

# SAS/STAT® 14.3 User's Guide The PRINCOMP Procedure

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#### SAS/STAT® 14.3 User's Guide

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## Chapter 93

### The PRINCOMP Procedure

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### **Overview: PRINCOMP Procedure**

The PRINCOMP procedure performs principal component analysis. As input, you can use raw data, a correlation matrix, a covariance matrix, or a sum-of-squares-and-crossproducts (SSCP) matrix. You can create output data sets that contain eigenvalues, eigenvectors, and standardized or unstandardized principal component scores.

Principal component analysis is a multivariate technique for examining relationships among several quantitative variables. The choice between using factor analysis and using principal component analysis depends in part on your research objectives. You should use the PRINCOMP procedure if you are interested in summarizing data and detecting linear relationships. You can use principal component analysis to reduce the

number of variables in regression, clustering, and so on. For a detailed comparison of the PRINCOMP and FACTOR procedures, see Chapter 9, "Introduction to Multivariate Procedures."

You can use ODS Graphics to display the scree plot, component pattern plot, component pattern profile plot, matrix plot of component scores, and component score plots. These plots are especially valuable tools in exploratory data analysis.

Principal component analysis was originated by Pearson (1901) and later developed by Hotelling (1933). The application of principal components is discussed by Rao (1964); Cooley and Lohnes (1971); Gnanadesikan (1977). Excellent statistical treatments of principal components are found in Kshirsagar (1972); Morrison (1976); Mardia, Kent, and Bibby (1979).

If you have a data set that contains p numeric variables, you can compute p principal components. Each principal component is a linear combination of the original variables, with coefficients equal to the eigenvectors of the correlation or covariance matrix. The eigenvectors are usually taken with unit length. The principal components are sorted by descending order of the eigenvalues, which are equal to the variances of the components.

Principal components have a variety of useful properties (Rao 1964; Kshirsagar 1972):

- The eigenvectors are orthogonal, so the principal components represent jointly perpendicular directions through the space of the original variables.
- The principal component scores are jointly uncorrelated. Note that this property is quite distinct from the previous one.
- The first principal component has the largest variance of any unit-length linear combination of the observed variables. The *j*th principal component has the largest variance of any unit-length linear combination orthogonal to the first j-1 principal components. The last principal component has the smallest variance of any linear combination of the original variables.
- The scores on the first *j* principal components have the highest possible generalized variance of any set of unit-length linear combinations of the original variables.
- The first *j* principal components provide a least squares solution to the model

$$Y = XB + E$$

where **Y** is an  $n \times p$  matrix of the centered observed variables; **X** is the  $n \times j$  matrix of scores on the first j principal components; **B** is the  $j \times p$  matrix of eigenvectors; **E** is an  $n \times p$  matrix of residuals; and you want to minimize trace(**E**'**E**), the sum of all the squared elements in **E**. In other words, the first j principal components are the best linear predictors of the original variables among all possible sets of j variables, although any nonsingular linear transformation of the first j principal components would provide equally good prediction. The same result is obtained if you want to minimize the determinant or the Euclidean (Schur, Frobenius) norm of **E**'**E** rather than the trace.

• In geometric terms, the *j*-dimensional linear subspace that is spanned by the first *j* principal components provides the best possible fit to the data points as measured by the sum of squared perpendicular distances from each data point to the subspace. This contrasts with the geometric interpretation of least squares regression, which minimizes the sum of squared vertical distances. For example, suppose you have two variables. Then, the first principal component minimizes the sum of squared perpendicular distances from the points to the first principal axis. This contrasts with least squares, which would minimize the sum of squared vertical distances from the points to the fitted line.

Principal component analysis can also be used for exploring polynomial relationships and for multivariate outlier detection (Gnanadesikan 1977), and it is related to factor analysis, correspondence analysis, allometry, and biased regression techniques (Mardia, Kent, and Bibby 1979).

### **Getting Started: PRINCOMP Procedure**

The following data provide crime rates per 100,000 people in seven categories for each of the 50 US states in 1977. Because there are seven numeric variables, it is impossible to plot all the variables simultaneously. You can use principal components to summarize the data in two or three dimensions, and they help you visualize the data. The following statements produce Figure 93.1 through Figure 93.5:

```
title 'Crime Rates per 100,000 Population by State';
data Crime;
   input State $1-15 Murder Rape Robbery Assault
          Burglary Larceny Auto_Theft;
   datalines;
Alabama
                14.2 25.2 96.8 278.3 1135.5 1881.9 280.7
               10.8 51.6 96.8 284.0 1331.7 3369.8 753.3
Alaska
Arizona
                9.5 34.2 138.2 312.3 2346.1 4467.4 439.5
Arkansas 8.8 27.6 83.2 203.4 972.6 1862.1 183.4 California 11.5 49.4 287.0 358.0 2139.4 3499.8 663.5
Connecticut
                4.2 16.8 129.5 131.8 1346.0 2620.7 593.2
Delaware 6.0 24.9 157.0 194.2 1682.6 3678.4 467.0 Florida 10.2 39.6 187.9 449.1 1859.9 3840.5 351.4 Georgia 11.7 31.1 140.5 256.5 1351.1 2170.2 297.9 Hawaii 7.2 25.5 128.0 64.1 1911.5 3920.4 489.4
                 7.2 25.5 128.0 64.1 1911.5 3920.4 489.4
Hawaii
Idaho
Illinois
                  5.5 19.4 39.6 172.5 1050.8 2599.6 237.6
                9.9 21.8 211.3 209.0 1085.0 2828.5 528.6
Indiana
                7.4 26.5 123.2 153.5 1086.2 2498.7 377.4
                2.3 10.6 41.2 89.8 812.5 2685.1 219.9
Iowa
                 6.6 22.0 100.7 180.5 1270.4 2739.3 244.3
Kansas
Kentucky 10.1 19.1 81.1 123.3 872.2 1662.1 245.4 Louisiana 15.5 30.9 142.9 335.5 1165.5 2469.9 337.7
Maine
                 2.4 13.5 38.7 170.0 1253.1 2350.7 246.9
Maryland 2.4 13.5 38.7 170.0 1253.1 2350.7 246.9 Maryland 8.0 34.8 292.1 358.9 1400.0 3177.7 428.5
Massachusetts 3.1 20.8 169.1 231.6 1532.2 2311.3 1140.1
               9.3 38.9 261.9 274.6 1522.7 3159.0 545.5
Michigan
                2.7 19.5 85.9 85.8 1134.7 2559.3 343.1
Minnesota
Mississippi 14.3 19.6 65.7 189.1 915.6 1239.9 144.4
                9.6 28.3 189.0 233.5 1318.3 2424.2 378.4
Missouri
                 5.4 16.7 39.2 156.8 804.9 2773.2 309.2
Montana
                3.9 18.1 64.7 112.7 760.0 2316.1 249.1
Nebraska
               15.8 49.1 323.1 355.0 2453.1 4212.6 559.2
Nevada
New Hampshire 3.2 10.7 23.2 76.0 1041.7 2343.9 293.4
New Jersey
                5.6 21.0 180.4 185.1 1435.8 2774.5 511.5
                 8.8 39.1 109.6 343.4 1418.7 3008.6 259.5
New Mexico
New York 10.7 29.4 472.6 319.1 1728.0 2782.0 745.8
North Carolina 10.6 17.0 61.3 318.3 1154.1 2037.8 192.1
```

```
North Dakota
               0.9 9.0 13.3 43.8 446.1 1843.0 144.7
Ohio
              7.8 27.3 190.5 181.1 1216.0 2696.8 400.4
             8.6 29.2 73.8 205.0 1288.2 2228.1 326.8
Oklahoma
              4.9 39.9 124.1 286.9 1636.4 3506.1 388.9
Oregon
Pennsylvania 5.6 19.0 130.3 128.0 877.5 1624.1 333.2
Rhode Island 3.6 10.5 86.5 201.0 1489.5 2844.1 791.4
South Carolina 11.9 33.0 105.9 485.3 1613.6 2342.4 245.1
South Dakota 2.0 13.5 17.9 155.7 570.5 1704.4 147.5
Tennessee 10.1 29.7 145.8 203.9 1259.7 1776.5 314.0
            13.3 33.8 152.4 208.2 1603.1 2988.7 397.6
Texas
              3.5 20.3 68.8 147.3 1171.6 3004.6 334.5
Utah
             1.4 15.9 30.8 101.2 1348.2 2201.0 265.2
Vermont
Virginia
             9.0 23.3 92.1 165.7 986.2 2521.2 226.7
Washington
             4.3 39.6 106.2 224.8 1605.6 3386.9 360.3
West Virginia 6.0 13.2 42.2 90.9 597.4 1341.7 163.3
Wisconsin
               2.8 12.9 52.2 63.7 846.9 2614.2 220.7
             5.4 21.9 39.7 173.9 811.6 2772.2 282.0
Wyoming
ods graphics on;
proc princomp out=Crime_Components plots= score(ellipse ncomp=3);
  id State;
run;
```

Figure 93.1 displays the PROC PRINCOMP output, beginning with simple statistics and followed by the correlation matrix. By default, the PROC PRINCOMP statement requests principal components that are computed from the correlation matrix, so the total variance is equal to the number of variables, 7.

Figure 93.1 Number of Observations and Simple Statistics from the PRINCOMP Procedure

#### Crime Rates per 100,000 Population by State

#### The PRINCOMP Procedure

Observations 50 7 Variables

	Simple Statistics						
	Murder	Rape	Robbery	Assault	Burglary	Larceny	Auto_Theft
Mean	7.444000000	25.73400000	124.0920000	211.3000000	1291.904000	2671.288000	377.5260000
StD	3.866768941	10.75962995	88.3485672	100.2530492	432.455711	725.908707	193.3944175

	Correlation Matrix						
	Murder	Rape	Robbery	Assault	Burglary	Larceny	Auto_Theft
Murder	1.0000	0.6012	0.4837	0.6486	0.3858	0.1019	0.0688
Rape	0.6012	1.0000	0.5919	0.7403	0.7121	0.6140	0.3489
Robbery	0.4837	0.5919	1.0000	0.5571	0.6372	0.4467	0.5907
Assault	0.6486	0.7403	0.5571	1.0000	0.6229	0.4044	0.2758
Burglary	0.3858	0.7121	0.6372	0.6229	1.0000	0.7921	0.5580
Larceny	0.1019	0.6140	0.4467	0.4044	0.7921	1.0000	0.4442
Auto_Theft	0.0688	0.3489	0.5907	0.2758	0.5580	0.4442	1.0000

Figure 93.2 displays the eigenvalues. The first principal component accounts for about 58.8% of the total variance, the second principal component accounts for about 17.7%, and the third principal component accounts for about 10.4%. Note that the eigenvalues sum to the total variance.

