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SAS/STAT[®] 13.2 User's Guide The ICPHREG Procedure

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Chapter 51

The ICPHREG Procedure

Contents

Overview: ICPHREG Procedure	3934
Comparison with the PHREG Procedure	3934
Getting Started: ICPHREG Procedure	3935
Syntax: ICPHREG Procedure	3940
PROC ICPHREG Statement	3940
BASELINE Statement	3946
BY Statement	3950
CLASS Statement	3950
FREQ Statement	3953
HAZARDRATIO Statement	3954
MODEL Statement	3956
TEST Statement	3959
Details: ICPHREG Procedure	3959
Model and Likelihood	3959
Baseline Parameterization	3961
Specification of Effects	3962
Computational Details	3963
Predicted Values	3965
Hazard Ratios	3966
Input and Output Data Sets	3969
Missing Values	3969
Displayed Output	3969
ODS Table Names	3971
ODS Graphics	3972
Examples: ICPHREG Procedure	3973
Example 51.1: Fitting Cubic Spline Models	3973
Example 51.2: Plotting Predicted Survival and Cumulative Hazard Functions	3976
References	3979

Overview: ICPHREG Procedure

The ICPHREG procedure is designed to fit proportional hazards regression models to interval-censored data. It can also fit proportional hazards regression models to failure time data that are uncensored, right censored, or left censored. The survival time of each member of a population is assumed to follow its own hazard function, $\lambda_i(t)$, which is expressed as

$$\lambda_i(t) = \lambda(t; \mathbf{Z}_i) = \lambda_0(t) \exp(\mathbf{Z}_i' \boldsymbol{\beta})$$

where $\lambda_0(t)$ is the baseline hazard function, \mathbf{Z}_i is the vector of explanatory variables for the i th individual, and $\boldsymbol{\beta}$ is the vector of unknown regression coefficients that is associated with the explanatory variables. The vector $\boldsymbol{\beta}$ is assumed to be the same for all individuals.

The ICPHREG procedure enables you to use a variety of configurations with respect to the baseline function to fit a proportional hazards model; these configurations include a piecewise constant model (Friedman 1982) and a cubic spline model (Royston and Parmar 2002). To estimate the regression coefficients and the baseline parameters, the ICPHREG procedure maximizes the full likelihood instead of the Cox partial likelihood. Standard errors of the estimates are obtained by inverting the observed information matrix, which is derived from the full likelihood.

The ICPHREG procedure also enables you to do the following: include an offset variable in the model, weight the observations in the input data, test linear hypotheses about the regression coefficients, compute customized hazard ratios, and estimate and plot the survival function and the cumulative hazard function for a new set of covariates.

The ICPHREG procedure uses ODS Graphics to create graphs as part of its output. For general information about ODS Graphics, see Chapter 21, “[Statistical Graphics Using ODS](#).”

Comparison with the PHREG Procedure

The ICPHREG procedure compares most closely to the PHREG procedure. Both procedures can fit proportional hazards models. They differ in the types of censored data that they are designed to handle and the forms of the baseline function. [Table 51.1](#) matches the procedures with the types of censored data they can analyze and the form of the baseline function.

Table 51.1 Proportional Hazards Modeling

Data Type	Baseline	PROC ICPHREG	PROC PHREG
Interval-censored	Piecewise constant	Y	
	Cubic splines	Y	
	Unspecified		
Right-censored	Piecewise constant	Y	Y
	Cubic splines	Y	
	Unspecified		Y

The PHREG procedure deals exclusively with right-censored data, and it mainly adopts a *semiparametric* approach by leaving the baseline hazard function unspecified. The ICPHREG procedure is specifically designed to handle interval-censored data and offers different options to parameterize the baseline hazard function. You can use the ICPHREG procedure to analyze data that are left-censored, interval-censored, or right-censored. However, if the data to be analyzed contain only exact or right-censored observations, it is recommended that you use the PHREG procedure because it provides specialized methods for dealing with right-censored data. For more information about PROC PHREG, see Chapter 73, “[The PHREG Procedure](#).”

Both the LIFEREG procedure and the ICPHREG procedure can handle interval-censored data. The LIFEREG procedure focuses on parametric analysis that uses accelerated failure time models, and it can fit only a proportional hazards model that assumes a Weibull baseline hazard function.

Getting Started: ICPHREG Procedure

This example demonstrates how you can fit a proportional hazards model on an interval-censored data set. By default, PROC ICPHREG uses a piecewise constant baseline hazard to fit the model.

The AIDS data (Larder, Darby, and Richman 1989) consist of observations from 31 patients who were followed up for the development of drug resistance to zidovudine. The following DATA step creates the SAS data set HIV:

```
data hiv;
    input Left Right Stage Dose CdLow CdHigh;
    if (Left=0) then Left=.;
    if (Right>=26) then Right=.;
    datalines;
0 16 0 0 0 1
15 26 0 0 0 1
12 26 0 0 0 1
17 26 0 0 0 1
13 26 0 0 0 1
0 24 0 0 1 0
6 26 0 1 1 0
0 15 0 1 1 0
14 26 0 1 1 0
12 26 0 1 1 0
13 26 0 1 0 1
12 26 0 1 1 0
12 26 0 1 1 0
0 18 0 1 0 1
0 14 0 1 0 1
0 17 0 1 1 0
0 15 0 1 1 0
3 26 1 0 0 1
4 26 1 0 0 1
1 11 1 0 0 1
13 19 1 0 0 1
0 6 1 0 0 1
```

```

0 11 1 1 0 0
6 26 1 1 0 0
0 6 1 1 0 0
2 12 1 1 0 0
1 17 1 1 1 0
0 14 1 1 0 0
0 25 1 1 0 1
2 11 1 1 0 0
0 14 1 1 0 0
;

```

The data set HIV contains the variables Left and Right, which are the starting time and ending time, both in months since the start of study; the variable Stage, which indicates the stage of disease (early (0) or late (1)); the variable Dose, a binary variable that indicates whether the dose is low (0) or high (1); the variable CdLow, which indicates whether the CD4 lymphocyte count is less than 100; and the variable CdHigh, which indicates that a count greater than or equal to 400 is recorded.

The following statements use PROC ICPHREG to fit a proportional hazards model to these data:

```

proc icphreg data=hiv;
  class Stage Dose / desc;
  model (Left, Right) = Stage Dose;
run;

```

The CLASS statement specifies that the variables Stage and Dose are classification variables. The DESC option sets the lower formatted value as the reference level for each CLASS variable. The MODEL statement specifies that the observed intervals are formed by Left and Right.

By default, the preceding statements produce information about the input data and the fitted model, as shown in Figure 51.1.

Figure 51.1 Model and Data Information from the ICPHREG Procedure

The ICPHREG Procedure	
Model Information	
Data Set	WORK.HIV
Left Boundary	Left
Right Boundary	Right
Baseline Hazard	Piecewise Constant
<hr/>	
Number of Observations Read	31
Number of Observations Used	31
Right Censored Observations	13
Interval Censored Observations	5
Left Censored Observations	13

Figure 51.1 shows 13 left-censored observations, 13 right-censored observations, and 5 interval-censored observations.

Figure 51.2 displays the “Class Level Information” table, which identifies the levels of the classification variables that are used in the model.

Figure 51.2 CLASS Variables Information from the ICPHREG Procedure

Class Level Information		
Name	Levels	Values
Stage	2	1 0
Dose	2	1 0

By default, PROC ICPHREG uses a baseline hazard that is partitioned into five disjoint intervals to fit a proportional hazards model. Figure 51.3 displays details about this partition.

Figure 51.3 Interval Partition

Constant Hazard Time Intervals		
Interval		Hazard
[Lower	Upper)	Parameter
0	5.5	Haz1
5.5	8	Haz2
8	12.5	Haz3
12.5	17	Haz4
17	Infty	Haz5

PROC ICPHREG determines the break points so that each time interval contains approximately an equal number of imputed middle points and boundary values in the input data set after excluding the right-censored observations. For more information about this method, see the section “[Choosing Break Points](#)” on page 3964. You can supply your own partition by using the INTERVALS= option in the MODEL statement.

The “Fit Statistics” table, shown in Figure 51.4, contains several statistics that summarize how well the model fits the data. These statistics are helpful in judging the adequacy of a model and in comparing it with other models under consideration.

Figure 51.4 Model Fit Statistics from the ICPHREG Procedure

Fit Statistics	
-2 Log Likelihood	21.813
AIC (Smaller is Better)	31.813
AICC (Smaller is Better)	34.213
BIC (Smaller is Better)	38.983

The table of parameter estimates is displayed in Figure 51.5. The columns display the parameter name, the degrees of freedom that are associated with the parameter, the estimated parameter value, the standard error of the parameter estimate, the confidence limits, the Wald chi-square statistic, and the associated *p*-value for testing the significance of the parameter. If a parameter has been fixed during the optimization process, or if a column of the Hessian matrix that corresponds to that parameter is found to linearly depend on columns that correspond to preceding model parameters, PROC ICPHREG assigns zero degrees of freedom to that parameter and displays a value of zero for its standard error.

Figure 51.5 Model Parameter Estimates from the ICPHREG Procedure

Analysis of Maximum Likelihood Parameter Estimates								
Effect	Stage	Dose	DF	Estimate	Standard Error	95% Confidence Limits		Chi-Square Pr > ChiSq
Haz1			0	0.0000				
Haz2			1	0.0167	0.0205	0.0000	0.0568	
Haz3			0	0.0000				
Haz4			1	0.0842	0.0655	0.0000	0.2126	
Haz5			1	2.5641	366.4263	0.0000	720.7464	
Stage	1		1	2.9597	0.9358	1.1255	4.7939	10.00 0.0016
Stage	0		0	0.0000				
Dose		1	1	1.6229	0.8410	-0.0255	3.2713	3.72 0.0537
Dose		0	0	0.0000				

Two types of parameters are present in [Figure 51.5](#): the hazard parameters (Haz1, Haz2, ..., Haz5) and the regression coefficients for the covariates. PROC ICPHREG does not display the chi-square statistic and associated *p*-value for the hazard parameters.

Two of the hazard parameters are constrained at 0, a sign of overparameterization that results from too many hazard parameters in the model. For more information about how the constraints are constructed, see the section “[NOPOLISH](#)” on page 3958. You can use fewer break points to fit the model by using the NINTERVAL= option or the INTERVALS= option. For example, the following statements request a model that has exactly two hazard parameters by specifying one break point at 10:

```
proc icphreg data=hiv ithistory;
  class Stage Dose / desc;
  model (Left, Right) = Stage Dose / basehaz=pch(intervals=(10));
run;
```

The table of parameter estimates is displayed in [Figure 51.6](#). None of the hazard parameters are constrained.

Figure 51.6 Model Parameter Estimates from the ICPHREG Procedure

Analysis of Maximum Likelihood Parameter Estimates								
Effect	Stage	Dose	DF	Estimate	Standard Error	95% Confidence Limits		Chi-Square Pr > ChiSq
Haz1			1	0.0042	0.0051	0.0000	0.0142	
Haz2			1	0.0590	0.0360	0.0000	0.1296	
Stage	1		1	2.0810	0.7298	0.6506	3.5114	8.13 0.0044
Stage	0		0	0.0000				
Dose		1	1	1.0907	0.6766	-0.2354	2.4167	2.60 0.1069
Dose		0	0	0.0000				

The ITHISTORY option outputs the iteration history of the fitting algorithm, which is shown in [Figure 51.7](#). This option also produces the gradient and Hessian of the likelihood function at the last evaluation. In [Figure 51.7](#), all values of the gradient are close to zero.

Figure 51.7 Iteration History from the ICPHREG Procedure

Likelihood Optimization Iteration History												
Parameter Values					Gradient Values							
Iteration	Evaluations	-2 Log Likelihood	Change	Max Gradient	Stage1	Dose1	Haz1	Haz2	Stage1	Dose1	Haz1	Haz2
0	2	47.8895	.	74.9948	0	0	0.1245	0.0741	-1.8827	3.6394	74.9948	5.0972
1	10	39.1668	-8.7227	47.5072	0.1816	0.3012	0.0559	0.0848	-3.6580	0.5057	47.5072	-1.3723
2	6	37.6893	-1.4775	32.3796	0.2453	0.3347	0.0440	0.0944	-3.9790	-0.2883	32.3796	-1.7277
3	3	35.3576	-2.3317	50.9346	0.4701	0.4206	0.0185	0.1168	-4.6140	-2.0073	-50.9346	-3.9286
4	3	32.5990	-2.7586	6.4037	0.8039	0.5075	0.0200	0.1003	-2.8566	-0.7001	6.4037	0.3183
5	3	30.1026	-2.4964	94.9226	1.3800	0.7032	0.00785	0.0839	-2.1446	-1.3702	-94.9226	-6.0631
6	3	29.0224	-1.0802	23.8304	1.7623	0.8588	0.00724	0.0699	-0.3881	-0.2204	23.8304	-0.6369
7	3	28.8561	-0.1663	103.7	2.0115	1.0376	0.00384	0.0622	-0.5201	-0.4868	-103.7	-2.6791
8	3	28.7697	-0.0863	1.9794	2.0740	1.0858	0.00418	0.0593	-0.0194	-0.0145	-1.9794	-0.0585
9	3	28.7696	-0.00013	0.00309	2.0799	1.0898	0.00416	0.0590	-0.00170	-0.00121	0.00309	-0.00077
10	3	28.7696	-3.01E-6	0.000803	2.0809	1.0906	0.00416	0.0590	-0.00015	-0.00012	-0.00080	-0.00004
11	3	28.7696	-2.5E-8	6.991E-6	2.0810	1.0907	0.00416	0.0590	-6.99E-6	-5.67E-6	-6.93E-6	-1.38E-7
12	2	28.7696	0	6.991E-6	2.0810	1.0907	0.00416	0.0590	-6.99E-6	-5.67E-6	-6.93E-6	-1.38E-7

Last Evaluation of the Negative of
the Gradient

Haz1	Haz2	Stage1	Dose1
-6.93E-6	-1.38E-7	-6.99E-6	-5.67E-6

Last Evaluation of the Negative of the
Hessian

	Haz1	Haz2	Stage1	Dose1
Haz1	139133	4906.9	605.6	626.1
Haz2	4906.9	1967.0	46.4218	78.7404
Stage1	605.6	46.4218	5.2554	2.5003
Dose1	626.1	78.7404	2.5003	7.2471

One reason for fitting a proportional hazards model is to evaluate the hazard ratios between various disease groups. You can request customized hazard ratios by using the HAZARDRATIO statement, as follows:

```
proc icphreg data=hiv;
  class Stage / desc;
  model (Left, Right) = Stage / basehaz=pch(intervals=(10));
  hazardratio Stage;
run;
```

Figure 51.8 shows the estimated hazard ratio between the values 1 and 0 of the Stage variable and the corresponding 95% confidence limits.

