

SAS/STAT® 12.3 User's Guide The CANCORR Procedure (Chapter)



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Chapter 28

The CANCORR Procedure

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Overview: CANCORR Procedure

The CANCORR procedure performs canonical correlation, partial canonical correlation, and canonical redundancy analysis.

Canonical correlation is a generalization of multiple correlation for analyzing the relationship between two sets of variables. In multiple correlation, you examine the relationship between a linear combination of a set of explanatory variables, **X**, and a *single* response variable, **Y**. In canonical correlation, you examine the relationship between linear combinations of the set of **X** variables and linear combinations of a *set* of **Y** variables. These linear combinations are called *canonical variables* or *canonical variates*. Either set of variables can be considered explanatory or response variables, since the statistical model is symmetric in the two sets of variables. Simple and multiple correlation are special cases of canonical correlation in which one or both sets contain a single variable.

The CANCORR procedure tests a series of hypotheses that each canonical correlation and all smaller canonical correlations are zero in the population. PROC CANCORR uses an F approximation (Rao 1973; Kshirsagar 1972) that gives better small sample results than the usual χ^2 approximation. At least one of the two sets of variables should have an approximate multivariate normal distribution in order for the probability levels to be valid.

Both standardized and unstandardized canonical coefficients are computed, as well as the four *canonical structure* matrices showing correlations between the two sets of canonical variables and the two sets of original variables. A canonical redundancy analysis (Stewart and Love 1968; Cooley and Lohnes 1971) can also be done. PROC CANCORR provides multiple regression analysis options to aid in interpreting the canonical correlation analysis. You can examine the linear regression of each variable on the opposite set of variables.

PROC CANCORR can produce a data set containing the scores of each observation on each canonical variable, and you can use the PRINT procedure to list these values. A plot of each canonical variable against its counterpart in the other group is often useful, and you can use PROC SGPLOT with the output data set to produce these plots. A second output data set contains the canonical correlations, coefficients, and most other statistics computed by the procedure.

Background

Canonical correlation was developed by Hotelling (1935, 1936).

The application of canonical correlation is discussed by Cooley and Lohnes (1971); Tatsuoka (1971); Mardia, Kent, and Bibby (1979). One of the best theoretical treatments is given by Kshirsagar (1972).

Given a set of p X variables and q Y variables, the CANCORR procedure finds the linear combinations

$$w_1 = a_{11}x_1 + a_{21}x_2 + \dots + a_{p1}x_p$$

$$v_1 = b_{11}y_1 + b_{21}y_2 + \dots + b_{a1}y_a$$

such that the two canonical variables, w_1 and v_1 , have the largest possible correlation. This maximized correlation between the two canonical variables is the first canonical correlation. The coefficients of the linear combinations are canonical coefficients or canonical weights. It is customary to normalize the canonical coefficients so that each canonical variable has a variance of 1.

PROC CANCORR continues by finding a second set of canonical variables, uncorrelated with the first pair, that produces the second-highest correlation coefficient. That is, the second pair of canonical variables is

$$w_2 = a_{12}x_1 + a_{22}x_2 + \dots + a_{p2}x_p$$

$$v_2 = b_{12}y_1 + b_{22}y_2 + \dots + b_{q2}y_q$$

such that w_2 is uncorrelated with w_1 and v_1 , v_2 is uncorrelated with w_1 and v_1 , and w_2 and v_2 have the largest possible correlation subject to these constraints. The process of constructing canonical variables continues until the number of pairs of canonical variables is $\min(p,q)$, the number of variables in the smaller group.

Each canonical variable is uncorrelated with all the other canonical variables of either set except for the one corresponding canonical variable in the opposite set. The canonical coefficients are not generally orthogonal, however, so the canonical variables do not represent jointly perpendicular directions through the space of the original variables.

The first canonical correlation is at least as large as the multiple correlation between any variable and the opposite set of variables. It is possible for the first canonical correlation to be very large while all the multiple correlations for predicting one of the original variables from the opposite set of canonical variables are small. Canonical redundancy analysis (Stewart and Love 1968; Cooley and Lohnes 1971; van den Wollenberg 1977) examines how well the original variables can be predicted from the canonical variables.

PROC CANCORR can also perform partial canonical correlation, which is a multivariate generalization of ordinary partial correlation (Cooley and Lohnes 1971; Timm 1975). Most commonly used parametric statistical methods, ranging from *t* tests to multivariate analysis of covariance, are special cases of partial canonical correlation.

Getting Started: CANCORR Procedure

The following example demonstrates how you can use the CANCORR procedure to calculate and test canonical correlations between two sets of variables.

Suppose you want to determine the degree of correspondence between a set of job characteristics and measures of employee satisfaction. Using a survey instrument for employees, you calculate three measures of job satisfaction. With another instrument designed for supervisors, you calculate the corresponding job characteristics profile.

Your three variables associated with job satisfaction are as follows:

- career track satisfaction: employee satisfaction with career direction and the possibility of future advancement, expressed as a percent
- management and supervisor satisfaction: employee satisfaction with supervisor's communication and management style, expressed as a percent
- financial satisfaction: employee satisfaction with salary and other benefits, using a scale measurement from 1 to 10 (1=unsatisfied, 10=satisfied)

The three variables associated with job characteristics are as follows:

- task variety: degree of variety involved in tasks, expressed as a percent
- feedback: degree of feedback required in job tasks, expressed as a percent
- autonomy: degree of autonomy required in job tasks, expressed as a percent

The following statements create the SAS data set Jobs and request a canonical correlation analysis:

```
data Jobs;
  input Career Supervisor Finance Variety Feedback Autonomy;
  label Career
                 ='Career Satisfaction' Variety ='Task Variety'
        Supervisor='Supervisor Satisfaction' Feedback='Amount of Feedback'
        Finance ='Financial Satisfaction' Autonomy='Degree of Autonomy';
  datalines;
72 26 9
                 10 11
                         70
63 76 7
                 85 22
                         93
96 31 7
                 83 63
                         73
                 82 75
96 98 6
                         97
84 94 6
                 36 77
                         97
66 10 5
                 28 24
                         75
                 64 23
                         75
31 40
       9
45 14
       2
                 19 15
                         50
42 18 6
                         70
                 33 13
79 74 4
                 23 14 90
39 12 2
                 37 13
                         70
54 35 3
                 23 74 53
60 75 5
                 45 58
                         83
63 45 5
                 22 67 53
proc cancorr data=Jobs
            vprefix=Satisfaction wprefix=Characteristics
            vname='Satisfaction Areas' wname='Job Characteristics';
  var Career Supervisor Finance;
  with Variety Feedback Autonomy;
run;
```

The DATA= option in the PROC CANCORR statement specifies Jobs as the SAS data set to be analyzed. The VPREFIX and WPREFIX options specify the prefixes for naming the canonical variables from the VAR statement and the WITH statement, respectively. The VNAME option specifies 'Satisfaction Areas' to refer to the set of variables from the VAR statement. Similarly, the WNAME option specifies 'Job Characteristics' to refer to the set of variables from the WITH statement.

The VAR statement defines the first of the two sets of variables to be analyzed as Career, Supervisor, and Finance. The WITH statement defines the second set of variables to be Variety, Feedback, and Autonomy. The results of this analysis are displayed in Figure 28.1 to Figure 28.4.

Figure 28.1 displays the canonical correlation, adjusted canonical correlation, approximate standard error, and squared canonical correlation for each pair of canonical variables. The first canonical correlation (the correlation between the first pair of canonical variables) is 0.9194. This value represents the highest possible correlation between any linear combination of the job satisfaction variables and any linear combination of the job characteristics variables.

Figure 28.1 also lists the likelihood ratio and associated statistics for testing the hypothesis that the canonical correlations in the current row and all that follow are zero.