The eigenvalues indicate that two or three components provide a good summary of the data: two components account for 76% of the total variance, and three components account for 87%. Subsequent components account for less than 5% each.

=: 000	D 11 (D) 1 1		DDGG DDILLGGLID
<b>Figure 93.2</b>	Results of Principal	Component Analysis:	PROC PRINCOMP

Eigenvalues of the Correlation Matrix					
Eigenvalue	Difference	Proportion	Cumulative		
<b>1</b> 4.11495951	2.87623768	0.5879	0.5879		
<b>2</b> 1.23872183	0.51290521	0.1770	0.7648		
<b>3</b> 0.72581663	0.40938458	0.1037	0.8685		
<b>4</b> 0.31643205	0.05845759	0.0452	0.9137		
<b>5</b> 0.25797446	0.03593499	0.0369	0.9506		
<b>6</b> 0.22203947	0.09798342	0.0317	0.9823		
<b>7</b> 0.12405606		0.0177	1.0000		

Figure 93.3 displays the eigenvectors. From the eigenvectors matrix, you can represent the first principal component, Prin1, as a linear combination of the original variables:

$$\begin{array}{lll} {\sf Prin1} = & 0.300279 \times {\sf Murder} \\ & + & 0.431759 \times {\sf Rape} \\ & + & 0.396875 \times {\sf Robbery} \\ & \cdot & \cdot \\ & \cdot & \cdot \\ & + & 0.295177 \times {\sf Auto\_Theft} \end{array}$$

Similarly, the second principal component, Prin2, is

$$\begin{array}{lll} {\sf Prin2} = & - & 0.629174 \times {\sf Murder} \\ & - & 0.169435 \times {\sf Rape} \\ & + & 0.042247 \times {\sf Robbery} \\ & \cdot & \cdot \\ & \cdot & \cdot \\ & - & 0.502421 \times {\sf Auto\_Theft} \end{array}$$

where the variables are standardized.

			Eigenve	ectors			
	Prin1	Prin2	Prin3	Prin4	Prin5	Prin6	Prin7
Murder	0.300279	629174	0.178245	232114	0.538123	0.259117	0.267593
Rape	0.431759	169435	244198	0.062216	0.188471	773271	296485
Robbery	0.396875	0.042247	0.495861	557989	519977	114385	003903
Assault	0.396652	343528	069510	0.629804	506651	0.172363	0.191745
Burglary	0.440157	0.203341	209895	057555	0.101033	0.535987	648117
Larceny	0.357360	0.402319	539231	234890	0.030099	0.039406	0.601690
Auto Theft	0.295177	0.502421	0.568384	0.419238	0.369753	057298	0.147046

Figure 93.3 Results of Principal Component Analysis: PROC PRINCOMP

The first component is a measure of the overall crime rate because the first eigenvector shows approximately equal loadings on all variables. The second eigenvector has high positive loadings on the variables Auto Theft and Larceny and high negative loadings on the variables Murder and Assault. There is also a small positive loading on the variable Burglary and a small negative loading on the variable Rape. This component seems to measure the preponderance of property crime compared to violent crime. The interpretation of the third component is not obvious.

The ODS GRAPHICS statement enables the creation of graphs. For more information, see Chapter 21, "Statistical Graphics Using ODS." The option PLOTS=SCORE(ELLIPSE NCOMP=3) in the PROC PRINCOMP statement requests the pairwise component score plots for the first three components, with a 95% prediction ellipse overlaid on each scatter plot. Figure 93.4 shows the plot of the first two components. You can identify regional trends in the plot of the first two components. Nevada and California are at the extreme right, with high overall crime rates but an average ratio of property crime to violent crime. North Dakota and South Dakota are at the extreme left, with low overall crime rates. Southeastern states tend to be at the bottom of the plot, with a higher-than-average ratio of violent crime to property crime. New England states tend to be in the upper part of the plot, with a higher-than-average ratio of property crime to violent crime. Assuming that the first two components are from a bivariate normal distribution, the ellipse identifies Nevada as a possible outlier.

Figure 93.5 shows the plot of the first and third components. Assuming that the first and third components are from a bivariate normal distribution, the ellipse identifies Nevada, Massachusetts, and New York as possible outliers.

The most striking feature of the plot of the first and third principal components is that Massachusetts and New York are outliers on the third component.

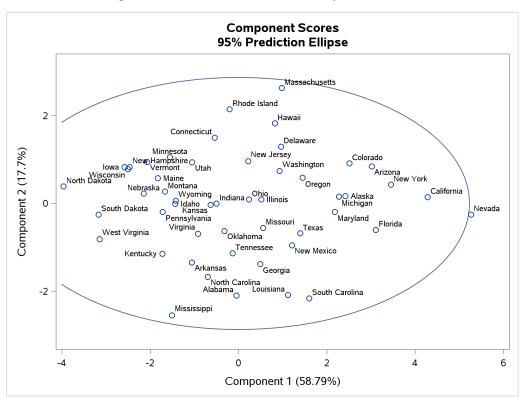
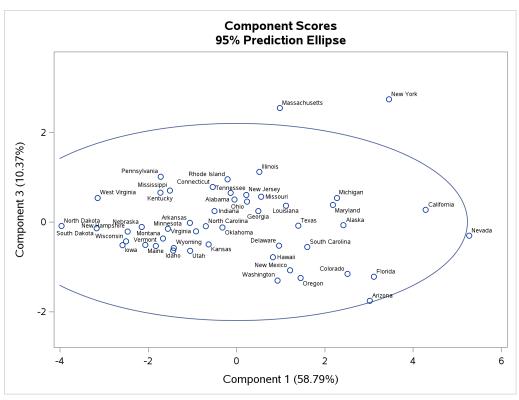


Figure 93.4 Plot of the First Two Component Scores

Figure 93.5 Plot of the First and Third Component Scores



### **Syntax: PRINCOMP Procedure**

The following statements are available in the PRINCOMP procedure:

```
PROC PRINCOMP < options > ;
   BY variables;
   FREQ variable;
   ID variables;
   PARTIAL variables;
   VAR variables;
   WEIGHT variable;
```

Usually only the VAR statement is used in addition to the PROC PRINCOMP statement. The rest of this section provides detailed syntax information for each of the preceding statements, beginning with the PROC PRINCOMP statement. The remaining statements are described in alphabetical order.

#### **PROC PRINCOMP Statement**

```
PROC PRINCOMP < options> ;
```

The PROC PRINCOMP statement invokes the PRINCOMP procedure. Optionally, it also identifies input and output data sets, specifies the analyses that are performed, and controls displayed output. Table 93.1 summarizes the options available in the PROC PRINCOMP statement.

Table 93.1 Summary of PROC PRINCOMP Statement Options

Option	Description
Specify Data Se	ets
DATA=	Specifies the name of the input data set
OUT=	Specifies the name of the output data set
OUTSTAT=	Specifies the name of the output data set that contains various statistics
<b>Specify Details</b>	of Analysis
COV	Computes the principal components from the covariance matrix
N=	Specifies the number of principal components to be computed
NOINT	Omits the intercept from the model
PREFIX=	Specifies a prefix for naming the principal components
PARPREFIX=	Specifies a prefix for naming the residual variables
SINGULAR=	Specifies the singularity criterion
STD	Standardizes the principal component scores
VARDEF=	Specifies the divisor used in calculating variances and standard deviations
Suppress the D	isplay of Output
NOPRINT	Suppresses the display of all output
Specify ODS G	raphics Details
PLOTS=	Specifies options that control the details of the plots

The following list provides details about these *options*.

#### **COVARIANCE**

#### COV

computes the principal components from the covariance matrix. If you omit the COV option, the correlation matrix is analyzed. The COV option causes variables that have large variances to be more strongly associated with components that have large eigenvalues, it and causes variables that have small variances to be more strongly associated with components that have small eigenvalues. You should not specify the COV option unless the units in which the variables are measured are comparable or the variables are standardized in some way.

#### DATA=SAS-data-set

specifies the SAS data set to be analyzed. The data set can be an ordinary SAS data set or a TYPE=ACE, TYPE=CORR, TYPE=COV, TYPE=FACTOR, TYPE=SSCP, TYPE=UCORR, or TYPE=UCOV data set (see Appendix A, "Special SAS Data Sets"). Also, the PRINCOMP procedure can read the \_TYPE\_='COVB' matrix from a TYPE=EST data set. If you omit the DATA= option, the procedure uses the most recently created SAS data set.

#### N=number

specifies the number of principal components to be computed. The default is the number of variables. The value of the N= option must be an integer greater than or equal to 0.

#### **NOINT**

omits the intercept from the model. In other words, the NOINT option requests that the covariance or correlation matrix not be corrected for the mean. When you specify the NOINT option, the covariance matrix and, hence, the standard deviations are not corrected for the mean.

If you use a TYPE=SSCP data set as input to the PRINCOMP procedure and list the variable Intercept in the VAR statement, the procedure acts as if you had also specified the NOINT option. If you use the NOINT option and also create an OUTSTAT= data set, the data set is TYPE=UCORR or TYPE=UCOV rather than TYPE=CORR or TYPE=COV.

#### **NOPRINT**

suppresses the display of all output. This option temporarily disables the Output Delivery System (ODS). For more information about ODS, see Chapter 20, "Using the Output Delivery System."

#### **OUT=**SAS-data-set

creates an output SAS data set to contain all the original data in addition to the principal component scores.

If you want to create a SAS data set in a permanent library, you must specify a two-level name. For more information about permanent libraries and SAS data sets, see *SAS Language Reference: Concepts*. For information about OUT= data sets, see the section "Output Data Sets" on page 7620.

