

SAS/STAT® 9.2 User's Guide The REG Procedure (Book Excerpt)



This document is an individual chapter from SAS/STAT® 9.2 User's Guide.

The correct bibliographic citation for the complete manual is as follows: SAS Institute Inc. 2008. SAS/STAT® 9.2 User's Guide. Cary, NC: SAS Institute Inc.

Copyright © 2008, SAS Institute Inc., Cary, NC, USA

All rights reserved. Produced in the United States of America.

For a Web download or e-book: Your use of this publication shall be governed by the terms established by the vendor at the time you acquire this publication.

U.S. Government Restricted Rights Notice: Use, duplication, or disclosure of this software and related documentation by the U.S. government is subject to the Agreement with SAS Institute and the restrictions set forth in FAR 52.227-19, Commercial Computer Software-Restricted Rights (June 1987).

SAS Institute Inc., SAS Campus Drive, Cary, North Carolina 27513.

1st electronic book, March 2008 2nd electronic book, February 2009

SAS[®] Publishing provides a complete selection of books and electronic products to help customers use SAS software to its fullest potential. For more information about our e-books, e-learning products, CDs, and hard-copy books, visit the SAS Publishing Web site at **support.sas.com/publishing** or call 1-800-727-3228.

 $SAS^{\textcircled{@}}$ and all other SAS Institute Inc. product or service names are registered trademarks or trademarks of SAS Institute Inc. in the USA and other countries. @ indicates USA registration.

Other brand and product names are registered trademarks or trademarks of their respective companies.

Chapter 73

The REG Procedure

Overview: REG	Procedure	542
Getting Started:	REG Procedure	54 3
Simple Li	inear Regression	543
Polynomi	al Regression	543
Using PR	OC REG Interactively	544
Syntax: REG Pr	rocedure	544
PROC RI	EG Statement	544
ADD Stat	tement	546
BY States	ment	540
DELETE	Statement	54
FREQ Sta	atement	54
ID Staten	nent	54
MODEL	Statement	54
MTEST S	Statement	54
OUTPUT	Statement	54
PAINT St	tatement	54
PLOT Sta	ntement	54
PRINT S	tatement	54
REFIT St	atement	54
RESTRIC	CT Statement	54
REWEIG	HT Statement	54
TEST Sta	itement	55
VAR Stat	ement	55
WEIGHT	Statement	55
Details: REG P	rocedure	55
Missing V	Values	55
Input Dat	a Sets	55
Output D	ata Sets	55
Interactiv	e Analysis	55
Model-Se	election Methods	55
Criteria U	Used in Model-Selection Methods	55
Limitatio	ns in Model-Selection Methods	55
Parameter	r Estimates and Associated Statistics	55

	Line Printer Scatter Plot Features	5528
	Traditional Graphics	5541
	Models of Less Than Full Rank	5547
	Collinearity Diagnostics	5549
	Model Fit and Diagnostic Statistics	5551
	Influence Statistics	5553
	Reweighting Observations in an Analysis	5563
	Testing for Heteroscedasticity	5569
	Testing for Lack of Fit	5570
	Multivariate Tests	5571
	Autocorrelation in Time Series Data	5575
	Computations for Ridge Regression and IPC Analysis	5577
	Construction of Q-Q and P-P Plots	5577
	Computational Methods	5578
	Computer Resources in Regression Analysis	5578
	Displayed Output	5578
	ODS Table Names	5581
	ODS Graphics	5583
Exam	pples: REG Procedure	5586
	Example 73.1: Modeling Salaries of Major League Baseball Players	5586
	Example 73.2: Aerobic Fitness Prediction	5602
	Example 73.3: Predicting Weight by Height and Age	5621
	Example 73.4: Regression with Quantitative and Qualitative Variables	5627
	Example 73.5: Ridge Regression for Acetylene Data	5632
	Example 73.6: Chemical Reaction Response	5636
Refer	rences	5638

Overview: REG Procedure

The REG procedure is one of many regression procedures in the SAS System. It is a general-purpose procedure for regression, while other SAS regression procedures provide more specialized applications.

Other SAS/STAT procedures that perform at least one type of regression analysis are the CATMOD, GENMOD, GLM, LOGISTIC, MIXED, NLIN, ORTHOREG, PROBIT, RSREG, and TRANSREG procedures. SAS/ETS procedures are specialized for applications in time series or simultaneous systems. These other SAS/STAT regression procedures are summarized in Chapter 4, "Introduction to Regression Procedures," which also contains an overview of regression techniques and defines many of the statistics computed by PROC REG and other regression procedures.