Figure 51.8 Hazard Ratio Estimate between Stage Values 1 and 0

The ICPHREG Procedure			
Hazard Ratios for Stage			
Description	Point Estimate	95% Wald Confidence Limits	
		Limits	
Stage 1 vs 0	5.624	1.734	18.241

The estimate of 5.624 indicates that patients who have Stage 1 disease tend to have a much higher risk of developing AIDS than those who have Stage 0. However, the confidence limits are wide due to small sample size.

Syntax: ICPHREG Procedure

The following statements are available in the ICPHREG procedure:

```
PROC ICPHREG < options > ;
  BASELINE < OUT=SAS-data-set > < COVARIATES=SAS-data-set > < TIMELIST=list >
    < keyword=name ... keyword=name > < / options > ;
  BY variables ;
  CLASS variable < (options) > ... < variable < (options) > > < / global-options > ;
  FREQ variable < / option > ;
  HAZARDRATIO < 'label' > variable < / options > ;
  MODEL (t1, t2)= effects < / options > ;
  TEST < model-effects > < / options > ;
```

The MODEL statement is required, and only one MODEL statement is allowed. If multiple MODEL statements are present, only the last one is used. You can specify main effects and interaction terms in the MODEL statement, as in the GLM procedure. The CLASS statement, if present, must precede the MODEL statement. The BASELINE and HAZARDRATIO statements, if present, must come after the MODEL statement.

The following sections describe the PROC ICPHREG statement and then describe the other statements in alphabetical order.

PROC ICPHREG Statement

```
PROC ICPHREG < options > ;
```

The PROC ICPHREG statement invokes the ICPHREG procedure. [Table 51.2](#) summarizes the *options* available in the PROC ICPHREG statement.

Table 51.2 PROC ICPHREG Statement Options

Option	Description
ALPHA=	Specifies the level for confidence limits
DATA=	Names the SAS data set to be analyzed
ITHISTORY	Displays the iteration history, final gradient, and second derivative matrix
NAMELEN=	Specifies the length of effect names
NLOPTIONS	Specifies optimization parameters for fitting the specified model
NOPRINT	Suppresses all displayed output
NOTHEADS	Requests a single-threaded mode for the computation
PLOTS=	Controls the plots that are produced through ODS Graphics
SINGULAR=	Specifies the singularity tolerance
THREADS=	Specifies the number of threads for the computation

You can specify the following *options* in the PROC ICPHREG statement.

ALPHA=number

specifies the α level for $100(1 - \alpha)\%$ confidence limits. The *number* must be between 0 and 1; the default value is 0.05, which results in 95% intervals. This value is used as the default level for confidence limits that are computed by the BASELINE, HAZARDRATIO, and MODEL statements. You can override this default by specifying the ALPHA= option in these statements.

DATA=SAS-data-set

names the SAS data set that contains the data to be analyzed. If you omit this option, the procedure uses the most recently created SAS data set.

ITHISTORY

displays the iteration history for computing maximum likelihood estimates, the final evaluation of the gradient, and the final evaluation of the negative of the second derivative matrix (that is, the negative of the Hessian).

NAMELEN=n

specifies the maximum length of effect names in tables and output data sets to be *n* characters, where *n* is a value between 20 and 200. By default, NAMELEN=20.

NLOPTIONS(options)

specifies options for the nonlinear optimization methods that are used for fitting the specified model. You can specify the following *options*:

ABSCONV=r**ABSTOL=r**

specifies an absolute function convergence criterion by which minimization stops when $f(\boldsymbol{\psi}^{(k)}) \leq r$, where $\boldsymbol{\psi}$ is the vector of parameters in the optimization and $f(\cdot)$ is the objective function. The default value of *r* is the negative square root of the largest double-precision value, which serves only as a protection against overflows.

ABSFCNV=*r***ABSFTOL=*r***

specifies an absolute function difference convergence criterion. For all techniques except NMSIMP, termination requires a small change of the function value in successive iterations,

$$|f(\boldsymbol{\psi}^{(k-1)}) - f(\boldsymbol{\psi}^{(k)})| \leq r$$

where $\boldsymbol{\psi}$ denotes the vector of parameters that participate in the optimization and $f(\cdot)$ is the objective function. The same formula is used for the NMSIMP technique, but $\boldsymbol{\psi}^{(k)}$ is defined as the vertex that has the lowest function value, and $\boldsymbol{\psi}^{(k-1)}$ is defined as the vertex that has the highest function value in the simplex. By default, ABSFCNV=0.

ABSGCNV=*r***ABSGTOL=*r***

specifies an absolute gradient convergence criterion. Termination requires the maximum absolute gradient element to be small,

$$\max_j |g_j(\boldsymbol{\psi}^{(k)})| \leq r$$

where $\boldsymbol{\psi}$ denotes the vector of parameters that participate in the optimization and $g_j(\cdot)$ is the gradient of the objective function with respect to the j th parameter. This criterion is not used by the NMSIMP technique. The default value is $r = 1\text{E-}5$.

FCNV=*r***FTOL=*r***

specifies a relative function convergence criterion. For all techniques except NMSIMP, termination requires a small relative change of the function value in successive iterations,

$$\frac{|f(\boldsymbol{\psi}^{(k)}) - f(\boldsymbol{\psi}^{(k-1)})|}{|f(\boldsymbol{\psi}^{(k-1)})|} \leq r$$

where $\boldsymbol{\psi}$ denotes the vector of parameters that participate in the optimization and $f(\cdot)$ is the objective function. The same formula is used for the NMSIMP technique, but $\boldsymbol{\psi}^{(k)}$ is defined as the vertex that has the lowest function value, and $\boldsymbol{\psi}^{(k-1)}$ is defined as the vertex that has the highest function value in the simplex. The default is $r = 10^{-\text{FDIGITS}}$, where FDIGITS is by default $-\log_{10}\{\epsilon\}$ and ϵ is the machine precision.

GCONV=*r***GTOL=*r***

specifies a relative gradient convergence criterion. For all techniques except CONGRA and NMSIMP, termination requires the normalized predicted function reduction to be small,

$$\frac{\mathbf{g}(\boldsymbol{\psi}^{(k)})' [\mathbf{H}^{(k)}]^{-1} \mathbf{g}(\boldsymbol{\psi}^{(k)})}{|f(\boldsymbol{\psi}^{(k)})|} \leq r$$

where $\boldsymbol{\psi}$ denotes the vector of parameters that participate in the optimization, $f(\cdot)$ is the objective function, and $\mathbf{g}(\cdot)$ is the gradient. For the CONGRA technique (in which a reliable Hessian estimate \mathbf{H} is not available), the following criterion is used:

$$\frac{\|\mathbf{g}(\boldsymbol{\psi}^{(k)})\|_2^2}{\|\mathbf{g}(\boldsymbol{\psi}^{(k)}) - \mathbf{g}(\boldsymbol{\psi}^{(k-1)})\|_2 |f(\boldsymbol{\psi}^{(k)})|} \leq r$$

This criterion is not used by the NMSIMP technique. The default value is $r = 1\text{E-}8$.

MAXFUNC=*n***MAXFU=*n***

specifies the maximum number of function calls in the optimization process. The default values are as follows, depending on the optimization technique (which you can specify in the **TECHNIQUE=** option):

- TRUREG, NRRIDG, and NEWRAP: 125
- QUANEW and DBLDOG: 500
- CONGRA: 1000
- NMSIMP: 3000

The optimization can terminate only after completing a full iteration. Therefore, the number of function calls that are actually performed can exceed *n*.

MAXITER=*n***MAXIT=*n***

specifies the maximum number of iterations in the optimization process. The default values are as follows, depending on the optimization technique (which you can specify in the **TECHNIQUE=** option):

- TRUREG, NRRIDG, and NEWRAP: 50
- QUANEW and DBLDOG: 200
- CONGRA: 400
- NMSIMP: 1000

These default values also apply when *n* is specified as a missing value.

MAXTIME=*r*

specifies an upper limit of *r* seconds of CPU time for the optimization process. The time is checked only at the end of each iteration. Therefore, the actual run time might be longer than *r*. By default, CPU time is not limited.

MINITER=*n***MINIT=*n***

specifies the minimum number of iterations. If you request more iterations than are actually needed for convergence to a stationary point, the optimization algorithms can behave strangely. For example, the effect of rounding errors can prevent the algorithm from continuing for the required number of iterations. By default, **MINITER=0**.

TECHNIQUE=keyword

specifies the optimization technique to obtain maximum likelihood estimates. You can choose from the following techniques:

CONGRA	performs a conjugate-gradient optimization.
DBLDOG	performs a version of double-dogleg optimization.
NEWRAP	performs a Newton-Raphson optimization that combines a line-search algorithm with ridging.
NMSIMP	performs a Nelder-Mead simplex optimization.

NONE	performs no optimization.
NRRIDG	performs a Newton-Raphson optimization with ridging.
QUANEW	performs a dual quasi-Newton optimization.
TRUREG	performs a trust-region optimization.

By default, **TECHNIQUE=NEWRAP**.

For more information about these optimization methods, see the section “[Choosing an Optimization Algorithm](#)” on page 501 in Chapter 19, “[Shared Concepts and Topics](#).”

NOPRINT

suppresses all displayed output. This option temporarily disables the Output Delivery System (ODS); For more information, see Chapter 20, “[Using the Output Delivery System](#).”

NOTHEADS

forces single-threaded execution of the analytic computations. This option overrides the SAS system option **THREADS** | **NOTHEADS**. Specifying this option is equivalent to specifying the **THREADS=1** option.

PLOTS<(*global-plot-options*)> = *plot-request*

PLOTS<(*global-plot-options*)> = (*plot-request* < . . . < *plot-request* >)
requests plots of survival functions and cumulative hazard functions.

You can specify the following *global-plot-options*:

CL

displays the pointwise confidence limits for the plot.

OVERLAY <= *overlay-option* >

specifies how to overlay the functions that are plotted for the covariate sets. You can specify the following *overlay-options*:

BYGROUP

GROUP

overlays onto the same plot all functions that are plotted for the covariate sets and have the same **GROUP=** value in the **COVARIATES=** data set.

INDIVIDUAL

IND

displays a separate plot for each covariate set.

By default, **OVERLAY=BYGROUP** if the **GROUP=** option is specified in the **BASELINE** statement or if the **COVARIATES=** data set contains the **_GROUP_** variable; otherwise, by default, **OVERLAY=INDIVIDUAL**.

TIMERANGE=(< *min* > < , *max* >)

TIMERANGE= < *min* > < , *max* >

RANGE=(< *min* > < , *max* >)

RANGE= < *min* > < , *max* >

specifies the range of values on the time axis to clip the display. The *min* and *max* values are the lower and upper bounds of the range. By default, *min* is 0 and *max* is the largest boundary value.

You can specify the following *plot-requests*:

CUMHAZ

plots the estimated cumulative hazard function for each set of covariates in the data set that is specified in the COVARIATES= option in the BASELINE statement. If the COVARIATES= data set is not specified, the estimated cumulative hazard function is plotted for the reference set of covariates, which consists of reference levels for the CLASS variables and average values for the continuous variables.

NONE

suppresses all the plots in the procedure. Specifying this option is equivalent to disabling ODS Graphics for the entire procedure.

SURVIVAL**S****SURV****SUR**

plots the estimated survival function for each set of covariates in the data set that is specified in the COVARIATES= option in the BASELINE statement. If the COVARIATES= data set is not specified, the estimated survival function is plotted for the reference set of covariates, which consists of reference levels for the CLASS variables and average values for the continuous variables.

Each observation in the data set that is specified in the COVARIATES= option in the BASELINE statement provides a set of covariates for which a plot is produced for each *plot-request*. You can use the ROWID= option in the BASELINE statement to specify a variable in the COVARIATES= data set for identifying the functions that are plotted for the covariate sets. If the ROWID= option is not specified, the plots are identified by the covariate values if there is only a single covariate or by the observation numbers of the COVARIATES= data set if the model has two or more covariates. If the COVARIATES= data set is not specified, a reference set of covariates that consists of the reference levels for the CLASS variables and the average values for the continuous variables is used. When plotting more than one function, you can use the OVERLAY= option to group the functions. When you specify only one *plot-request*, you can omit the parentheses around the plot request. Here are some examples:

```
plots=survival
plots=(survival cumhaz)
```

ODS Graphics must be enabled before plots can be requested. For example:

```
ods graphics on;
proc icphreg plots(cl)=survival;
  model (Left, Right)=X1-X5;
  baseline covariates=One;
run;
```

For more information about enabling and disabling ODS Graphics, see the section “[Enabling and Disabling ODS Graphics](#)” on page 606 in Chapter 21, “[Statistical Graphics Using ODS](#).”

SINGULAR=*number***EPSILON=***number*

specifies the tolerance for testing the singularity of the $\mathbf{Z}'\mathbf{Z}$ matrix that is formed from the design matrix \mathbf{Z} and for testing the singularity of the Hessian matrix upon convergence of the optimization algorithm. Appropriately, the test requires that a pivot be at least this number times the original diagonal value. By default, *number* is 10^7 times the machine epsilon. On most machines, the default *number* is approximately 10^{-9} .

THREADS=*n***NOTHEADS=***n*

specifies the number of threads for analytic computations and overrides the SAS system option **THREADS** | **NOTHEADS**. If you do not specify the **THREADS=** option or if you specify **THREADS=0**, the number of threads is determined based on the data size and the number of CPUs on the host on which the analytic computations execute.

BASELINE Statement

BASELINE <**OUT=***SAS-data-set*> <**COVARIATES=***SAS-data-set*> <**TIMELIST=***list*> <**keyword=***name*
 ... **keyword=***name*> </ options> ;

The **BASELINE** statement creates a SAS data set (named by the **OUT=** option) that contains the predicted values at specified times that partition the time axis for every set of covariates in the **COVARIATES=** data set. If the **COVARIATES=** data set is not specified, PROC ICPHREG uses a reference set of covariates that consists of the reference levels for the **CLASS** variables and the average values for the continuous variables.

Table 51.3 summarizes the options that you can specify in the **BASELINE** statement.