#### OUTSTAT=SAS-data-set

creates an output SAS data set to contain means, standard deviations, number of observations, correlations or covariances, eigenvalues, and eigenvectors. If you specify the COV option, the data set is TYPE=COV or TYPE=UCOV, depending on the NOINT option, and it contains covariances; otherwise, the data set is TYPE=CORR or TYPE=UCORR, depending on the NOINT option, and it contains correlations. If you specify the PARTIAL statement, the OUTSTAT= data set also contains R squares.

If you want to create a SAS data set in a permanent library, you must specify a two-level name. For more information about permanent libraries and SAS data sets, see *SAS Language Reference: Concepts*. For more information about OUTSTAT= data sets, see the section "Output Data Sets" on page 7620.

```
PLOTS < (global-plot-options) > <= plot-request < (options) >>
```

PLOTS < (global-plot-options) > <= (plot-request < (options) > < ... plot-request < (options) > >) > controls the plots that are produced through ODS Graphics. When you specify only one plot request, you can omit the parentheses around the plot request. Here are some examples:

```
plots=none
plots=(scatter pattern)
plots(unpack)=scree
plots(ncomp=3 flip)=(pattern(circles=0.5 1.0) score)
```

ODS Graphics must be enabled before plots can be requested. For example:

```
ods graphics on;
proc princomp plots=all;
  var x1--x10;
run;
ods graphics off;
```

For more information about enabling and disabling ODS Graphics, see the section "Enabling and Disabling ODS Graphics" on page 615 in Chapter 21, "Statistical Graphics Using ODS."

If ODS Graphics is enabled but you do not specify the PLOTS= option, PROC PRINCOMP produces the scree plot by default.

You can specify the following *global-plot-options*:

#### **FLIP**

flips or interchanges the X-axis and Y-axis dimensions of the component score plots and the component pattern plots. For example, if you have three components, the default plots (y \* x) are Component 2 \* Component 1, Component 3 \* Component 1, and Component 3 \* Component 2. When you specify PLOTS(FLIP), the plots are Component 1 \* Component 2, Component 1 \* Component 3, and Component 2 \* Component 3.

#### NCOMP=n

specifies the number of components  $n(\geq 2)$  to be plotted for the component pattern plots and the component score plots. If you specify the NCOMP= option again in an individual plot, such as PLOTS=SCORE(NCOMP= m), the value m determines the number of components to be plotted in the component score plots. Be aware that the number of plots  $(n \times (n-1)/2)$  that are produced grows quadratically when n increases. The default is 5 or the total number of components  $m(\geq 2)$ , whichever is smaller. If n > m, NCOMP=m is used.

#### **ONLY**

suppresses the default plots. Only plots that you specifically request are displayed.

#### UNPACKPANEL

#### **UNPACK**

suppresses paneling in the scree plot. By default, multiple plots can appear in an output panel. Specify UNPACKPANEL to get each plot to appear in a separate panel. You can specify PLOTS(UNPACKPANEL) to unpack the default plots. You can also specify UNPACKPANEL as a suboption with the SCREE option (such as PLOTS=SCREE(UNPACKPANEL)).

You can specify the following *plot-requests*:

#### **ALL**

produces all appropriate plots. You can specify other options along with ALL; for example, to request all plots and unpack only the scree plot, specify PLOTS=(ALL SCREE(UNPACKPANEL)).

#### EIGEN | EIGENVALUE | SCREE < (UNPACKPANEL) >

produces the scree plot of eigenvalues and proportion variance explained. By default, both plots appear in the same panel. Specify PLOTS= SCREE(UNPACKPANEL) to get each plot to appear in a separate panel.

#### **MATRIX**

produces the matrix plot of principal component scores.

#### **NONE**

suppresses the display of all graphics output.

#### PATTERN < (pattern-options) >

produces the pairwise component pattern plots. Each variable is plotted as an observation whose coordinates are correlations between the variable and the two corresponding components in the plot. Use the NCOMP= option (for instance, PLOTS=PATTERN(NCOMP=3)) as described in the following list to control the number of plots to display.

You can specify the following pattern-options:

#### CIRCLES < = number-list >

plots the variance percentage circles. For each number c ( $0 < c \le 1$ ) that is specified, a ( $c \times 100\%$ ) variance circle is displayed. For each number c (c > 1) that is specified, a c% variance circle is displayed. You can specify either CIRCLES=0.05 1 or CIRCLES=5 100 to display 5% and 100% variance circles. PLOTS=PATTERN(CIRCLES) and PLOTS=PATTERN(VECTOR) both display a unit circle (100% variance). By default, no circle is displayed when you specify PLOTS=PATTERN.

#### **FLIP**

flips or interchanges the X-axis and Y-axis dimensions of the component pattern plots. Specify PLOTS=PATTERN(FLIP) to flip the X-axis and Y-axis dimensions.

#### NCOMP=n

specifies the number of components  $n \ge 2$  to be plotted. The default is 5 or the total number of components  $m \ge 2$ , whichever is smaller. If n > m, NCOMP=m is used. Be aware that the number of plots  $(n \times (n-1)/2)$  that are produced grows quadratically when n increases.

**VECTOR** 

plots the pattern in a vector form.

#### PATTERNPROFILE | PROFILE

produces the pattern profile plot. Each component has its own profile. The Y-axis value represents the correlation between the variable (corresponding to the X-axis value) and the profiled principal component.

#### SCORE < (score-options) >

produces the pairwise component score plots. Use the NCOMP= option (for example, PLOTS=SCORE(NCOMP=3)) as described in the following list to control the number of plots to display.

You can specify the following score-options.

#### ALPHA=number list

specifies a list of numbers for the prediction ellipses to be displayed in the score plots. Each value ( $\alpha$ ) in the list must be greater than 0. If  $\alpha$  is greater than or equal to 1, it is interpreted as a percentage and divided by 100; ALPHA=0.05 and ALPHA=5 are equivalent.

#### **ELLIPSE**

requests prediction ellipses for the principal component scores of a new observation to be created in the principal component score plots. For information about the computation of a prediction ellipse, see the section "Confidence and Prediction Ellipses" in "The CORR Procedure" (Base SAS Procedures Guide: Statistical Procedures).

#### **FLIP**

flips or interchanges the X-axis and Y-axis dimensions of the component score plots. Specify PLOTS=SCORE(FLIP) to flip the X-axis and Y-axis dimensions.

#### NCOMP=n

specifies the number of components  $n \ge 2$  to be plotted. The default is 5 or the total number of components  $m \ge 2$ , whichever is smaller. If n > m, NCOMP=m is used. Be aware that the number of plots  $(n \times (n-1)/2)$  that are produced grows quadratically when n increases.

#### PAINT <=position>

creates plots of component *i* versus component *j*, painted by component *k*. When you have at least three components, the PLOTS=SCORE option is specified, and the PAINT option is not specified, a painted score plot for component 3 versus component 2, painted by component 1, is produced. Use the PAINT option when you want to create painted score plots that involve other triples of components.

PLOTS=SCORE(PAINT), PLOTS=SCORE(PAINT=F), and PLOTS=SCORE(PAINT=FIRST) are all equivalent and create painted plots of  $i \times j$ , painted by k for triples (i, j, k), where k < j < i.

PLOTS=SCORE(PAINT=L) and PLOTS=SCORE(PAINT=LAST) are equivalent and create painted plots of  $i \times j$ , painted by k for triples (i, j, k), where j < i < k.

PLOTS=SCORE(PAINT=M) and PLOTS=SCORE(PAINT=MIDDLE) are equivalent and create painted plots of  $i \times j$ , painted by k for triples (i, j, k), where j < k < i.

#### PREFIX=name

specifies a prefix for naming the principal components. By default, the names are Prin1, Prin2, ..., Prinn. If you specify PREFIX=Abc, the components are named Abc1, Abc2, Abc3, and so on. The number of characters in the prefix plus the number of digits required to designate the variables should not exceed the current name length that is defined by the VALIDVARNAME= system option.

#### **PARPREFIX**=name

#### **PPREFIX**=name

#### RPREFIX=name

specifies a prefix for naming the residual variables in the OUT= data set and the OUTSTAT= data set. By default, the prefix is R\_. The number of characters in the prefix plus the maximum length of the variable names should not exceed the current name length that is defined by the VALIDVARNAME= system option.

#### SINGULAR=p

#### SING=p

specifies the singularity criterion, where 0 . If a variable in a PARTIAL statement has an R square as large as <math>1 - p when predicted from the variables listed before it in the statement, the variable is assigned a standardized coefficient of 0. By default, SINGULAR=1E-8.

#### **STANDARD**

#### STD

standardizes the principal component scores in the OUT= data set and in plots to unit variance. If you omit the STANDARD option, the scores have variance equal to the corresponding eigenvalue. Note that the STANDARD option has no effect on the eigenvalues themselves.

#### VARDEF=DF | N | WDF | WEIGHT | WGT

specifies the divisor to be used in calculating variances and standard deviations. By default, VARDEF=DF. The following table displays the values and associated divisors:

Value	Divisor	Formula	
DF	Error degrees of freedom	n-i	(before partialing)
		n-p-i	(after partialing)
N	Number of observations	n	
WEIGHT   WGT	Sum of weights	$\sum_{j=1}^{n} w_j$	
WDF	Sum of weights minus one	$\left(\sum_{j=1}^{n} w_{j}\right) - i$ $\left(\sum_{j=1}^{n} w_{j}\right) - p - i$	(before partialing)
		$\left(\sum_{j=1}^{n} w_j\right) - p - i$	(after partialing)

In the formulas for VARDEF=DF and VARDEF=WDF, p is the number of degrees of freedom of the variables in the PARTIAL statement, and i is 0 if the NOINT option is specified and 1 otherwise.

#### **BY Statement**

#### BY variables:

You can specify a BY statement with PROC PRINCOMP to obtain separate analyses of observations in groups that are defined by the BY variables. When a BY statement appears, the procedure expects the input data set to be sorted in order of the BY variables. If you specify more than one BY statement, only the last one specified is used.

If your input data set is not sorted in ascending order, use one of the following alternatives:

- Sort the data by using the SORT procedure with a similar BY statement.
- Specify the NOTSORTED or DESCENDING option in the BY statement for the PRINCOMP procedure. The NOTSORTED option does not mean that the data are unsorted but rather that the data are arranged in groups (according to values of the BY variables) and that these groups are not necessarily in alphabetical or increasing numeric order.
- Create an index on the BY variables by using the DATASETS procedure (in Base SAS software).

