<tr>
<td>Treatment</td>
<td>2</td>
<td>45.2008</td>
<td>&lt;.0001</td>
<td>1.7261</td>
<td>0.1889</td>
<td>Treatment Indicator</td>
</tr>
<tr>
<td>Age</td>
<td>3</td>
<td>46.3012</td>
<td>&lt;.0001</td>
<td>1.1004</td>
<td>0.2942</td>
<td>Age in Years</td>
</tr>
<tr>
<td>Prior</td>
<td>4</td>
<td>46.4134</td>
<td>&lt;.0001</td>
<td>0.1122</td>
<td>0.7377</td>
<td>Prior Treatment?</td>
</tr>
<tr>
<td>DiagTime</td>
<td>5</td>
<td>46.4200</td>
<td>&lt;.0001</td>
<td>0.00665</td>
<td>0.9350</td>
<td>Months till Randomization</td>
</tr>
</tbody>
</table>

You can establish this forward stepwise entry of prognostic factors by passing the matrix corresponding to the log-rank test to the RSQUARE method in the REG procedure, as follows. PROC REG finds the sets of variables that yield the largest chi-square statistics.

```sas
data RSq;
   set Test;
   if _type_='LOG RANK';
   _type_='cov';
run;
proc print data=RSq;
run;
proc reg data=RSq(type=COV);
   model SurvTime=Age Prior DiagTime Kps Treatment
       / selection=rsquare;
   title 'All Possible Subsets of Covariates for the log-rank Test';
run;
```

Output 74.1.11 displays the univariate statistics and their covariance matrix for the log-rank test.

Output 74.1.11 Log-Rank Statistics and Covariance Matrix

<table>
<thead>
<tr>
<th>Obs</th>
<th><em>TYPE</em></th>
<th><em>NAME</em></th>
<th>SurvTime</th>
<th>Age</th>
<th>Prior</th>
<th>DiagTime</th>
<th>Kps</th>
<th>Treatment</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>cov</td>
<td>SurvTime</td>
<td>46.42</td>
<td>-40.74</td>
<td>-19.94</td>
<td>-115.86</td>
<td>1123.14</td>
<td>-4.208</td>
</tr>
<tr>
<td>2</td>
<td>cov</td>
<td>Age</td>
<td>-40.74</td>
<td>11775.44</td>
<td>-301.23</td>
<td>-892.24</td>
<td>-2948.45</td>
<td>119.297</td>
</tr>
<tr>
<td>3</td>
<td>cov</td>
<td>Prior</td>
<td>-19.94</td>
<td>-301.23</td>
<td>2207.46</td>
<td>2010.85</td>
<td>78.64</td>
<td>13.875</td>
</tr>
<tr>
<td>5</td>
<td>cov</td>
<td>Kps</td>
<td>1123.14</td>
<td>-2948.45</td>
<td>78.64</td>
<td>-2295.32</td>
<td>29015.62</td>
<td>61.945</td>
</tr>
<tr>
<td>6</td>
<td>cov</td>
<td>Treatment</td>
<td>-4.21</td>
<td>119.30</td>
<td>13.87</td>
<td>21.86</td>
<td>61.95</td>
<td>25.409</td>
</tr>
</tbody>
</table>
Results of the best subset regression are shown in Output 74.1.12. The variable Kps generates the largest univariate test statistic among all the covariates, the pair Kps and Age generate the largest test statistic among any other pairs of covariates, and so on. The entry order of covariates is identical to that of PROC LIFETEST.

**Output 74.1.12** Best Subset Regression from the REG Procedure

**All Possible Subsets of Covariates for the log-rank Test**

<table>
<thead>
<tr>
<th>Number in Model</th>
<th>R-Square</th>
<th>Variables in Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.9366</td>
<td>Kps</td>
</tr>
<tr>
<td>1</td>
<td>0.0302</td>
<td>DiagTime</td>
</tr>
<tr>
<td>1</td>
<td>0.0150</td>
<td>Treatment</td>
</tr>
<tr>
<td>1</td>
<td>0.0039</td>
<td>Prior</td>
</tr>
<tr>
<td>1</td>
<td>0.0032</td>
<td>Age</td>
</tr>
<tr>
<td>2</td>
<td>0.9737</td>
<td>Kps Treatment</td>
</tr>
<tr>
<td>2</td>
<td>0.9472</td>
<td>Age Kps</td>
</tr>
<tr>
<td>2</td>
<td>0.9417</td>
<td>Prior Kps</td>
</tr>
<tr>
<td>2</td>
<td>0.9382</td>
<td>DiagTime Kps</td>
</tr>
<tr>
<td>2</td>
<td>0.0434</td>
<td>DiagTime Treatment</td>
</tr>
<tr>
<td>2</td>
<td>0.0353</td>
<td>Age DiagTime</td>
</tr>
<tr>
<td>2</td>
<td>0.0304</td>
<td>Prior DiagTime</td>
</tr>
<tr>
<td>2</td>
<td>0.0181</td>
<td>Prior Treatment</td>
</tr>
<tr>
<td>2</td>
<td>0.0159</td>
<td>Age Treatment</td>
</tr>
<tr>
<td>2</td>
<td>0.0075</td>
<td>Age Prior</td>
</tr>
<tr>
<td>3</td>
<td>0.9974</td>
<td>Age Kps Treatment</td>
</tr>
<tr>
<td>3</td>
<td>0.9774</td>
<td>Prior Kps Treatment</td>
</tr>
<tr>
<td>3</td>
<td>0.9747</td>
<td>DiagTime Kps Treatment</td>
</tr>
<tr>
<td>3</td>
<td>0.9515</td>
<td>Age Prior Kps</td>
</tr>
<tr>
<td>3</td>
<td>0.9481</td>
<td>Age DiagTime Kps</td>
</tr>
<tr>
<td>3</td>
<td>0.9418</td>
<td>Prior DiagTime Kps</td>
</tr>
<tr>
<td>3</td>
<td>0.0456</td>
<td>Age DiagTime Treatment</td>
</tr>
<tr>
<td>3</td>
<td>0.0438</td>
<td>Prior DiagTime Treatment</td>
</tr>
<tr>
<td>3</td>
<td>0.0355</td>
<td>Age Prior DiagTime</td>
</tr>
<tr>
<td>3</td>
<td>0.0192</td>
<td>Age Prior Treatment</td>
</tr>
<tr>
<td>4</td>
<td>0.9999</td>
<td>Age Prior Kps Treatment</td>
</tr>
<tr>
<td>4</td>
<td>0.9976</td>
<td>Age DiagTime Kps Treatment</td>
</tr>
<tr>
<td>4</td>
<td>0.9774</td>
<td>Prior DiagTime Kps Treatment</td>
</tr>
<tr>
<td>4</td>
<td>0.9515</td>
<td>Age Prior DiagTime Kps</td>
</tr>
<tr>
<td>4</td>
<td>0.0459</td>
<td>Age Prior DiagTime Treatment</td>
</tr>
<tr>
<td>5</td>
<td>1.0000</td>
<td>Age Prior DiagTime Kps</td>
</tr>
</tbody>
</table>
Example 74.2: Enhanced Survival Plot and Multiple-Comparison Adjustments

This example highlights a number of features in the survival plot that uses ODS Graphics. Also shown in this example are comparisons of survival curves based on multiple comparison adjustments. Data of 137 bone marrow transplant patients extracted from Klein and Moeschberger (1997) have been saved in the data set BMT in the Sashelp library. At the time of transplant, each patient is classified into one of three risk categories: ALL (acute lymphoblastic leukemia), AML (acute myelocytic leukemia)-Low Risk, and AML-High Risk. The endpoint of interest is the disease-free survival time, which is the time to death or relapse or to the end of the study in days. In this data set, the variable Group represents the patient’s risk category, the variable T represents the disease-free survival time, and the variable Status is the censoring indicator, with the value 1 indicating an event time and the value 0 a censored time.