Table 51.3 BASELINE Statement Options

Option	Description
Data Set and Time List Options	
OUT=	Specifies the output BASELINE data set
COVARIATES=	Specifies the SAS data set that contains the explanatory variables
TIMELIST=	Specifies a list of time points for computing the predicted values
Keyword Options for Variables	
CUMHAZ=	Specifies the cumulative hazard function estimate
LOGLOGS=	Specifies the log of the negative log of the survival function
LOGSURV=	Specifies the log of the survival function
LOWERCUMHAZ=	Specifies the lower pointwise confidence limit for the cumulative hazard function
LOWER=	Specifies the lower pointwise confidence limit for the survival function
STDCUMHAZ=	Specifies the estimated standard error of the cumulative hazard function
STDERR=	Specifies the standard error of the survival function
STDXBETA=	Specifies the estimated standard error of the linear predictor estimator
SURVIVAL=	Specifies the survival function estimate

Table 51.3 *continued*

Options	Description
UPPERCUMHAZ=	Specifies the upper pointwise confidence limit for the cumulative hazard function
UPPER=	Specifies the upper pointwise confidence limit for the survival function
XBETA=	Specifies the estimate of the linear predictor $\mathbf{z}'\boldsymbol{\beta}$
Other Options	
ALPHA=	Specifies the level of the confidence interval for the survival function
CLTYPE=	Specifies the transformation that is used to compute confidence limits for the survival function
GROUP=	Names a variable whose values identify or group predicted survival or cumulative hazard functions in plots
ROWID=	Names the variable in the COVARIATES= data set for identifying the predicted survival or cumulative hazard functions in plots

You can specify the following options in the BASELINE statement.

OUT=SAS-data-set

names the output data set. If you omit the OUT= option, the data set is created and given a default name by using the DATA n convention. For more information, see the section “OUT= Output Data Set in the BASELINE Statement” on page 3969.

COVARIATES=SAS-data-set

names the SAS data set that contains the sets of explanatory variable values for which the functions of interest are estimated. All variables in the COVARIATES= data set are copied to the OUT= data set. Thus, any variable in the COVARIATES= data set can be used to identify the covariate sets in the OUT= data set.

TIMELIST=list

specifies a list of time points at which the predicted values are computed. The following specifications are equivalent:

```
timelist=5,20 to 50 by 10
timelist=5 20 30 40 50
```

If you do not specify this option, predicted values are computed at all the times that partition the time axis.

keyword=name

specifies the statistics to be included in the OUT= data set and assigns names to the variables that contain these statistics. Specify a *keyword* for each desired statistic, an equal sign, and the name of the variable for the statistic. You can specify the following *keywords*:

CUMHAZ=*name*

specifies the cumulative hazard function estimate. Specifying CUMHAZ=_ALL_ is equivalent to specifying CUMHAZ=CumHaz, STDCUMHAZ=StdErrCumHaz, LOWERCUMHAZ=LowerCumHaz, and UPPERCUMHAZ=UpperCumHaz.

LOGLOGS=*name***CLOGLOGS=*name***

specifies the log of the negative log of the estimated survival function.

LOGSURV=*name*

specifies the log of the estimated survival function.

LOWER=*name***L=*name*****LOWERSDF=*name***

specifies the lower pointwise confidence limit for the survival function. The confidence level is determined by the ALPHA= option.

LOWERCUMHAZ=*name*

specifies the lower pointwise confidence limit for the cumulative hazard function. The confidence level is determined by the ALPHA= option.

STDERR=*name***STDSDF=*name***

specifies the standard error of the survival function estimator.

STDCUMHAZ=*name*

specifies the estimated standard error of the cumulative hazard function estimator.

STDXBETA=*name*

specifies the estimated standard error of the linear predictor estimator.

SURVIVAL=*name***SDF=*name***

specifies the estimated survival function ($S(t) = [S_0(t)]^{\exp(\mathbf{z}'\boldsymbol{\beta})}$). Specifying SURVIVAL=_ALL_ is equivalent to specifying SURVIVAL=Survival, STDERR=StdErrSurvival, LOWER=LowerSurvival, and UPPER=UpperSurvival.

UPPER=*name***U=*name*****UPPERSDF=*name***

specifies the upper pointwise confidence limit for the survival function. The confidence level is determined by the ALPHA= option.

UPPERCUMHAZ=*name*

specifies the upper pointwise confidence limit for the cumulative hazard function. The confidence level is determined by the ALPHA= option.

XBETA=*name*

specifies the estimate of the linear predictor $\mathbf{z}'\boldsymbol{\beta}$. If there is an offset, it is added to the predictor.

You can specify the following *options* after a slash (/).

ALPHA=*value*

specifies the level of the confidence interval for the survival function. The *value* must be between 0 and 1. The default is the value of the ALPHA= option in the PROC ICPHREG statement, or 0.05 if that option is not specified.

CLTYPE=*method*

CITYPE=*method*

TYPE=*method*

CLTRANSFORM=*method*

TRANSFORM=*method*

specifies the transformation that is used to compute the confidence limits for $S(t, \mathbf{z})$, which is the survival function for a subject that has a fixed covariate vector \mathbf{z} at event time t . You can specify the following *methods*:

LOG

uses normal theory approximation to compute the confidence limits for $\log(S(t, \mathbf{z}))$. The confidence limits for $S(t, \mathbf{z})$ are obtained by back-transforming the confidence limits for $\log(S(t, \mathbf{z}))$.

LOGLOG

uses normal theory approximation to compute the confidence limits for the $\log(-\log(S(t, \mathbf{z})))$. The confidence limits for $S(t, \mathbf{z})$ are obtained by back-transforming the confidence limits for $\log(-\log(S(t, \mathbf{z})))$.

NORMAL

IDENTITY

LINEAR

PLAIN

DIRECT

uses normal theory approximation to compute the confidence limits for $S(t, \mathbf{z})$.

By default, CLTYPE=LOG.

GROUP=*variable*

names a variable whose values identify or group the predicted curves. The *variable* must be a numeric variable in the **COVARIATES=** data set. Survival curves for observations that have the same value of the *variable* are overlaid in the same plot.

ROWID=*variable***ID=***variable***ROW=***variable*

names a variable in the COVARIATES= data set for identifying plotted survival functions and cumulative hazard functions. This option has no effect if the PLOTS= option in the PROC ICPHREG statement is not specified. Values of this variable are used to label the plotted functions for the corresponding rows in the COVARIATES= data set. You can specify ROWID=_OBS_ to use the observation numbers in the COVARIATES= data set for identification.

BY Statement

BY *variables* ;

You can specify a BY statement with PROC ICPHREG to obtain separate analyses of observations in groups that are defined by the BY variables. When a BY statement appears, the procedure expects the input data set to be sorted in order of the BY variables. If you specify more than one BY statement, only the last one specified is used.

If your input data set is not sorted in ascending order, use one of the following alternatives:

- Sort the data by using the SORT procedure with a similar BY statement.
- Specify the NOTSORTED or DESCENDING option in the BY statement for the ICPHREG procedure. The NOTSORTED option does not mean that the data are unsorted but rather that the data are arranged in groups (according to values of the BY variables) and that these groups are not necessarily in alphabetical or increasing numeric order.
- Create an index on the BY variables by using the DATASETS procedure (in Base SAS software).

For more information about BY-group processing, see the discussion in *SAS Language Reference: Concepts*. For more information about the DATASETS procedure, see the discussion in the *Base SAS Procedures Guide*.

CLASS Statement

CLASS *variable* <(*options*)> ... <*variable* <(*options*)>> </*global-options*> ;

The CLASS statement names the classification variables to be used as explanatory variables in the analysis.

The CLASS statement must precede the **MODEL** statement. Most options can be specified either as individual variable *options* or as *global-options*. You can specify *options* for each variable by enclosing the options in parentheses after the variable name. You can also specify *global-options* for the CLASS statement by placing them after a slash (/). *Global-options* are applied to all the variables specified in the CLASS statement. If you specify more than one CLASS statement, the *global-options* specified in any one CLASS statement apply to all CLASS statements. However, individual CLASS variable *options* override the *global-options*. You can specify the following values for either an *option* or a *global-option*:

CPREFIX=*n*

specifies that, at most, the first *n* characters of a CLASS variable name be used in creating names for the corresponding design variables. The default is $32 - \min(32, \max(2, f))$, where *f* is the formatted length of the CLASS variable.

DESCENDING**DESC**

reverses the sort order of the classification variable. If both the DESCENDING and **ORDER=** options are specified, PROC ICPHREG orders the categories according to the **ORDER=** option and then reverses that order.

LPREFIX=*n*

specifies that, at most, the first *n* characters of a CLASS variable label be used in creating labels for the corresponding design variables. The default is $256 - \min(256, \max(2, f))$, where *f* is the formatted length of the CLASS variable.

MISSING

treats missing values (., _., .A, ..., .Z for numeric variables and blanks for character variables) as valid values for the CLASS variable.

ORDER=DATA | FORMATTED | FREQ | INTERNAL

specifies the sort order for the levels of classification variables. This ordering determines which parameters in the model correspond to each level in the data, so the **ORDER=** option can be useful when you use the HAZARDRATIO statement. By default, **ORDER=FORMATTED**. For **ORDER=FORMATTED** and **ORDER=INTERNAL**, the sort order is machine-dependent. When **ORDER=FORMATTED** is in effect for numeric variables for which you have supplied no explicit format, the levels are ordered by their internal values.

The following table shows how PROC ICPHREG interprets values of the **ORDER=** option.

Value of ORDER=	Levels Sorted By
DATA	Order of appearance in the input data set
FORMATTED	External formatted values, except for numeric variables with no explicit format, which are sorted by their unformatted (internal) values
FREQ	Descending frequency count; levels with more observations come earlier in the order
INTERNAL	Unformatted value

For more information about sort order, see the chapter on the SORT procedure in the *Base SAS Procedures Guide* and the discussion of BY-group processing in *SAS Language Reference: Concepts*.

PARAM=keyword

specifies the parameterization method for the classification variable or variables. You can specify any of the *keywords* shown in the following table.

Design matrix columns are created from CLASS variables according to the corresponding coding schemes:

Value of PARAM=	Coding
EFFECT	Effect coding
GLM	Less-than-full-rank reference cell coding (this <i>keyword</i> can be used only in a global option)
ORDINAL THERMOMETER	Cumulative parameterization for an ordinal CLASS variable
POLYNOMIAL POLY	Polynomial coding
REFERENCE REF	Reference cell coding
ORTHEFFECT	Orthogonalizes PARAM=EFFECT coding
ORTHORDINAL ORTHOTHERM	Orthogonalizes PARAM=ORDINAL coding
ORTHPOLY	Orthogonalizes PARAM=POLYNOMIAL coding
ORTHREF	Orthogonalizes PARAM=REFERENCE coding

All parameterizations are full rank, except for the GLM parameterization. The [REF=](#) option in the CLASS statement determines the reference level for EFFECT and REFERENCE coding and for their orthogonal parameterizations. It also indirectly determines the reference level for a singular GLM parameterization through the order of levels.

If PARAM=ORTHPOLY or PARAM=POLY and the classification variable is numeric, then the [ORDER=](#) option in the CLASS statement is ignored, and the internal unformatted values are used. See the section “[Other Parameterizations](#)” on page 391 in Chapter 19, “[Shared Concepts and Topics](#),” for further details.

REF= *'level'* | *keyword*

specifies the reference level for [PARAM=EFFECT](#), [PARAM=REFERENCE](#), and their orthogonalizations. For [PARAM=GLM](#), the REF= option specifies a level of the classification variable to be put at the end of the list of levels. This level thus corresponds to the reference level in the usual interpretation of the linear estimates with a singular parameterization.

For an individual variable REF= option (but not for a global REF= option), you can specify the *level* of the variable to use as the reference level. Specify the formatted value of the variable if a format is assigned. For a global or individual variable REF= option, you can use one of the following *keywords*. The default is REF=LAST.

- FIRST** designates the first ordered level as reference.
- LAST** designates the last ordered level as reference.

TRUNCATE < =*n* >

specifies the length *n* of CLASS variable values to use in determining CLASS variable levels. The default is to use the full formatted length of the CLASS variable. If you specify TRUNCATE without the length *n*, the first 16 characters of the formatted values are used. When formatted values are longer

than 16 characters, you can use this option to revert to the levels as determined in releases before SAS 9. The TRUNCATE option is available only as a global option.

Class Variable Default Parameterization

If you do not specify the PARAM= option, the default PARAM=GLM parameterization is used.

Class Variable Naming Convention

Parameter names for a CLASS predictor variable are constructed by concatenating the CLASS variable name with the CLASS levels. However, for the POLYNOMIAL and orthogonal parameterizations, parameter names are formed by concatenating the CLASS variable name and keywords that reflect the parameterization. See the section “Other Parameterizations” on page 391 in Chapter 19, “Shared Concepts and Topics,” for examples and further details.

Class Variable Parameterization with Unbalanced Designs

PROC ICPHREG initially parameterizes the CLASS variables by looking at the levels of the variables across the complete data set. If you have an *unbalanced* replication of levels across variables or BY groups, then the design matrix and the parameter interpretation might be different from what you expect. For instance, suppose you have a model with one CLASS variable A with three levels (1, 2, and 3), and another CLASS variable B with two levels (1 and 2). If the third level of A occurs only with the first level of B, if you use the EFFECT parameterization, and if your model contains the effect A(B) and an intercept, then the design for A within the second level of B is not a differential effect. In particular, the design looks like the following:

		Design Matrix			
		A(B=1)		A(B=2)	
B	A	A1	A2	A1	A2
1	1	1	0	0	0
1	2	0	1	0	0
1	3	-1	-1	0	0
2	1	0	0	1	0
2	2	0	0	0	1

PROC ICPHREG detects linear dependency among the last two design variables and sets the parameter for A2(B=2) to zero, resulting in an interpretation of these parameters as if they were reference- or dummy-coded. The REFERENCE or GLM parameterization might be more appropriate for such problems.

FREQ Statement

FREQ *variable* </option> ;

The FREQ statement identifies the *variable* (in the input data set) that contains the frequency of occurrence of each observation. PROC ICPHREG treats each observation as if it appears *n* times, where *n* is the value of the FREQ variable for the observation. If the frequency value is not an integer, it is truncated to an integer. If the frequency value is missing, the observation is not used in the estimation of the regression coefficients.

You can specify the following *option* after a slash (/):

NOTRUNCATE

NOTRUNC

specifies that frequency values are not truncated to integers.

HAZARDRATIO Statement

HAZARDRATIO <'label'> *variable* </options> ;

The HAZARDRATIO statement enables you to request hazard ratios for any variable in the model at customized settings. For example, if the model contains the interaction of a CLASS variable A and a continuous variable X, the following specification displays a table of hazard ratios that compares the hazards of each pair of levels of A at X = 3:

```
hazardratio A / at (X=3);
```

The HAZARDRATIO statement identifies the variable whose hazard ratios are to be evaluated. If the variable is a continuous variable, the hazard ratio compares the hazards for a particular change (by default, an increase of 1 unit) in the variable. For a CLASS variable, a hazard ratio compares the hazards of two levels of the variable. You can specify more than one HAZARDRATIO statement, and you can provide an optional label (specified as a quoted string) to identify the output.

Table 51.4 summarizes the *options* that you can specify in the HAZARDRATIO statement.