For more information about BY-group processing, see the discussion in SAS Language Reference: Concepts. For more information about the DATASETS procedure, see the discussion in the Base SAS Procedures Guide.

#### **FREQ Statement**

#### FREQ variable;

The FREQ statement specifies a variable that provides frequencies for each observation in the DATA= data set. Specifically, if n is the value of the FREQ variable for a given observation, then that observation is used n times.

The analysis that you produce by using a FREQ statement reflects the expanded number of observations. The total number of observations is considered to be equal to the sum of the FREQ variable. You could produce the same analysis (without the FREQ statement) by first creating a new data set that contains the expanded number of observations. For example, if the value of the FREQ variable is 5 for the first observation, the first five observations in the new data set are identical. Each observation in the old data set would be replicated  $n_i$  times in the new data set, where  $n_i$  is the value of the FREQ variable for that observation.

If the value of the FREQ variable is missing or is less than 1, the observation is not used in the analysis. If the value is not an integer, only the integer portion is used.

#### ID Statement

#### ID variables;

The ID statement labels observations by using values from the first ID variable in the principal component score plot. If one or more ID variables are specified, their values are displayed in tooltips of the component score plot and the matrix plot of component scores.

#### **PARTIAL Statement**

#### **PARTIAL** variables:

If you want to analyze a partial correlation or covariance matrix, specify the names of the numeric variables to be partialed out in the PARTIAL statement. The PRINCOMP procedure computes the principal components of the residuals from the prediction of the VAR variables by the PARTIAL variables. If you request an OUT= or OUTSTAT= data set, the residual variables are named by prefixing the characters R\_ by default or the string specified in the PARPREFIX= option to the VAR variables.

#### **VAR Statement**

#### **VAR** variables:

The VAR statement lists the numeric variables to be analyzed. If you omit the VAR statement, all numeric variables not specified in other statements are analyzed. However, if the DATA= data set is TYPE=SSCP, the default set of variables used as VAR variables does not include Intercept so that the correlation or covariance matrix is constructed correctly. If you want to analyze Intercept as a separate variable, you should specify it in the VAR statement.

#### **WEIGHT Statement**

#### **WEIGHT** variable;

To use relative weights for each observation in the input data set, place the weights in a variable in the data set and specify the name in a WEIGHT statement. This is often done when the variance associated with each observation is different and the values of the weight variable are proportional to the reciprocals of the variances.

The observation is used in the analysis only if the value of the WEIGHT statement variable is nonmissing and is greater than 0.

### **Details: PRINCOMP Procedure**

### Missing Values

Observations that have missing values for any variable in the VAR, PARTIAL, FREQ, or WEIGHT statement are omitted from the analysis and are given missing values for principal component scores in the OUT= data set. If a correlation, covariance, or SSCP matrix is read, it can contain missing values as long as every pair of variables has at least one nonmissing entry.

### **Output Data Sets**

#### **OUT= Data Set**

The OUT= data set contains all the variables in the original data set plus new variables that contain the principal component scores. The N= option determines the number of new variables. The names of the new variables are formed by concatenating the value given by the PREFIX= option (or Prin if PREFIX= is omitted) to the numbers 1, 2, 3, and so on. The new variables have mean 0 and variance equal to the corresponding eigenvalue, unless you specify the STANDARD option to standardize the scores to unit variance. Also, if you specify the COV option, PROC PRINCOMP computes the principal component scores from the corrected or uncorrected (if the NOINT option is specified) variables rather than from the standardized variables.

If you use a PARTIAL statement, the OUT= data set also contains the residuals from predicting the VAR variables from the PARTIAL variables.

You cannot create an OUT= data set if the DATA= data set is TYPE=ACE, TYPE=CORR, TYPE=COV, TYPE=EST, TYPE=FACTOR, TYPE=SSCP, TYPE=UCORR, or TYPE=UCOV.

#### OUTSTAT= Data Set

The OUTSTAT= data set is similar to the TYPE=CORR data set that the CORR procedure produces. The following table relates the TYPE= value for the OUTSTAT= data set to the options that are specified in the PROC PRINCOMP statement:

Options	TYPE=
(Default)	CORR
COV	COV
NOINT	UCORR
COV NOINT	UCOV

Note that the default (neither the COV nor NOINT option) produces a TYPE=CORR data set.

The new data set contains the following variables:

- the BY variables, if any
- two new variables, \_TYPE\_ and \_NAME\_, both character variables
- the variables that are analyzed (that is, those in the VAR statement); or, if there is no VAR statement, all numeric variables not listed in any other statement; or, if there is a PARTIAL statement, the residual variables as described in the section "OUT= Data Set" on page 7620

Each observation in the new data set contains some type of statistic, as indicated by the TYPE variable. The values of the TYPE variable are as follows:

#### \_TYPE\_ **Contents**

**MEAN** mean of each variable. If you specify the PARTIAL statement, this observation is omitted. STD

standard deviations. If you specify the COV option, this observation is omitted, so the SCORE procedure does not standardize the variables before computing scores. If you use the PARTIAL statement, the standard deviation of a variable is computed as its root mean squared error as predicted from the PARTIAL variables.

**USTD** 

uncorrected standard deviations. When you specify the NOINT option in the PROC PRINCOMP statement, the OUTSTAT= data set contains standard deviations not corrected for the mean. However, if you also specify the COV option in the PROC PRINCOMP statement, this observation is omitted.

N

number of observations on which the analysis is based. This value is the same for each variable. If you specify the PARTIAL statement and the value of the VARDEF= option is DF or unspecified, then the number of observations is decremented by the degrees of freedom of the PARTIAL variables.

**SUMWGT** 

the sum of the weights of the observations. This value is the same of each variable. If you specify the PARTIAL statement and VARDEF=WDF, then the sum of the weights is decremented by the degrees of freedom of the PARTIAL variables. This observation is output only if the value is different from that in the observation for which \_TYPE\_='N'.

**CORR** 

correlations between each variable and the variable specified by the \_NAME\_ variable. The number of observations for which \_TYPE\_='CORR' is equal to the number of variables being analyzed. If you specify the COV option, no \_TYPE\_='CORR' observations are produced. If you use the PARTIAL statement, the partial correlations, not the raw correlations, are output.

**UCORR** 

uncorrected correlation matrix. When you specify the NOINT option without the COV option in the PROC PRINCOMP statement, the OUTSTAT= data set contains a matrix of correlations not corrected for the means. However, if you also specify the COV option in the PROC PRINCOMP statement, this observation is omitted.

COV

covariances between each variable and the variable specified by the \_NAME\_ variable. \_TYPE\_='COV' observations are produced only if you specify the COV option. If you use the PARTIAL statement, the partial covariances, not the raw covariances, are output.

**UCOV** 

uncorrected covariance matrix. When you specify the NOINT and COV options in the PROC PRINCOMP statement, the OUTSTAT= data set contains a matrix of covariances not corrected for the means.

**EIGENVAL** 

eigenvalues. If the N= option requests fewer principal components than the maximum number, only the specified number of eigenvalues is produced, with missing values filling out the observation.

**SCORE** 

eigenvectors. The \_NAME\_ variable contains the name of the corresponding principal component as constructed from the PREFIX= option. The number of observations for which \_TYPE\_='SCORE' equals the number of principal components computed. The eigenvectors have unit length unless you specify the STD option, in which case the unit-length eigenvectors are divided by the square roots of the eigenvalues to produce scores that have unit standard deviations.

When you do not specify the COV option, you can produce the principal component scores by multiplying the standardized data by these coefficients. When you specify the COV option, you can produce the principal component scores by multiplying the centered data by these coefficients. You should use the means, obtained from the observation

USCORE scoring coefficients to be applied without subtracting the mean from the raw variables.

Observations for which \_TYPE\_='USCORE' are produced when you specify the NOINT

option in the PROC PRINCOMP statement.

To obtain the principal component scores, these coefficients should be multiplied by the data that are standardized by the uncorrected standard deviations obtained from the

observation for which \_TYPE\_='USTD'.

RSQUARED R squares for each VAR variable as predicted by the PARTIAL variables

B regression coefficients for each VAR variable as predicted by the PARTIAL variables.

This observation is produced only if you specify the COV option.

STB standardized regression coefficients for each VAR variable as predicted by the PARTIAL

variables. If you specify the COV option, this observation is omitted.

You can use the data set with the SCORE procedure to compute principal component scores, or you can use it as input to the FACTOR procedure and specify METHOD=SCORE to rotate the components. If you use the PARTIAL statement, the scoring coefficients should be applied to the residuals, not to the original variables.

### **Computational Resources**

Let

n = number of observations

v = number of VAR variables

p = number of PARTIAL variables

c = number of components

• The minimum allocated memory required (in bytes) is

$$232v + 120p + 48c + \max(8cv, 8vp + 4(v + p)(v + p + 1))$$

• The time required to compute the correlation matrix is approximately proportional to

$$n(v+p)^2 + \frac{p}{2}(v+p)(v+p+1)$$

- The time required to compute eigenvalues is approximately proportional to  $v^3$ .
- The time required to compute eigenvectors is approximately proportional to  $cv^2$ .

### **Displayed Output**

The PRINCOMP procedure displays the following items if the DATA= data set is not TYPE=CORR, TYPE=COV, TYPE=SSCP, TYPE=UCORR, or TYPE=UCOV:

- simple statistics, including the mean and standard deviation (StD) for each variable. If you specify the NOINT option, the uncorrected standard deviation (UStD) is displayed.
- the correlation or, if you specify the COV option, the covariance matrix

The PRINCOMP procedure displays the following items if you use the PARTIAL statement:

- regression statistics, giving the R square and root mean squared error (RMSE) for each VAR variable as predicted by the PARTIAL variables (not shown)
- standardized regression coefficients or, if you specify the COV option, regression coefficients for predicting the VAR variables from the PARTIAL variables (not shown)
- the partial correlation matrix or, if you specify the COV option, the partial covariance matrix (not shown)

The PRINCOMP procedure displays the following item if you specify the COV option:

• the total variance

The PRINCOMP procedure displays the following items unless you specify the NOPRINT option:

- eigenvalues of the correlation or covariance matrix, in addition to the difference between successive eigenvalues, the proportion of variance explained by each eigenvalue, and the cumulative proportion of variance explained
- the eigenvectors

#### **ODS Table Names**

PROC PRINCOMP assigns a name to each table that it creates. You can use these names to reference the ODS table when using the Output Delivery System (ODS) to select tables and create output data sets. These names are listed in Table 93.2. For more information about ODS, see Chapter 20, "Using the Output Delivery System."