The following step displays the first 10 observations of the BMT data set in Output 74.2.1. The data set is available in the Sashelp library.

```
proc print data=Sashelp.BMT(obs=10);
run;
```

**Output 74.2.1** A Subset of the Bone Marrow Transplant Data

<table>
<thead>
<tr>
<th>Obs</th>
<th>Group</th>
<th>T</th>
<th>Status</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>ALL</td>
<td>2081</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>ALL</td>
<td>1602</td>
<td>0</td>
</tr>
<tr>
<td>3</td>
<td>ALL</td>
<td>1496</td>
<td>0</td>
</tr>
<tr>
<td>4</td>
<td>ALL</td>
<td>1462</td>
<td>0</td>
</tr>
<tr>
<td>5</td>
<td>ALL</td>
<td>1433</td>
<td>0</td>
</tr>
<tr>
<td>6</td>
<td>ALL</td>
<td>1377</td>
<td>0</td>
</tr>
<tr>
<td>7</td>
<td>ALL</td>
<td>1330</td>
<td>0</td>
</tr>
<tr>
<td>8</td>
<td>ALL</td>
<td>996</td>
<td>0</td>
</tr>
<tr>
<td>9</td>
<td>ALL</td>
<td>226</td>
<td>0</td>
</tr>
<tr>
<td>10</td>
<td>ALL</td>
<td>1199</td>
<td>0</td>
</tr>
</tbody>
</table>

In the following statements, PROC LIFETEST is invoked to compute the product-limit estimate of the survivor function for each risk category. Using ODS Graphics, you can display the number of subjects at risk in the survival plot. The PLOTS= option requests that the survival curves be plotted, and the ATRISK= suboption specifies the time points at which the at-risk numbers are displayed. In the STRATA statement, the ADJUST=SIDAK option requests the Šidák multiple-comparison adjustment, and by default, all paired comparisons are carried out.

```
ods graphics on;

proc lifetest data=sashelp.BMT plots=survival(atrisk=0 to 2500 by 500);
   time T * Status(0);
   strata Group / test=logrank adjust=sidak;
run;
```

**Output 74.2.2** displays the estimated disease-free survival for the three leukemia groups with the number of subjects at risk at 0, 500, 1,000, 1,500, 2,000, and 2,500 days. Patients in the AML-Low Risk group experience a longer disease-free survival than those in the ALL group, who in turn fare better than those in the AML-High Risk group.
Example 74.2: Enhanced Survival Plot and Multiple-Comparison Adjustments

**Output 74.2.2** Estimated Disease-Free Survival for 137 Bone Marrow Transplant Patients

The log-rank test (**Output 74.2.3**) shows that the disease-free survival times for these three risk groups are significantly different ($p = 0.001$).

**Output 74.2.3** Log-Rank Test of Disease Group Homogeneity

<table>
<thead>
<tr>
<th>Test of Equality over Strata</th>
<th>Pr &gt; Chisq</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log-Rank</td>
<td>0.0010</td>
</tr>
</tbody>
</table>

The Šidák multiple-comparison results are shown in **Output 74.2.4**. There is no significant difference in disease-free survivor functions between the ALL and AML-High Risk groups ($p = 0.2779$). The difference between the ALL and AML-Low Risk groups is marginal ($p = 0.0685$), but the AML-Low Risk and AML-High Risk groups have significantly different disease-free survivor functions ($p = 0.0006$).
Suppose you consider the AML-Low Risk group as the reference group. You can use the `DIFF=` option in the STRATA statement to designate this risk group as the control and apply a multiple-comparison adjustment to the \( p \)-values for the paired comparison between the AML-Low Risk group with each of the other groups. Consider the Šidák correction again. You specify the `ADJUST=` and `DIFF=` options as in the following statements:

```plaintext
proc lifetest data=sashelp.BMT notable plots=none;
  time T * Status(0);
  strata Group / test=logrank adjust=sidak diff=control('AML-Low Risk');
run;
```

Output 74.2.5 shows that although both the ALL and AML-High Risk groups differ from the AML-Low Risk group at the 0.05 level, the difference between the AML-High Risk and the AML-Low Risk group is highly significant \( (p = 0.0004) \).

The survival plot that is displayed in Output 74.2.2 might be sufficient for many purposes, but you might have other preferences. Typical alternatives include displaying the number of subjects at risk outside the plot area, reordering the stratum labels in the survival plot legend, and displaying the strata in the at-risk table by using their full labels. PROC LIFETEST provides options that you can use to make these changes without requiring template changes. In the `sashelp.BMT` data set, the variable `Group` that represents the strata is a character variable with three values, namely (in alphabetical order), ALL, AML-High Risk, and AML-Low Risk. It might be desirable to present the strata in the order ALL, AML-Low Risk, and AML-High Risk. The `ORDER=INTERNAL` option in the STRATA statement enables you to order the strata by their internal values. In the following statements, the new data set `Bmt2` is a copy of `sashelp.BMT` with the variable `Group` changed to a numeric variable with values 1, 2, and 3 representing ALL, AML-Low Risk, and AML-High Risk, respectively. The original character values of `Group` are kept as the formatted values, which are used to label the strata in the printed output.
Example 74.2: Enhanced Survival Plot and Multiple-Comparison Adjustments

```
proc format;
  invalue $bmtifmt 'ALL' = 1 'AML-Low Risk' = 2 'AML-High Risk' = 3;
  value bmtfmt 1 = 'ALL' 2 = 'AML-Low Risk' 3 = 'AML-High Risk';
run;

data Bmt2;
  set sashelp.BMT(rename=(Group=G));
  Group = input(input(G, $bmtifmt.), 1.);
  label Group = 'Disease Group';
  format Group bmtfmt.;
run;
```

The following statements produce a survival plot that has all the aforementioned modifications. The new data set Bmt2 is used as the input data. The OUTSIDE and MAXLEN= options are specified in the PLOTS= option. The OUTSIDE option draws the at-risk table outside the plot area. Because the longest label of the strata has 13 characters, specifying MAXLEN=13 is sufficient to display all the stratum labels in the at-risk table. The ORDER=INTERNAL option in the STRATA statement orders the strata by their numerical values 1, 2, and 3, which represent the order ALL, AML-Low Risk, and AML-High Risk, respectively.

```
proc LIFETEST data=Bmt2 plots=s(atrisk(outside maxlen=13)=0 to 2500 by 500);
  time T*Status(0);
  strata Group / order=internal;
run;
```

The modified survival plot is displayed in Output 74.2.6. The most noticeable change from Output 74.2.2 is that the number of subjects at risk is displayed below the time axis. Other changes include displaying the full labels of the strata in the at-risk table and presenting the strata in the order ALL, AML-Low Risk, and AML-High Risk.
Klein and Moeschberger (1997, Section 4.4) describe in detail how to compute the Hall-Wellner (HW) and equal-precision (EP) confidence bands for the survivor function. You can output these simultaneous confidence intervals to a SAS data set by using the CONFBAND= and OUTSURV= options in the PROC LIFETEST statement. You can display survival curves with pointwise and simultaneous confidence limits through ODS Graphics. When the survival data are stratified, displaying all the survival curves and their confidence limits in the same plot can make the plot appear cluttered. In the following statements, the PLOTS= specification requests that the survivor functions be displayed along with their pointwise confidence limits (CL) and Hall-Wellner confidence bands (CB=HW). The STRATA=PANEL specification requests that the survival curves be displayed in a panel of three plots, one for each risk group.

```sas
proc lifetest data=Bmt2 plots=survival(cl cb=hw strata=panel);
   time T * Status(0);
   strata Group/order=internal;
run;
ods graphics off;
```
Example 74.3: Life-Table Estimates for Males with Angina Pectoris

The data in this example come from Lee (1992, p. 91) and represent the survival rates of males with angina pectoris. Survival time is measured as years from the time of diagnosis. In the following DATA step, the data are read as number of events and number of withdrawals in each one-year time interval for 16 intervals. Three variables are constructed from the data: Years (an artificial time variable with values that are the midpoints of the time intervals), Censored (a censoring indicator variable with the value 1 indicating censored observations and the value 0 indicating event observations), and Freq (the frequency variable). Two observations are created for each interval, one representing the event observations and the other representing the censored observations.
title 'Survival of Males with Angina Pectoris';

data Males;
  keep Freq Years Censored;
  retain Years -.5;
  input fail withdraw @@;
  Years + 1;
  Censored=0;
  Freq=fail;
  output;
  Censored=1;
  Freq=withdraw;
  output;
  datalines;
456 0 226 39 152 22 171 23 135 24 125 107
83 133 74 102 51 68 42 64 43 45 34 53
18 33 9 27 6 23 0 30
;

In the following statements, the ODS GRAPHICS ON specification enables ODS Graphics. PROC LIFETEST
is invoked to compute the various life-table survival estimates, the median residual time, and their standard
errors. The life-table method of computing estimates is requested by specifying METHOD=LT. The intervals
are specified by the INTERVAL= option. Graphical displays of the life-table survivor function estimate,
negative log of the estimate, log of negative log of the estimate, estimated density function, and estimated
hazard function are requested by the PLOTS= option. No tests for homogeneity are carried out because the
data are not stratified.