PROC REG provides the following capabilities:

- multiple MODEL statements
- nine model-selection methods
- interactive changes both in the model and the data used to fit the model
- linear equality restrictions on parameters
- tests of linear hypotheses and multivariate hypotheses
- collinearity diagnostics

....

- predicted values, residuals, studentized residuals, confidence limits, and influence statistics
- correlation or crossproduct input
- requested statistics available for output through output data sets
- ODS Graphics is now available. For more information, see the section "ODS Graphics" on page 5583. These plots are available in addition to the line printer and the traditional graphics currently available in PROC REG.

Nine model-selection methods are available in PROC REG. In the simplest method, PROC REG fits the complete model that you specify. The other eight methods involve various ways of including or excluding variables from the model. You specify these methods with the SELECTION= option in the MODEL statement.

The methods are identified in the following list and are explained in detail in the section "Model-Selection Methods" on page 5517.

NONE	no model selection. This is the default. The complete model specified in the
	MODEL statement is fit to the data.
EODIMADD	

FORWARD forward selection. This method starts with no variables in the model and adds variables.

BACKWARD backward elimination. This method starts with all variables in the model and deletes variables.

defetes variables.

STEPWISE stepwise regression. This is similar to the FORWARD method except that vari-

ables already in the model do not necessarily stay there.

MAXR forward selection to fit the best one-variable model, the best two-variable model,

and so on. Variables are switched so that R^2 is maximized.

MINR similar to the MAXR method, except that variables are switched so that the in-

crease in R^2 from adding a variable to the model is minimized.

RSQUARE finds a specified number of models with the highest R^2 in a range of model sizes. ADJRSQ finds a specified number of models with the highest adjusted R^2 in a range of

model sizes.

CP finds a specified number of models with the lowest C_p in a range of model sizes.

Getting Started: REG Procedure

Simple Linear Regression

Suppose that a response variable Y can be predicted by a linear function of a regressor variable X. You can estimate β_0 , the intercept, and β_1 , the slope, in

$$Y_i = \beta_0 + \beta_1 X_i + \epsilon_i$$

for the observations i = 1, 2, ..., n. Fitting this model with the REG procedure requires only the following MODEL statement, where y is the outcome variable and x is the regressor variable.

```
proc reg;
  model y=x;
run;
```

For example, you might use regression analysis to find out how well you can predict a child's weight if you know that child's height. The following data are from a study of nineteen children. Height and weight are measured for each child.

```
title 'Simple Linear Regression';
data Class;
   input Name $ Height Weight Age @@;
   datalines;

Alfred 69.0 112.5 14 Alice 56.5 84.0 13 Barbara 65.3 98.0 13
Carol 62.8 102.5 14 Henry 63.5 102.5 14 James 57.3 83.0 12
Jane 59.8 84.5 12 Janet 62.5 112.5 15 Jeffrey 62.5 84.0 13
John 59.0 99.5 12 Joyce 51.3 50.5 11 Judy 64.3 90.0 14
Louise 56.3 77.0 12 Mary 66.5 112.0 15 Philip 72.0 150.0 16
Robert 64.8 128.0 12 Ronald 67.0 133.0 15 Thomas 57.5 85.0 11
William 66.5 112.0 15
```

The equation of interest is

```
Weight = \beta_0 + \beta_1 Height + \epsilon
```

The variable Weight is the response or dependent variable in this equation, and β_0 and β_1 are the unknown parameters to be estimated. The variable Height is the regressor or independent variable, and ϵ is the unknown error. The following commands invoke the REG procedure and fit this model to the data.

```
ods graphics on;
proc reg;
  model Weight = Height;
run;
ods graphics off;
```

Figure 73.1 includes some information concerning model fit.

The F statistic for the overall model is highly significant (F=57.076, p<0.0001), indicating that the model explains a significant portion of the variation in the data.

The degrees of freedom can be used in checking accuracy of the data and model. The model degrees of freedom are one less than the number of parameters to be estimated. This model estimates two parameters, β_0 and β_1 ; thus, the degrees of freedom should be 2-1=1. The corrected total degrees of freedom are always one less than the total number of observations in the data set, in this case 19-1=18.