All the tables are created by specifying the PROC PRINCOMP statement; a few tables need an additional PARTIAL statement.

ODS Table Name	Description	Statement / Option
Corr	Correlation matrix	Default
Cov	Covariance matrix	COV
Eigenvalues	Eigenvalues	Default
Eigenvectors	Eigenvectors	Default
NObsNVar	Number of observations, variables, and partial vari-	Default
	ables	
ParCorr	Partial correlation matrix	PARTIAL statement
ParCov	Uncorrected partial covariance matrix	PARTIAL statement and COV
RegCoef	Regression coefficients	PARTIAL statement and COV
RSquareRMSE	Regression statistics: R squares and RMSEs	PARTIAL statement
SimpleStatistics	Simple statistics	Default
StdRegCoef	Standardized regression coefficients	PARTIAL statement
TotalVariance	Total variance	COV

Table 93.2 ODS Tables Produced by PROC PRINCOMP

### **ODS Graphics**

Statistical procedures use ODS Graphics to create graphs as part of their output. ODS Graphics is described in detail in Chapter 21, "Statistical Graphics Using ODS."

Before you create graphs, ODS Graphics must be enabled (for example, by specifying the ODS GRAPH-ICS ON statement). For more information about enabling and disabling ODS Graphics, see the section "Enabling and Disabling ODS Graphics" on page 615 in Chapter 21, "Statistical Graphics Using ODS."

The overall appearance of graphs is controlled by ODS styles. Styles and other aspects of using ODS Graphics are discussed in the section "A Primer on ODS Statistical Graphics" on page 614 in Chapter 21, "Statistical Graphics Using ODS."

Some graphs are produced by default; other graphs are produced by using statements and options. You can reference every graph produced through ODS Graphics by name. The names of the graphs that PROC PRINCOMP generates are listed in Table 93.3, along with a description of each graph and the required statements and options.

	<u> </u>	
<b>ODS Graph Name</b>	Plot Description	Statement and Option
PaintedScorePlot	Score plot of component <i>i</i> versus component <i>j</i> , painted by component <i>k</i>	PLOTS=SCORE when number of variables > 3
PatternPlot	Component pattern plot	PLOTS=PATTERN
PatternProfilePlot	Component pattern profile plot	PLOTS=PATTERNPROFILE
ScoreMatrixPlot	Matrix plot of component scores	PLOTS=MATRIX
ScorePlot	Component score plot	PLOTS=SCORE
ScreePlot	Scree and variance plots	Default and PLOTS=SCREE
VariancePlot	Variance proportion explained plot	PLOTS=SCREE(UNPACKPANEL)

Table 93.3 Graphs Produced by PROC PRINCOMP

### **Examples: PRINCOMP Procedure**

### **Example 93.1: Analyzing Mean Temperatures of US Cities**

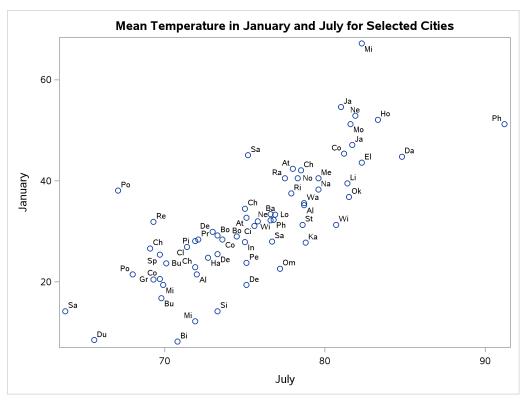
This example analyzes mean daily temperatures of selected US cities in January and July. Both the raw data and the principal components are plotted to illustrate that principal components are orthogonal rotations of the original variables.

The following statements create the Temperature data set:

The following statements plot the Temperature data set. The variable Cityid instead of City is used as a data label in the scatter plot to avoid label collisions.

```
title 'Mean Temperature in January and July for Selected Cities';
proc sgplot data=Temperature;
   scatter x=July y=January / datalabel=CityId;
run;
```

The results are displayed in Output 93.1.1, which shows a scatter plot of the 64 pairs of data points in which July temperatures are plotted against January temperatures.



Output 93.1.1 Plot of Raw Data

The following step requests a principal component analysis of the Temperature data set:

```
ods graphics on;
title 'Mean Temperature in January and July for Selected Cities';
proc princomp data=Temperature cov plots=score(ellipse);
  var July January;
  id CityId;
run;
```

Output 93.1.2 displays the PROC PRINCOMP output. The standard deviation of January (11.712) is higher than the standard deviation of July (5.128). The COV option in the PROC PRINCOMP statement requests that the principal components be computed from the covariance matrix. The total variance is 163.474. The first principal component accounts for about 94% of the total variance, and the second principal component accounts for only about 6%. The eigenvalues sum to the total variance.

Note that January receives a higher loading on Prin1 because it has a higher standard deviation than July. Also note that the PRINCOMP procedure calculates the scores by using the centered variables rather than the standardized variables.

Output 93.1.2 Results of Principal Component Analysis

#### Mean Temperature in January and July for Selected Cities

#### The PRINCOMP Procedure

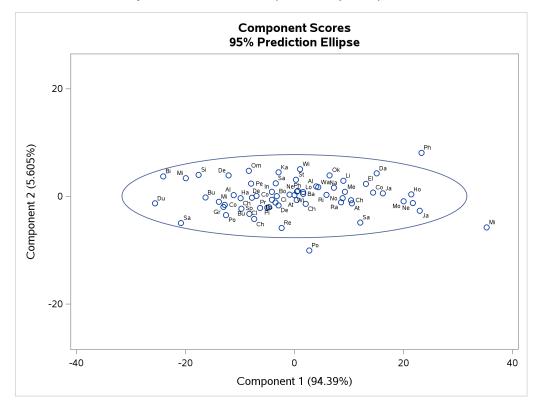
	Observation	s 64
	Variables	2
	Simple Stati	stics
	July	January
Mean	75.60781250	32.09531250
StD	5.12761910	11.71243309
	Covariance N	/latrix
	July	January
July	26.2924777	46.8282912
January	46.8282912	137.1810888

Eigenvalues of the Covariance Matrix								
	Eigenvalue	Difference	Proportion	Cumulative				
1	154.310607	145.147647	0.9439	0.9439				
2	9.162960		0.0561	1.0000				

**Total Variance** 163.47356647

Eigenvectors							
	Prin1	Prin2					
July	0.343532	0.939141					
January	0.939141	343532					

The PLOTS=SCORE option in the PROC PRINCOMP statement requests a plot of the second principal component against the first principal component, as shown in Output 93.1.3. It is clear from this plot that the principal components are orthogonal rotations of the original variables and that the first principal component has a larger variance than the second principal component. In fact, the first component has a larger variance than either of the original variables, July and January. The ellipse indicates that Miami, Phoenix, and Portland are possible outliers.



Output 93.1.3 Plot of Component 2 by Component 1

### Example 93.2: Analyzing Rankings of US College Basketball Teams

The data in this example are rankings of 35 US college basketball teams. The rankings were made before the start of the 1985–86 season by 10 news services. The purpose of the principal component analysis is to compute a single variable that best summarizes all 10 preseason rankings. Note that the various news services rank different numbers of teams, ranging from 20 to 30 (one of the variables, WashPost, has a missing rank). And, of course, not all news services rank the same teams, so there are missing values in these data. Each of the 35 teams is ranked by at least one news service.

The PRINCOMP procedure omits observations that have missing values. To obtain principal component scores for all the teams, you must replace the missing values. Because it is the best teams that are ranked, it is not appropriate to replace missing values with the mean of the nonmissing values. Instead, an ad hoc method is used that replaces missing values with the mean of the unassigned ranks. For example, if a news service ranks 20 teams, then ranks 21 through 35 are unassigned. The mean of ranks 21 through 35 is 28, so missing values for that variable are replaced by the value 28. To prevent the method of missing-value replacement from having an undue effect on the analysis, each observation is weighted according to the number of nonmissing values that it has. For an alternative analysis of these data, see Example 94.2 in Chapter 94, "The PRINQUAL Procedure."