ods graphics on;
proc lifetest data=Males method=lt intervals=(0 to 15 by 1)
  plots=(s,ls,lls,h,p);
  time Years*Censored(1);
  freq Freq;
run;
ods graphics off;

Results of the life-table estimation are shown in Output 74.3.1. The five-year survival rate is 0.5193 with
a standard error of 0.0103. The estimated median residual lifetime, which is 5.33 years initially, reaches a
maximum of 6.34 years at the beginning of the second year and decreases gradually to a value lower than the
initial 5.33 years at the beginning of the seventh year.
### Output 74.3.1 Life-Table Survivor Function Estimate

**Survival of Males with Angina Pectoris**

#### The LIFETEST Procedure

#### Life Table Survival Estimates

<table>
<thead>
<tr>
<th>Interval</th>
<th>Number Failed</th>
<th>Number Censored</th>
<th>Effective Sample Size</th>
<th>Conditional Probability of Failure</th>
<th>Survival Failure</th>
<th>Conditional Probability Standard Error</th>
<th>Survival Standard Error</th>
<th>Median Residual Lifetime</th>
<th>Median Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1</td>
<td>0</td>
<td>2418.0</td>
<td>0.1886</td>
<td>0.0796</td>
<td></td>
<td></td>
<td></td>
<td>0.1749</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
<td>39</td>
<td>1942.5</td>
<td>0.1163</td>
<td>0.0728</td>
<td>0.1886</td>
<td>0.00796</td>
<td>6.2499</td>
<td>0.2001</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>22</td>
<td>1686.0</td>
<td>0.0902</td>
<td>0.0698</td>
<td>0.2830</td>
<td>0.00918</td>
<td>6.3432</td>
<td>0.2361</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
<td>23</td>
<td>1511.5</td>
<td>0.1131</td>
<td>0.0815</td>
<td>0.3476</td>
<td>0.00973</td>
<td>6.2262</td>
<td>0.2361</td>
</tr>
<tr>
<td>4</td>
<td>5</td>
<td>24</td>
<td>1317.0</td>
<td>0.1025</td>
<td>0.0836</td>
<td>0.4214</td>
<td>0.0101</td>
<td>6.2185</td>
<td>0.1853</td>
</tr>
<tr>
<td>5</td>
<td>6</td>
<td>107</td>
<td>1116.5</td>
<td>0.1120</td>
<td>0.0944</td>
<td>0.4807</td>
<td>0.0103</td>
<td>5.9077</td>
<td>0.1806</td>
</tr>
<tr>
<td>6</td>
<td>7</td>
<td>133</td>
<td>871.5</td>
<td>0.0952</td>
<td>0.0994</td>
<td>0.5389</td>
<td>0.0104</td>
<td>5.5962</td>
<td>0.1855</td>
</tr>
<tr>
<td>7</td>
<td>8</td>
<td>102</td>
<td>671.0</td>
<td>0.1103</td>
<td>0.0121</td>
<td>0.5828</td>
<td>0.0105</td>
<td>5.1671</td>
<td>0.2713</td>
</tr>
<tr>
<td>8</td>
<td>9</td>
<td>64</td>
<td>512.0</td>
<td>0.0996</td>
<td>0.0132</td>
<td>0.6288</td>
<td>0.0106</td>
<td>4.9421</td>
<td>0.2763</td>
</tr>
<tr>
<td>9</td>
<td>10</td>
<td>64</td>
<td>395.0</td>
<td>0.1063</td>
<td>0.0155</td>
<td>0.6658</td>
<td>0.0107</td>
<td>4.8258</td>
<td>0.4141</td>
</tr>
<tr>
<td>10</td>
<td>11</td>
<td>45</td>
<td>298.5</td>
<td>0.1441</td>
<td>0.0203</td>
<td>0.7013</td>
<td>0.0109</td>
<td>4.6888</td>
<td>0.4183</td>
</tr>
<tr>
<td>11</td>
<td>12</td>
<td>53</td>
<td>206.5</td>
<td>0.1646</td>
<td>0.0258</td>
<td>0.7443</td>
<td>0.0111</td>
<td></td>
<td></td>
</tr>
<tr>
<td>12</td>
<td>13</td>
<td>33</td>
<td>129.5</td>
<td>0.1390</td>
<td>0.0304</td>
<td>0.7864</td>
<td>0.0114</td>
<td></td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>14</td>
<td>27</td>
<td>81.5</td>
<td>0.1104</td>
<td>0.0347</td>
<td>0.8161</td>
<td>0.0118</td>
<td></td>
<td></td>
</tr>
<tr>
<td>14</td>
<td>15</td>
<td>23</td>
<td>47.5</td>
<td>0.1263</td>
<td>0.0482</td>
<td>0.8364</td>
<td>0.0123</td>
<td></td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>.</td>
<td>30</td>
<td>15.0</td>
<td>0</td>
<td>0</td>
<td>0.8571</td>
<td>0.0133</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

#### Evaluated at the Midpoint of the Interval

<table>
<thead>
<tr>
<th>Interval</th>
<th>PDF Standard Error</th>
<th>Hazard Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.1886</td>
<td>0.00796</td>
</tr>
<tr>
<td>1</td>
<td>0.0944</td>
<td>0.00598</td>
</tr>
<tr>
<td>2</td>
<td>0.0646</td>
<td>0.00507</td>
</tr>
<tr>
<td>3</td>
<td>0.0738</td>
<td>0.00543</td>
</tr>
<tr>
<td>4</td>
<td>0.0593</td>
<td>0.00495</td>
</tr>
<tr>
<td>5</td>
<td>0.0581</td>
<td>0.00503</td>
</tr>
<tr>
<td>6</td>
<td>0.0439</td>
<td>0.00469</td>
</tr>
<tr>
<td>7</td>
<td>0.0460</td>
<td>0.00518</td>
</tr>
<tr>
<td>8</td>
<td>0.0370</td>
<td>0.00502</td>
</tr>
<tr>
<td>9</td>
<td>0.0355</td>
<td>0.00531</td>
</tr>
<tr>
<td>10</td>
<td>0.0430</td>
<td>0.00627</td>
</tr>
<tr>
<td>11</td>
<td>0.0421</td>
<td>0.00685</td>
</tr>
<tr>
<td>12</td>
<td>0.0297</td>
<td>0.00668</td>
</tr>
<tr>
<td>13</td>
<td>0.0203</td>
<td>0.00651</td>
</tr>
<tr>
<td>14</td>
<td>0.0207</td>
<td>0.00804</td>
</tr>
<tr>
<td>15</td>
<td>.</td>
<td>.</td>
</tr>
</tbody>
</table>
The breakdown of event and censored observations in the data is shown in Output 74.3.2. Note that 32.8% of the patients have withdrawn from the study.

**Output 74.3.2** Summary of Censored and Event Observations

<table>
<thead>
<tr>
<th>Total</th>
<th>Failed</th>
<th>Censored</th>
<th>Percent Censored</th>
</tr>
</thead>
<tbody>
<tr>
<td>2418</td>
<td>1625</td>
<td>793</td>
<td>32.80</td>
</tr>
</tbody>
</table>

*Note: 2 observations with invalid time, censoring, or frequency values were deleted.*

Output 74.3.3 displays the graph of the life-table survivor function estimate. The median survival time, read from the survivor function curve, is 5.33 years, and the 25th and 75th percentiles are 1.04 and 11.13 years, respectively.

**Output 74.3.3** Life-Table Survivor Function Estimate
An exponential model might be appropriate for the survival of these male patients with angina pectoris since the curve of the negative log of the survivor function estimate versus the survival time (Output 74.3.4) approximates a straight line through the origin. Note that the graph of the log of the negative log of the survivor function estimate versus the log of time (Output 74.3.5) is practically a straight line.

**Output 74.3.4** Negative Log of Survivor Function Estimate

As discussed in Lee (1992), the graph of the estimated hazard function (Output 74.3.6) shows that the death rate is highest in the first year of diagnosis. From the end of the first year to the end of the tenth year, the death rate remains relatively constant, fluctuating between 0.09 and 0.12. The death rate is generally higher after the tenth year. This could indicate that a patient who has survived the first year has a better chance than a patient who has just been diagnosed. The profile of the median residual lifetimes also supports this interpretation.
Output 74.3.5 Log of Negative Log of Survivor Function Estimate
Output 74.3.6 Hazard Function Estimate

The density estimate is shown in (Output 74.3.7). Visually, it resembles the density function of an exponential distribution.
Example 74.4: Nonparametric Analysis of Competing-Risks Data

Bone marrow transplant (BMT) is a standard treatment for acute leukemia. Klein and Moeschberger (1997) present a set of BMT data for 137 patients, grouped into three disease categories based on their status at the time of transplantation: acute lymphoblastic leukemia (ALL), acute myelocytic leukemia (AML) low-risk, and AML high-risk. During the follow-up period, some patients might relapse or some patients might die while in remission. Relapse and death in remission are competing events, and the disease-free survival time is the time from transplant to the occurrence of the earlier of these two events.