Figure 28.1 Canonical Correlations, Eigenvalues, and Likelihood Tests

| | Th | e CANCORR Proce | edure | | |
|---|---------------|-----------------|----------------|-------|-----------|
| | Canoni | cal Correlation | n Analysis | | |
| | | Adjusted | Approximat | e | Squared |
| | Canonical | Canonical | Standar | ď | Canonical |
| | Correlation | Correlation | Erro | r Co | rrelation |
| 1 | 0.919412 | 0.898444 | 0.04290 | 1 | 0.845318 |
| 2 | 0.418649 | 0.276633 | 0.22874 | 0 | 0.175267 |
| 3 | 0.113366 | • | 0.27378 | 6 | 0.012852 |
| | | Eigenvalues | s of Inv(E) *H | I | |
| | | = CanRsq | (1-CanRsq) | | |
| | Eigenvalue | Difference | Proportion | Cur | nulative |
| 1 | 5.4649 | 5.2524 | 0.9604 | | 0.9604 |
| 2 | 0.2125 | 0.1995 | 0.0373 | | 0.9977 |
| 3 | 0.0130 | | 0.0023 | | 1.0000 |
| | Test of H0: T | he canonical co | orrelations i | n the | |
| | current row | and all that i | follow are ze | ro | |
| | Likelihood | Approximate | | | |
| | Ratio | F Value | Num DF D | en DF | Pr > F |
| 1 | 0.12593148 | 2.93 | 9 1 | 9.621 | 0.0223 |
| 2 | 0.81413359 | 0.49 | 4 | 18 | 0.7450 |
| 3 | 0.98714819 | 0.13 | 1 | 10 | 0.7257 |

The first approximate F value of 2.93 corresponds to the test that all three canonical correlations are zero. Since the p-value is small (0.0223), you would reject the null hypothesis at the 0.05 level. The second approximate F value of 0.49 corresponds to the test that both the second and the third canonical correlations are zero. Since the p-value is large (0.7450), you would fail to reject the hypothesis and conclude that only the first canonical correlation is significant.

Figure 28.2 lists several multivariate statistics and tests that use approximations based on the *F* distribution for the null hypothesis that all canonical correlations are zero. Alternatively, you can specify MSTAT=EXACT to compute exact *p*-values for three of the four tests (Wilks' Lambda, the Hotelling-Lawley Trace, and Roy's greatest root) and an improved *F* approximation for the fourth (Pillai's Trace). These statistics are described in the section "Multivariate Tests" on page 92 in Chapter 4, "Introduction to Regression Procedures."

Figure 28.2 Multivariate Statistics and F Approximations

| | S=3 M=-0 | .5 N=3 | | | |
|------------------------|------------|---------|--------|--------|--------|
| Statistic | Value | F Value | Num DF | Den DF | Pr > F |
| Wilks' Lambda | 0.12593148 | 2.93 | 9 | 19.621 | 0.0223 |
| Pillai's Trace | 1.03343732 | 1.75 | 9 | 30 | 0.1204 |
| Hotelling-Lawley Trace | 5.69042615 | 4.76 | 9 | 9.8113 | 0.0119 |
| Roy's Greatest Root | 5.46489324 | 18.22 | 3 | 10 | 0.0002 |

The small p-values for these tests (< 0.05), except for Pillai's trace, suggest rejecting the null hypothesis that all canonical correlations are zero in the population, confirming the results of the preceding likelihood ratio test (Figure 28.1). With only one of the tests resulting in a p-value larger than 0.05, you can assume that the first canonical correlation is significant. The next step is to interpret or identify the two canonical variables corresponding to this significant correlation.

Even though canonical variables are artificial, they can often be "identified" in terms of the original variables. This is done primarily by inspecting the standardized coefficients of the canonical variables and the correlations between the canonical variables and their original variables. Since only the first canonical correlation is significant, only the first pair of canonical variables (Satisfaction1 and Characteristics1) need to be identified.

PROC CANCORR calculates and displays the raw canonical coefficients for the job satisfaction variables and the job characteristic variables. However, since the original variables do not necessarily have equal variance and are not measured in the same units, the raw coefficients must be standardized to allow interpretation. The coefficients are standardized by multiplying the raw coefficients with the standard deviation of the associated variable.

The standardized canonical coefficients in Figure 28.3 show that the first canonical variable for the Satisfaction group is a weighted sum of the variables Supervisor (0.7854) and Career (0.3028), with the emphasis on Supervisor. The coefficient for the variable Finance is near 0. Thus, a person satisfied with his or her supervisor and with a large degree of career satisfaction would score high on the canonical variable Satisfaction1.

Figure 28.3 Standardized Canonical Coefficients from the CANCORR Procedure

| St | andardized Canonical Coef | ficients for th | e Satisfaction | Areas |
|------------|---------------------------|-----------------|----------------|---------------|
| | | Satisfaction1 | Satisfaction2 | Satisfaction3 |
| Career | Career Satisfaction | 0.3028 | -0.5416 | 1.0408 |
| Supervisor | Supervisor Satisfaction | 0.7854 | 0.1305 | -0.9085 |
| Finance | Financial Satisfaction | 0.0538 | 0.9754 | 0.3329 |

Figure 28.3 continued

| Stan | dardized Can | onical Coefficients | for the Job Ci | naracteristics |
|----------|--------------|----------------------|----------------|------------------|
| | | Char | acteristics1 | Characteristics2 |
| Variety | Task Var | riety | -0.1108 | 0.8095 |
| Feedback | Amount o | of Feedback | 0.5520 | -0.7722 |
| Autonomy | Degree o | of Autonomy | 0.8403 | 0.1020 |
| Sta | ndardized Ca | nonical Coefficients | for the Job (| Characteristics |
| | | | Charact | ceristics3 |
| | Variety | Task Variety | | 0.9071 |
| | Feedback | Amount of Feedbac | k | 0.4194 |
| | Autonomy | Degree of Autonom | _ | -0.8297 |

The coefficients for the job characteristics variables show that degree of autonomy (Autonomy) and amount of feedback (Feedback) contribute heavily to the Characteristics1 canonical variable (0.8403 and 0.5520, respectively).

Figure 28.4 shows the table of correlations between the canonical variables and the original variables.

Figure 28.4 Canonical Structure Correlations from the CANCORR Procedure

| | | The CANCOR | RR Procedure | | | |
|---------------------------------|---|---|---|--------------------------------------|--------------------------------|--|
| | | Canonical | l Structure | | | |
| Correlat | tions Between | the Satisfaction | on Areas and | Their | Canonical | Variables |
| | | Sa | atisfaction1 | Satis | faction2 | Satisfaction3 |
| Career | Career Satis | faction | 0.7499 | | -0.2503 | 0.6123 |
| Supervisor | Supervisor S | atisfaction | 0.9644 | | 0.0362 | -0.2618 |
| Finance | Financial Sa | tisfaction | 0.2873 | | 0.8814 | 0.3750 |
| Correlat | tions Between | the Job Charact | ceristics and | d Their | Canonica | l Variables |
| Correlat | tions Between | the Job Charact | | | | l Variables |
| Correlat Variety | | | Characteris | | Chara | |
| | Task Var | | Characteris | stics1 | Char | acteristics2 |
| Variety | Task Var Amount o | iety | Characteris (| stics1 | Char | acteristics2 |
| Variety Feedback Autonomy | Task Var Amount o Degree o | iety f Feedback | Characteris (| stics1 0.4863 0.6216 0.8459 | Char | 0.6592 -0.5452 0.4451 |
| Variety Feedback Autonomy | Task Var Amount o Degree o | iety f Feedback f Autonomy | Characteris (| stics1 0.4863 0.6216 0.8459 | Char | 0.6592 -0.5452 0.4451 |
| Variety Feedback Autonomy | Task Var Amount o Degree o | iety f Feedback f Autonomy the Job Charact | Characteris (((ceristics and | stics1 0.4863 0.6216 0.8459 | Chara | 0.6592 -0.5452 0.4451 1 Variables |
| Variety Feedback Autonomy | Task Var Amount o Degree o Lions Between | iety f Feedback f Autonomy the Job Charact Task Variety | Characteris ((((ceristics and | stics1 0.4863 0.6216 0.8459 | Chara Canonica teristics | 0.6592 -0.5452 0.4451 1 Variables |