Because the first principal component accounts for 78% of the variance, there is substantial agreement among the rankings. The eigenvector shows that all the news services are about equally weighted; this is also suggested by the nearly horizontal line of the pattern profile plot in Output 93.2.3. So a simple average would work almost as well as the first principal component. The following statements produce Output 93.2.1.

```
/*----*/
/*
/* Pre-season 1985 College Basketball Rankings
                                                         */
/* (rankings of 35 teams by 10 news services)
                                                        */
/*
                                                         */
/* Note: (a) news services rank varying numbers of teams; */
        (b) not all teams are ranked by all news services; */
/*
       (c) each team is ranked by at least one service; */
/*
       (d) rank 20 is missing for UPI.
                                                         */
/*
                                                         */
data HoopsRanks;
   input School $13. CSN DurSun DurHer WashPost USAToday
        Sport InSports UPI AP SI;
   label CSN = 'Community Sports News (Chapel Hill, NC)'
        DurSun = 'Durham Sun'
        DurHer = 'Durham Morning Herald'
        WashPost = 'Washington Post'
        USAToday = 'USA Today'
        Sport = 'Sport Magazine'
        InSports = 'Inside Sports'
        UPI = 'United Press International'
        AP
               = 'Associated Press'
        SI
               = 'Sports Illustrated'
   format CSN--SI 5.1;
   datalines;
Louisville 1 8 1 9 8 9 6 10 9 9 Georgia Tech 2 2 4 3 1 1 1 2 1 1
Kansas 3 4 5 1 5 11 8 4 5 7
Michigan 4 5 9 4 2 5 3 1 3 2
Michigan
Duke
            5 6 7 5 4 10 4 5 6 5
             6 1 2 2 3 4 2 3 2 3
UNC
Georgetown 12 7 8 6 9 2 9 8 8 4
Navy 13 20 23 10 18 13 15 . 20 .
Illinois 14 3 3 7 7 3 10 7 7 6
Iowa
           15 16 . . 23 . . 14 . 20
Arkansas 16 . . . 25 . . . . 16
Memphis State 17 . 11 . 16 8 20 . 15 12
UAB
     19 13 10 . 12 17 . 16 16 15
UNLV
           20 18 18 19 22 . 14 18 18 .
NC State 21 17 14 16 15 . 12 15 17 18 Maryland 22 . . . 19 . . . 19 14
Pittsburgh 23 . . . . . . . . .
Oklahoma 24 19 17 17 17 12 17 . 13 17 Indiana 25 12 20 18 21 . . . . .
```

```
Virginia
            26 . 22 . . 18 . . . .
Old Dominion 27 . . . .
Auburn 28 11 12 8 10 7 7 11 10 11
St. Johns 29 . . . 14 . . .
UCLA
                    . . . . 19 .
          30 . .
St. Joseph's . . 19 . . . . .
Tennessee . . 24 . . 16 .
Montana
Houston
            . . . 20 . . .
            . . . . 24 . . .
/* PROC MEANS is used to output a data set containing the
                                                        */
/* maximum value of each of the newspaper and magazine
                                                        */
/* rankings. The output data set, maxrank, is then used
                                                        */
/* to set the missing values to the next highest rank plus
                                                        */
/* thirty-six, divided by two (that is, the mean of the
                                                        */
/* missing ranks). This ad hoc method of replacing missing
                                                        */
/* values is based more on intuition than on rigorous
                                                        */
/* statistical theory. Observations are weighted by the
                                                        */
/* number of nonmissing values.
                                                        */
/*
                                                        */
title 'Pre-Season 1985 College Basketball Rankings';
proc means data=HoopsRanks;
  output out=MaxRank
        max=CSNMax DurSunMax DurHerMax
            WashPostMax USATodayMax SportMax
            InSportsMax UPIMax APMax SIMax;
run;
```

Output 93.2.1 Summary Statistics for Basketball Rankings from Using PROC MEANS

#### Pre-Season 1985 College Basketball Rankings

#### The MEANS Procedure

Variable	Label	Ν	Mean	Std Dev	Minimum	Maximum
CSN	Community Sports News (Chapel Hill, NC)	30	15.5000000	8.8034084	1.0000000	30.0000000
DurSun	Durham Sun	20	10.5000000	5.9160798	1.0000000	20.0000000
DurHer	Durham Morning Herald	24	12.5000000	7.0710678	1.0000000	24.0000000
WashPost	Washington Post	19	10.4210526	6.0673607	1.0000000	20.0000000
USAToday	USA Today	25	13.0000000	7.3598007	1.0000000	25.0000000
Sport	Sport Magazine	20	10.5000000	5.9160798	1.0000000	20.0000000
InSports	Inside Sports	20	10.5000000	5.9160798	1.0000000	20.0000000
UPI	United Press International	19	10.0000000	5.6273143	1.0000000	19.0000000
AP	Associated Press	20	10.5000000	5.9160798	1.0000000	20.0000000
SI	Sports Illustrated	20	10.5000000	5.9160798	1.0000000	20.0000000

The following statements produce Output 93.2.2 and Output 93.2.3:

```
data Basketball;
   set HoopsRanks;
   if _n_=1 then set MaxRank;
   array Services{10} CSN--SI;
   array MaxRanks{10} CSNMax--SIMax;
   keep School CSN--SI Weight;
   Weight=0;
   do i=1 to 10;
      if Services{i}=. then Services{i}=(MaxRanks{i}+36)/2;
      else Weight=Weight+1;
   end;
run;
ods graphics on;
proc princomp data=Basketball n=1 out=PCBasketball standard
              plots=patternprofile;
   var CSN--SI;
   weight Weight;
```

Output 93.2.2 Principal Component Analysis of Basketball Rankings by Using PROC PRINCOMP

#### Pre-Season 1985 College Basketball Rankings

#### The PRINCOMP Procedure

Observations 35 Variables 10

Simple Statistics								
	CSN	DurSun	DurHer	WashPost	USAToday	Sport		
Mean	13.33640553	13.06451613	12.88018433	13.83410138	12.55760369	13.83870968		
StD	22.08036285	21.66394183	21.38091837	23.47841791	20.48207965	23.37756267		

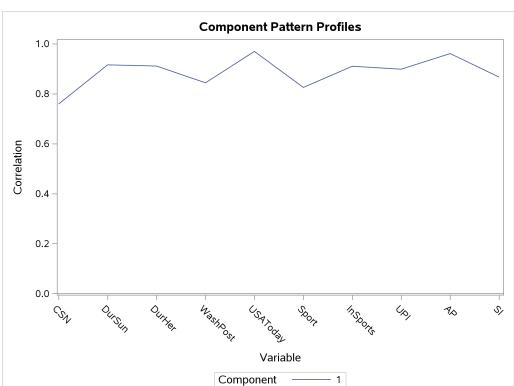
Simple Statistics								
	InSports	UPI	AP	SI				
Mean	13.24423963	13.59216590	12.83410138	13.52534562				
StD	22.20231526	23.25602811	21.40782406	22.93219584				

Output 93.2.2 continued

	Correlation Matrix										
		CSN	DurSun	DurHer	WashPost	USAToday	Sport	InSports	UPI	AP	SI
CSN	Community Sports News (Chapel Hill, NC)	1.0000	0.6505	0.6415	0.6121	0.7456	0.4806	0.6558	0.7007	0.6779	0.6135
DurSun	Durham Sun	0.6505	1.0000	0.8341	0.7667	0.8860	0.6940	0.7702	0.9015	0.8437	0.7518
DurHer	Durham Morning Herald	0.6415	0.8341	1.0000	0.7035	0.8877	0.7788	0.7900	0.7676	0.8788	0.7761
WashPost	Washington Post	0.6121	0.7667	0.7035	1.0000	0.7984	0.6598	0.8717	0.6953	0.7809	0.5952
USAToday	USA Today	0.7456	0.8860	0.8877	0.7984	1.0000	0.7716	0.8475	0.8539	0.9479	0.8426
Sport	Sport Magazine	0.4806	0.6940	0.7788	0.6598	0.7716	1.0000	0.7176	0.6220	0.8217	0.7701
InSports	Inside Sports	0.6558	0.7702	0.7900	0.8717	0.8475	0.7176	1.0000	0.7920	0.8830	0.7332
UPI	United Press International	0.7007	0.9015	0.7676	0.6953	0.8539	0.6220	0.7920	1.0000	0.8436	0.7738
AP	Associated Press	0.6779	0.8437	0.8788	0.7809	0.9479	0.8217	0.8830	0.8436	1.0000	0.8212
SI	Sports Illustrated	0.6135	0.7518	0.7761	0.5952	0.8426	0.7701	0.7332	0.7738	0.8212	1.0000

Eigenvalues of the Correlation Matrix							
Eigenvalue Differen	ce Proportion	Cumulative					
<b>1</b> 7.88601647	0.7886	0.7886					

	Eigenvectors	
		Prin1
CSN	Community Sports News (Chapel Hill, NC)	0.270205
DurSun	Durham Sun	0.326048
DurHer	Durham Morning Herald	0.324392
WashPost	Washington Post	0.300449
USAToday	USA Today	0.345200
Sport	Sport Magazine	0.293881
InSports	Inside Sports	0.324088
UPI	United Press International	0.319902
AP	Associated Press	0.342151
SI	Sports Illustrated	0.308570



Output 93.2.3 Pattern Profile Plot

The following statements produce Output 93.2.4:

```
proc sort data=PCBasketball;
   by Prin1;
run;

proc print;
  var School Prin1;
  title 'Pre-Season 1985 College Basketball Rankings';
  title2 'College Teams as Ordered by PROC PRINCOMP';
run;
```

### Pre-Season 1985 College Basketball Rankings College Teams as Ordered by PROC PRINCOMP

Obs	School	Prin1
1	Georgia Tech	-0.58068
2	UNC	-0.53317
3	Michigan	-0.47874
4	Kansas	-0.40285
5	Duke	-0.38464
6	Illinois	-0.33586
7	Syracuse	-0.31578
8	Louisville	-0.31489
9	Georgetown	-0.29735
10	Auburn	-0.09785
11	Kentucky	0.00843
12	LSU	0.00872
13	Notre Dame	0.09407
14	NC State	0.19404
15	UAB	0.19771
16	Oklahoma	0.23864
17	Memphis State	0.25319
18	Navy	0.28921
19	UNLV	0.35103
20	DePaul	0.43770
21	lowa	0.50213
22	Indiana	0.51713
23	Maryland	0.55910
24	Arkansas	0.62977
25	Virginia	0.67586
26	Washington	0.67756
27	Tennessee	0.70822
28	St. Johns	0.71425
29	Virginia Tech	0.71638
30	St. Joseph's	0.73492
31	UCLA	0.73965
32	Pittsburgh	0.75078
33	Houston	0.75534
	Montana	0.75790
35	Old Dominion	0.76821

### **Example 93.3: Analyzing Job Ratings of Police Officers**

This example uses the PRINCOMP procedure to analyze job performance. Police officers were rated by their supervisors in 14 categories as part of standard police department administrative procedure.

The following statements create the Jobratings data set:

```
options validvarname=any;
data Jobratings;
  input 'Communication Skills'n
                                  'Problem Solving'n
       'Learning Ability'n
                                  'Judgment Under Pressure'n
       'Observational Skills'n
                                 'Willingness to Confront Problems'n
       'Interest in People'n
                                 'Interpersonal Sensitivity'n
       'Desire for Self-Improvement'n 'Appearance'n
       'Dependability'n
                                  'Physical Ability'n
                                  'Overall Rating'n @@;
       'Integrity'n
  datalines;
2 6 8 3 8 8 5 3 8 7 9 8 6 7 7 4 7 5 8 8 7 6 8 5 7 6 6 7 5 6 7 5 7 8 6 3 7 7 5
8 8 8 7 9 9 8 9 9 9 9 8 8 9 8 9 9 7 9 8 8 7 7 9 4 7 9 8 4 6 8 8 8 6 3 5 6 5 2
  ... more lines ...
7899799799989989989976656399567486
```

The Jobratings data set contains 14 variables. Each variable contains the job ratings, which use a scale measurement from 1 to 10 (1=fail to comply, 10=exceptional). The last variable, Overall Rating, contains a score as an overall index of how each officer performs.