The following DATA step creates the data set Bmt. (This Bmt data set is not identical to the Sashelp.Bmt data set in Example 74.2, but both are derived from the same study.) The variable Disease denotes the disease group of a patient, which is either ALL, AML-low risk, or AML-high risk. The variable Dftime represents the disease-free survival time, which is the time to relapse, the time to death, or censored. The failure time is expressed in years by dividing the time in days by 356.25. The variable Status has three values: 0 for censored observations, 1 for relapsed patients, and 2 for patients who die before experiencing a relapse. The variable Gender, which indicates the gender of the BMT patients, is included to illustrate how to conduct a stratified test.
proc format;
   value diseaseLabel 1='ALL' 2='AML-Low Risk' 3='AML-High Risk';
   value genderLabel 0='Female' 1='Male';
run;

data Bmt;
   input Disease Dftime Status Gender@@;
   Dftime= Dftime / 365.25;
   label Dftime='Disease-Free Survival Time (Years)' Disease='Disease Group';
datalines;
1 2081 0 1 1 1602 0 1
1 1496 0 1 1 1462 0 0
1 1433 0 1 1 1377 0 1
1 1330 0 1 1 996 0 1
... more lines ...
3 625 1 0 3 48 1 0
3 273 1 1 3 63 2 1
3 76 1 1 3 113 1 0
3 363 2 1
;

For competing-risks data, PROC LIFETEST estimates the cumulative incidence function (CIF). If you have multiple samples of data, it estimates the CIF for each sample and compares the CIFs between samples by using Gray’s test (Gray 1988). The estimated CIF is a step function with a jump at each distinct time when the event of interest occurred. If there are a large number of such event times, the table of the estimated CIF could be quite lengthy. If you are interested in the cumulative incidence at specific time points, you can use the TIMELIST= option in the PROC LIFETEST statement to specify these time points, and PROC LIFETEST prints the CIF estimates only at these time points.

Consider relapse as the event of interest. The following statements use PROC LIFETEST to estimate the CIF for relapse. To designate relapse (Status=1) as the event of interest, you specify the option FAILCODE=1 in the TIME statement. The TIMELIST= option in the PROC LIFETEST statement specifies the time points to display the CIF estimate, at half a year, one year, one and a half years, two years, four years, and six years. The STRATA statement identifies the disease groups as different samples of data. The PLOTS= option requests a plot of the estimated CIF, with an inset that shows the p-value of Gray’s test.

    ods graphics on;
    proc lifetest data=Bmt plots=cif(test) timelist=0.5 1.0 1.5 2.0 4.0 6.0;
       time Dftime*Status(0)/eventcode=1;
       strata Disease / order=internal;
       format Disease diseaseLabel. Gender genderLabel.;
    run;

Output 74.4.1 tabulates the number of patients in each disease group who experience the event of interest (relapse) and those who experience the competing event (death in remission).
Output 74.4.1 Distribution of Events and Censored Observations

The LIFETEST Procedure

Failed Event: Status=1

Summary of Failure Outcomes

<table>
<thead>
<tr>
<th>Stratum</th>
<th>Disease</th>
<th>Failed Events</th>
<th>Competing Events</th>
<th>Censored</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>ALL</td>
<td>12</td>
<td>12</td>
<td>14</td>
<td>38</td>
</tr>
<tr>
<td>2</td>
<td>AML-Low Risk</td>
<td>9</td>
<td>16</td>
<td>29</td>
<td>54</td>
</tr>
<tr>
<td>3</td>
<td>AML-High Risk</td>
<td>21</td>
<td>13</td>
<td>11</td>
<td>45</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>42</td>
<td>41</td>
<td>54</td>
<td>137</td>
</tr>
</tbody>
</table>

Output 74.4.2 displays the CIF estimate of relapse for the ALL patients at the selected time points. The predicted CIF at half a year after transplant is 0.1842, with a 95% confidence interval of (0.0798, 0.3224). At two years after transplant, the estimated CIF is 0.3243, with a 95% confidence interval of (0.1778, 0.4787). It is not feasible to estimate the cumulative incidence at a time beyond the largest observed time, which is 5.6975 years in the ALL group. That is why the estimates are missing at six years.

Output 74.4.2 Estimated CIF for ALL Patients

<table>
<thead>
<tr>
<th>Timelist</th>
<th>Cumulative Incidence</th>
<th>Standard Error</th>
<th>95% Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>0.353183</td>
<td>0.0639</td>
<td>(0.0798, 0.3224)</td>
</tr>
<tr>
<td>1</td>
<td>0.629706</td>
<td>0.0705</td>
<td>(0.1164, 0.3836)</td>
</tr>
<tr>
<td>1.5</td>
<td>1.048597</td>
<td>0.0733</td>
<td>(0.1360, 0.4140)</td>
</tr>
<tr>
<td>2</td>
<td>1.812457</td>
<td>0.0791</td>
<td>(0.1788, 0.4787)</td>
</tr>
<tr>
<td>4</td>
<td>2.047912</td>
<td>0.0791</td>
<td>(0.1788, 0.4787)</td>
</tr>
<tr>
<td>6</td>
<td>.</td>
<td>.</td>
<td>.</td>
</tr>
</tbody>
</table>

Output 74.4.3 and Output 74.4.4 display the CIF estimates at the selected times for AML-low risk and AML-high risk patients, respectively.

Output 74.4.3 Estimated CIF for AML-Low Risk Patients

<table>
<thead>
<tr>
<th>Timelist</th>
<th>Cumulative Incidence</th>
<th>Standard Error</th>
<th>95% Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>0.0744695</td>
<td>0.0360</td>
<td>(0.0234, 0.1646)</td>
</tr>
<tr>
<td>1</td>
<td>1.330595</td>
<td>0.0463</td>
<td>(0.0563, 0.2344)</td>
</tr>
<tr>
<td>2</td>
<td>1.659138</td>
<td>0.0489</td>
<td>(0.0685, 0.2565)</td>
</tr>
<tr>
<td>4</td>
<td>2.047912</td>
<td>0.0514</td>
<td>(0.0813, 0.2783)</td>
</tr>
<tr>
<td>6</td>
<td>2.047912</td>
<td>0.0514</td>
<td>(0.0813, 0.2783)</td>
</tr>
</tbody>
</table>
Output 74.4.4 Estimated CIF for AML-High Risk Patients

<table>
<thead>
<tr>
<th>Timelist</th>
<th>Dftime</th>
<th>Cumulative Incidence</th>
<th>Standard Error</th>
<th>95% Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>0.429843</td>
<td>0.2889</td>
<td>0.0686</td>
<td>0.1642 0.4259</td>
</tr>
<tr>
<td>1</td>
<td>0.747433</td>
<td>0.3556</td>
<td>0.0726</td>
<td>0.2181 0.4955</td>
</tr>
<tr>
<td>1.5</td>
<td>1.278576</td>
<td>0.4444</td>
<td>0.0757</td>
<td>0.2940 0.5844</td>
</tr>
<tr>
<td>2</td>
<td>1.711157</td>
<td>0.4667</td>
<td>0.0761</td>
<td>0.3137 0.6059</td>
</tr>
<tr>
<td>4</td>
<td>1.711157</td>
<td>0.4667</td>
<td>0.0761</td>
<td>0.3137 0.6059</td>
</tr>
<tr>
<td>6</td>
<td>1.711157</td>
<td>0.4667</td>
<td>0.0761</td>
<td>0.3137 0.6059</td>
</tr>
</tbody>
</table>

Output 74.4.5 displays the homogeneity test of Gray (1988), which indicates strong evidence of a significant difference in the CIF for relapse among the three disease groups ($p = 0.0028$).