Figure 28.4 continued

| orrelations Betwee Canonical Varial | | | he |
|--|---|--|---|
| Canonical Varial | oles of the Joh | | |
| | ores or the bob | Characteristics | |
| | Chara | acteristics1 | Characteristics2 |
| Career Satisfaction | on | 0.6895 | -0.1048 |
| Supervisor Satisfa | action | 0.8867 | 0.0152 |
| inancial Satisfa | ction | 0.2642 | 0.3690 |
| orrelations Betwee | en the Satisfact | ion Areas and t | he |
| Canonical Varial | oles of the Job | Characteristics | |
| | | Characteri | stics3 |
| Career S | Satisfaction | | 0.0694 |
| visor Supervi | sor Satisfaction | n - | 0.0297 |
| ce Financia | al Satisfaction | | 0.0425 |
| Correlations Bots | woon the Job Ch | ragtoristics an | a |
| | | | - |
| | Satisfaction1 | Satisfaction2 | Satisfaction3 |
| : Variety | 0.4471 | 0.2760 | 0.0650 |
| - | 0.5715 | -0.2283 | 0.0638 |
| ee of Autonomy | 0.7777 | 0.1863 | -0.0333 |
| | Supervisor Satisfa Financial Satisfa orrelations Betwee Canonical Varial Career S visor Supervisoe Financia Correlations Between | Canonical Variables of the Job Career Satisfaction Visor Supervisor Satisfaction Correlations Between the Job Charache Canonical Variables of the Satisfaction Satisfaction1 C Variety 0.4471 ant of Feedback 0.5715 | Supervisor Satisfaction 0.8867 Financial Satisfaction 0.2642 Dirrelations Between the Satisfaction Areas and to Canonical Variables of the Job Characteristics Characterian Career Satisfaction Visor Supervisor Satisfaction Correlations Between the Job Characteristics and the Canonical Variables of the Satisfaction Area Satisfaction1 Satisfaction2 Covered Career Satisfaction Satisfaction Area Satisfaction1 Satisfaction2 Covered Canonical Variables of the Satisfaction Area Satisfaction1 Satisfaction2 |

Although these univariate correlations must be interpreted with caution since they do not indicate how the original variables contribute *jointly* to the canonical analysis, they are often useful in the identification of the canonical variables.

Figure 28.4 shows that the supervisor satisfaction variable Supervisor is strongly associated with the Satisfaction1 canonical variable, with a correlation of 0.9644. Slightly less influential is the variable Career, which has a correlation with the canonical variable of 0.7499. Thus, the canonical variable Satisfaction1 seems to represent satisfaction with supervisor and career track.

The correlations for the job characteristics variables show that the canonical variable Characteristics1 seems to represent all three measured variables, with degree of autonomy variable (Autonomy) being the most influential (0.8459).

Hence, you can interpret these results to mean that job characteristics and job satisfaction are related—jobs that possess a high degree of autonomy and level of feedback are associated with workers who are more satisfied with their supervisor and their career. While financial satisfaction is a factor in job satisfaction, it is not as important as the other measured satisfaction-related variables.

Syntax: CANCORR Procedure

The following statements are available in the CANCORR procedure:

```
PROC CANCORR < options > ;
WITH variables;
BY variables;
FREQ variable;
PARTIAL variables;
VAR variables;
WEIGHT variable;
```

The PROC CANCORR statement and the WITH statement are required. The rest of this section provides detailed syntax information for each of the preceding statements, beginning with the PROC CANCORR statement. The remaining statements are covered in alphabetical order.

PROC CANCORR Statement

PROC CANCORR < options > ;

The PROC CANCORR statement invokes the CANCORR procedure. Optionally, it also identifies input and output data sets, specifies the analyses performed, and controls displayed output. Table 28.1 summarizes the options available in the PROC CANCORR statement.

Table 28.1 Summary of PROC CANCORR Statement Options

| | <u> </u> | | | | |
|---------------------|--|--|--|--|--|
| Option | Description | | | | |
| Specify computat | Specify computational details | | | | |
| EDF= | Specifies error degrees of freedom if input observations are regression residuals | | | | |
| MSTAT= | Specifies the method of evaluating the multivariate test statistics | | | | |
| NOINT | Omits intercept from canonical correlation and regression models | | | | |
| RDF= | Specifies regression degrees of freedom if input observations are regression residuals | | | | |
| SINGULAR= | Specifies the singularity criterion | | | | |
| Specify input and | d output data sets | | | | |
| DATA= | Specifies input data set name | | | | |
| OUT= | Specifies output data set name | | | | |
| OUTSTAT= | Specifies output data set name containing various statistics | | | | |
| Specify labeling of | options | | | | |
| PARPREFIX= | Specifies a prefix for naming residual variables | | | | |
| VNAME= | Specifies a name to refer to VAR statement variables | | | | |
| VPREFIX= | Specifies a prefix for naming VAR statement canonical variables | | | | |
| WNAME= | Specifies a name to refer to WITH statement variables | | | | |
| WPREFIX= | Specifies a prefix for naming WITH statement canonical variables | | | | |

Table 28.1 continued

| Option | Description |
|--------------------|--|
| Control amount o | f output |
| ALL | Produces simple statistics, input variable correlations, and canonical re- |
| | dundancy analysis |
| CORR | Produces input variable correlations |
| NCAN= | Specifies number of canonical variables for which full output is desired |
| NOPRINT | Suppresses all displayed output |
| REDUNDANCY | Produces canonical redundancy analysis |
| SHORT | Suppresses default output from canonical analysis |
| SIMPLE | Produces means and standard deviations |
| Request regressio | n analyses |
| VDEP | Requests multiple regression analyses with the VAR variables as depen- |
| | dents and the WITH variables as regressors |
| VREG | Requests multiple regression analyses with the VAR variables as regressors |
| | and the WITH variables as dependents |
| WDEP | Same as VREG |
| WREG | Same as VDEP |
| Specify regression | ı statistics |
| ALL | Produces all regression statistics and includes these statistics in the OUT- |
| | STAT= data set |
| В | Produces raw regression coefficients |
| CLB | Produces 95% confidence interval limits for the regression coefficients |
| CORRB | Produces correlations among regression coefficients |
| INT | Requests statistics for the intercept when you specify the B, CLB, SEB, T, |
| | or PROBT option |
| PCORR | Displays partial correlations between regressors and dependents |
| PROBT | Displays probability levels for <i>t</i> statistics |
| SEB | Displays standard errors of regression coefficients |
| SMC | Displays squared multiple correlations and F tests |
| SPCORR | Displays semipartial correlations between regressors and dependents |
| SQPCORR | Displays squared partial correlations between regressors and dependents |
| SQSPCORR | Displays squared semipartial correlations between regressors and depen- |
| | dents |
| STB | Displays standardized regression coefficients |
| T | Displays t statistics for regression coefficients |

Following are explanations of the options that can be used in the PROC CANCORR statement (in alphabetic order).

ALL

displays simple statistics, correlations among the input variables, the confidence limits for the regression coefficients, and the canonical redundancy analysis. If you specify the VDEP or WDEP option, the ALL option displays all related regression statistics (unless the NOPRINT option is specified) and includes these statistics in the OUTSTAT= data set.

В

produces raw regression coefficients from the regression analyses.

CLB

produces the 95% confidence limits for the regression coefficients from the regression analyses.

CORR

C

produces correlations among the original variables. If you include a PARTIAL statement, the CORR option produces a correlation matrix for all variables in the analysis, the regression statistics (R square, RMSE), the standardized regression coefficients for both the VAR and WITH variables as predicted from the PARTIAL statement variables, and partial correlation matrices.

CORRB

produces correlations among the regression coefficient estimates.