Several simple statistics follow the ANOVA table. The Root MSE is an estimate of the standard deviation of the error term. The coefficient of variation, or Coeff Var, is a unitless expression of the variation in the data. The R-square and Adj R-square are two statistics used in assessing the fit of the model; values close to 1 indicate a better fit. The R-square of 0.77 indicates that Height accounts for 77% of the variation in Weight.

Figure 73.1 ANOVA Table

	Siı	mple Linear Reg	ression		
		The REG Proced	lure		
		Model: MODEI	.1		
	Depe	ndent Variable:	Weight		
	i	Analysis of Var	riance		
		Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > F
Model	1	7193.24912	7193.24912	57.08	<.0001
Error	17	2142.48772	126.02869		
Corrected Total	18	9335.73684			
Root MS	SE	11.22625	R-Square	0.7705	
Depende	ent Mean	100.02632	Adj R-Sq		
Coeff V		11.22330			

The "Parameter Estimates" table in Figure 73.2 contains the estimates of β_0 and β_1 . The table also contains the t statistics and the corresponding p-values for testing whether each parameter is significantly different from zero. The p-values (t = -4.43, p = 0.0004 and t = 7.55, p < 0.0001) indicate that the intercept and Height parameter estimates, respectively, are highly significant.

From the parameter estimates, the fitted model is

Weight =
$$-143.0 + 3.9 \times \text{Height}$$

Figure 73.2 Parameter Estimates

		Parameter	Estimates		
		Parameter	Standard		
Variable	DF	Estimate	Error	t Value	Pr > t
Intercept	1	-143.02692	32.27459	-4.43	0.0004
Height	1	3.89903	0.51609	7.55	<.0001

If you enable ODS Graphics with an ODS GRAPHICS statement, then PROC REG produces a variety of useful plots. Figure 73.3 shows a plot of the residuals versus the regressor and Figure 73.4 shows a panel of diagnostic plots.

Figure 73.3 Residuals vs. Regressor

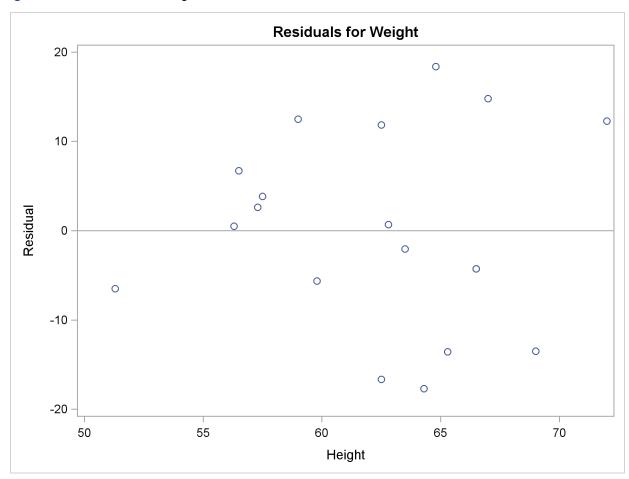
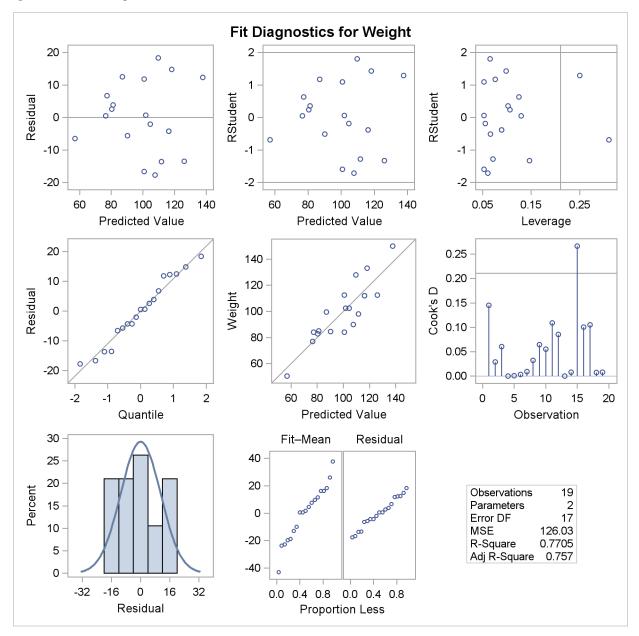


Figure 73.4 Fit Diagnostics



A trend in the residuals would indicate nonconstant variance in the data. The plot of residuals by predicted values in the upper-left corner of the diagnostics panel in Figure 73.4 might indicate a slight trend in the residuals; they appear to increase slightly as the predicted values increase. A fan-shaped trend might indicate the need for a variance-stabilizing transformation. A curved trend (such as a semicircle) might indicate the need for a quadratic term in the model. Since these residuals have no apparent trend, the analysis is considered to be acceptable.