Output 74.4.5 Homogeneity Test of CIFs for Relapse

<table>
<thead>
<tr>
<th>Gray's Test for Equality of Cumulative Incidence Functions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chi-Square</td>
</tr>
<tr>
<td>-------------</td>
</tr>
<tr>
<td>11.9229</td>
</tr>
</tbody>
</table>

The PLOTS= option produces a plot of the estimated CIFs (Output 74.4.5). Note that the range of each curve is from 0 to the largest observed time of the corresponding disease group, which is 5.6975 years for ALL patients, 7.0335 years for AML-low risk patients, and 7.2279 years for AML-high risk patients. With PLOTS=CIF(TEST) specified, that plot displays the $p$-value of the homogeneity test for the disease groups. The cumulative incidences of relapse are smallest for the AML-low risk patients and highest for the AML-high risk patients, with the ALL patients in between.
When you specify the GROUP= option in the STRATA statement, PROC LIFETEST enables you to perform a stratified test to evaluate the homogeneity of the CIFs between groups. Consider Gender as the stratifying variable for the stratified test. You specify Gender in the STRATA statement with the GROUP=DISEASE option as follows:

```r
proc lifetest data=bmt plots=cif(test);
  time Dftime*Status(0)/eventcode=1;
  strata Gender/group=Disease order=internal;
  format Disease diseaseLabel. Gender genderLabel.;
run;
ods graphics off;
```

PROC LIFETEST summarizes the number of events and censored observations in each disease group by gender (Output 74.4.7). PROC LIFETEST computes a separate CIF estimate for each disease category for the female patients (Output 74.4.8) and likewise for the male patients (not shown here).
### Output 74.4.7  Distribution of Events and Censored Observations

**The LIFETEST Procedure**

**Failed Event: Status=1**

<table>
<thead>
<tr>
<th>Stratum</th>
<th>Gender</th>
<th>Disease</th>
<th>Failed Events</th>
<th>Competing Events</th>
<th>Censored</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Female</td>
<td>ALL</td>
<td>5</td>
<td>3</td>
<td>4</td>
<td>12</td>
</tr>
<tr>
<td>1</td>
<td>Female</td>
<td>AML-Low Risk</td>
<td>3</td>
<td>7</td>
<td>14</td>
<td>24</td>
</tr>
<tr>
<td>1</td>
<td>Female</td>
<td>AML-High Risk</td>
<td>12</td>
<td>6</td>
<td>3</td>
<td>21</td>
</tr>
<tr>
<td>Subtotal</td>
<td></td>
<td></td>
<td>20</td>
<td>16</td>
<td>21</td>
<td>57</td>
</tr>
<tr>
<td>2</td>
<td>Male</td>
<td>ALL</td>
<td>7</td>
<td>9</td>
<td>10</td>
<td>26</td>
</tr>
<tr>
<td>2</td>
<td>Male</td>
<td>AML-Low Risk</td>
<td>6</td>
<td>9</td>
<td>15</td>
<td>30</td>
</tr>
<tr>
<td>2</td>
<td>Male</td>
<td>AML-High Risk</td>
<td>9</td>
<td>7</td>
<td>8</td>
<td>24</td>
</tr>
<tr>
<td>Subtotal</td>
<td></td>
<td></td>
<td>22</td>
<td>25</td>
<td>33</td>
<td>80</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td></td>
<td>42</td>
<td>41</td>
<td>54</td>
<td>137</td>
</tr>
</tbody>
</table>

### Output 74.4.8  CIF Estimates for Female Patients

**Cumulative Incidence Function Estimates**

**Stratum 1: Gender = Female**

<table>
<thead>
<tr>
<th>Disease</th>
<th>Dftime</th>
<th>Cumulative Incidence</th>
<th>Standard Error</th>
<th>95% Confidence Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>ALL</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>ALL</td>
<td>0.150582</td>
<td>0.0833</td>
<td>0.0833</td>
<td>0.00422 0.3233</td>
</tr>
<tr>
<td>ALL</td>
<td>0.301164</td>
<td>0.1667</td>
<td>0.1126</td>
<td>0.0235 0.4250</td>
</tr>
<tr>
<td>ALL</td>
<td>0.334018</td>
<td>0.2500</td>
<td>0.1312</td>
<td>0.0544 0.5168</td>
</tr>
<tr>
<td>ALL</td>
<td>0.353183</td>
<td>0.3333</td>
<td>0.1433</td>
<td>0.0938 0.6004</td>
</tr>
<tr>
<td>ALL</td>
<td>0.629706</td>
<td>0.4333</td>
<td>0.1591</td>
<td>0.0138 0.7022</td>
</tr>
<tr>
<td>AML-Low Risk</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>AML-Low Risk</td>
<td>0.744695</td>
<td>0.0417</td>
<td>0.0419</td>
<td>0.00271 0.1810</td>
</tr>
<tr>
<td>AML-Low Risk</td>
<td>1.043121</td>
<td>0.0833</td>
<td>0.0580</td>
<td>0.0135 0.2381</td>
</tr>
<tr>
<td>AML-Low Risk</td>
<td>1.330595</td>
<td>0.1250</td>
<td>0.0695</td>
<td>0.0299 0.2918</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.131417</td>
<td>0.0476</td>
<td>0.0477</td>
<td>0.00303 0.2023</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.175222</td>
<td>0.0952</td>
<td>0.0658</td>
<td>0.0153 0.2665</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.229979</td>
<td>0.1429</td>
<td>0.0785</td>
<td>0.0339 0.3267</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.25462</td>
<td>0.1905</td>
<td>0.0882</td>
<td>0.0569 0.3832</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.309377</td>
<td>0.2381</td>
<td>0.0958</td>
<td>0.0832 0.4368</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.314853</td>
<td>0.2857</td>
<td>0.1018</td>
<td>0.1122 0.4879</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.328542</td>
<td>0.3333</td>
<td>0.1064</td>
<td>0.1435 0.5370</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.429843</td>
<td>0.3810</td>
<td>0.1098</td>
<td>0.1768 0.5841</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>0.733744</td>
<td>0.4286</td>
<td>0.1125</td>
<td>0.2113 0.6302</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>1.155373</td>
<td>0.4762</td>
<td>0.1144</td>
<td>0.2467 0.6748</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>1.278576</td>
<td>0.5238</td>
<td>0.1154</td>
<td>0.2834 0.7178</td>
</tr>
<tr>
<td>AML-High Risk</td>
<td>1.711157</td>
<td>0.5714</td>
<td>0.1155</td>
<td>0.3212 0.7590</td>
</tr>
</tbody>
</table>
Chapter 74: The LIFETEST Procedure

Output 74.4.9 shows the results of the stratified test with a $p$-value of 0.0026, which is essentially the same as the $p$-value of the nonstratified test. The PLOTS= option creates a panel plot with two cells: one cell for female patients and the other cell for male patients. Each cell contains three CIF curves, one for each disease group (Output 74.4.10). Regardless of the gender of the patient, an AML-high risk patient is more likely to relapse than an ALL patient, and an ALL patient is more likely to relapse than an AML-low risk patient. This ordering of probabilities is revealed in the panel plots in Output 74.4.10.

**Output 74.4.9** Stratified Gray's Test

<table>
<thead>
<tr>
<th>Gray's Test for Equality of Cumulative Incidence Functions</th>
<th>( \text{Pr} &gt; )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chi-Square</td>
<td>DF</td>
</tr>
<tr>
<td>11.7625</td>
<td>2</td>
</tr>
</tbody>
</table>

**Output 74.4.10** Panel Plots of CIFs for Relapse
Example 74.5: Restricted Mean Analysis

This example illustrates how to perform nonparametric analyses with respect to the restricted mean survival time (RMST) and the restricted mean time lost (RMTL). Consider the VALung data set in Example 74.1. The failure time variable is SurvTime. The censoring indicator variable is Censor, which has a value of 1 for a censored observation and a value of 0 for an uncensored observation. Each patient has one of the four types of cancer cells (adenocarcinoma, large cell, small cell, and squamous) that are identified by the variable Cell.

The following statements use PROC LIFETEST to perform analyses of the restricted mean survival time (RMST) and restricted mean time lost (RMTL) in addition to the standard analyses:

```plaintext
ods graphics on;
proc lifetest data=VALung plots=(rmst rmtl) rmst rmtl(tau=90) maxtime=600;
   time SurvTime*Censor(1);
   strata Cell;
run;
ods graphics off;
```

The RMST and RMTL options estimate the restricted mean survival time and the restricted mean time lost, respectively. The variable Cell is specified in the STRATA statement to compute the RMST for each type of cancer cell. ODS Graphics must be enabled for graphs to be produced. Graphical displays of the RMST and RMTL curves are requested through the PLOTS= option in the PROC LIFETEST statement. Because of a few large survival times, a MAXTIME= option value of 600 is used to set the upper limit of the time axis; that is, the time horizon extends from 0 to a maximum of 600 days in the plots.