DATA=SAS-data-set

names the SAS data set to be analyzed by PROC CANCORR. It can be an ordinary SAS data set or a TYPE=CORR, COV, FACTOR, SSCP, UCORR, or UCOV data set. By default, the procedure uses the most recently created SAS data set.

EDF=error-df

specifies the error degrees of freedom if the input observations are residuals from a regression analysis. The effective number of observations is the EDF= value plus one. If you have 100 observations, then specifying EDF=99 has the same effect as omitting the EDF= option.

INT

requests that statistics for the intercept be included when B, CLB, SEB, T, or PROBT is specified for the regression analyses.

MSTAT=FAPPROX | EXACT

specifies the method of evaluating the multivariate test statistics. The default is MSTAT=FAPPROX, which specifies that the multivariate tests are evaluated using the usual approximations based on the F distribution, as discussed in the section "Multivariate Tests" on page 92 in Chapter 4, "Introduction to Regression Procedures." Alternatively, you can specify MSTAT=EXACT to compute exact p-values for three of the four tests (Wilks' lambda, the Hotelling-Lawley trace, and Roy's greatest root) and an improved F approximation for the fourth (Pillai's trace). While MSTAT=EXACT provides better control of the significance probability for the tests, especially for Roy's greatest root, computations for the exact p-values can be appreciably more demanding, and are in fact infeasible for large problems (many dependent variables). Thus, although MSTAT=EXACT is more accurate for most data, it is not the default method.

NCAN=number

specifies the number of canonical variables for which full output is desired. The *number* must be less than or equal to the number of canonical variables in the analysis.

The value of the NCAN= option specifies the number of canonical variables for which canonical coefficients and canonical redundancy statistics are displayed, and the number of variables shown in the canonical structure matrices. The NCAN= option does not affect the number of displayed canonical correlations.

If an OUTSTAT= data set is requested, the NCAN= option controls the number of canonical variables for which statistics are output. If an OUT= data set is requested, the NCAN= option controls the number of canonical variables for which scores are output.

NOINT

omits the intercept from the canonical correlation and regression models. Standard deviations, variances, covariances, and correlations are not corrected for the mean. If you use a TYPE=SSCP data set as input to the CANCORR procedure and list the variable Intercept in the VAR or WITH statement, the procedure runs as if you also specified the NOINT option. If you use NOINT and also create an OUTSTAT= data set, the data set is TYPE=UCORR.

NOPRINT

suppresses the display of all output. Note that this option temporarily disables the Output Delivery System (ODS). For more information, see Chapter 20, "Using the Output Delivery System."

OUT=SAS-data-set

creates an output SAS data set to contain all the original data plus scores on the canonical variables. The OUT= option cannot be used when the DATA= data set is TYPE=CORR, COV, FACTOR, SSCP, UCORR, or UCOV. For details about OUT= data sets, see the section "Output Data Sets" on page 1729. If you want to create a SAS data set in a permanent library, you must specify a two-level name. For more information about permanent libraries and SAS data sets, see SAS Language Reference: Concepts.

OUTSTAT=SAS-data-set

creates an output SAS data set containing various statistics, including the canonical correlations and coefficients and the multiple regression statistics you request. For details about OUTSTAT= data sets, see the section "Output Data Sets" on page 1729. If you want to create a SAS data set in a permanent library, you must specify a two-level name. For more information about permanent libraries and SAS data sets, see SAS Language Reference: Concepts.

PCORR

produces partial correlations between regressors and dependent variables, removing from each dependent variable and regressor the effects of all other regressors.

PROBT

produces probability levels for the t statistics in the regression analyses.

RDF=regression-df

specifies the regression degrees of freedom if the input observations are residuals from a regression analysis. The effective number of observations is the actual number minus the RDF= value. The degrees of freedom for the intercept should not be included in the RDF= option.

REDUNDANCY

RED

produces canonical redundancy statistics.

PARPREFIX=name

PPREFIX=name

specifies a prefix for naming the residual variables in the OUT= data set and the OUTSTAT= data set. By default, the prefix is R_. The number of characters in the prefix plus the maximum length of the variable names should not exceed the current name length defined by the VALIDVARNAME= system option.

SEB

produces standard errors of the regression coefficients.

SHORT

suppresses all default output from the canonical analysis except the tables of canonical correlations and multivariate statistics.

SIMPLE

S

produces means and standard deviations.

SINGULAR=p

SING=p

specifies the singularity criterion, where 0 . If a variable in the PARTIAL statement has an R square as large as <math>1 - p (where p is the value of the SINGULAR= option) when predicted from the variables listed before it in the statement, the variable is assigned a standardized regression coefficient of 0, and the SAS log generates a linear dependency warning message. By default, SINGULAR=1E-8.

SMC

produces squared multiple correlations and F tests for the regression analyses.

SPCORR

produces semipartial correlations between regressors and dependent variables, removing from each regressor the effects of all other regressors.

SQPCORR

produces squared partial correlations between regressors and dependent variables, removing from each dependent variable and regressor the effects of all other regressors.

SQSPCORR

produces squared semipartial correlations between regressors and dependent variables, removing from each regressor the effects of all other regressors.

STB

produces standardized regression coefficients.

Т

produces t statistics for the regression coefficients.

VDEP

WREG

requests multiple regression analyses with the VAR variables as dependent variables and the WITH Variables as regressors.

VNAME=label

VN=label

specifies a character constant to refer to variables from the VAR statement in the output. Enclose the constant in single or double quotes. If you omit the VNAME= option, these variables are referred to as the VAR variables. The number of characters in the label should not exceed the label length defined by the VALIDVARNAME= system option. For more information about the VALIDVARNAME= system option, see *SAS System Options: Reference*.

VPREFIX=name

VP=name

specifies a prefix for naming canonical variables from the VAR statement. By default, these canonical variables are given the names V1, V2, and so on. If you specify VPREFIX=ABC, the names are ABC1, ABC2, and so on. The number of characters in the prefix plus the number of digits required to designate the variables should not exceed the name length defined by the VALIDVARNAME= system option. For more information about the VALIDVARNAME= system option, see SAS System Options: Reference.

WDEP

VREG

requests multiple regression analyses with the WITH variables as dependent variables and the VAR variables as regressors.

WNAME=label

WN=label

specifies a character constant to refer to variables in the WITH statement in the output. Enclose the constant in single or double quotes. If you omit the WNAME= option, these variables are referred to as the WITH variables. The number of characters in the label should not exceed the label length defined by the VALIDVARNAME= system option. For more information about the VALIDVARNAME= system option, see *SAS System Options: Reference*.

WPREFIX=name

WP=name

specifies a prefix for naming canonical variables from the WITH statement. By default, these canonical variables are given the names W1, W2, and so on. If you specify WPREFIX=XYZ, the names are XYZ1, XYZ2, and so on. The number of characters in the prefix plus the number of digits required to designate the variables should not exceed the label length defined by the VALIDVARNAME= system option. For more information about the VALIDVARNAME= system option, see SAS System Options: Reference.

BY Statement

BY variables;

You can specify a BY statement with PROC CANCORR to obtain separate analyses of observations in groups that are defined by the BY variables. When a BY statement appears, the procedure expects the input data set to be sorted in order of the BY variables. If you specify more than one BY statement, only the last one specified is used.

If your input data set is not sorted in ascending order, use one of the following alternatives:

- Sort the data by using the SORT procedure with a similar BY statement.
- Specify the NOTSORTED or DESCENDING option in the BY statement for the CANCORR procedure. The NOTSORTED option does not mean that the data are unsorted but rather that the data are arranged in groups (according to values of the BY variables) and that these groups are not necessarily in alphabetical or increasing numeric order.
- Create an index on the BY variables by using the DATASETS procedure (in Base SAS software).

For more information about BY-group processing, see the discussion in SAS Language Reference: Concepts. For more information about the DATASETS procedure, see the discussion in the Base SAS Procedures Guide.