Polynomial Regression

Consider a response variable Y that can be predicted by a polynomial function of a regressor variable X. You can estimate β_0 , the intercept; β_1 , the slope due to X; and β_2 , the slope due to X^2 , in

$$Y_i = \beta_0 + \beta_1 X_i + \beta_2 X_i^2 + \epsilon_i$$

for the observations i = 1, 2, ..., n.

Consider the following example on population growth trends. The population of the United States from 1790 to 2000 is fit to linear and quadratic functions of time. Note that the quadratic term, YearSq, is created in the DATA step; this is done since polynomial effects such as Year*Year cannot be specified in the MODEL statement in PROC REG. The data are as follows:

```
data USPopulation;
   input Population @@;
   retain Year 1780;
   Year
             = Year+10;
   YearSq
            = Year*Year;
   Population = Population/1000;
datalines;
3929 5308 7239 9638 12866 17069 23191 31443 39818 50155
62947 75994 91972 105710 122775 131669 151325 179323 203211
226542 248710 281422
ods graphics on;
proc reg data=USPopulation plots=ResidualByPredicted;
   var YearSq;
   model Population=Year / r clm cli;
```

The DATA option ensures that the procedure uses the intended data set. Any variable that you might add to the model but that is not included in the first MODEL statement must appear in the VAR statement.

The "Analysis of Variance" and "Parameter Estimates" tables are displayed in Figure 73.5.

Figure 73.5 ANOVA Table and Parameter Estimates

			Procedure MODEL1	е			
	Dep	endent Varia	ble: Popu	ulation			
		Analysis	of Varia	nce			
		Su	m of	1	Mean		
Source	D	F Squ	ares	Sq	uare	F Value	Pr > F
Model		1 14	6869	14	6869	228.92	<.0001
Error	2	20 1	2832	641.5	8160		
Corrected Total	2	21 15	9700				
Ro	ot MSE	25.3	2946 1	R-Square	e (0.9197	
De	pendent Mea	ın 94.6		Adj R-S		0.9156	
	eff Var	26.7		,	-		
		Parameter	Estimate	es			
		Parameter	Stand	dard			
Variable	DF	Estimate		rror	t Valu	ie Pr	> t
Intercept	1 -2	345.85498	161.3	9279	-14.5	54 <	.0001
Year	1	1.28786	0.08	8512	15 1	L3 <	.0001

The Model F statistic is significant (F=228.92, p<0.0001), indicating that the model accounts for a significant portion of variation in the data. The R-square indicates that the model accounts for 92% of the variation in population growth. The fitted equation for this model is

Population =
$$-2345.85 + 1.29 \times \text{Year}$$

In the MODEL statement, three options are specified: R requests a residual analysis to be performed, CLI requests 95% confidence limits for an individual value, and CLM requests these limits for the expected value of the dependent variable. You can request specific $100(1-\alpha)\%$ limits with the ALPHA= option in the PROC REG or MODEL statement.

Figure 73.6 shows the "Output Statistics" table. The residual, its standard error, and the studentized residuals are displayed for each observation. The studentized residual is the residual divided by its standard error. The magnitude of each studentized residual is shown in a print plot. Studentized residuals follow a t distribution and can be used to identify outlying or extreme observations. Asterisks (*) extending beyond the dashed lines indicate that the residual is more than three standard errors from zero. Many observations having absolute studentized residuals greater than two might indicate an inadequate model. Cook's D is a measure of the change in the predicted values upon deletion of that observation from the data set; hence, it measures the influence of the observation on the estimated regression coefficients.