Table 51.4 HAZARDRATIO Statement Options

Option	Description
ALPHA=	Specifies the alpha level
AT	Specifies the variables that interact with the variable of interest
DIFF=	Specifies which differences to consider
E	Displays the log-hazard ratio
UNITS=	Specifies the units of change for a continuous variable of interest

You can specify the following *options* after a slash (/).

ALPHA=number

specifies the level of confidence intervals for the hazard ratios. The *number* must be between 0 and 1. The default is the value of the ALPHA= option in the PROC ICPHREG statement, or 0.05 if that option is not specified.

AT (variable=ALL | REF | list <... variable=ALL | REF | list >)

specifies the variables that interact with the variable of interest and the corresponding values of the interacting variables. If the interacting variable is continuous and you specify a numeric *list* after the equal sign, hazard ratios are computed for each value in the list. If the interacting variable is a CLASS variable, you can specify, after the equal sign, a *list* of quoted strings that correspond to various levels of the CLASS variable, or you can specify the keyword ALL or REF. Hazard ratios are computed at each value of the list if you specify a *list*, at each level of the interacting variable if you specify ALL, or at the reference level of the interacting variable if you specify REF.

If you do not specify the AT option, PROC ICPHREG finds all the variables that interact with the variable of interest. If an interacting variable is a CLASS variable, *variable*=ALL is the default; if the interacting variable is continuous, *variable*=*m* is the default, where *m* is the average of all the sampled values of the continuous variable.

Suppose the model contains two interactions: an interaction A*B of CLASS variables A and B, and another interaction A*X of A with a continuous variable X. If 3.5 is the average of the sampled values of X, the following two HAZARDRATIO statements are equivalent:

```
hazardratio A;
hazardratio A / at (B=ALL X=3.5);
```

DIFF=diff-request

specifies which differences to consider for the level comparisons of a CLASS variable. This option is ignored in the estimation of hazard ratios for a continuous variable. You can specify the following *diff-requests*:

DISTINCT

DISTINCTPAIRS

ALL

requests all comparisons of only the distinct combinations of pairs.

PAIRWISE

PERM

PERMUTATIONS

requests all possible pairwise comparisons of levels.

REF

REFERENCE

requests comparisons between the reference level and all other levels of the CLASS variable.

For example, let A be a CLASS variable that has three levels (A1, A2, and A3), and suppose A3 is specified as the reference level. The following table shows the hazard ratios that are displayed for the three alternatives of the DIFF= option:

DIFF=option	Hazard Ratios Displayed					
	A1 vs A2	A2 vs A1	A1 vs A3	A3 vs A1	A2 vs A3	A3 vs A2
DISTINCT	✓		✓		✓	
PAIRWISE	✓	✓	✓	✓	✓	✓
REF			✓		✓	

By default, DIFF=DISTINCT.

E

displays the vector **h** of linear coefficients such that $\mathbf{h}'\boldsymbol{\beta}$ is the log-hazard ratio, where $\boldsymbol{\beta}$ is the vector of regression coefficients.

UNITS=value

specifies the units of change in the continuous explanatory variable for which the customized hazard ratio is estimated. By default, UNITS=1. This option is ignored in the computation of the hazard ratios for a CLASS variable.

MODEL Statement

MODEL (*t1*, *t2*)= *effects* </ *options* > ;

The MODEL statement identifies the variables to be used as the failure-time variables and the explanatory effects, including covariates, main effects, interactions, nested effects. For more information, see the section “Specification of Effects” on page 3453 in Chapter 45, “The GLM Procedure.”

The MODEL syntax specifies two variables, *t1* and *t2*, that contain values of the endpoints of the censoring interval. Only nonnegative values are accepted. If the two values are the same (and not missing), it is assumed that there is no censoring and the actual response value is observed. If the lower value is missing, then the upper value is used as a left-censored value. If the upper value is missing, then the lower value is used as a right-censored value. If both values are present and the lower value is less than the upper value, it is assumed that the values specify a censoring interval. If the lower value is greater than the upper value or both values are missing, then the observation is not used in the analysis.

The following table summarizes the ways of specifying censoring.

Lower Value	Upper Value	Comparison	Interpretation
Not missing	Not missing	Equal	No censoring
Not missing	Not missing	Lower < upper	Censoring interval
Missing	Not missing		Upper used as left-censoring value
Not missing	Missing		Lower used as right-censoring value
Not missing	Not missing	Lower > upper	Observation not used
Missing	Missing		Observation not used

Table 51.5 summarizes the *options* that you can specify in the MODEL statement.

Table 51.5 MODEL Statement Options

Option	Description
Model Specification Options	
ALPHA=	Specifies the confidence level
BASE=	Specifies the functional form for the baseline function
NOPOLISH	Suppresses polishing of parameter estimates of the hazard function
OFFSET=	Specifies an offset variable to be added to the linear predictor
HAZSCALE=	Requests parameterization of the hazard function in the original scale or in log scale

Table 51.5 *continued*

Option	Description
Output Options	
CORRB	Displays the estimated correlation matrix
COVB	Displays the estimated covariance matrix

ALPHA=*value*

specifies the level for the confidence intervals for parameters. The *value* must be between 0 and 1. By default, ALPHA=0.05.

CORRB

displays the estimated correlation matrix of the parameter estimates.

COVB

displays the estimated covariance matrix of the parameter estimates.

BASE=*baseline-type***BASEHAZ=***baseline-type***B=***baseline-type*

specifies a functional form for the baseline function. You can specify one of the following *baseline-types*:

PCH (< **NINTERVAL=***number* >, < **INTERVALS=**(*numeric-list*) >)

PIECEWISE (< **NINTERVAL=***number* >, < **INTERVALS=**(*numeric-list*) >)

PIECEWISEEXPONENTIAL (< **NINTERVAL=***number* >, < **INTERVALS=**(*numeric-list*) >)

PCBH (< **NINTERVAL=***number* >, < **INTERVALS=**(*numeric-list*) >)

partitions the time scale into disjoint intervals and assumes the baseline hazard function is piecewise constant within intervals. The parameters are the piecewise constant values of the baseline hazard functions and are named Haz1, Haz2, . . . , and so on. If HAZARDSCALE=LOGHAZ is specified, the names are LogHaz1, LogHaz2, . . . , and so on.

You can specify one of the following two options to control how to partition the time axis into intervals of constant baseline hazards:

NINTERVAL=*number*

N=*number*

specifies the number of intervals that have a constant hazard rate in each interval. PROC ICPHREG partitions the time axis into the *number* of intervals so that each interval contains an approximately equal number of unique boundary values and imputed middle points.

INTERVALS=(*numeric-list*)

INTERVAL=(*numeric-list*)

specifies a list of numbers that partition the time axis into disjoint intervals that have constant hazard rate in each interval. For example, INTERVALS=(100, 150, 200, 250, 300) specifies a model that has a constant hazard in the intervals [0,100), [100,150), [150,200), [200,250), [250,300), and [300,∞).

If you specify neither **NINTERVAL=** nor **INTERVAL=**, NINTERVAL=5 by default.

SPLINES (< DF=*number* >)**CUBICSPLINES** (< DF=*number* >)

models the baseline cumulative hazard function by cubic splines (Royston and Parmar 2002). The parameters are the spline coefficients and are named Coef1, Coef2, . . . , and so on.

You can specify the degrees of freedom in the DF=*number* option, where *number* must be an integer. The number of knots equals *number* plus one. The actual positions of the knots are determined from an imputed data set as follows. First, PROC ICPHREG imputes a middle point for each observation in the input data set that is not right-censored. Then, it sorts these imputed times and the input boundary values in increasing order and selects only unique values. PROC ICPHREG places the *terminal knots* at the minimum and maximum of this sequence and chooses the *interval knots* by using the same method it uses to choose the break points for the piecewise constant model. For more information, see the section “[Choosing Break Points](#)” on page 3964.

By default, DF=2.

If you do not specify the BASEHAZ= option, the ICPHREG procedure fits a piecewise constant model as if NINTERVAL=5.

NOPOLISH

suppresses polishing of parameter estimates of the baseline function. Occasionally, the parameter estimates of the baseline function can reach the default optimization lower bounds. This might indicate that the model is overparameterized. By default, the ICPHREG procedure “polishes” the hazard estimates by fixing these parameters at the lower bound value and refitting the model.

The lower bound values are set 0 if the baseline parameters are on the original scale (HAZSCALE=HAZARD). The values are set to –10.0 if they are on the log scale (HAZSCALE=LOGHAZ).

This option does not apply to the cubic spline model because its baseline parameters are unbounded.

OFFSET=*variable*

specifies a variable in the input data set to be used as an offset variable. This variable cannot be a CLASS variable, the response variable, or any of the explanatory variables.

HAZSCALE=*hazard-type*

specifies a transformation to be applied to the baseline parameters for fitting the piecewise constant model. You can choose either of the following two options:

LOGHAZ**LOG****LOGHAZARD**

uses the log transformed baseline parameters.

HAZARD**HAZ**

does not transform the baseline parameters. A lower bound of 0 is used for fitting the models.

This option does not apply to the cubic spline model.

TEST Statement

TEST < *model-effects* > < / *options* > ;

The TEST statement enables you to perform Wald tests for model effects that test Type I, Type II, or Type III hypotheses. For more information about constructing of Type I, II, and III estimable functions, see Chapter 15, “[The Four Types of Estimable Functions](#).”

Table 51.6 summarizes the *options* that you can specify in the TEST statement.

Table 51.6 TEST Statement Options

Option	Description
E	Requests Type I, Type II, and Type III coefficients
E1	Requests Type I coefficients
E2	Requests Type II coefficients
E3	Requests Type III coefficients
HTYPE=	Indicates the type of hypothesis test to perform

For information about the syntax of the TEST statement, see the section “[TEST Statement](#)” on page 509 in Chapter 19, “[Shared Concepts and Topics](#).”

Details: ICPHREG Procedure

Model and Likelihood

Suppose that the observations to be analyzed consist of interval-censored outcomes $\{[L_i, R_i]; \mathbf{Z}_i\}$, $i = 1, \dots, n$, where n is the number of subjects. \mathbf{Z}_i denotes a p -dimensional vector of covariates for the i th subject. This notation allows for exact event times, right-censored data and left-censored data as special cases. When $L_i = R_i$, the observation is an exact time; when $R_i = \infty$, the observation is right-censored; when $L_i = 0$, the observation is left-censored.

Let $S(t; \mathbf{Z}_i)$ denote the survival function for a subject whose covariate is \mathbf{Z}_i . Assuming that t is continuous, denote $f(t; \mathbf{Z}_i)$ as the density function for the subject. The hazard function for the subject, $\lambda(t; \mathbf{Z}_i)$, is defined as the instantaneous failure rate at time t . Mathematically, the hazard function is determined as a ratio between the density function and the survival function:

$$\lambda(t; \mathbf{Z}_i) = f(t; \mathbf{Z}_i) / S(t; \mathbf{Z}_i)$$

A quantity that is closely related to the survival function is the cumulative hazard function, defined as

$$\Lambda(t; \mathbf{Z}_i) = \int_0^t \lambda(u; \mathbf{Z}_i) du$$

In turn, the cumulative hazard function determines the survival function:

$$S(t; \mathbf{Z}_i) = \exp(-\Lambda(t; \mathbf{Z}_i))$$

If some of the responses are left-, right-, or interval-censored, the log likelihood can be written as

$$\begin{aligned}\log(L) &= \sum \log [f(L_i; \mathbf{Z}_i)] + \sum \log [S(L_i; \mathbf{Z}_i)] \\ &+ \sum \log [1 - S(R_i; \mathbf{Z}_i)] + \sum \log [S(L_i; \mathbf{Z}_i) - S(R_i; \mathbf{Z}_i)]\end{aligned}$$

where the first sum is the total of the uncensored observations, the second sum is the total of the right-censored observations, the third sum is the total of the left-censored observations, and the last sum is the total of the interval-censored observations.

For the i th subject, the proportional hazards model (Cox 1972) assumes that

$$\lambda(t; \mathbf{Z}_i) = \lambda_0(t) \exp(\mathbf{Z}_i' \boldsymbol{\beta})$$

where $\boldsymbol{\beta}$ is a p -dimensional vector of coefficients for the covariate vector \mathbf{Z}_i and $\lambda_0(t)$ is the baseline hazard function, which is the hazard rate when all the coefficients for the covariates are equal to 0.

Under the proportional hazards model, the cumulative hazard function for the i th subject is

$$\Lambda(t; \mathbf{Z}_i) = \int_0^t \lambda(u; \mathbf{Z}_i) du = \int_0^t \lambda_0(u) du \exp(\mathbf{Z}_i' \boldsymbol{\beta}) = \Lambda_0(t) \exp(\mathbf{Z}_i' \boldsymbol{\beta})$$

The survival function for the i th subject is

$$S(t; \mathbf{Z}_i) = \exp[-\Lambda(t; \mathbf{Z}_i)] = S_0(t)^{\exp(\mathbf{Z}_i' \boldsymbol{\beta})}$$

where $S_0(t)$ denotes the baseline survival function and $S_0(t) = \exp[-\Lambda_0(t)]$.

The density function for the subject is obtained by differentiating the survival function:

$$f(t; \mathbf{Z}_i) = -\frac{S(t; \mathbf{Z}_i)}{dt} = \lambda(t; \mathbf{Z}_i) S(t; \mathbf{Z}_i) = \lambda_0(t) \exp(\mathbf{Z}_i' \boldsymbol{\beta}) S_0(t)^{\exp(\mathbf{Z}_i' \boldsymbol{\beta})}$$

Given these quantities, the likelihood function under the proportional hazards model can be expressed as

$$\begin{aligned}\log(L) &= \sum \log [\lambda_0(L_i) \exp(\mathbf{Z}_i' \boldsymbol{\beta}) S_0(L_i)^{\exp(\mathbf{Z}_i' \boldsymbol{\beta})}] + \sum \log [S_0(L_i)^{\exp(\mathbf{Z}_i' \boldsymbol{\beta})}] \\ &+ \sum \log [1 - S_0(R_i)^{\exp(\mathbf{Z}_i' \boldsymbol{\beta})}] + \sum \log [S_0(L_i)^{\exp(\mathbf{Z}_i' \boldsymbol{\beta})} - S_0(R_i)^{\exp(\mathbf{Z}_i' \boldsymbol{\beta})}]\end{aligned}$$

where the first sum is the total of the uncensored observations, the second sum is the total of the right-censored observations, the third sum is the total of the left-censored observations, and the last sum is the total of the interval-censored observations.

This likelihood function is often referred as the *full likelihood* as compared to the partial likelihood (Cox 1972) because it involves parameters for the baseline hazard function in addition to the regression coefficients $\boldsymbol{\beta}$. The full likelihood is often used for analyzing interval-censored data because constructing a likelihood function that contains only the regression coefficients as conveniently as the Cox partial likelihood does for right-censored data is not straightforward (Finkelstein 1986).