FREQ Statement

FREQ variable;

If one variable in your input data set represents the frequency of occurrence for other values in the observation, specify the variable's name in a FREQ statement. PROC CANCORR then treats the data set as if each observation appeared n times, where n is the value of the FREQ variable for the observation. If the value of the FREQ variable is less than one, the observation is not used in the analysis. Only the integer portion of the value is used. The total number of observations is considered to be equal to the sum of the FREQ variable when PROC CANCORR calculates significance probabilities.

PARTIAL Statement

PARTIAL variables;

You can use the PARTIAL statement to base the canonical analysis on partial correlations. The variables in the PARTIAL statement are partialed out of the VAR and WITH variables. If you request an OUT= or OUTSTAT= data set, the residual variables are named by prefixing the characters R_ by default or the string specified in the RPREFIX= option to the VAR variables.

VAR Statement

VAR variables;

The VAR statement lists the variables in the first of the two sets of variables to be analyzed. The variables must be numeric. If you omit the VAR statement, all numeric variables not mentioned in other statements make up the first set of variables. If, however, the DATA= data set is TYPE=SSCP, the default set of variables used as VAR variables does not include the variable Intercept.

WEIGHT Statement

WEIGHT variable;

If you want to compute weighted product-moment correlation coefficients, specify the name of the weighting variable in a WEIGHT statement. The WEIGHT and FREQ statements have a similar effect, except the WEIGHT statement does not alter the degrees of freedom or number of observations. An observation is used in the analysis only if the WEIGHT variable is greater than zero.

WITH Statement

WITH variables;

The WITH statement lists the variables in the second set of variables to be analyzed. The variables must be numeric. The WITH statement is required.

Details: CANCORR Procedure

Missing Values

If an observation has a missing value for any of the variables in the analysis, that observation is omitted from the analysis.

Formulas

Assume without loss of generality that the two sets of variables, X with p variables and Y with q variables, have means of zero. Let n be the number of observations, and let m be n-1.

Note that the scales of eigenvectors and canonical coefficients are arbitrary. PROC CANCORR follows the usual procedure of rescaling the canonical coefficients so that each canonical variable has a variance of one.

There are several different sets of formulas that can be used to compute the canonical correlations, ρ_i , $i = 1, ..., \min(p, q)$, and unscaled canonical coefficients:

- 1. Let $S_{XX} = X'X/m$ be the covariance matrix of X, $S_{YY} = Y'Y/m$ be the covariance matrix of Y, and $S_{XY} = X'Y/m$ be the covariance matrix between X and Y. Then the eigenvalues of $S_{YY}^{-1}S_{XY}'S_{XX}^{-1}S_{XY}$ are the squared canonical correlations, and the right eigenvectors are raw canonical coefficients for the Y variables. The eigenvalues of $S_{XX}^{-1}S_{XY}S_{YY}^{-1}S_{XY}'$ are the squared canonical correlations, and the right eigenvectors are raw canonical coefficients for the X variables.
- 2. Let T = Y'Y and $H = Y'X(X'X)^{-1}X'Y$. The eigenvalues ξ_i of $T^{-1}H$ are the squared canonical correlations, ρ_i^2 , and the right eigenvectors are raw canonical coefficients for the Y variables. Interchange X and Y in the preceding formulas, and the eigenvalues remain the same, but the right eigenvectors are raw canonical coefficients for the X variables.
- 3. Let $\mathbf{E} = \mathbf{T} \mathbf{H}$. The eigenvalues of $\mathbf{E}^{-1}\mathbf{H}$ are $\lambda_i = \rho_i^2/(1-\rho_i^2)$. The right eigenvectors of $\mathbf{E}^{-1}\mathbf{H}$ are the same as the right eigenvectors of $\mathbf{T}^{-1}\mathbf{H}$.
- 4. Canonical correlation can be viewed as a principal component analysis of the predicted values of one set of variables from a regression on the other set of variables, in the metric of the error covariance matrix. For example, regress the Y variables on the X variables. Call the predicted values $P = X(X'X)^{-1}X'Y$ and the residuals $R = Y P = (I X(X'X)^{-1}X')Y$. The error covariance matrix is R'R/m. Choose a transformation Q that converts the error covariance matrix to an identity—that is, (RQ)'(RQ) = Q'R'RQ = mI. Apply the same transformation to the predicted values to yield, say, Z = PQ. Now do a principal component analysis on the covariance matrix of Z, and you get the eigenvalues of $E^{-1}H$. Repeat with X and Y variables interchanged, and you get the same eigenvalues.

To show this relationship between canonical correlation and principal components, note that P'P = H, R'R = E, and $QQ' = mE^{-1}$. Let the covariance matrix of Z be G. Then G = Z'Z/m = (PQ)'PQ/m = Q'P'PQ/m = Q'HQ/m. Let U be an eigenvector of U and U be the corresponding eigenvalue. Then by definition, $U = \kappa U$; hence U hence U hence U is an eigenvector of U and U is also an eigenvalue of U.

5. If the covariance matrices are replaced by correlation matrices, the preceding formulas yield standardized canonical coefficients instead of raw canonical coefficients.

The formulas for multivariate test statistics are shown in the section "Multivariate Tests" on page 92 in Chapter 4, "Introduction to Regression Procedures." Formulas for linear regression are provided in other sections of that chapter.

Output Data Sets

OUT= Data Set

The OUT= data set contains all the variables in the original data set plus new variables containing the canonical variable scores. The number of new variables is twice that specified by the NCAN= option. The names of the new variables are formed by concatenating the values given by the VPREFIX= and WPREFIX= options (the defaults are V and W) with the numbers 1, 2, 3, and so on. The new variables have mean 0 and variance equal to 1. An OUT= data set cannot be created if the DATA= data set is TYPE=CORR, COV, FACTOR, SSCP, UCORR, or UCOV.

If you use a PARTIAL statement, the OUT= data set also contains the residuals from predicting the VAR variables from the PARTIAL variables. The names of the residual variables are formed by concatenating the values given by the PARPREFIX= option (the default is R_) with the numbers 1, 2, 3, and so on.

OUTSTAT= Data Set

The OUTSTAT= data set is similar to the TYPE=CORR or TYPE=UCORR data set produced by the CORR procedure, but it contains several results in addition to those produced by PROC CORR.

The new data set contains the following variables:

- the BY variables, if any
- two new character variables, _TYPE_ and _NAME_
- Intercept, if the INT option is used
- the variables analyzed (those in the VAR statement and the WITH statement)

Each observation in the new data set contains some type of statistic as indicated by the _TYPE_ variable. The values of the _TYPE_ variable are as follows.

| _TYPE_ | Contents |
|--------|--|
| MEAN | means |
| STD | standard deviations |
| USTD | uncorrected standard deviations. When you specify the NOINT option in the PROC CANCORR statement, the OUTSTAT= data set contains standard deviations not corrected for the mean (_TYPE_='USTD'). |
| N | number of observations on which the analysis is based. This value is the same for each variable. |
| SUMWGT | sum of the weights if a WEIGHT statement is used. This value is the same for each variable. |
| CORR | correlations. The _NAME_ variable contains the name of the variable corresponding to each row of the correlation matrix. |
| UCORR | uncorrected correlation matrix. When you specify the NOINT option in the PROC CANCORR statement, the OUTSTAT= data set contains a matrix of correlations not corrected for the means. |
| CORRB | correlations among the regression coefficient estimates |
| STB | standardized regression coefficients. The _NAME_ variable contains the name of the dependent variable. |

B raw regression coefficients

SEB standard errors of the regression coefficients

LCLB 95% lower confidence limits for the regression coefficients
UCLB 95% upper confidence limits for the regression coefficients

T t statistics for the regression coefficients

PROBT probability levels for the *t* statistics

SPCORR semipartial correlations between regressors and dependent variables

SQSPCORR squared semipartial correlations between regressors and dependent variables

PCORR partial correlations between regressors and dependent variables

SQPCORR squared partial correlations between regressors and dependent variables

RSQUARED R squares for the multiple regression analyses

ADJRSQ adjusted R squares

LCLRSQ approximate 95% lower confidence limits for the R squares UCLRSQ approximate 95% upper confidence limits for the R squares

F statistics for the multiple regression analyses

PROBF probability levels for the *F* statistics

CANCORR canonical correlations

SCORE standardized canonical coefficients. The NAME variable contains the name of the

canonical variable.