Figure 73.6 Output Statistics

The REG Procedure

Model: MODEL1

Dependent Variable: Population

Output Statistics

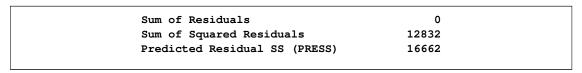
	Dependent	Predicted	Std Error					
Obs	Variable	Value	Mean Predict	95% CL	Mean	95% CL	Predict	Residual
1	3.9290	-40.5778	10.4424	-62.3602	-18.7953	-97.7280	16.5725	44.5068
2	5.3080	-27.6991	9.7238	-47.9826	-7.4156	-84.2950	28.8968	33.0071
3	7.2390	-14.8205	9.0283	-33.6533	4.0123	-70.9128	41.2719	22.0595
4	9.6380	-1.9418	8.3617	-19.3841	15.5004	-57.5827	53.6991	11.5798
5	12.8660	10.9368	7.7314	-5.1906	27.0643	-44.3060	66.1797	1.9292
6	17.0690	23.8155	7.1470	8.9070	38.7239	-31.0839	78.7148	-6.7465
7	23.1910	36.6941	6.6208	22.8834	50.5048	-17.9174	91.3056	-13.5031
8	31.4430	49.5727	6.1675	36.7075	62.4380	-4.8073	103.9528	-18.1297
9	39.8180	62.4514	5.8044	50.3436	74.5592	8.2455	116.6573	-22.6334
10	50.1550	75.3300	5.5491	63.7547	86.9053	21.2406	129.4195	-25.1750
11	62.9470	88.2087	5.4170	76.9090	99.5084	34.1776	142.2398	-25.2617
12	75.9940	101.0873	5.4170	89.7876	112.3870	47.0562	155.1184	-25.0933
13	91.9720	113.9660	5.5491	102.3907	125.5413	59.8765	168.0554	-21.9940
14	105.7100	126.8446	5.8044	114.7368	138.9524	72.6387	181.0505	-21.1346
15	122.7750	139.7233	6.1675	126.8580	152.5885	85.3432	194.1033	-16.9483
16	131.6690	152.6019	6.6208	138.7912	166.4126	97.9904	207.2134	-20.9329
17	151.3250	165.4805	7.1470	150.5721	180.3890	110.5812	220.3799	-14.1555
18	179.3230	178.3592	7.7314	162.2317	194.4866	123.1163	233.6020	0.9638
19	203.2110	191.2378	8.3617	173.7956	208.6801	135.5969	246.8787	11.9732
20	226.5420	204.1165	9.0283	185.2837	222.9493	148.0241	260.2088	22.4255
21	248.7100	216.9951	9.7238	196.7116	237.2786	160.3992	273.5910	31.7149
22	281.4220	229.8738	10.4424	208.0913	251.6562	172.7235	287.0240	51.5482

Output Statistics

	Std Error	Student				Cook's
Obs	Residual	Residual	-	-2-1 0 1 2		D
1	23.077	1.929	- 1	***	-	0.381
2	23.389	1.411	- 1	**	-	0.172
3	23.666	0.932	- 1	*	-	0.063
4	23.909	0.484	- 1	1	-	0.014
5	24.121	0.0800	- 1	1	-	0.000
6	24.300	-0.278	- 1	1	-	0.003
7	24.449	-0.552	- 1	*	-	0.011
8	24.567	-0.738	- 1	*	-	0.017
9	24.655	-0.918	- 1	*	-	0.023
10	24.714	-1.019	- 1	**	1	0.026
11	24.743	-1.021	- 1	**	-	0.025
12	24.743	-1.014	- 1	**	-	0.025
13	24.714	-0.890	- 1	*	-	0.020
14	24.655	-0.857	- 1	*	-	0.020
15	24.567	-0.690	- 1	*	-	0.015
16	24.449	-0.856	- 1	*	-	0.027
17	24.300	-0.583	- 1	*	1	0.015
18	24.121	0.0400	- 1	1	-	0.000
19	23.909	0.501	- 1	*	-	0.015
20	23.666	0.948	- 1	*	1	0.065
21	23.389	1.356	- 1	**	1	0.159
22	23.077	2.234	- 1	***	1	0.511

Figure 73.7 shows the residual statistics table. A fairly close agreement between the PRESS statistic (see Table 73.8) and the Sum of Squared Residuals indicates that the MSE is a reasonable measure of the predictive accuracy of the fitted model (Neter, Wasserman, and Kutner 1990).