Output 74.5.1 displays the value that the RMST analysis uses. If you omit the TAU= option, PROC LIFETEST uses the smallest value among the largest observed times across the strata as the \(\tau\) value.

```
Output 74.5.1 RMST Analysis Information

The LIFETEST Procedure

<table>
<thead>
<tr>
<th>RMST Analysis Information</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tau 186</td>
</tr>
</tbody>
</table>
```

Output 74.5.2 displays the RMST estimates for the four cell types.

```
Output 74.5.2 RMST Estimates

<table>
<thead>
<tr>
<th>Stratum</th>
<th>Cell Type</th>
<th>Estimate</th>
<th>Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>adeno</td>
<td>65.5556</td>
<td>9.9303</td>
</tr>
<tr>
<td>2</td>
<td>large</td>
<td>128.0370</td>
<td>11.9858</td>
</tr>
<tr>
<td>3</td>
<td>small</td>
<td>64.20647</td>
<td>8.2859</td>
</tr>
<tr>
<td>4</td>
<td>squamous</td>
<td>113.8040</td>
<td>12.3703</td>
</tr>
</tbody>
</table>
```

Output 74.5.3 displays information for the RMTL analysis. A \(\tau\) value of 90 is shown; this is the value specified in the TAU= option.
Output 74.5.3  RMTL Analysis Information

<table>
<thead>
<tr>
<th>RMTL</th>
<th>Analysis Information</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tau</td>
<td>90</td>
</tr>
</tbody>
</table>

Output 74.5.4 displays the RMTL estimates for the four cell types at $\tau = 90$.

Output 74.5.4  RMTL Estimates at $\tau = 90$

<table>
<thead>
<tr>
<th>Stratum</th>
<th>Cell Type</th>
<th>Estimate</th>
<th>Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>adeno</td>
<td>36.54321</td>
<td>6.3206</td>
</tr>
<tr>
<td>2</td>
<td>large</td>
<td>14.33333</td>
<td>4.9560</td>
</tr>
<tr>
<td>3</td>
<td>small</td>
<td>41.27083</td>
<td>4.6763</td>
</tr>
<tr>
<td>4</td>
<td>squamous</td>
<td>22.99365</td>
<td>5.6430</td>
</tr>
</tbody>
</table>

The graph of the estimated RMST curves is shown in Output 74.5.5. These curves exhibit a behavior similar to that of the survival curves in Example 74.1: the adeno cell curve and the small cell curve are much closer to each other than they are to the large cell curve or the squamous cell curve. The shapes of the large cell curve and the squamous cell curve are quite different, although both increase more rapidly than those of the adeno and small cells. The squamous cell curve initially increases less rapidly than the large cell curve, but the role is reversed in the later period.
The graph of the estimated RMTL curves is displayed in **Output 74.5.6**. Again, the adeno cell curve and the small cell curve are much closer to each other and farther away from the large cell and squamous cell curves.
Results of the homogeneity test for the RMST across cell types are given in Output 74.5.7. The table displays the approximate chi-square statistic, degrees of freedom, and $p$-value. The test results indicate strong evidence that the RMSTs for the four types of cancer cells are not the same ($p < 0.0001$).

![Output 74.5.6 RMTL Curves](image)

Output 74.5.7 Homogeneity Tests across Cell Types

<table>
<thead>
<tr>
<th>Source</th>
<th>Chi-Square</th>
<th>DF</th>
<th>Pr &gt; ChiSq</th>
</tr>
</thead>
<tbody>
<tr>
<td>Strata</td>
<td>28.4427</td>
<td>3</td>
<td>&lt;0.0001</td>
</tr>
</tbody>
</table>

The homogeneity test does not identify which pairs of the RMSTs are different. In the following statements, you use the DIFF= option to compute the paired differences of the RMST among the groups. To protect yourself from falsely significant results, you use the ADJUST= option to make multiple-comparison adjustments to the resulting $p$-values.

```bash
proc lifetest data=VALung rmst;
   time SurvTime*Censor(1);
   strata Cell / diff=all adj=sidak;
run;
```
The Šidák multiple-comparison results are shown in Output 74.5.8.

**Output 74.5.8** All Paired Comparisons

The **LIFETEST** Procedure

<table>
<thead>
<tr>
<th>Stratum Comparison</th>
<th>Difference</th>
<th>Standard Error</th>
<th>Chi-Square</th>
<th>Unadjusted Pr &gt; ChiSq</th>
<th>Adjusted Pr &gt; ChiSq</th>
</tr>
</thead>
<tbody>
<tr>
<td>adeno large</td>
<td>-62.4815</td>
<td>15.5650</td>
<td>16.1141</td>
<td>&lt;.0001</td>
<td>0.0004</td>
</tr>
<tr>
<td>adeno small</td>
<td>1.349087</td>
<td>12.9332</td>
<td>0.0109</td>
<td>0.9169</td>
<td>1.0000</td>
</tr>
<tr>
<td>adeno squamous</td>
<td>-48.2485</td>
<td>15.8630</td>
<td>9.2511</td>
<td>0.0024</td>
<td>0.0140</td>
</tr>
<tr>
<td>large small</td>
<td>63.83057</td>
<td>14.5710</td>
<td>19.1901</td>
<td>&lt;.0001</td>
<td>&lt;.0001</td>
</tr>
<tr>
<td>large squamous</td>
<td>14.23303</td>
<td>17.2245</td>
<td>0.6828</td>
<td>0.4086</td>
<td>0.9572</td>
</tr>
<tr>
<td>small squamous</td>
<td>-49.5975</td>
<td>14.8889</td>
<td>11.0967</td>
<td>0.0009</td>
<td>0.0052</td>
</tr>
</tbody>
</table>

The results suggest that you can divide the four risk groups into two classes. The first class consists of the small and adeno cell types, and there is no significant difference in the RMST between them \((p = 1.0000)\). The second class consists of the large and squamous cell types, and the paired comparison is not significant \((p = 0.9572)\). However, there is significant difference in any paired comparison between the two classes.

Suppose you consider the small cell type to be the reference group. You can use the **DIFF=** option in the STRATA statement to designate this risk group as the control and apply a multiple-comparison adjustment to the \(p\)-values for the paired comparison between the small cell type and the other cell types. Consider the Šidák correction again. You specify the **ADJUST=** and **DIFF=** options as in the following statements:

```plaintext
proc lifetest data=VALung rmst;
   time SurvTime*Censor(1);
   strata Cell / adj=sidak diff=control('small');
run;
```

Output 74.5.9 shows that both the large and squamous cell types differ from the small cell type at the 0.05 level, whereas the difference between the adeno and small cell types is not significant \((p = 0.9994)\).

**Output 74.5.9** Comparisons to the Reference Group

The **LIFETEST** Procedure

<table>
<thead>
<tr>
<th>Stratum Comparison</th>
<th>Difference</th>
<th>Standard Error</th>
<th>Chi-Square</th>
<th>Unadjusted Pr &gt; ChiSq</th>
<th>Adjusted Pr &gt; ChiSq</th>
</tr>
</thead>
<tbody>
<tr>
<td>adeno small</td>
<td>1.349087</td>
<td>12.9332</td>
<td>0.0109</td>
<td>0.9169</td>
<td>0.9994</td>
</tr>
<tr>
<td>large small</td>
<td>63.83057</td>
<td>14.5710</td>
<td>19.1901</td>
<td>&lt;.0001</td>
<td>&lt;.0001</td>
</tr>
<tr>
<td>squamous small</td>
<td>49.59754</td>
<td>14.8889</td>
<td>11.0967</td>
<td>0.0009</td>
<td>0.0026</td>
</tr>
</tbody>
</table>
References