To obtain the canonical variable scores, these coefficients should be multiplied by the standardized data, using means obtained from the observation with _TYPE_='MEAN'

and standard deviations obtained from the observation with TYPE ='STD'.

RAWSCORE raw canonical coefficients.

To obtain the canonical variable scores, these coefficients should be multiplied by the raw data centered by means obtained from the observation with _TYPE_='MEAN'.

USCORE scoring coefficients to be applied without subtracting the mean from the raw variables.

These are standardized canonical coefficients computed under a NOINT model.

To obtain the canonical variable scores, these coefficients should be multiplied by the data that are standardized by the uncorrected standard deviations obtained from the ob-

servation with _TYPE_='USTD'.

STRUCTUR canonical structure.

Computational Resources

Notation

Let

n = number of observations

v = number of variables

w = number of WITH variables

 $p = \max(v, w)$

 $q = \min(v, w)$

b = v + w

t = total number of variables (VAR, WITH, and PARTIAL)

Time Requirements

The time required to compute the correlation matrix is roughly proportional to

$$n(p+q)^2$$

The time required for the canonical analysis is roughly proportional to

$$\frac{1}{6}p^3 + p^2q + \frac{3}{2}pq^2 + 5q^3$$

but the coefficient for q^3 varies depending on the number of QR iterations in the singular value decomposition.

Memory Requirements

The minimum memory required is approximately

$$4(v^2 + w^2 + t^2)$$

bytes. Additional memory is required if you request the VDEP or WDEP option.

Displayed Output

If the SIMPLE option is specified, PROC CANCORR produces means and standard deviations for each input variable. If the CORR option is specified, PROC CANCORR produces correlations among the input variables. Unless the NOPRINT option is specified, PROC CANCORR displays a table of canonical correlations containing the following:

- Canonical Correlations. These are always nonnegative.
- Adjusted Canonical Correlations (Lawley 1959), which are asymptotically less biased than the raw
 correlations and can be negative. The adjusted canonical correlations might not be computable, and
 they are displayed as missing values if two canonical correlations are nearly equal or if some are close
 to zero. A missing value is also displayed if an adjusted canonical correlation is larger than a previous
 adjusted canonical correlation.
- Approx Standard Errors, which are the approximate standard errors of the canonical correlations
- Squared Canonical Correlations
- Eigenvalues of INV(E)*H, which are equal to CanRsq/(1–CanRsq), where CanRsq is the corresponding squared canonical correlation. Also displayed for each eigenvalue is the Difference from the next eigenvalue, the Proportion of the sum of the eigenvalues, and the Cumulative proportion.
- Likelihood Ratio for the hypothesis that the current canonical correlation and all smaller ones are zero in the population. The likelihood ratio for all canonical correlations equals Wilks' lambda.
- Approx F statistic based on Rao's approximation to the distribution of the likelihood ratio (Rao 1973, p. 556; Kshirsagar 1972, p. 326)
- Num DF and Den DF (numerator and denominator degrees of freedom) and Pr > F (probability level) associated with the F statistic

Unless you specify the NOPRINT option, PROC CANCORR produces a table of multivariate statistics for the null hypothesis that all canonical correlations are zero in the population. These statistics, as described in the section "Multivariate Tests" on page 92 in Chapter 4, "Introduction to Regression Procedures," are as follows:

- Wilks' lambda
- Pillai's trace
- Hotelling-Lawley trace
- Roy's greatest root

For each of the preceding statistics, PROC CANCORR displays the following, depending on the specification of the MSTAT= option.

If you specify MSTAT=FAPPROX (also the default value), the following statistics are displayed:

- an F approximation or upper bound
- Num DF, the numerator degrees of freedom

- Den DF, the denominator degrees of freedom
- Pr > F, the probability level

If you specify MSTAT=EXACT, the following statistic is displayed:

• a t value

Unless you specify the SHORT or NOPRINT option, PROC CANCORR displays the following:

- both Raw (unstandardized) and Standardized Canonical Coefficients normalized to give canonical variables with unit variance. Standardized coefficients can be used to compute canonical variable scores from the standardized (zero mean and unit variance) input variables. Raw coefficients can be used to compute canonical variable scores from the input variables without standardizing them.
- all four Canonical Structure matrices, giving Correlations Between the canonical variables and the original variables

If you specify the REDUNDANCY option, PROC CANCORR displays the following:

- the Canonical Redundancy Analysis (Stewart and Love 1968; Cooley and Lohnes 1971), including Raw (unstandardized) and Standardized Variance and Cumulative Proportion of the Variance of each set of variables Explained by Their Own Canonical Variables and Explained by The Opposite Canonical Variables
- the Squared Multiple Correlations of each variable with the first *m* canonical variables of the opposite set, where *m* varies from 1 to the number of canonical correlations

If you specify the VDEP option, PROC CANCORR performs multiple regression analyses with the VAR variables as dependent variables and the WITH variables as regressors. If you specify the WDEP option, PROC CANCORR performs multiple regression analyses with the WITH variables as dependent variables and the VAR variables as regressors. If you specify the VDEP or WDEP option and also specify the ALL option, PROC CANCORR displays the following items. You can also specify individual options to request a subset of the output generated by the ALL option; or you can suppress the output by specifying the NOPRINT option.

SMC

Squared Multiple Correlations and F Tests. For each regression model, identified by its dependent variable name, PROC CANCORR displays the R square, Adjusted R square (Wherry 1931), F Statistic, and $\Pr > F$. Also for each regression model, PROC CANCORR displays an Approximate 95% Confidence Interval for the population R square Helland (1987). These confidence limits are valid only when the regressors are random and when the regressors and dependent variables are approximately distributed according to a multivariate normal distribution. The average R squares for the models considered, unweighted and weighted by variance, are also given.

CORRB Correlations Among the Regression Coefficient Estimates

STB Standardized Regression Coefficients

B Raw Regression Coefficients

| SEB | Standard Errors of the Regression Coefficients |
|----------|---|
| CLB | 95% confidence limits for the regression coefficients |
| T | T Statistics for the Regression Coefficients |
| PROBT | Probability > T for the Regression Coefficients |
| SPCORR | Semipartial Correlations between regressors and dependent variables, Removing from Each Regressor the Effects of All Other Regressors |
| SQSPCORR | Squared Semipartial Correlations between regressors and dependent variables, Removing from Each Regressor the Effects of All Other Regressors |
| PCORR | Partial Correlations between regressors and dependent variables, Removing the Effects of All Other Regressors from Both Regressor and Criterion |
| SQPCORR | Squared Partial Correlations between regressors and dependent variables, Removing the Effects of All Other Regressors from Both Regressor and Criterion |

ODS Table Names

PROC CANCORR assigns a name to each table it creates. You can use these names to reference the table when using the Output Delivery System (ODS) to select tables and create output data sets. These names are listed in Table 28.2.

For more information about ODS, see Chapter 20, "Using the Output Delivery System."

All of the tables in Table 28.2 are created with the specification of the PROC CANCORR statement; a few tables need an additional PARTIAL statement.