Figure 73.7 Residual Statistics



Graphical representations are very helpful in interporting the information in the "Output Statistics" table. When you enable ODS Graphics, the REG procedure produces a default set of diagnostic plots that are appropriate for the requested analysis.

Figure 73.8 displays a panel of diagnostics plots. These diagnostics indicate an inadequate model:

- The plots of residual and studentized residual versus predicted value show a clear quadratic pattern.
- The plot of studentized residual versus leverage seems to indicate that there are two outlying data points. However, the plot of Cook's *D* distance versus observation number reveals that these two points are just the data points for the endpoint years 1790 and 2000. These points show up as apparent outliers because the departure of the linear model from the underlying quadratic behavior in the data shows up most strongly at these endpoints.
- The normal quantile plot of the residuals and the residual histogram are not consistent with the assumption of Gaussian errors. This occurs as the residuals themselves still contain the quadratic behavior that is not captured by the linear model.
- The plot of the dependent variable versus the predicted value exhibits a quadratic form around the 45-degree line that represents a perfect fit.
- The "Residual-Fit" (or RF) plot consisting of side-by-side quantile plots of the centered fit and the residuals shows that the spread in the residuals is no greater than the spread in the centered fit. For inappropriate models, the spread of the residuals in such a plot is often greater than the spread of the centered fit. In this case, the RF plot shows that the linear model does indeed capture the increasing trend in the data, and hence accounts for much of the variation in the response.

Figure 73.8 Diagnostics Panel

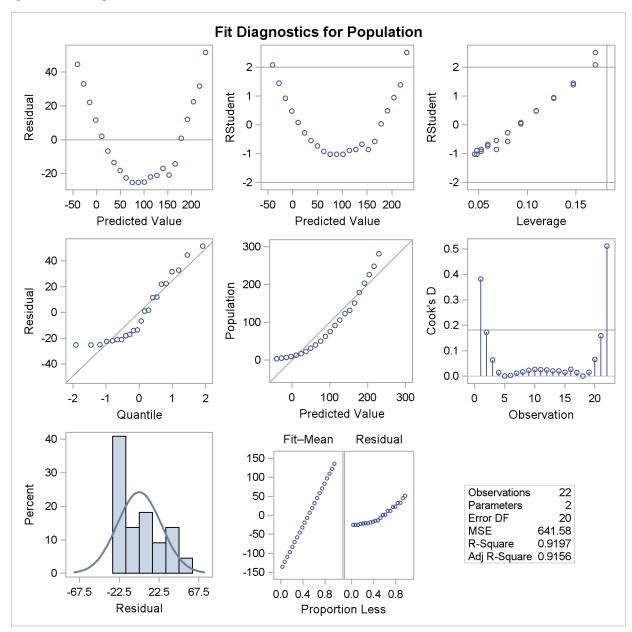


Figure 73.9 shows a plot of residuals versus Year. Again you can see the quadratic pattern that strongly indicates that a quadratic term should be added to the model.

Figure 73.9 Residual Plot

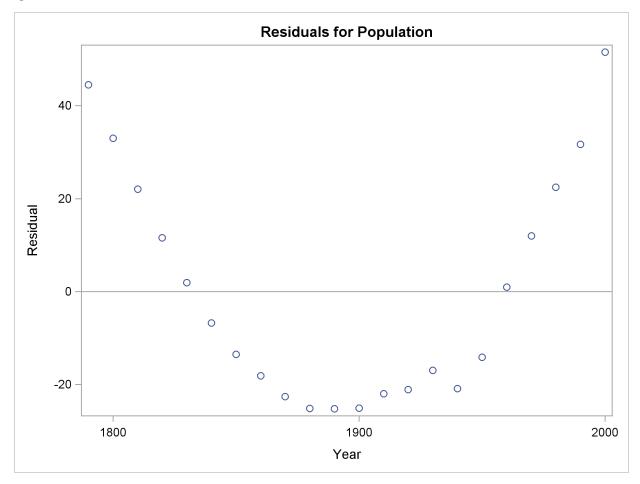
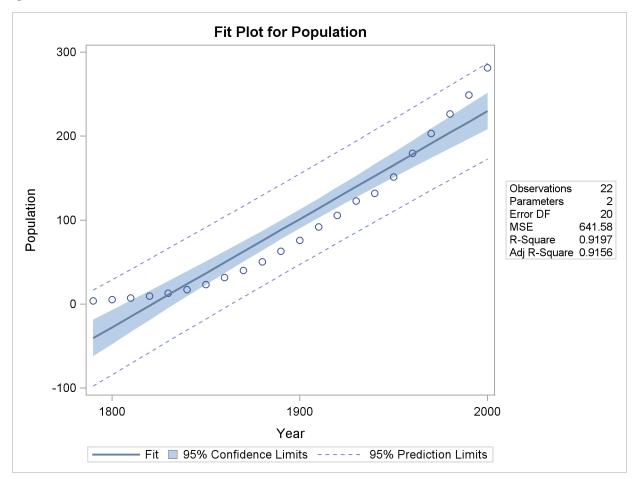