Baseline Parameterization

Because any one of the baseline hazard, cumulative hazard, and survival functions determines the others, it is sufficient to parameterize one of them. For the baseline function, PROC ICPHREG supports the parameterizations that are described in the following subsections.

Piecewise Constant Model

As its name suggests, the piecewise constant hazard rate model parameterizes the baseline hazard function as a union of several disjoint intervals, within each of which the hazard rate is constant:

$$\lambda_0(t) = r_j \text{ if } a_{j-1} \leq t < a_j, j = 1, \dots, J$$

It follows that the baseline cumulative hazard function is

$$\Lambda_0(t) = \sum_{j=1}^J r_j \Delta_j(t)$$

where

$$\Delta_j(t) = \begin{cases} 0 & t < a_{j-1} \\ t - a_{j-1} & a_{j-1} \leq t < a_j \\ a_j - a_{j-1} & t \geq a_j \end{cases}$$

To produce a meaningful hazard function, the r_j need to be bounded below by 0. Such a constraint can be removed by transforming the parameters to a natural log scale:

$$\alpha_j = \log(r_j), \quad j = 1, \dots, J$$

PROC ICPHREG uses either the original or the transformed scale to fit piecewise constant models. You can change the scale by using the HAZSCALE= option. By default, the original scale is used.

Cubic Splines Model

For the proportional hazards model, Royston and Parmar (2002) propose modeling the log of the baseline cumulative hazard function in terms of natural cubic splines,

$$\log[\Lambda_0(t)] = \gamma_0 + \gamma_1 x + \gamma_2 v_1(x) + \dots + \gamma_{m+1} v_J(x)$$

where $x = \log(t)$ represents the time on a log scale. The v_j are the basis functions, which are computed as

$$v_j(x) = (x - k_j)_+^3 - e_j(x - k_{\min})_+^3 - (1 - e_j)(x - k_{\max})_+^3$$

where

$$e_j = \frac{k_{\max} - k_j}{k_{\max} - k_{\min}}$$

$$(x - a)_+ = \max(0, x - a)$$

Here, k_{\min} and k_{\max} are two terminal knots, and $k_1 < \dots < k_J$ are m interval knots that are placed between k_{\min} and k_{\max} . The degrees of freedom equals $m + 1$. When $m = 0$, the log of the baseline hazard becomes $\gamma_0 + \gamma_1 x$, which corresponds to a common form of the Weibull model. When $\gamma_1 = 1$, the Weibull model further reduces to the exponential model.

Specification of Effects

Each term in a model is called an effect. You specify effects in the MODEL statement by using a special notation that uses variable names and operators. There are two types of variables: *classification* (CLASS) variables and *continuous* variables. There are two primary types of operators: *crossing* and *nesting*. A third type, the *bar* operator, is used to simplify effect specification.

Variables that identify classification levels are called CLASS variables in SAS and are identified in a CLASS statement. These might also be called *categorical*, *qualitative*, *discrete*, or *nominal* variables. CLASS variables can be either character or numeric. The values of CLASS variables are called *levels*. For example, the CLASS variable Sex could have the levels “male” and “female.”

In a model, an explanatory variable that is not declared in a CLASS statement is assumed to be continuous. Continuous variables must be numeric. For example, the heights and weights of subjects in an experiment are continuous variables.

The following list shows types of effects that are often useful in practice, where A, B, and C are classification variables and X1 and X2 are continuous variables:

- Regressor effects are specified by writing continuous variables by themselves: X1, X2.
- Polynomial effects are specified by joining two or more continuous variables with asterisks: X1*X2.
- Main effects are specified by writing classification variables by themselves: A, B, C.
- Crossed effects (interactions) are specified by using asterisks to join two or more classification variables: A*B, B*C, A*B*C.
- Nested effects are specified by following a main effect or crossed effect with a classification variable or list of classification variables that are enclosed in parentheses: B(A), C(B A), A*B(C). In the preceding example, B(A) is “B nested within A.”
- Combinations of continuous and classification variables can be specified in the same way by using the crossing and nesting operators.

The bar operator uses a vertical bar (|) to join two effects. The bar operator is shorthand notation for including the left-hand side, the right-hand side, and the cross between them as effects in the model. For example, A | B is equivalent to A B A*B. The effects that are joined by the bar operator can be classification variables, continuous variables, or combinations of effects that are defined by using operators. Multiple bars are permitted. For example, A | B | C means A B C A*B A*C B*C A*B*C.

You can specify the maximum number of variables in any effect that results from bar evaluation by specifying the maximum number, preceded by an @ sign. For example, A | B | C@2 results in effects that involve two or fewer variables: A B C A*B A*C B*C.

Computational Details

Design Matrix

The linear predictor part of a proportional hazards model is

$$\mu = \mathbf{Z}'\boldsymbol{\beta}$$

where $\boldsymbol{\beta}$ is a vector of unknown regression coefficients and \mathbf{Z} is a known design matrix. The ordering of these parameters is displayed in the “CLASS Level Information” table and in tables that display the parameter estimates of the fitted model.

When you use the **PARAM=GLM** option in the CLASS statement to specify an overparameterized model, some columns of \mathbf{Z} can be linearly dependent on other columns. For example, when you specify a model that consists of a classification variable, the column that corresponds to any one of the levels of the classification variable is linearly dependent on the other columns of \mathbf{Z} . The columns of $\mathbf{Z}'\mathbf{Z}$ are checked in the order in which the model is specified for dependence on preceding columns. If a dependency is found, the parameter that corresponds to the dependent column and its standard error are set to 0 to indicate that it is not estimated. The test for linear dependence is controlled by the **SINGULAR=** option in the MODEL statement. You can use the **ORDER=** option in the CLASS statement to specify the order in which the levels of a classification variable are checked for dependencies. For full-rank parameterizations, the columns of the \mathbf{Z} matrix are designed to be linearly independent.

Initial Values

The initial values of the regression coefficients $\boldsymbol{\beta}$ are all set to 0.

For the piecewise constant model, the initial values of the hazard parameters are set equal to the exponential rate that is estimated from an imputed data set. The data set is obtained by imputing a middle point for the interval-censored and left-censored observations while retaining the right-censored and exact observations. For the cubic spline model, the first spline coefficient, γ_0 , is set to be the log of the exponential rate estimated with the previous imputed data, and the second spline coefficient, γ_1 , is set to 1. The remaining spline coefficients, if there are any, are set to 0.

Maximum Likelihood Estimation

By default, the ICPHREG procedure uses a Newton-Raphson algorithm to maximize the log-likelihood function with respect to the parameters.

Denote the set of parameters that need to be estimated as $\boldsymbol{\omega} = \{\omega_j\}$, which consists of the parameters that determine baseline hazard function $\Lambda_0(t)$ and the regression coefficients $\boldsymbol{\beta}$. On the r th iteration, the algorithm updates the parameter vector $\boldsymbol{\omega}_r$ with

$$\boldsymbol{\omega}_{r+1} = \boldsymbol{\omega}_r - \mathbf{H}^{-1}\mathbf{g}$$

where \mathbf{H} is the Hessian (second derivative) matrix, and \mathbf{g} is the gradient (first derivative) vector of the log-likelihood function, both evaluated at the current value of the parameter vector. That is,

$$\mathbf{g} = [g_j] = \left[\frac{\partial l}{\partial \omega_j} \right]$$

and

$$\mathbf{H} = [h_{ij}] = \left[\frac{\partial^2 l}{\partial \omega_i \partial \omega_j} \right]$$

The ICPHREG procedure also supports other optimization methods, such as quasi-Newton and Newton-Raphson with ridging. These methods are described in the section “[Choosing an Optimization Algorithm](#)” on page 501 in Chapter 19, “[Shared Concepts and Topics](#).”

Covariance and Correlation Matrix

The estimated covariance matrix of the parameter estimator is

$$\mathbf{\Sigma} = -\mathbf{H}^{-1}$$

where \mathbf{H} is the Hessian matrix that is evaluated using the parameter estimates on the last iteration. If some parameters in the baseline function are held fixed, they are not incorporated in \mathbf{H} . Rows and columns that correspond to aliased parameters are not included in $\mathbf{\Sigma}$.

The correlation matrix is the normalized covariance matrix. That is, if σ_{ij} is an element of $\mathbf{\Sigma}$, then the corresponding element of the correlation matrix is $\sigma_{ij}/\sigma_i\sigma_j$, where $\sigma_i = \sqrt{\sigma_{ii}}$.

Choosing Break Points

There are no obvious ways to choose break points for parameterizing the baseline function in terms of a piecewise constant function or a cubic spline curve. For right-censored data, PROC PHREG chooses a set of points such that the resulting time intervals contain approximately equal numbers of event times. This is difficult for interval-censored data because event times are not fully observed. Friedman (1982) recommends choosing the points so that the expected number of events is comparable among the time intervals. For an interval-censored spline model, Cai and Betensky (2003) propose an ad hoc approach that uses the quantile values of the unique time points among $\{L_i, R_i, (L_i + R_i)/2, i = 1, \dots, n\}$ for choosing the knot values.

Ibrahim, Chen, and Sinha (2001) propose the equally spaced quantile partition (ESQP) method for selecting break points in the right-censored data to fit the piecewise constant model. Suppose there are Q break points to be determined. The ICPHREG procedure modifies this method to handle interval-censored data. First, it imputes a middle point for each observation that is not right-censored. Then, it merges these values with the observed boundary values in the input data set, except for the right-censored observations. Next, it sorts these values in increasing order.

Suppose the unique values of the sorted sequence are $u_1 < u_2 < \dots < u_M$. First, PROC ICPHREG computes the targeted quantile for each break point as $q_j = j/(Q + 1)$ ($j = 1, \dots, Q$). Then, it chooses the point u_{m+1} , where m equals the integer part of the product $q_j M$. If $q_j M$ is already an integer, then the chosen break point is set to be $(u_m + u_{m+1})/2$. When there are no ties in the sorted sequence for right-censored data, this method is identical to the original ESQP method.

Fit Statistics

Suppose that the model contains q estimated parameters and that n observations are used in model fitting. The fit criteria displayed by the ICPHREG procedure are calculated as follows:

- $-2 \log$ likelihood:

$$-2\log(L)$$

where L is the maximized likelihood for the model.

- Akaike's information criterion:

$$\text{AIC} = -2\log(L) + 2q$$

- corrected Akaike's information criterion:

$$\text{AICC} = \text{AIC} + \frac{2q(q+1)}{n-q-1}$$

- Bayesian information criterion:

$$\text{BIC} = -2\log(L) + q \log(n)$$

For more information about AIC and BIC, see Akaike (1981, 1979). For a discussion of using AIC, AICC, and BIC in statistical modeling, see Simonoff (2003).

Predicted Values

Given a new vector of covariates \mathbf{Z}_{new} , the linear predictor is computed as $\hat{\mu}_{\mathbf{Z}_{\text{new}}} = \mathbf{Z}'_{\text{new}}\hat{\boldsymbol{\beta}}$, where $\hat{\boldsymbol{\beta}}$ is the maximum likelihood estimate of $\boldsymbol{\beta}$. The variance of $\hat{\mu}_{\mathbf{Z}_{\text{new}}}$ is estimated by

$$\hat{\sigma}_{\mathbf{Z}_{\text{new}}}^2 = \mathbf{Z}'_{\text{new}} \boldsymbol{\Sigma}_{\hat{\boldsymbol{\beta}}} \mathbf{Z}_{\text{new}}$$

where $\boldsymbol{\Sigma}_{\hat{\boldsymbol{\beta}}}$ denotes the estimated covariance matrix for $\hat{\boldsymbol{\beta}}$.

Suppose the estimated baseline hazard is $\hat{\Lambda}_0(t)$. Given \mathbf{Z}_{new} , the cumulative hazard function can be predicted by

$$\hat{\Lambda}(t; \mathbf{Z}_{\text{new}}) = \hat{\Lambda}_0(t) e^{\mathbf{Z}'_{\text{new}} \hat{\boldsymbol{\beta}}}$$

Denote the vector of parameters that is used for obtaining $\hat{\Lambda}_0(t)$ as $\boldsymbol{\tau}$. It is apparent that $\boldsymbol{\tau} \cap \boldsymbol{\beta} = \emptyset$. The vector of parameters that need to be estimated can be represented as $\boldsymbol{\omega} = (\boldsymbol{\beta}, \boldsymbol{\tau})$.

The variance of $\hat{\Lambda}(t; \mathbf{Z}_{\text{new}})$ can be estimated by applying the delta method:

$$\hat{\sigma}^2(\hat{\Lambda}(t; \mathbf{Z}_{\text{new}})) = P(t, \hat{\boldsymbol{\omega}})' \boldsymbol{\Sigma} P(t, \hat{\boldsymbol{\omega}})$$

where

$$P(t, \boldsymbol{\omega}) = \frac{\partial \Lambda(t; \mathbf{Z}_{\text{new}})}{\partial \boldsymbol{\omega}}$$

and $\boldsymbol{\Sigma}$ denotes the estimated covariance matrix for $\hat{\boldsymbol{\omega}}$.

Given \mathbf{Z}_{new} , the predicted survival function is estimated by

$$\hat{S}(t; \mathbf{Z}_{\text{new}}) = \exp(\hat{\Lambda}(t; \mathbf{Z}_{\text{new}}))$$

The standard error of $\hat{S}(t; \mathbf{Z}_{\text{new}})$ can be conveniently estimated by an application of the delta method:

$$\hat{\sigma}(\hat{S}(t; \mathbf{Z}_{\text{new}})) = \hat{S}(t; \mathbf{Z}_{\text{new}}) \hat{\sigma}(\hat{\Lambda}(t; \mathbf{Z}_{\text{new}}))$$

By default, a natural log transformation is applied to obtain the pointwise confidence limits for $S(t; \mathbf{Z}_{\text{new}})$ and $\Lambda(t; \mathbf{Z}_{\text{new}})$. You can use the **CLTYPE=** option to specify a different transformation for $S(t; \mathbf{Z}_{\text{new}})$.

Hazard Ratios

Consider a dichotomous risk factor variable X that takes the value 1 if the risk factor is present and 0 if the risk factor is absent. The log-hazard function is

$$\log[\lambda(t|X)] = \log[\lambda_0(t)] + \beta_1 X$$

where $\lambda_0(t)$ is the baseline hazard function.

The hazard ratio ψ is defined as the ratio of the hazard for those who have the risk factor ($X = 1$) to the hazard for those who do not have the risk factor ($X = 0$). The log of the hazard ratio is

$$\log(\psi) \equiv \log[\psi(X = 1, X = 0)] = \log[\lambda(t|X = 1)] - \log[\lambda(t|X = 0)] = \beta_1$$

In general, the hazard ratio can be computed by exponentiating the difference of the log-hazard between any two population profiles. This is the approach taken by the **HAZARDRATIO** statement, so the computations are available regardless of parameterization, interactions, and nestings. However, as shown in the preceding equation for $\log(\psi)$, hazard ratios of main effects can be computed as functions of the parameter estimates. The remainder of this section is concerned with this methodology.