Subject Index

<table>
<thead>
<tr>
<th>Term</th>
<th>Page Numbers</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>actuarial estimates, see</td>
<td></td>
<td>life-table estimates</td>
</tr>
<tr>
<td>alpha level</td>
<td></td>
<td>LIFETEST procedure, 5578</td>
</tr>
<tr>
<td>annotate</td>
<td></td>
<td>traditional graphics (LIFETEST), 5632</td>
</tr>
<tr>
<td>arcsine-square root transformation</td>
<td></td>
<td>confidence intervals (LIFETEST), 5579, 5602, 5604</td>
</tr>
<tr>
<td>association tests</td>
<td></td>
<td>LIFETEST procedure, 5567, 5574, 5651</td>
</tr>
<tr>
<td>at-risk</td>
<td></td>
<td>product-limit estimates (LIFETEST), 5578</td>
</tr>
<tr>
<td>Bonferroni adjustment</td>
<td></td>
<td>LIFETEST procedure, 5590</td>
</tr>
<tr>
<td>Breslow estimates</td>
<td></td>
<td>LIFETEST procedure, 5566, 5596</td>
</tr>
<tr>
<td>Breslow test, see Wilcoxon test</td>
<td></td>
<td>for homogeneity</td>
</tr>
<tr>
<td>catalog</td>
<td></td>
<td>traditional graphics (LIFETEST), 5633</td>
</tr>
<tr>
<td>CDF, see cumulative distribution function</td>
<td></td>
<td>LIFETEST procedure, 5566, 5594</td>
</tr>
<tr>
<td>censored</td>
<td></td>
<td>traditional graphics (LIFETEST), 5632</td>
</tr>
<tr>
<td>character set</td>
<td></td>
<td>line printer plots (LIFETEST), 5633</td>
</tr>
<tr>
<td>confidence bands</td>
<td></td>
<td>LIFETEST procedure, 5578, 5603</td>
</tr>
<tr>
<td>confidence limits</td>
<td></td>
<td>LIFETEST procedure, 5601, 5620</td>
</tr>
<tr>
<td>cumulative distribution function</td>
<td></td>
<td>LIFETEST procedure, 5566</td>
</tr>
<tr>
<td>cumulative incidence function</td>
<td></td>
<td>LIFETEST procedure, 5619</td>
</tr>
<tr>
<td>cumulative incidence function</td>
<td></td>
<td>estimates</td>
</tr>
<tr>
<td>estimation method</td>
<td></td>
<td>LIFETEST procedure, 5628</td>
</tr>
<tr>
<td>density function, see</td>
<td></td>
<td>probability density function</td>
</tr>
<tr>
<td>description</td>
<td></td>
<td>traditional graphics (LIFETEST), 5632</td>
</tr>
<tr>
<td>Dunnett’s adjustment</td>
<td></td>
<td>LIFETEST procedure, 5590</td>
</tr>
<tr>
<td>effective sample size</td>
<td></td>
<td>LIFETEST procedure, 5600</td>
</tr>
<tr>
<td>equal-precision bands</td>
<td></td>
<td>LIFETEST procedure, 5578, 5605, 5658</td>
</tr>
<tr>
<td>event symbol</td>
<td></td>
<td>traditional graphics (LIFETEST), 5633</td>
</tr>
<tr>
<td>Fleming-Harrington estimates</td>
<td></td>
<td>LIFETEST procedure, 5566, 5596</td>
</tr>
<tr>
<td>Fleming-Harrington $G_p$ test for homogeneity</td>
<td></td>
<td>LIFETEST procedure, 5566, 5593</td>
</tr>
<tr>
<td>Gehan test, see Wilcoxon test</td>
<td></td>
<td>for homogeneity</td>
</tr>
<tr>
<td>Hall-Wellner bands</td>
<td></td>
<td>LIFETEST procedure, 5578, 5604, 5658</td>
</tr>
<tr>
<td>hazard function</td>
<td></td>
<td>LIFETEST procedure, 5566, 5665</td>
</tr>
<tr>
<td>homogeneity tests</td>
<td></td>
<td>LIFETEST procedure, 5566, 5573, 5607, 5650</td>
</tr>
<tr>
<td>interval determination</td>
<td></td>
<td>LIFETEST procedure, 5601</td>
</tr>
<tr>
<td>interval width</td>
<td></td>
<td>life-table method (LIFETEST), 5587</td>
</tr>
<tr>
<td>intervals</td>
<td></td>
<td>life-table estimates (LIFETEST), 5579</td>
</tr>
<tr>
<td>k-sample tests, see</td>
<td></td>
<td>homogeneity tests</td>
</tr>
<tr>
<td>Kaplan-Meier estimates, see</td>
<td></td>
<td>product-limit estimates</td>
</tr>
<tr>
<td>kernel-smoothed hazard</td>
<td></td>
<td>LIFETEST procedure, 5583, 5605</td>
</tr>
<tr>
<td>life-table estimates</td>
<td></td>
<td>LIFETEST procedure, 5566, 5624, 5662</td>
</tr>
<tr>
<td>LIFETEST procedure</td>
<td></td>
<td>alpha level, 5578</td>
</tr>
<tr>
<td></td>
<td></td>
<td>association tests, 5567, 5574, 5611, 5640, 5651</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Bonferroni adjustment, 5590</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Breslow estimates, 5566, 5580, 5596</td>
</tr>
<tr>
<td></td>
<td></td>
<td>censored, 5566, 5594</td>
</tr>
<tr>
<td></td>
<td></td>
<td>computational formulas, 5596</td>
</tr>
<tr>
<td></td>
<td></td>
<td>confidence bands, 5578, 5603</td>
</tr>
<tr>
<td></td>
<td></td>
<td>confidence limits, 5601, 5620</td>
</tr>
<tr>
<td></td>
<td></td>
<td>cumulative distribution function, 5566</td>
</tr>
<tr>
<td></td>
<td></td>
<td>cumulative incidence estimate, 5666</td>
</tr>
<tr>
<td></td>
<td></td>
<td>cumulative incidence function estimates, 5628</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Dunnett’s adjustment, 5590</td>
</tr>
<tr>
<td></td>
<td></td>
<td>effective sample size, 5600</td>
</tr>
<tr>
<td></td>
<td></td>
<td>equal-precision bands, 5605, 5658</td>
</tr>
<tr>
<td></td>
<td></td>
<td>estimation method, 5580</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Fleming-Harrington estimates, 5566, 5580, 5596</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Fleming-Harrington $G_p$ test for homogeneity, 5566, 5593</td>
</tr>
</tbody>
</table>
Hall-Wellner bands, 5604, 5658
hazard function, 5566, 5665
homogeneity tests, 5566, 5573, 5607, 5650
input data set, 5579
interval determination, 5601
kernel-smoothed hazard, 5583, 5605
life-table estimates, 5566, 5580, 5600, 5624, 5659, 5662
likelihood ratio test for homogeneity, 5566, 5607
log-rank test for association, 5567, 5612
log-rank test for homogeneity, 5566, 5593, 5607
maximum time, 5578, 5580
median residual time, 5624
minimum time, 5578
missing stratum values, 5580, 5589, 5593
missing values, 5596
modified Peto-Peto test for homogeneity, 5566, 5594
Nelson-Aalen estimates, 5580
ODS graph names, 5638
ODS Graphics, 5577
ODS table names, 5635
output data sets, 5618
partial listing, 5587
Peto-Peto test for homogeneity, 5566, 5594
probability density function, 5566, 5666
product-limit estimates, 5566, 5569, 5580, 5596, 5621–5623, 5640
restricted mean survival time, 5616
restricted mean time lost, 5617
RMST analysis, 5581
RMST estimates, 5629, 5673
RMST homogeneity tests, 5676
RMST tests, 5673
RMTL analysis, 5581
RMTL estimates, 5630
Scheffe’s adjustment, 5591
Sidak’s adjustment, 5591
simulated adjustment, 5591
stratified test, 5592
stratified tests, 5566, 5567, 5574, 5576, 5609, 5626
studentized maximum modulus adjustment, 5591
survival distribution function, 5566, 5596
Tarone-Ware test for homogeneity, 5566, 5594
traditional graphics, 5632
transformations for confidence intervals, 5579
trend tests, 5566, 5593, 5611, 5626
Tukey’s adjustment, 5591
variance estimator, 5579
Wilcoxon test for association, 5567, 5612
Wilcoxon test for homogeneity, 5566, 5594, 5607
likelihood ratio test for homogeneity