Figure 73.10 shows the "FitPlot" consisting of a scatter plot of the data overlaid with the regression line, and 95% confidence and prediction limits. Note that this plot also indicates that the model fails to capture the quadratic nature of the data. This plot is produced for models containing a single regressor. You can use the ALPHA= option in the model statement to change the significance level of the confidence band and prediction limits.

Figure 73.10 Fit Plot



These default plots provide strong evidence that the Yearsq needs to be added to the model. You can use the interactive feature of PROC REG to do this by specifying the following statements:

```
add YearSq;
print;
run;
```

The ADD statement requests that YearSq be added to the model, and the PRINT command causes the model to be refit and displays the ANOVA and parameter estimates for the new model. The print statement also produces updated ODS graphical displays.

Figure 73.11 displays the ANOVA table and parameter estimates for the new model.

Figure 73.11 ANOVA Table and Parameter Estimates

		Ana	lysis	of Varia	ance				
			Su	m of		Mean			
Source		DF	Squ	ares	5	Square	F V	/alue	Pr > I
Model		2	15	9529		79765	886	4.19	<.0001
Error		19	170.9	7193	8.	99852			
Corrected Tot	al	21	15	9700					
	Root MSE		2.9	9975	R-Squa	are	0.998	39	
	Dependent	Mean	94.6	4800	Adj R-	-Sq	0.998	88	
	Coeff Var		3.1	6938					
		Par	ameter	Estimat	es				
		Parame	ter	Star	ndard				
Variable	DF	Estim	ate	I	Error	t Val	Lue	Pr >	t
Intercept	. 1	21	631	639.5	0181	33	. 82	<.0	0001
Year	1	-24.04	581	0.6	57547	-35	. 60	<.0	0001
YearSq	1	0.00	668	0.0001	7820	37.	. 51	<.0	0001

The overall F statistic is still significant (F=8864.19, p<0.0001). The R-square has increased from 0.9197 to 0.9989, indicating that the model now accounts for 99.9% of the variation in Population. All effects are significant with p<0.0001 for each effect in the model.

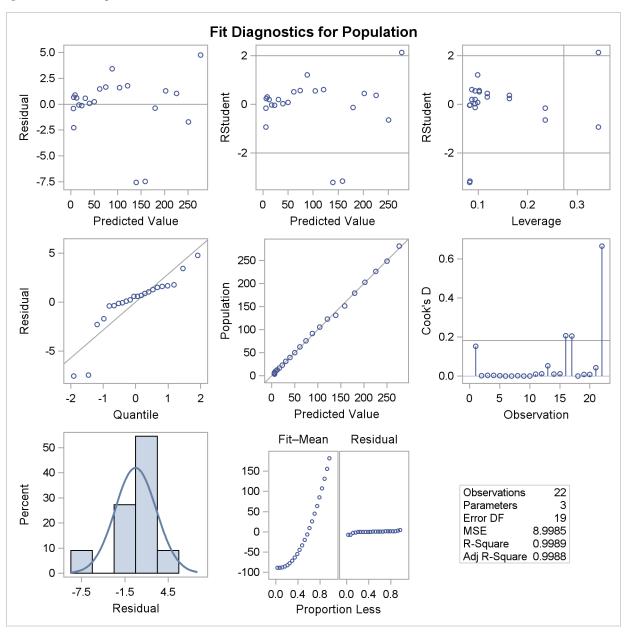
The fitted equation is now

Population =
$$21631 - 24.046 \times \text{Year} + 0.0067 \times \text{Yearsq}$$

Figure 73.12 show the panel of diagnostics for this quadratic polynomial model. These diagnostics indicate that this model is considerably more successful than the corresponding linear model:

- The plots of residuals and studentized residuals versus predicted values exhibit no obvious patterns.
- The points on the plot of the dependent variable versus the predicted values lie along a 45-degree line, indicating that the model successfully predicts the behavior of the dependent variable.
- The plot of studentized residual versus leverage shows that the years 1790 and 2000 are leverage points with 2000 showing up as an outlier. This is confirmed by the plot of Cook's *D* distance versus observation number. This suggests that while the quadratic model fits the current data well, the model might not be quite so successful over a wider range of data. You might want to investigate whether the population trend over the last couple of decades is growing slightly faster than quadratically.