The parameter β_1 that is associated with X represents the change in the log-hazard from $X = 0$ to $X = 1$. So the hazard ratio is obtained by simply exponentiating the value of the parameter that is associated with the risk factor. The hazard ratio indicates how the hazard changes as you change X from 0 to 1. For example, $\psi = 2$ means that the hazard when $X = 1$ is twice the hazard when $X = 0$.

Suppose the values of the dichotomous risk factor are coded as constants a and b instead of 0 and 1. The hazard when $X = a$ becomes $\lambda(t) \exp(a\beta_1)$, and the hazard when $X = b$ becomes $\lambda(t) \exp(b\beta_1)$. The hazard ratio that corresponds to an increase in X from a to b is

$$\psi = \exp[(b - a)\beta_1] = [\exp(\beta_1)]^{b-a} \equiv [\exp(\beta_1)]^c$$

Note that for any a and b such that $c = b - a = 1$, $\psi = \exp(\beta_1)$. So the hazard ratio can be interpreted as the change in the hazard for any increase of one unit in the corresponding risk factor. However, the change in hazard for some amount other than one unit is often of greater interest. For example, a change of one pound in body weight might be too small to be considered important, whereas a change of 10 pounds might be more meaningful. The hazard ratio for a change in X from a to b is estimated by raising the hazard ratio estimate for a unit change in X to the power of $c = b - a$ as shown previously.

For a polytomous risk factor, the computation of hazard ratios depends on how the risk factor is parameterized. For illustration, suppose that Cell is a risk factor that has four categories: Adeno, Large, Small, and Squamous. For the effect parameterization scheme (**PARAM=EFFECT**) with Squamous as the reference group, the design variables for Cell are as follows:

Cell	Design Variables		
	X_1	X_2	X_3
Adeno	1	0	0
Large	0	1	0
Small	0	0	1
Squamous	-1	-1	-1

The log-hazard for Adeno is

$$\begin{aligned}\log[\lambda(t|\text{Adeno})] &= \log[\lambda_0(t)] + \beta_1(X_1 = 1) + \beta_2(X_2 = 0) + \beta_3(X_3 = 0) \\ &= \lambda_0(t) + \beta_1\end{aligned}$$

The log-hazard for Squamous is

$$\begin{aligned}\log[\lambda(t|\text{Squamous})] &= \log[\lambda_0(t)] + \beta_1(X_1 = -1) + \beta_2(X_2 = -1) + \beta_3(X_3 = -1) \\ &= \log[\lambda_0(t)] - \beta_1 - \beta_2 - \beta_3\end{aligned}$$

Therefore, the log-hazard ratio of Adeno versus Squamous

$$\begin{aligned}\log[\psi(\text{Adeno}, \text{Squamous})] &= \log[\lambda(t|\text{Adeno})] - \log[\lambda(t|\text{Squamous})] \\ &= 2\beta_1 + \beta_2 + \beta_3\end{aligned}$$

For the reference cell parameterization scheme (**PARAM=REF**) in which Squamous is the reference cell, the design variables for Cell are as follows:

Cell	Design Variables		
	X_1	X_2	X_3
Adeno	1	0	0
Large	0	1	0
Small	0	0	1
Squamous	0	0	0

The log-hazard ratio of Adeno versus Squamous is

$$\begin{aligned}\log(\psi(\text{Adeno}, \text{Squamous})) &= \log[\lambda(t|\text{Adeno})] - \log[\lambda(t|\text{Squamous})] \\ &= (\log[\lambda_0(t)] + \beta_1(X_1 = 1) + \beta_2(X_2 = 0) + \beta_3(X_3 = 0)) - \\ &\quad (\log[\lambda_0(t)] + \beta_1(X_1 = 0) + \beta_2(X_2 = 0) + \beta_3(X_3 = 0)) \\ &= \beta_1\end{aligned}$$

For the GLM parameterization scheme (**PARAM=GLM**), the design variables are as follows:

Cell	Design Variables			
	X_1	X_2	X_3	X_4
Adeno	1	0	0	0
Large	0	1	0	0
Small	0	0	1	0
Squamous	0	0	0	1

The log-hazard ratio of Adeno versus Squamous is

$$\begin{aligned}
 & \log(\psi(\text{Adeno}, \text{Squamous})) \\
 &= \log[\lambda(t|\text{Adeno})] - \log[\lambda(t|\text{Squamous})] \\
 &= \log[\lambda_0(t)] + \beta_1(X_1 = 1) + \beta_2(X_2 = 0) + \beta_3(X_3 = 0) + \beta_4(X_4 = 0) - \\
 & \quad (\log(\lambda_0(t)) + \beta_1(X_1 = 0) + \beta_2(X_2 = 0) + \beta_3(X_3 = 0) + \beta_4(X_4 = 1)) \\
 &= \beta_1 - \beta_4
 \end{aligned}$$

Consider Cell as the only risk factor. The computation of the hazard ratio of Adeno versus Squamous for various parameterization schemes is shown in Table 51.7.

Table 51.7 Hazard Ratio of Adeno to Squamous

PARAM=	Parameter Estimates				Hazard Ratio Estimates
	$\hat{\beta}_1$	$\hat{\beta}_2$	$\hat{\beta}_3$	$\hat{\beta}_4$	
EFFECT	0.5772	-0.2115	0.2454		$\exp(2 \times 0.5772 - 0.2115 + 0.2454) = 3.281$
REF	1.8830	0.3996	0.8565		$\exp(1.8830) = 3.281$
GLM	1.8830	0.3996	0.8565	0.0000	$\exp(1.8830) = 3.281$

The fact that the log-hazard ratio ($\log(\psi)$) is a linear function of the parameters enables the **HAZARDRATIO statement** to compute the hazard ratio of the main effect even in the presence of interactions and nest effects.

To customize hazard ratios for specific units of change for a continuous risk factor, you can use the **UNITS=** option in a **HAZARDRATIO statement** to specify a list of relevant units for each explanatory variable in the model. Estimates of these customized hazard ratios are shown in a separate table. Let (V_j, U_j) be a confidence interval for $\log(\psi)$. The corresponding lower and upper confidence limits for the customized hazard ratio $\exp(c\beta_j)$ are $\exp(cV_j)$ and $\exp(cU_j)$, respectively for $c > 0$, or $\exp(cU_j)$ and $\exp(cV_j)$, respectively for $c < 0$.

Let \mathbf{e}_j be the j th unit vector—that is, the j th entry of the vector is 1 and all other entries are 0. The hazard ratio for the explanatory variable with regression coefficient $\beta_j = \mathbf{e}_j' \boldsymbol{\beta}$ is defined as $\exp(\beta_j)$. In general, a log-hazard ratio can be written as $\mathbf{h}' \boldsymbol{\beta}$ (a linear combination of the regression coefficients), and the hazard ratio $\exp(\mathbf{h}' \boldsymbol{\beta})$ is obtained by replacing \mathbf{e}_j with \mathbf{h} .

Point Estimate

The hazard ratio $\exp(\mathbf{e}'_j \boldsymbol{\beta})$ is estimated by $\exp(\mathbf{e}'_j \hat{\boldsymbol{\beta}})$, where $\hat{\boldsymbol{\beta}}$ is the maximum likelihood estimate of the regression coefficients $\boldsymbol{\beta}$.

Wald's Confidence Limits

The $100(1 - \alpha)\%$ confidence limits for the hazard ratio are calculated as

$$\exp \left(\mathbf{e}'_j \hat{\boldsymbol{\beta}} \pm z_{\alpha/2} \sqrt{\mathbf{e}'_j \boldsymbol{\Sigma}_{\hat{\boldsymbol{\beta}}} \mathbf{e}_j} \right)$$

where $\boldsymbol{\Sigma}_{\hat{\boldsymbol{\beta}}}$ is estimated covariance matrix and $z_{\alpha/2}$ is the $100(1 - \alpha/2)$ percentile point of the standard normal distribution.

Input and Output Data Sets

OUT= Output Data Set in the BASELINE Statement

The **OUT=** data set in the BASELINE statement contains all the variables in the **COVARIATES=** data set, along with statistics you request by specifying *keyword=name* options. There are n observations in the **OUT=** data set for each observation in the **COVARIATES=** data set, where n is the number of break points for the fitted model.

Missing Values

Observations that contain a missing value for both the left boundary value and the right boundary value in the response are not used in the analysis. If a **FREQ** variable value is missing or 0, the observation is not used. If any explanatory variable that is specified in the **MODEL** statement has a missing value, that observation is not used in the model fitting. Predicted values are computed for all observations that have no missing explanatory variable values.

Displayed Output

PROC ICPHREG displays the following information as results of the model fitting.

Model Information

The “Model Information” table displays the two-level name of the input data set, the type of model fitted, the parameterization type that is used for the baseline function, and the name and label of the dependent variables. If you specify the **FREQ** statement, this table also displays the name and label of the frequency variable.

Class Level Information

If you specify a CLASS statement, PROC ICPHREG outputs the “Class Level Information” table. This table displays the design information for the classification variables when the parameterization is full rank.

Class Variable Levels

If you specify a CLASS statement, PROC ICPHREG outputs the “Class Variable Levels” table. This table displays the levels of classification variables when the parameterization is not full rank.

Fit Statistics

The “Fit Statistics” table displays the negative of twice the log likelihood, Akaike’s information criterion (AIC), the corrected Akaike’s information criterion (AICC), and the Bayesian information criterion (BIC). This table is displayed by default.

Analysis of Maximum Likelihood Parameter Estimates

The “Analysis of Maximum Likelihood Parameter Estimates” table displays the parameter name, the degrees of freedom for each parameter, the maximum likelihood estimate of each parameter, the estimated standard error of the parameter estimator, confidence limits for each parameter, a chi-square statistic for testing whether the parameter is 0, and the associated p -value for the statistic. This table is displayed by default.

Iteration History for Parameter Estimates

If you specify the ITHISTORY option in the PROC ICPHREG statement, the procedure outputs a table that contains the following for each iteration in the iterative procedure for model fitting: the iteration number, the negative of twice of the log likelihood, the gradient, and values of all parameters in the model.

Last Evaluation of the Gradient

If you specify the ITHISTORY option in the PROC ICPHREG statement, the procedure displays the last evaluation of the gradient vector.

Last Evaluation of the Hessian

If you specify the ITHISTORY option in the PROC ICPHREG statement, the procedure displays the last evaluation of the Hessian matrix.

Estimated Covariance Matrix

If you specify the COVB option in the MODEL statement, the procedure displays the estimated covariance matrix. This matrix is defined as the inverse of the information matrix at the final iteration and is based on the Hessian matrix that is used at the final iteration.

Estimated Correlation Matrix

If you specify the CORRB option in the MODEL statement, the procedure displays the estimated correlation matrix, which is based on the Hessian matrix that is used at the final iteration.

Hazard Ratios for *label*

If you specify the HAZARDRATIO statement, PROC ICPHREG outputs the “Hazard Ratios for *label*” table. The table displays the estimate and confidence limits for each hazard ratio. The ODS name of the “Hazard Ratios for *label*” table is HazardRatios.

Parameter Information

If you specify the ITHISTORY, COVB, or CORRB option in the MODEL statement, PROC ICPHREG outputs the “Parameter Information” table. This table displays the names of the parameters and the corresponding level information of effects that contain the CLASS variables. The ODS name of the “Parameter Information” table is ParmInfo.

Constant Hazard Time Intervals

If a piecewise constant model is used (the default model), PROC ICPHREG outputs the “Constant Hazard Time Intervals” table. This table displays information about the parameterization of the baseline function under the piecewise constant model. The ODS name of the “Constant Hazard Time Intervals” table is HazardParms.

Cubic Spline Parameters

If you fit a cubic spline model, PROC ICPHREG outputs the “Cubic Spline Parameters” table. This table displays information about the parameterization of the baseline function under the cubic spline model. The ODS name of the “Cubic Spline Parameters” table is HazardParms.

ODS Table Names

PROC ICPHREG assigns a name to each table it creates. You can use these names to refer to the table when you use the Output Delivery System (ODS) to select tables and create output data sets. These names are listed in Table 51.8. For more information about ODS, see Chapter 20, “Using the Output Delivery System.”

Table 51.8 ODS Tables Produced by PROC ICPHREG

ODS Table Name	Description	Statement	Option
ClassLevelInfo	Design information for CLASS variables	CLASS	
ClassLevels	Classification variables levels	CLASS	PARAM=GLM
ConvergenceStatus	Convergence status	MODEL	
CorrB	Parameter estimate correlation matrix	MODEL	CORRB
CovB	Parameter estimate covariance matrix	MODEL	COVB
FitStatistics	Fit statistics	MODEL	
HazardRatios	Customized hazard ratio estimates	HAZARDRATIO	
LastGrad	Last evaluation of the gradient	PROC	ITHISTORY
LastHess	Last evaluation of the Hessian	PROC	ITHISTORY

Table 51.8 *continued*

ODS Table Name	Description	Statement	Option
IterHist	Iteration history	PROC	ITHISTORY
ModelInfo	Model and data information	MODEL	
NObs	Number of observations	MODEL	
OptInfo	Optimization Information	MODEL	
ParameterEstimates	Parameter estimates	MODEL	
ParmInfo	Regression effect names	CLASS	
HazardParms	Baseline parameters	MODEL	

ODS Graphics

Statistical procedures use ODS Graphics to create graphs as part of their output. ODS Graphics is described in detail in Chapter 21, “[Statistical Graphics Using ODS](#).”

Before you create graphs, ODS Graphics must be enabled (for example, by specifying the ODS GRAPHICS ON statement). For more information about enabling and disabling ODS Graphics, see the section “[Enabling and Disabling ODS Graphics](#)” on page 606 in Chapter 21, “[Statistical Graphics Using ODS](#).”

The overall appearance of graphs is controlled by ODS styles. Styles and other aspects of using ODS Graphics are discussed in the section “[A Primer on ODS Statistical Graphics](#)” on page 605 in Chapter 21, “[Statistical Graphics Using ODS](#).”

PROC ICPHREG assigns a name to each table that it creates. You can use these names to refer to the table when you use the Output Delivery System (ODS) to select tables and create output data sets. These names are listed separately in [Table 51.9](#). For more information about ODS, see Chapter 20, “[Using the Output Delivery System](#).”

Table 51.9 Graphs Produced by PROC ICPHREG

ODS Graph Name	Plot Description	Statement	Option
CumhazPlot	Cumulative hazard function plot	PROC	PLOTS=CUMHAZ
SurvivalPlot	Survival function plot	PROC	PLOTS=SURVIVAL

Examples: ICPHREG Procedure

Example 51.1: Fitting Cubic Spline Models

This example illustrates how to use a cubic spline baseline hazard to fit a proportional hazards model.