Table 28.2 ODS Tables Produced by PROC CANCORR

| ODS Table Name | Description | Statement and Option |
|------------------|--------------------------------------|--------------------------|
| AvgRSquare | Average R squares (weighted and | VDEP, WDEP, SMC, or |
| | unweighted) | ALL |
| CanCorr | Canonical correlations | default |
| CanStructureVCan | Correlations between the VAR | default (if SHORT is not |
| | canonical variables and the VAR and | specified) |
| | WITH variables | _ |
| CanStructureWCan | Correlations between the WITH | default (if SHORT is not |
| | canonical variables and the WITH and | specified) |
| | VAR variables | |
| ConfidenceLimits | 95% confidence limits for the | VDEP, WDEP, CLB, or |
| | regression coefficients | ALL |
| Corr | Correlations among the original | CORR or ALL |
| | variables | |
| CorrOnPartial | Partial correlations | PARTIAL statement with |
| | | CORR or ALL |
| CorrRegCoefEst | Correlations among the regression | VDEP, WDEP, CORRB, or |
| | coefficient estimates | ALL |
| MultStat | Multivariate statistics | default |

Table 28.2 continued

| ODS Table Name | Description | Statement and Option |
|----------------------|--|-------------------------------------|
| NObsNVar | Number of observations and variables | SIMPLE or ALL |
| ParCorr | Partial correlations | VDEP, WDEP, PCORR, or ALL |
| ProbtRegCoef | Prob > t for the regression coefficients | VDEP, WDEP, PROBT, or ALL |
| RawCanCoefV | Raw canonical coefficients for the VAR variables | default (if SHORT is not specified) |
| RawCanCoefW | Raw canonical coefficients for the WITH variables | default (if SHORT is not specified) |
| RawRegCoef | Raw regression coefficients | VDEP, WDEP, B, or ALL |
| Redundancy | Canonical redundancy analysis | REDUNDANCY or ALL |
| Regression | Squared multiple correlations and <i>F</i> tests | VDEP, WDEP, SMC, or ALL |
| RSquareRMSEOnPartial | R squares and RMSEs on PARTIAL variables | PARTIAL statement with CORR or ALL |
| SemiParCorr | Semipartial correlations | VDEP, WDEP, SPCORR, or ALL |
| SimpleStatistics | Simple statistics | SIMPLE or ALL |
| SqMultCorr | Canonical redundancy analysis: squared multiple correlations | REDUNDANCY or ALL |
| SqParCorr | Squared partial correlations | VDEP, WDEP, SQPCORR, or ALL |
| SqSemiParCorr | Squared semipartial correlations | VDEP, WDEP, SQSPCORR, or ALL |
| StdCanCoefV | Standardized canonical coefficients for the VAR variables | default (if SHORT is not specified) |
| StdCanCoefW | Standardized canonical coefficients for the WITH variables | default (if SHORT is not specified) |
| StdErrRawRegCoef | Standard errors of the raw regression coefficients | VDEP, WDEP, SEB, or ALL |
| StdRegCoef | Standardized regression coefficients | VDEP, WDEP, STB, or ALL |
| StdRegCoefOnPartial | Standardized regression coefficients on PARTIAL variables | PARTIAL statement with CORR or ALL |
| tValueRegCoef | t values for the regression coefficients | VDEP, WDEP, T, or ALL |

Example: CANCORR Procedure

Example 28.1: Canonical Correlation Analysis of Fitness Club Data

Three physiological and three exercise variables are measured on 20 middle-aged men in a fitness club. You can use the CANCORR procedure to determine whether the physiological variables are related in any way to the exercise variables. The following statements create the SAS data set Fit and produce Output 28.1.1 through Output 28.1.5:

```
data Fit;
  input Weight Waist Pulse Chins Situps Jumps;
  datalines;
191 36 50
            5 162
                     60
189 37 52
           2 110
                     60
193 38 58 12 101 101
162 35 62 12 105
                    37
189 35 46 13 155
                    58
182 36 56 4 101
                    42
211 38 56 8 101
                    38
    34 60 6 125
167
                    40
176 31 74 15 200
                    40
154 33 56 17 251
                   250
169 34 50 17 120
                    38
166 33 52 13 210
                   115
154 34 64 14 215 105
247 46 50 1 50
                   50
193 36 46 6 70
                    31
202
    37 62 12 210
                   120
176 37 54 4 60
                   25
157 32 52 11 230
                    80
156 33 54 15 225
                    73
138
    33 68 2 110
                    43
proc cancorr data=Fit all
    vprefix=Physiological vname='Physiological Measurements'
    wprefix=Exercises wname='Exercises';
  var Weight Waist Pulse;
  with Chins Situps Jumps;
  title 'Middle-Aged Men in a Health Fitness Club';
  title2 'Data Courtesy of Dr. A. C. Linnerud, NC State Univ';
run;
```

Output 28.1.1 Correlations among the Original Variables

| | - | a Health Fitness Cl C. Linnerud, NC Sta | |
|-------------------|--------------------|--|--------------------|
| Data Co | dicesy of Di. A. (| S. Himeraa, NC Sca | ice oniv |
| | The CANCOR | R Procedure | |
| | 1110 0111100111 | . 110000010 | |
| Cor | relations Among th | ne Original Variabl | les |
| | • | • | |
| Correla | tions Among the Ph | nysiological Measur | rements |
| | | | |
| | Weight | Waist | Pulse |
| **. * . 1. 1 | 1 0000 | 0.0700 | 0.2650 |
| Weight Waist | 0.8702 | 0.8702 1.0000 | -0.3658 -0.3529 |
| | -0.3658 | | 1.0000 |
| Pulse | -0.3656 | -0.3529 | 1.0000 |
| | | | |
| | Correlations Amo | ong the Exercises | |
| | | | |
| | Chins | Situps | Jumps |
| | | | |
| Chins | | 0.6957 | 0.4958 |
| Situps | 0.6957 | | 0.6692 |
| Jumps | 0.4958 | 0.6692 | 1.0000 |
| | | | |
| Correlations Bet | ween the Physiolog | gical Measurements | and the Exercises |
| 33113113113113113 | | , | <u></u> |
| | Chins | Situps | Jumps |
| | | • | - |
| Weight | -0.3897 | -0.4931 | -0.2263 |
| Waist | -0.5522 | -0.6456 | -0.1915 |
| Pulse | 0.1506 | 0.2250 | 0.0349 |
| | | | |

Output 28.1.1 displays the correlations among the original variables. The correlations between the physiological and exercise variables are moderate, the largest being -0.6456 between Waist and Situps. There are larger within-set correlations: 0.8702 between Weight and Waist, 0.6957 between Chins and Situps, and 0.6692 between Situps and Jumps.

Output 28.1.2 Canonical Correlations and Multivariate Statistics

| Data Cour | cesy of i | Dr. A. C | . Linner | rud, NC S | tate | Univ | |
|-----------------------|-----------|--------------|---------------|-----------------------|-------|-----------|-------|
| | The | CANCORR | Procedu | ıre | | | |
| | Canonica | al Corre | lation A | nalysis | | | |
| | | Adju | sted | | | Squa | |
| | nical | | ical | Stand | ard | Canoni | cal |
| Correl | ation | Correla | tion | Er | ror | Correlat | ion |
| 1 0.7 | 95608 | 0.75 | 4056 | 0.084 | 197 | 0.632 | 992 |
| 2 0.2 | 00556 | 07 | 6399 | 0.220 | 188 | 0.040 | 223 |
| 3 0.0 | 72570 | | | 0.228 | 208 | 0.005 | 266 |
| | | | | of Inv(E) -CanRsq) | *H | | |
| Eige | nvalue | Differ | ence | Proporti | on | Cumulativ | re |
| 1 | 1.7247 | 1. | 6828 | 0.97 | 34 | 0.973 | 4 |
| 2 | 0.0419 | 0. | 0366 | 0.02 | 37 | 0.997 | 0 |
| 3 | 0.0053 | | | 0.00 | 30 | 1.000 | 0 |
| curr | | and all | that fol | elations low are | | he | |
| | atio | | | lum DF | Den | DF Pr > | F |
| 1 0.3503 | 9053 | 2 | . 05 | 9 | 34.2 | 23 0.06 | 35 |
| 2 0.9547 | 2266 | | | 4 | | 30 0.94 | 91 |
| 3 0.9947 | 3355 | 0 | .08 | 1 | | 16 0.77 | 48 |
| Multiva | riate Sta | atistics | and F A | pproxima | tions | | |
| | S=3 | M =-0 | .5 N = | :6 | | | |
| tatistic | | Value | F Valu | ie Num | DF | Den DF | Pr > |
| ilks' Lambda | 0.35 | 039053 | 2.0 | 15 | 9 | 34.223 | 0.063 |
| illai's Trace | | 848151 | 1.5 | 6 | 9 | 48 | 0.155 |
| otelling-Lawley Trace | | 194146 | 2.6 | | 9 | 19.053 | 0.035 |
| oy's Greatest Root | 1.72 | 473874 | 9.2 | 10 | 3 | 16 | 0.000 |

As Output 28.1.2 shows, the first canonical correlation is 0.7956, which would appear to be substantially larger than any of the between-set correlations. The probability level for the null hypothesis that all the canonical correlations are zero in the population is only 0.0635, so no firm conclusions can be drawn. The remaining canonical correlations are not worthy of consideration, as can be seen from the probability levels and especially from the negative adjusted canonical correlations.