LIFETEST procedure, 5566
line printer plots
LIFETEST procedure, 5631
linear rank tests, see association tests
linear transformation
confidence intervals (LIFETEST), 5579, 5602
local annotate
traditional graphics (LIFETEST), 5633
log transformation
confidence intervals (LIFETEST), 5579, 5602, 5604
log-log transformation
confidence intervals (LIFETEST), 5579, 5602, 5604
log-rank test for association
LIFETEST procedure, 5567
log-rank test for homogeneity
LIFETEST procedure, 5566, 5593, 5607
logit transformation
confidence intervals (LIFETEST), 5579, 5603, 5604
maximum time
confidence bands (LIFETEST), 5578
plots (LIFETEST), 5580
mean survival time
time limit (LIFETEST), 5587
median residual time
LIFETEST procedure, 5624
minimum time
confidence bands (LIFETEST), 5578
missing stratum values
LIFETEST procedure, 5580, 5589, 5593
missing values
LIFETEST procedure, 5596
modified Peto-Peto test for homogeneity
LIFETEST procedure, 5566, 5594
multiplicity adjustment
Bonferroni (LIFETEST), 5590
Dunnett (LIFETEST), 5590
Scheffe (LIFETEST), 5591
Sidak (LIFETEST), 5591
simulated (LIFETEST), 5591
studentized maximum modulus (LIFETEST), 5591
Tukey (LIFETEST), 5591
Nelson-Aalen estimates
LIFETEST procedure, 5580
number of intervals
life-table estimates (LIFETEST), 5580
ODS graph names
LIFETEST procedure, 5638
ODS Graphics
LIFETEST procedure, 5577
output data sets
LIFETEST procedure, 5618

partial listing
  product-limit estimate (LIFETEST), 5587
PDF, see probability density function
Peto-Peto test for homogeneity
  LIFETEST procedure, 5566, 5594
Peto-Peto-Prentice, see Peto-Peto test for homogeneity
  probability density function
  LIFETEST procedure, 5566, 5666
product-limit estimates
  LIFETEST procedure, 5566, 5569, 5596, 5621–5623

restricted mean survival time
  definition (LIFETEST), 5616
restricted mean time lost
definition (LIFETEST), 5617
RMST analysis
  LIFETEST procedure, 5581
RMST estimates
  LIFETEST procedure, 5629
RMST homogeneity tests
  LIFETEST procedure, 5676
RMTL analysis
  LIFETEST procedure, 5581
RMTL estimates
  LIFETEST procedure, 5630

Scheffe’s adjustment
  LIFETEST procedure, 5591
SDF, see survival distribution function
Sidak’s adjustment
  LIFETEST procedure, 5591
simulated adjustment
  LIFETEST procedure, 5591
stratified test
  LIFETEST procedure, 5592
stratified tests
  LIFETEST procedure, 5566, 5567, 5574, 5576, 5609, 5626
studentized maximum modulus adjustment
  LIFETEST procedure, 5591
survival distribution function
  LIFETEST procedure, 5566, 5596, 5621
survivor function, see survival distribution function

Tarone-Ware test for homogeneity
  LIFETEST procedure, 5566, 5594
traditional graphics
  LIFETEST procedure, 5632
transformations for confidence intervals
  LIFETEST procedure, 5579
Syntax Index

ADJUST= option
   STRATA statement (LIFETEST), 5590
ALPHA= option
   PROC LIFETEST statement, 5578
ALPHAQT= option
   PROC LIFETEST statement, 5578
ANNOTATE= option
   PROC LIFETEST statement, 5632
ATRISK option
   PROC LIFETEST statement, 5578
BANDMAX= option, see BANDMAXTIME= option
BANDMAXTIME= option
   PROC LIFETEST statement, 5578
BANDMIN= option, see BANDMINTIME= option
BANDMINTIME= option
   PROC LIFETEST statement, 5578
BY statement
   LIFETEST procedure, 5588
CENSOREDSYMBOL= option
   PROC LIFETEST statement, 5632
CIFVAR= option
   PROC LIFETEST statement, 5578
CONFBAND= option
   PROC LIFETEST statement, 5578
CONFTYPE= option
   PROC LIFETEST statement, 5579
DATA= option
   PROC LIFETEST statement, 5579
DESCRIPTION= option
   PROC LIFETEST statement, 5632
DIFF= option
   STRATA statement (LIFETEST), 5592
ERROR= option
   PROC LIFETEST statement, 5579
EVENTSYMBOL= option
   PROC LIFETEST statement, 5633
FORMCHAR= option
   PROC LIFETEST statement, 5633
FREQ statement
   LIFETEST procedure, 5588
GOUT= option
   PROC LIFETEST statement, 5633
GROUP= option
   STRATA statement (LIFETEST), 5592
ID statement
   LIFETEST procedure, 5589
INTERVALS= option
   PROC LIFETEST statement, 5579
LANNOTATE= option
   PROC LIFETEST statement, 5633
LIFETEST procedure, 5566
   BY statement, 5587
   FREQ statement, 5588
   ID statement, 5589
   PROC LIFETEST statement, 5576
   STRATA statement, 5589
   syntax, 5576
   TEST statement, 5594
   TIME statement, 5594, 5595
LIFETEST procedure, BY statement, 5588
LIFETEST procedure, FREQ statement, 5588
   NOTRUNCATE option, 5588
LIFETEST procedure, ID statement, 5589
LIFETEST procedure, PROC LIFETEST statement, 5576
   ALPHA= option, 5578
   ALPHAQT= option, 5578
   ANNOTATE= option, 5632
   ATRISK option, 5578
   BANDMAXTIME= option, 5578
   BANDMINTIME= option, 5578
   CENSOREDSYMBOL= option, 5632
   CIFVAR= option, 5578
   CONFBAND= option, 5578
   CONFTYPE= option, 5579
   DATA= option, 5579
   DESCRIPTION= option, 5632
   ERROR= option, 5579
   EVENTSYMBOL= option, 5633
   FORMCHAR= option, 5633
   GOUT= option, 5633
   INTERVALS= option, 5579
   LANNOTATE= option, 5579
   LINEPRINTER option, 5633
   MAXTIME= option, 5580, 5633
   METHOD= option, 5580
   MISSING option, 5580
   NELSON option, 5580
   NINTERVAL= option, 5580
   NOCENSPLOT option, 5634
NOLEFT option, 5581
NOPRINT option, 5581
NOTABLE option, 5581
OUTCIF= option, 5581
OUTSURV= option, 5581
OUTTEST= option, 5581
PLOTS= option, 5582, 5634, 5635
REDUCEOUT option, 5587
RMST option, 5581
RMTL option, 5581
SINGULAR= option, 5587
STDERR option, 5587
TIMELIM= option, 5587
TIMELIST= option, 5587
WIDTH= option, 5587
LIFETEST procedure, STRATA statement, 5589
ADJUST= option, 5590
DIFF= option, 5592
GROUP= option, 5592
MISSING option, 5593
NODETAIL option, 5593
NOLABEL option, 5593
NOTEST option, 5593
ORDER= option, 5593
TEST= option, 5593
TREND option, 5593
LIFETEST procedure, TEST statement, 5594
LIFETEST procedure, TIME statement, 5594
LIFETEST procedure, WEIGHT statement, 5595
LINEPRINTER option
PROC LIFETEST statement, 5633
MAXTIME= option
PROC LIFETEST statement, 5580, 5633
METHOD= option
PROC LIFETEST statement, 5580
MISSING option
PROC LIFETEST statement, 5580
STRATA statement (LIFETEST), 5593
NELSON option
PROC LIFETEST statement, 5580
NINTERVAL= option
PROC LIFETEST statement, 5580
NOCENS PLOT option
PROC LIFETEST statement, 5634
NODETAIL option
STRATA statement (LIFETEST), 5593
NOLABEL option
STRATA statement (LIFETEST), 5593
NOLEFT option
PROC LIFETEST statement, 5581
NOPRINT option
PROC LIFETEST statement, 5581
NOTABLE option
PROC LIFETEST statement, 5581
NOTEST option
STRATA statement (LIFETEST), 5593
NOTRUNCATE option
FREQ statement, 5588
ORDER= option
STRATA statement (LIFETEST), 5593
OUTCIF= option
PROC LIFETEST statement, 5581
OUTSURV= option
PROC LIFETEST statement, 5581
OUTTEST= option
PROC LIFETEST statement, 5581
PLOTS= option
PROC LIFETEST statement, 5582, 5634, 5635
PROC LIFETEST statement
LIFETEST procedure, 5576
REDUCEOUT option
PROC LIFETEST statement, 5587
RMST option
PROC LIFETEST statement, 5581
RMTL option
PROC LIFETEST statement, 5581
SINGULAR= option
PROC LIFETEST statement, 5587
STDERR option
PROC LIFETEST statement, 5587
STRATA statement
LIFETEST procedure, 5589
TEST statement
LIFETEST procedure, 5594
TEST= option
STRATA statement (LIFETEST), 5593
TIME statement
LIFETEST procedure, 5594, 5595
TIMELIM= option
PROC LIFETEST statement, 5587
TIMELIST= option
PROC LIFETEST statement, 5587
TREND option
STRATA statement (LIFETEST), 5593
WIDTH= option
PROC LIFETEST statement, 5587