Consider the HIV data set in the section “[Getting Started: ICPHREG Procedure](#)” on page 3935. The following statements request a cubic spline proportional hazards model and the hazard ratio between the two levels of the Stage variable.

```
proc icphreg data=hiv;
  class Stage / desc;
  model (Left, Right) = Stage / basehaz=splines;
  hazardratio Stage;
run;
```

[Output 51.1.1](#) displays information about the fitted spline model.

Output 51.1.1 Model Information

The ICPHREG Procedure

Model Information	
Data Set	WORK.HIV
Left Boundary	Left
Right Boundary	Right
Baseline Hazard	Cubic Splines

If no suboption is specified for the spline model, PROC ICPHREG uses three knots, generating three spline coefficients. [Output 51.1.2](#) shows the selected knots.

Output 51.1.2 Cubic Spline Coefficients

Cubic Spline Parameters	
Coefficient	Knot
Coef1	1
Coef2	11
Coef3	25

The table of parameter estimates for the spline model is displayed in [Output 51.1.3](#).

Output 51.1.3 Parameter Estimates for the Spline Model

Analysis of Maximum Likelihood Parameter Estimates							
Effect	Stage	DF	Estimate	Standard Error	95% Confidence Limits		Chi-Square Pr > ChiSq
Coef1		1	-6.0630	3.2263	-12.3865	0.2605	
Coef2		1	1.4921	2.2568	-2.9311	5.9152	
Coef3		1	-0.3086	0.6708	-1.6233	1.0060	
Stage 1		1	1.9016	0.6662	0.5959	3.2072	8.15 0.0043
Stage 0		0	0.0000				

Output 51.1.4 shows the estimated hazard ratio between the two stages and the 95% confidence limits.

Output 51.1.4 Hazard Ratio Estimate for Stage Values 1 and 0

Hazard Ratios for Stage			
Description	Point Estimate	95% Wald Confidence Limits	
Stage 1 vs 0	6.697	1.815	24.711

The cubic spline model can be considered a generalization of the Weibull proportional hazards model. It reduces to the Weibull model when there are only two knots, in which case the degrees of freedom is one (DF=1). The Weibull model assumes that the cumulative hazard function is a straight line in the log time scale whereas cubic splines offer a richer set of shapes that have more knots. The following statements fit the spline model with DF=1:

```
proc icphreg data=hiv;
  class Stage / desc;
  model (Left, Right) = Stage / basehaz=splines(df=1);
  hazardratio Stage;
run;
```

The “Fit Statistics” table is displayed in Output 51.1.5.

Output 51.1.5 Fit Statistics for the Spline Model When DF=1**The ICPHREG Procedure**

Fit Statistics	
-2 Log Likelihood	30.025
AIC (Smaller is Better)	36.025
AICC (Smaller is Better)	36.914
BIC (Smaller is Better)	40.327

The table of parameter estimates for the fitted spline model is displayed in Output 51.1.6.

Output 51.1.6 Parameter Estimates for the Spline Model When DF=1

Analysis of Maximum Likelihood Parameter Estimates							
Effect	Stage	DF	Estimate	Standard Error	95% Confidence Limits		Chi-Square Pr > ChiSq
Coef1		1	-7.3481	2.4438	-12.1378	-2.5584	
Coef2		1	2.5420	0.8974	0.7831	4.3008	
Stage 1		1	1.8265	0.6132	0.6247	3.0283	8.87 0.0029
Stage 0		0	0.0000				

You can request that PROC LIFEREG fit an accelerated failure lifetime model by using the default distribution (Weibull). This would be equivalent to fitting the proportional hazards model by using a Weibull baseline hazard (Klein and Moeschberger 1997). The following statements fit the Weibull model:

```
proc lifereg data=hiv;
  class Stage;
  model (Left, Right) = Stage;
run;
```

The table of fit statistics is displayed in [Output 51.1.7](#).

Output 51.1.7 Fit Statistics That Are Produced by PROC LIFEREG**The LIFEREG Procedure**

Fit Statistics (Unlogged Response)	
-2 Log Likelihood	30.025
Weibull AIC (smaller is better)	36.025
Weibull AICC (smaller is better)	36.914
Weibull BIC (smaller is better)	40.327

The table of parameter estimates for the Weibull model is displayed in [Output 51.1.8](#).

Output 51.1.8 Parameter Estimates That Are Produced PROC LIFEREG

Analysis of Maximum Likelihood Parameter Estimates							
Parameter	DF	Estimate	Standard Error	95% Confidence Limits		Chi-Square	Pr > ChiSq
Intercept	1	2.1722	0.1791	1.8211	2.5233	147.06	<.0001
Stage	0 1	0.7185	0.2711	0.1871	1.2499	7.02	0.0080
Stage	1 0	0.0000
Scale	1	0.3934	0.1389	0.1969	0.7858		
Weibull Shape	1	2.5420	0.8974	1.2726	5.0776		

Comparing [Output 51.1.7](#) with [Output 51.1.5](#), you can see that the two model fits produce identical likelihood values.

The Weibull shape estimate is equal to the second spline coefficient, but the rest of the parameter estimates are different. This is because PROC LIFEREG fits the Weibull model under the configuration of accelerated failure time models. The estimates of regression coefficients from PROC LIFEREG and PROC ICPHREG

are proportional; their ratio equals the negative of the Weibull shape parameter. For example, the estimate -0.7185 from PROC LIFEREG can also be obtained by dividing the estimate 1.8265 from PROC ICPHREG by -2.5420 .

Example 51.2: Plotting Predicted Survival and Cumulative Hazard Functions

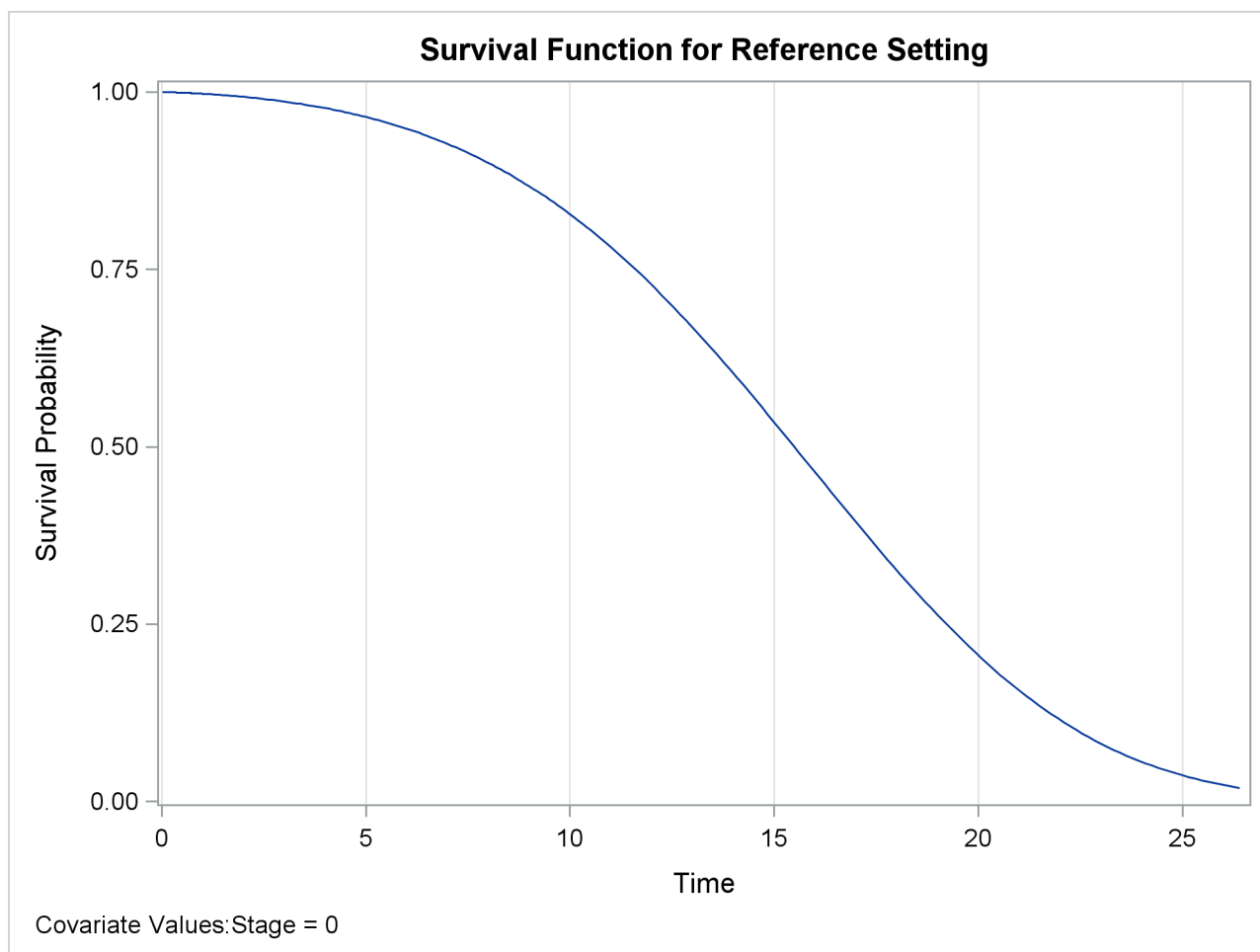
This example illustrates how to plot the predicted survival and cumulative hazard functions for specified covariate patterns.

The following statements request a plot of the estimated baseline survival function:

```
ods graphics on;
proc icphreg data=hiv plot=surv;
  class Stage / desc;
  model (Left, Right) = Stage / basehaz=splines;
run;
```

Output 51.2.1 shows the predicted survival curve at the reference level.

Output 51.2.1 Estimated Survival Curve for the Reference Set



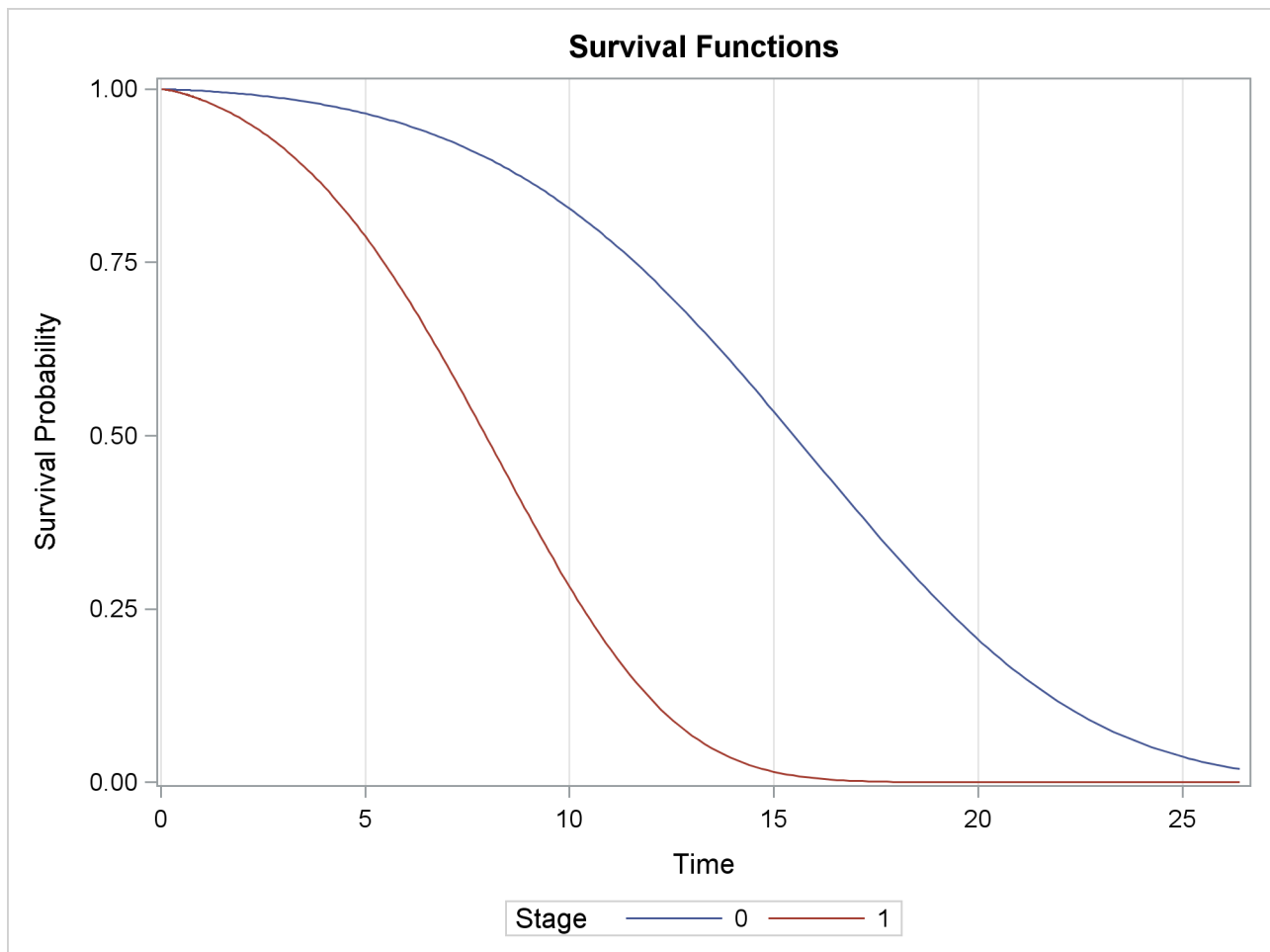
To produce curves for general covariate patterns, you can specify the `COVARIATES=` option in the `BASELINE` statement. The following statements create observations for two levels of `Stage` and plot the corresponding predicted curves:

```
data cov;
  Stage=0; output;
  Stage=1; output;
run;

proc icphreg data=hiv plot=surv;
  class Stage / desc;
  model (Left, Right) = Stage / basehaz=splines;
  baseline covariates=cov;
run;
```

Under the proportional hazards assumption, the two curves do not cross each other. As shown in [Output 51.2.2](#), patients at Stage 1 have much lower survival rates than patients at Stage 0.