Because the variables are not measured in the same units, the standardized coefficients rather than the raw coefficients should be interpreted. The correlations given in the canonical structure matrices should also be examined.

Output 28.1.3 Raw and Standardized Canonical Coefficients

| Weight Waist Pulse | Physiological1 -0.031404688 0.4932416756 | Physiological2 -0.076319506 | Physiological3 |
|--------------------------|--|--------------------------------|---------------------|
| Waist | | -0 076319506 | |
| | 0.4932416756 | -0.076319306 | -0.007735047 |
| Pulse | | 0.3687229894 | 0.1580336471 |
| | -0.008199315 | -0.032051994 | 0.1457322421 |
| 1 | Raw Canonical Coef | ficients for the Ex | ercises |
| | Exercises1 | Exercises2 | Exercises3 |
| Chins | -0.066113986 | -0.071041211 | -0.245275347 |
| Situps | -0.016846231 | 0.0019737454 | 0.0197676373 |
| Jumps | 0.0139715689 | 0.0207141063 | -0.008167472 |
| Standardized (| Canonical Coefficie | ents for the Physic | logical Measurement |
| | Physiological1 | Physiological2 | Physiological3 |
| Weight | -0.7754 | -1.8844 | -0.1910 |
| Waist | 1.5793 | 1.1806 | 0.5060 |
| Pulse | -0.0591 | -0.2311 | 1.0508 |
| Stand | ardized Canonical (| Coefficients for th | e Exercises |
| | Exercises1 | Exercises2 | Exercises3 |
| Chins | -0.3495 | -0.3755 | -1.2966 |
| Situp | s -1.0540 | 0.1235 | 1.2368 |

The first canonical variable for the physiological variables, displayed in Output 28.1.3, is a weighted difference of Waist (1.5793) and Weight (-0.7754), with more emphasis on Waist. The coefficient for Pulse is near 0. The correlations between Waist and Weight and the first canonical variable are both positive, 0.9254 for Waist and 0.6206 for Weight. Weight is therefore a suppressor variable, meaning that its coefficient and its correlation have opposite signs.

The first canonical variable for the exercise variables also shows a mixture of signs, subtracting Situps (–1.0540) and Chins (–0.3495) from Jumps (0.7164), with the most weight on Situps. All the correlations are negative, indicating that Jumps is also a suppressor variable.

It might seem contradictory that a variable should have a coefficient of opposite sign from that of its correlation with the canonical variable. In order to understand how this can happen, consider a simplified situation: predicting Situps from Waist and Weight by multiple regression. In informal terms, it seems plausible that obese people should do fewer sit-ups than skinny people. Assume that the men in the sample do

not vary much in height, so there is a strong correlation between Waist and Weight (0.8702). Examine the relationships between obesity and the independent variables:

- People with large waists tend to be more obese than people with small waists. Hence, the correlation between Waist and Situps should be negative.
- People with high weights tend to be more obese than people with low weights. Therefore, Weight should correlate negatively with Situps.
- For a fixed value of Weight, people with large waists tend to be shorter and more obese. Thus, the multiple regression coefficient for Waist should be negative.
- For a fixed value of Waist, people with higher weights tend to be taller and skinnier. The multiple regression coefficient for Weight should therefore be positive, of opposite sign from the correlation between Weight and Situps.

Therefore, the general interpretation of the first canonical correlation is that Weight and Jumps act as suppressor variables to enhance the correlation between Waist and Situps. This canonical correlation might be strong enough to be of practical interest, but the sample size is not large enough to draw definite conclusions.

The canonical redundancy analysis (Output 28.1.4) shows that neither of the first pair of canonical variables is a good overall predictor of the opposite set of variables, the proportions of variance explained being 0.2854 and 0.2584. The second and third canonical variables add virtually nothing, with cumulative proportions for all three canonical variables being 0.2969 and 0.2767.

Output 28.1.4 Canonical Redundancy Analysis

| | | t 20:1:4 Garionic | odi ricadiladilay | 7 triary 515 | |
|-----------|-----------------|-------------------|-------------------|----------------|------------|
| | Middl | .e-Aged Men in a | a Health Fitne | ss Club | |
| | Data Court | esy of Dr. A. | C. Linnerud, N | C State Univ | |
| | | The CANCOR | R Procedure | | |
| | | Canonical Redu | ndancy Analysi | s | |
| Stand | lardized Varian | ce of the Phys: | iological Meas | urements Expla | ined by |
| | Thei | r Own | | The Op | posite |
| | Canonical | Variables | | Canonical | Variables |
| Canonical | | | | | |
| Variable | | Cumulative | Canonical | | Cumulative |
| Number | Proportion | Proportion | R-Square | Proportion | Proportion |
| 1 | 0.4508 | 0.4508 | 0.6330 | 0.2854 | 0.2854 |
| 2 | 0.2470 | 0.6978 | 0.0402 | 0.0099 | 0.2953 |
| 3 | 0.3022 | 1.0000 | 0.0053 | 0.0016 | 0.2969 |
| | | | | | |

Output 28.1.4 continued

| | Thei | <pre>d Variance of t r Own Variables</pre> | cne Exercises | The Op | posite Variables |
|---------------------------------|------------------|--|-----------------------|------------------|--------------------------|
| Canonical Variable Number | Proportion | Cumulative Proportion | Canonical R-Square | Proportion | Cumulative Proportion |
| 1 | 0.4081 | 0.4081 | 0.6330 | 0.2584 | 0.2584 |
| 2 | 0.4345 0.1574 | 0.8426 1.0000 | 0.0402 0.0053 | 0.0175 0.0008 | 0.2758 0.2767 |

The squared multiple correlations (Output 28.1.5) indicate that the first canonical variable of the physiological measurements has some predictive power for Chins (0.3351) and Situps (0.4233) but almost none for Jumps (0.0167). The first canonical variable of the exercises is a fairly good predictor of Waist (0.5421), a poorer predictor of Weight (0.2438), and nearly useless for predicting Pulse (0.0701).

Output 28.1.5 Canonical Redundancy Analysis

| Squared Multiple Cor | relations Bet | ween the Physio | logical Measurement |
|----------------------|----------------|-----------------|---------------------|
| and the Firs | t M Canonical | Variables of t | he Exercises |
| М | 1 | 2 | 3 |
| Weight | 0.2438 | 0.2678 | 0.2679 |
| Waist | 0.5421 | 0.5478 | 0.5478 |
| Pulse | 0.0701 | 0.0702 | 0.0749 |
| Squared Multiple Co | rrelations Bet | ween the Exerc | ises and the First |
| M Canonical Va | riables of the | Physiological | Measurements |
| М | 1 | 2 | 3 |
| Chins | 0.3351 | 0.3374 | 0.3396 |
| Situps | 0.4233 | 0.4365 | 0.4365 |
| | | | 0.0539 |

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