The following statements request a principal component analysis of the Jobratings data set, output the scores to the Scores data set (OUT= Scores), and produce default plots. Note that the variable Overall Rating is excluded from the analysis.

```
ods graphics on;
proc princomp data=Jobratings(drop='Overall Rating'n);
run;
```

Figure 93.3.1 and Figure 93.3.2 display the PROC PRINCOMP output, beginning with simple statistics and then the correlation matrix. By default, PROC PRINCOMP computes principal components from the correlation matrix, so the total variance is equal to the number of variables, 13. In this example, it would also be reasonable to use the COV option, which would cause variables that have a high variance (such as Dependability) to influence the results more than variables that have a low variance (such as Learning Ability). If you used the COV option, scores would be computed from centered rather than standardized variables.

Output 93.3.1 Simple Statistics and Correlation Matrix from Using PROC PRINCOMP

#### The PRINCOMP Procedure

Observations 103 Variables 13

	Simple Statistics								
	Communication Skills	Problem Solving	3	Judgment Under Pressure	Observational Skills	Willingness to Confront Problems	Interest in People		
Mean	6.650485437	6.631067961	6.990291262	6.737864078	6.932038835	7.291262136	6.708737864		
StD	1.764068036	1.590352602	1.339411238	1.731830976	1.761584269	1.525155524	1.892353385		

	Simple Statistics									
	Interpersonal	Desire for	A ==========	Danandahilih	Physical Ability	lmto evito r				
	Sensitivity	Self-Improvement	Appearance	Dependability	Ability	Integrity				
Mean	6.621359223	6.572815534	7.000000000	6.825242718	7.203883495	7.213592233				
StD	1.760773587	1.729796212	1.798692335	1.917040123	1.555251845	1.845240223				

Correlation Matrix							
	Communication Skills	Problem Solving	Learning Ability		Observational Skills	Willingness to Confront Problems	Interest in People
Communication Skills	1.0000	0.6280	0.5546	0.5538	0.5381	0.5265	0.4391
Problem Solving	0.6280	1.0000	0.5690	0.6195	0.4284	0.5015	0.3972
Learning Ability	0.5546	0.5690	1.0000	0.4892	0.6230	0.5245	0.2735
Judgment Under Pressure	0.5538	0.6195	0.4892	1.0000	0.3733	0.4004	0.6226
Observational Skills	0.5381	0.4284	0.6230	0.3733	1.0000	0.7300	0.2616
Willingness to Confront Problems	0.5265	0.5015	0.5245	0.4004	0.7300	1.0000	0.2233
Interest in People	0.4391	0.3972	0.2735	0.6226	0.2616	0.2233	1.0000
Interpersonal Sensitivity	0.5030	0.4398	0.1855	0.6134	0.1655	0.1291	0.8051
Desire for Self-Improvement	0.5642	0.4090	0.5737	0.4826	0.5985	0.5307	0.4857
Appearance	0.4913	0.3873	0.3988	0.2266	0.4177	0.4825	0.2679
Dependability	0.5471	0.4546	0.5110	0.5471	0.5626	0.4870	0.6074
Physical Ability	0.2192	0.3201	0.2269	0.3476	0.4274	0.4872	0.3768
Integrity	0.5081	0.3846	0.3142	0.5883	0.3906	0.3260	0.7452

Correlation Matrix						
	Interpersonal Sensitivity	Desire for Self-Improvement	Appearance		Physical Ability	Integrity
Communication Skills	0.5030	0.5642	0.4913	0.5471	0.2192	0.5081
Problem Solving	0.4398	0.4090	0.3873	0.4546	0.3201	0.3846
Learning Ability	0.1855	0.5737	0.3988	0.5110	0.2269	0.3142
Judgment Under Pressure	0.6134	0.4826	0.2266	0.5471	0.3476	0.5883
Observational Skills	0.1655	0.5985	0.4177	0.5626	0.4274	0.3906
Willingness to Confront Problems	0.1291	0.5307	0.4825	0.4870	0.4872	0.3260
Interest in People	0.8051	0.4857	0.2679	0.6074	0.3768	0.7452
Interpersonal Sensitivity	1.0000	0.3713	0.2600	0.5408	0.2182	0.6920
Desire for Self-Improvement	0.3713	1.0000	0.4474	0.5981	0.3752	0.5664
Appearance	0.2600	0.4474	1.0000	0.5089	0.3820	0.4135
Dependability	0.5408	0.5981	0.5089	1.0000	0.4461	0.6536
Physical Ability	0.2182	0.3752	0.3820	0.4461	1.0000	0.3810
Integrity	0.6920	0.5664	0.4135	0.6536	0.3810	1.0000

Figure 93.3.2 displays the eigenvalues. The first principal component accounts for about 50% of the total variance, the second principal component accounts for about 13.6%, and the third principal component accounts for about 7.7%. Note that the eigenvalues sum to the total variance. The eigenvalues indicate that three to five components provide a good summary of the data: three components account for about 71.7% of the total variance, and five components account for about 82.7%. Subsequent components account for less than 5% each.

Output 93.3.2 Eigenvalues and Eigenvectors from Using PROC PRINCOMP

_	Eigenvalues of the Correlation Matrix						
	Eigenvalue	Difference	Proportion	Cumulative			
1	6.54740242	4.77468744	0.5036	0.5036			
2	1.77271499	0.76747933	0.1364	0.6400			
3	1.00523565	0.26209665	0.0773	0.7173			
4	0.74313901	0.06479499	0.0572	0.7745			
5	0.67834402	0.22696368	0.0522	0.8267			
6	0.45138034	0.06922167	0.0347	0.8614			
7	0.38215866	0.08432613	0.0294	0.8908			
8	0.29783254	0.02340663	0.0229	0.9137			
9	0.27442591	0.01208809	0.0211	0.9348			
10	0.26233782	0.01778332	0.0202	0.9550			
11	0.24455450	0.04677622	0.0188	0.9738			
12	0.19777828	0.05508241	0.0152	0.9890			
13	0.14269586		0.0110	1.0000			

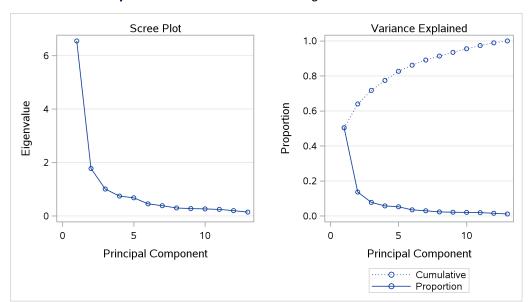
Output 93.3.2 continued

Eigenvectors							
	Prin1	Prin2	Prin3	Prin4	Prin5	Prin6	Prin7
Communication Skills	0.303548	0.052039	329181	227039	0.181087	416563	0.143543
Problem Solving	0.278034	0.057046	400112	0.300476	0.453604	0.096750	0.048904
Learning Ability	0.266521	0.288152	354591	020735	219329	0.578388	114808
Judgment Under Pressure	0.294376	199458	255164	0.397306	030188	0.102087	0.068204
Observational Skills	0.276641	0.366979	0.065959	0.035711	325257	301254	297894
Willingness to Confront Problems	0.267580	0.392989	0.098723	0.184409	0.038278	458585	044796
Interest in People	0.278060	432916	0.118113	0.046047	111279	0.030870	011105
Interpersonal Sensitivity	0.253814	495662	064547	060000	0.107807	170305	088194
Desire for Self-Improvement	0.299833	0.099077	0.061097	211279	427477	0.105369	0.689011
Appearance	0.237358	0.190065	0.248353	544587	0.568044	0.221643	0.049267
Dependability	0.319480	049742	0.169476	156070	130575	0.202301	594850
Physical Ability	0.213868	0.097499	0.614959	0.514519	0.203995	0.173168	0.169247
Integrity	0.298246	301812	0.190222	169062	130757	100039	0.029456

Eigenvectors						
	Prin8	Prin9	Prin10	Prin11	Prin12	Prin13
Communication Skills	0.333846	430955	0.375983	0.028370	252778	122809
Problem Solving	0.199259	0.256098	372914	434417	0.069863	116642
Learning Ability	0.064088	0.224706	0.287031	0.210540	284355	0.248555
Judgment Under Pressure	591822	358618	0.178270	0.118318	0.306490	126636
Observational Skills	0.163484	0.258377	0.223793	079692	0.565290	168555
Willingness to Confront Problems	365684	0.129976	330710	0.275249	386151	0.177688
Interest in People	0.154829	0.321200	081470	0.393841	210915	610215
Interpersonal Sensitivity	0.192725	0.137468	074821	0.285447	0.276824	0.643410
Desire for Self-Improvement	0.087453	121474	363854	052085	0.151436	0.053834
Appearance	257497	0.087395	0.061890	0.168369	0.236655	113705
Dependability	0.081242	495598	377561	164909	090904	018094
Physical Ability	0.302536	149625	0.258321	006202	055828	0.133430
Integrity	317545	0.271060	0.297010	612497	276273	0.114965

PROC PRINCOMP produces the scree plot as shown in Figure 93.3.3 by default when ODS Graphics is enabled. You can obtain more plots by specifying the PLOTS= option in the PROC PRINCOMP statement.

The scree plot on the left shows that the eigenvalue of the first component is approximately 6.5 and the eigenvalue of the second component is largely decreased to under 2.0. The variance explained plot on the right shows that the first four principal components account for nearly 80% of the total variance.



Output 93.3.3 Scree Plot from Using PROC PRINCOMP

The first component reflects overall performance, because the first eigenvector shows approximately equal loadings on all variables. The second eigenvector has high positive loadings on the variables Observational Skills and Willingness to Confront Problems but even higher negative loadings on the variables Interest in People and Interpersonal Sensitivity. This component seems to reflect the ability to take action, but it also reflects a lack of interpersonal skills. The third eigenvector has a very high positive loading on the variable Physical Ability and high negative loadings on the variables Problem Solving and Learning Ability. This component seems to reflect physical strength, but it also shows poor learning and problem-solving skills.