Output 51.2.2 Predicted Survival Curves for Specified Covariate Patterns

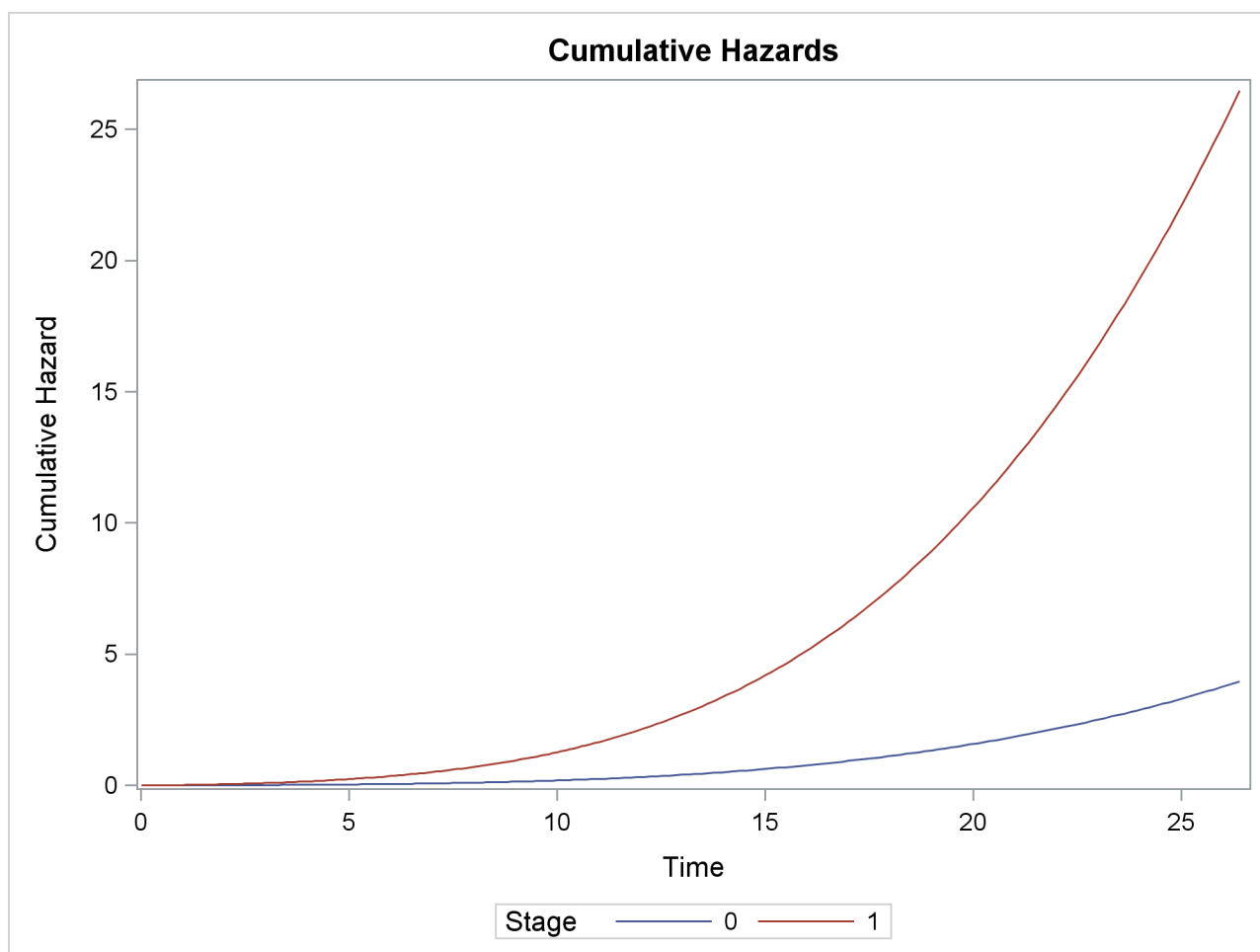


The following statements request a plot of the predicted cumulative hazard functions for the two levels of `Stage`:

```
proc icphreg data=hiv plot=cumhaz;  
  class Stage / desc;  
  model (Left, Right) = Stage / basehaz=splines;  
  baseline covariates=cov;  
run;
```

Output 51.2.3 shows the plot.

Output 51.2.3 Predicted Cumulative Hazards for Specified Covariate Patterns



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Subject Index

- alpha level
 - hazard ratio intervals (ICPHREG), 3954
 - ICPHREG procedure, 3941, 3949
- bar (|) operator
 - ICPHREG procedure, 3962
- baseline function
 - ICPHREG procedure, 3957, 3964
- baseline parameterization
 - ICPHREG procedure, 3961
- baseline statistics
 - ICPHREG procedure, 3947–3949
- classification variables
 - ICPHREG procedure, 3962
- continuous variables
 - ICPHREG procedure, 3962
- correlation matrix
 - ICPHREG procedure, 3957, 3964
- covariance matrix
 - ICPHREG procedure, 3957, 3964, 3965, 3969
- crossed effects
 - ICPHREG procedure, 3962
- cubic spline model
 - ICPHREG procedure, 3961
- design matrix
 - ICPHREG procedure, 3963
- effects
 - ICPHREG procedure, 3962
- estimation
 - maximum likelihood (ICPHREG), 3963
- exponential model
 - ICPHREG procedure, 3961
- fractional frequencies
 - ICPHREG procedure, 3954
- frequency variables
 - ICPHREG procedure, 3953
- full likelihood
 - ICPHREG procedure, 3960
- gradient
 - ICPHREG procedure, 3963
- hazard ratio
 - Wald's confidence limits (ICPHREG), 3969
- Hessian matrix
 - ICPHREG procedure, 3963
- ICPHREG procedure
 - alpha level, 3949, 3954
 - baseline function, 3957, 3964
 - baseline parameterization, 3961
 - baseline statistics, 3947–3949
 - break points, 3964
 - classification variables, 3962
 - computational details, 3963
 - continuous variables, 3962
 - correlation matrix, 3957, 3964
 - covariance matrix, 3957, 3964, 3965, 3969
 - crossed effects, 3962
 - cubic spline model, 3961
 - design matrix, 3963
 - effect specification, 3962
 - equally spaced quantile partition method, 3964
 - exponential model, 3961
 - fit statistics, 3964
 - fractional frequencies, 3954
 - full likelihood, 3960
 - gradient, 3963
 - hazard ratio, 3966, 3968
 - Hessian matrix, 3963
 - information matrix, 3934
 - initial values, 3963
 - input and output data sets, 3969
 - internal knots, 3961
 - linear hypotheses, 3934
 - linear predictor, 3949, 3963
 - log-hazard, 3966
 - main effects, 3962
 - maximum likelihood estimates, 3934
 - maximum likelihood estimation, 3963
 - missing values, 3969
 - nested effects, 3962
 - Newton-Raphson algorithm, 3963
 - ODS graph names, 3972
 - ODS table names, 3971
 - output data sets, 3969
 - parameter information, 3971
 - piecewise constant model, 3961
 - polynomial effects, 3962
 - predicted curves, 3944
 - predicted values, 3965
 - regressor effects, 3962
 - right-censored data, 3960, 3964

- spline parameters, 3971
- survival function, 3948
- terminal knots, 3961
- time intervals, 3971
- Weibull model, 3961, 3974
- information matrix
 - ICPHREG procedure, 3934
- internal knots
 - ICPHREG procedure, 3961
- linear hypotheses
 - ICPHREG procedure, 3934
- linear predictor
 - ICPHREG procedure, 3949, 3963
- linear transformation
 - baseline confidence intervals (ICPHREG), 3949
- log transformation
 - baseline confidence intervals (ICPHREG), 3949
- log-hazard
 - ICPHREG procedure, 3966
- log-log transformation
 - baseline confidence intervals (ICPHREG), 3949
- main effects
 - ICPHREG procedure, 3962
- maximum likelihood
 - ICPHREG procedure, 3934, 3963
- nested effects
 - ICPHREG procedure, 3962
- Newton-Raphson algorithm
 - ICPHREG procedure, 3963
- ODS graph names
 - ICPHREG procedure, 3972
- output data sets
 - ICPHREG procedure, 3969
- parameter information
 - ICPHREG procedure, 3971
- piecewise constant model
 - ICPHREG procedure, 3961
- polynomial effects
 - ICPHREG procedure, 3962
- predicted curves
 - ICPHREG procedure, 3944
- regressor effects
 - ICPHREG procedure, 3962
- right-censored data
 - ICPHREG procedure, 3960, 3964
- spline parameters
 - ICPHREG procedure, 3971
- standard error
 - ICPHREG procedure, 3948
- survival function
 - estimates (ICPHREG), 3948
- terminal knots
 - ICPHREG procedure, 3961
- time intervals
 - ICPHREG procedure, 3971
- Weibull model
 - ICPHREG procedure, 3961, 3974

Syntax Index

- ABSCONV option
 - PROC ICPHREG statement, [3941](#)
- ABSFCONV option
 - PROC ICPHREG statement, [3942](#)
- ABSGCONV option
 - PROC ICPHREG statement, [3942](#)
- ALPHA= option
 - BASELINE statement (ICPHREG), [3949](#)
 - HAZARDRATIO statement (ICPHREG), [3954](#)
 - MODEL statement (ICPHREG), [3957](#)
 - PROC ICPHREG statement, [3941](#)
- AT= option
 - HAZARDRATIO statement (ICPHREG), [3954](#)
- BASEHAZ= option
 - MODEL statement (ICPHREG), [3957](#)
- BASELINE statement
 - ICPHREG procedure, [3946](#)
- BY statement
 - ICPHREG procedure, [3950](#)
- CLASS statement
 - ICPHREG procedure, [3950](#)
- CLTYPE= option
 - BASELINE statement (ICPHREG), [3949](#)
- CORRB option
 - MODEL statement (ICPHREG), [3957](#)
- COVARIATES= option
 - BASELINE statement (ICPHREG), [3947](#)
- COVB option
 - MODEL statement (ICPHREG), [3957](#)
- CPREFIX= option
 - CLASS statement (ICPHREG), [3951](#)
- DATA= option
 - PROC ICPHREG statement, [3941](#)
- DESCENDING option
 - CLASS statement (ICPHREG), [3951](#)
- DIFF= option
 - HAZARDRATIO statement (ICPHREG), [3955](#)
- E option
 - HAZARDRATIO statement (ICPHREG), [3955](#)
- FCONV option
 - PROC ICPHREG statement, [3942](#)
- FREQ statement
 - ICPHREG procedure, [3953](#)
- GCONV option
 - PROC ICPHREG statement, [3942](#)
- GROUP= option
 - BASELINE statement (ICPHREG), [3949](#)
- HAZARDRATIO statement
 - ICPHREG procedure, [3954](#)
- HAZSCALE= option
 - MODEL statement (ICPHREG), [3958](#)
- ICPHREG procedure, [3940](#)
 - BASELINE statement, [3946](#)
 - BY statement, [3950](#)
 - FREQ statement, [3953](#)
 - HAZARDRATIO statement, [3954](#)
 - MODEL statement, [3956](#)
 - PROC ICPHREG statement, [3940](#)
 - syntax, [3940](#)
- ICPHREG procedure, BASELINE statement, [3946](#)
 - ALPHA= option, [3949](#)
 - CLTYPE= option, [3949](#)
 - COVARIATES= option, [3947](#)
 - GROUP= option, [3949](#)
 - keyword= option, [3947](#)
 - OUT= option, [3947](#)
 - ROWID= option, [3950](#)
 - TIMELIST= option, [3947](#)
- ICPHREG procedure, BY statement, [3950](#)
- ICPHREG procedure, FREQ statement, [3953](#)
 - NOTRUNCATE option, [3954](#)
- ICPHREG procedure, HAZARDRATIO statement, [3954](#)
 - ALPHA= option, [3954](#)
 - AT= option, [3954](#)
 - DIFF= option, [3955](#)
 - E option, [3955](#)
 - UNITS= option, [3956](#)
- ICPHREG procedure, MODEL statement, [3956](#)
 - ALPHA= option, [3957](#)
 - BASEHAZ= option, [3957](#)
 - CORRB option, [3957](#)
 - COVB option, [3957](#)
 - HAZSCALE= option, [3958](#)
 - NOPOLISH option, [3958](#)
 - OFFSET= option, [3958](#)
- ICPHREG procedure, PROC ICPHREG statement, [3940](#)
 - ABSCONV= option, [3941](#)
 - ABSFCONV= option, [3942](#)
 - ABSGCONV= option, [3942](#)

- ALPHA= option, 3941
- DATA= option, 3941
- FCONV= option, 3942
- GCONV= option, 3942
- ITHISTORY option, 3941
- MAXFUNC= option, 3943
- MAXITER= option, 3943
- MAXTIME= option, 3943
- NAMELEN= option, 3941
- NLOPTIONS option, 3941
- NOPRINT option, 3944
- NOTHEADS option, 3944
- PLOTS= option, 3944
- SINGULAR= option, 3946
- TECHNIQUE= option, 3943
- THREADS= option, 3946
- ICPHREG procedure, TEST statement, 3959
- ICPHREG procedure, CLASS statement, 3950
 - CPREFIX= option, 3951
 - DESCENDING option, 3951
 - LPREFIX= option, 3951
 - MISSING option, 3951
 - ORDER= option, 3951
 - PARAM= option, 3951
 - REF= option, 3952
 - TRUNCATE option, 3952
- ITHISTORY option
 - PROC ICPHREG statement, 3941
- keyword= option
 - BASELINE statement (ICPHREG), 3947
- LPREFIX= option
 - CLASS statement (ICPHREG), 3951
- MAXFUNC= option
 - PROC ICPHREG statement, 3943
- MAXITER= option
 - PROC ICPHREG statement, 3943
- MAXTIME= option
 - PROC ICPHREG statement, 3943
- MISSING option
 - CLASS statement (ICPHREG), 3951
- MODEL statement
 - ICPHREG procedure, 3956
- NAMELEN= option
 - PROC ICPHREG statement, 3941
- NLOPTIONS option
 - PROC ICPHREG statement, 3941
- NOPOLISH option
 - MODEL statement (ICPHREG), 3958
- NOPRINT option
 - PROC ICPHREG statement, 3944
- NOTHEADS option
 - PROC ICPHREG statement, 3944
- NOTRUNCATE option
 - FREQ statement (ICPHREG), 3954
- OFFSET= option
 - MODEL statement (ICPHREG), 3958
- ORDER= option
 - CLASS statement (ICPHREG), 3951
- OUT= option
 - BASELINE statement (ICPHREG), 3947
- PARAM= option
 - CLASS statement (ICPHREG), 3951
- PLOTS= option
 - PROC ICPHREG statement, 3944
- PROC ICPHREG statement
 - ICPHREG procedure, 3940
- REF= option
 - CLASS statement (ICPHREG), 3952
- ROWID= option
 - BASELINE statement (ICPHREG), 3950
- SINGULAR= option
 - PROC ICPHREG statement, 3946
- TECHNIQUE= option
 - PROC ICPHREG statement, 3943
- TEST statement
 - ICPHREG procedure, 3959
- THREADS= option
 - PROC ICPHREG statement, 3946
- TIMELIST= option
 - BASELINE statement (ICPHREG), 3947
- TRUNCATE option
 - CLASS statement (ICPHREG), 3952
- UNITS= option
 - HAZARDRATIO statement (ICPHREG), 3956