In short, the three components represent the following:

First component: overall performance

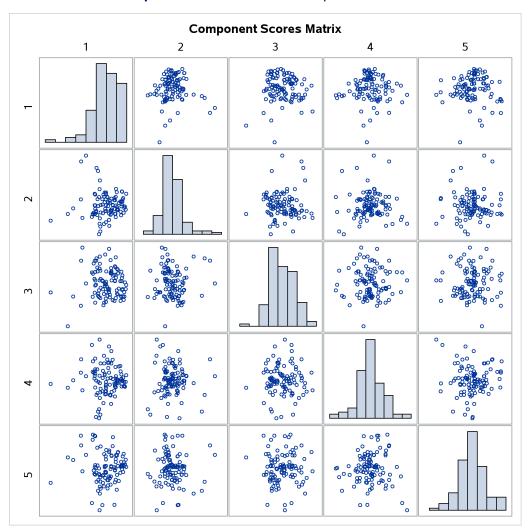
Second component: smartness, toughness, and introversion
Third component: superior strength and average intellect

PROC PRINCOMP also produces other plots besides the scree plot, that help interpret the results. The following statements request plots from the PRINCOMP procedure:

The N=5 option sets the number of principal components to five. The option PLOTS(NCOMP=3)=ALL produces all plots but limits to three the number of components that are displayed in the component pattern plots and the component score plots.

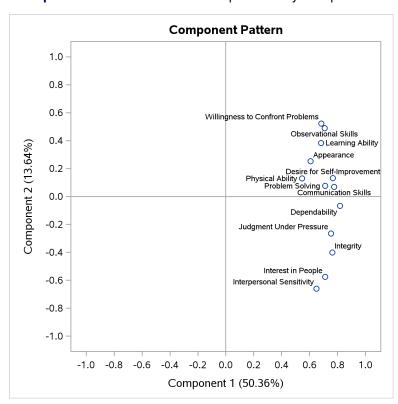
Output 93.3.4 shows a matrix plot of component scores for the first five principal components. The histogram of each component is displayed in the diagonal element of the matrix. The histograms indicate that the first principal component is skewed to the left and the second principal component is slightly skewed to the right.

Output 93.3.4 Matrix Plot of Component Scores



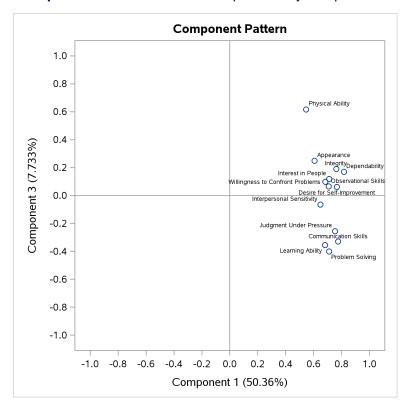
The pairwise component pattern plots are shown in Output 93.3.5 through Output 93.3.7. The pattern plots show the following:

- All variables positively and evenly correlate with the first principal component (Output 93.3.5 and Output 93.3.6).
- The variables Observational Skills and Willingness to Confront Problems correlate highly with the second component, and the variables Interest in People and Interpersonal Sensitivity correlate highly but negatively with the second component (Output 93.3.5).
- The variable Physical Ability correlates highly with the third component, and the variables Problem Solving and Learning Ability correlate highly but negatively with the third component (Output 93.3.6).
- The variables Observational Skills, Willingness to Confront Problems, Interest in People, and Interpersonal Sensitivity correlate highly (either positively or negatively) with the second component, but all these variables have very low correlations with the third component; the variables Physical Ability and Problem Solving correlate highly (either positively or negatively) with the third component, but both variables have very low correlations with the second component (Output 93.3.7).

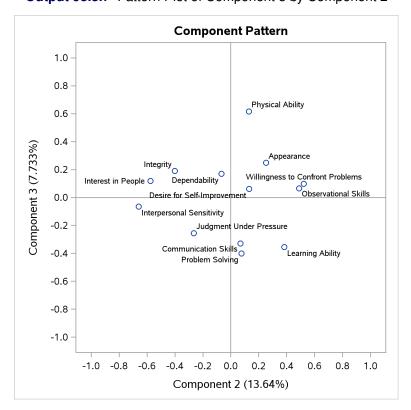


Output 93.3.5 Pattern Plot of Component 2 by Component 1

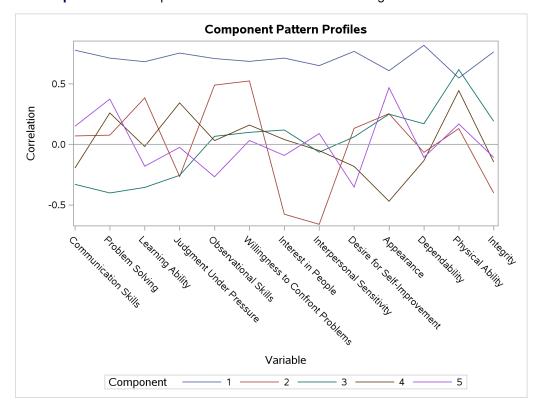
Output 93.3.6 Pattern Plot of Component 3 by Component 1



Output 93.3.7 Pattern Plot of Component 3 by Component 2



Output 93.3.8 shows a component pattern profile. As is shown in the pattern plots, the nearly horizontal profile from the first component indicates that the first component is mostly correlated evenly across all variables.



Output 93.3.8 Component Pattern Profile Plot from Using PROC PRINCOMP

Output 93.3.9 through Output 93.3.11 display the pairwise component score plots. Observation numbers are used as the plotting symbol.

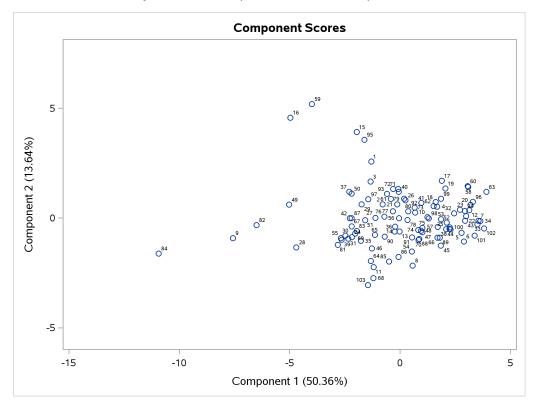
Output 93.3.9 shows a scatter plot of the first and second components. Observations 4 and 31 seem like outliers on the first component. Observations 22 and 30 can be potential outliers on the second component.

Output 93.3.10 shows a scatter plot of the first and third components. Observations 4 and 31 seem like outliers on the first component.

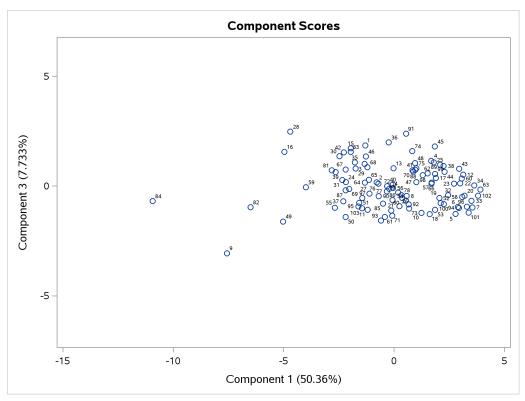
Output 93.3.11 shows a scatter plot of the second and third components. Observations 22 and 30 can be potential outliers on the second component.

Output 93.3.12 shows a scatter plot of the second and third components, displaying the first component in color. Color interpolation ranges from red (minimum) to blue (middle) to green (maximum).

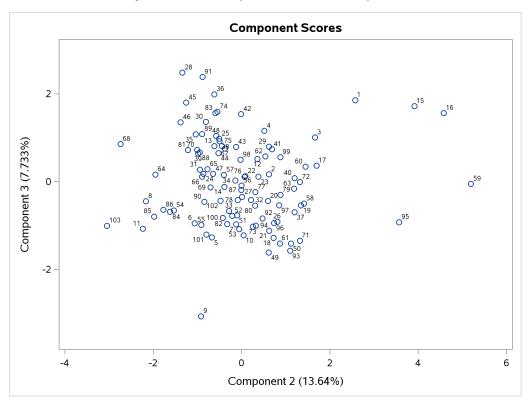
Output 93.3.9 Component 2 versus Component 1



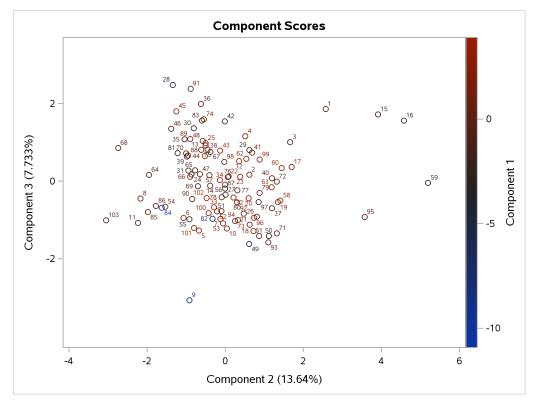
Output 93.3.10 Component 3 versus Component 1



Output 93.3.11 Component 3 versus Component 2



Output 93.3.12 Component 3 versus Component 2, Painted by Component 1



### **References**

Cooley, W. W., and Lohnes, P. R. (1971). Multivariate Data Analysis. New York: John Wiley & Sons.

Gnanadesikan, R. (1977). *Methods for Statistical Data Analysis of Multivariate Observations*. New York: John Wiley & Sons.

Hotelling, H. (1933). "Analysis of a Complex of Statistical Variables into Principal Components." *Journal of Educational Psychology* 24:417–441, 498–520.

Kshirsagar, A. M. (1972). Multivariate Analysis. New York: Marcel Dekker.

Mardia, K. V., Kent, J. T., and Bibby, J. M. (1979). Multivariate Analysis. London: Academic Press.

Morrison, D. F. (1976). Multivariate Statistical Methods. 2nd ed. New York: McGraw-Hill.

Pearson, K. (1901). "On Lines and Planes of Closest Fit to Systems of Points in Space." *Philosophical Magazine* 6:559–572.

Rao, C. R. (1964). "The Use and Interpretation of Principal Component Analysis in Applied Research." *Sankhyā*, *Series A* 26:329–358.

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