Figure 73.12 Diagnostics Panel

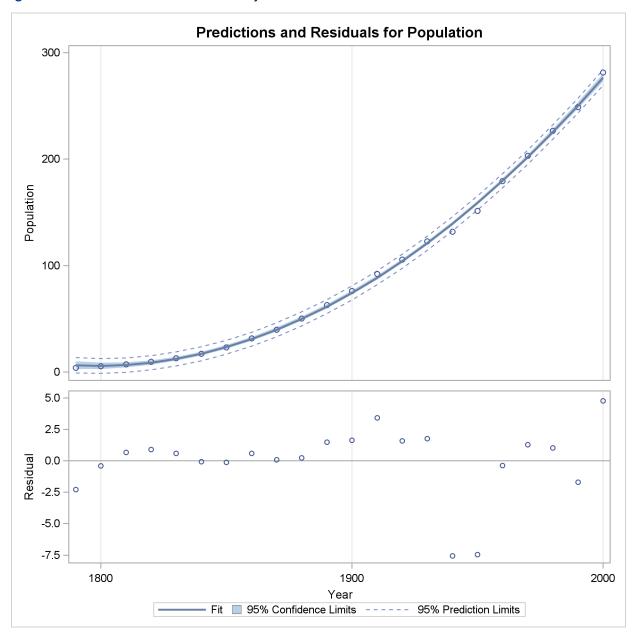


When a model contains more than one regressor, PROC REG does not produce a fit plot. However, when all the regressors in the model are functions of a single variable, it is appropriate to plot predictions and residuals as a function of that variable. You request such plots by using the PLOTS=PREDICTIONS option in the PROC REG statement, as the following code illustrates:

```
proc reg data=USPopulation plots=predictions(X=Year);
  model Population=Year Yearsq;
quit;
ods graphics off;
```

Figure 73.13 shows the data, predictions, and residuals by Year. These plots confirm that the quadratic polynomial model successfully model the growth in U.S. population between the years 1780 and 2000.

Figure 73.13 Predictions and Residuals by Year



To complete an analysis of these data, you might want to examine influence statistics and, since the data are essentially time series data, examine the Durbin-Watson statistic.

Using PROC REG Interactively

The REG procedure can be used interactively. After you specify a model with a MODEL statement and run PROC REG with a RUN statement, a variety of statements can be executed without reinvoking PROC REG.

The section "Interactive Analysis" on page 5513 describes which statements can be used interactively. These interactive statements can be executed singly or in groups by following the single statement or group of statements with a RUN statement. Note that the MODEL statement can be repeated. This is an important difference from the GLM procedure, which supports only one MODEL statement.

If you use PROC REG interactively, you can end the REG procedure with a DATA step, another PROC step, an ENDSAS statement, or a QUIT statement. The syntax of the QUIT statement is quit;

When you are using PROC REG interactively, additional RUN statements do not end PROC REG but tell the procedure to execute additional statements.

When a BY statement is used with PROC REG, interactive processing is not possible; that is, once the first RUN statement is encountered, processing proceeds for each BY group in the data set, and no further statements are accepted by the procedure.

When you use PROC REG interactively, you can fit a model, perform diagnostics, and then refit the model and perform diagnostics on the refitted model. Most of the interactive statements implicitly refit the model; for example, if you use the ADD statement to add a variable to the model, the regression equation is automatically recomputed. The two exceptions to this automatic recomputing are the PAINT and REWEIGHT statements. These two statements do not cause the model to be refitted. To refit the model, you can follow these statements either with a REFIT statement, which causes the model to be explicitly recomputed, or with another interactive statement that causes the model to be implicitly recomputed.

Syntax: REG Procedure

The following statements are available in PROC REG:

```
PROC REG < options>;
   < label: >MODEL dependents=< regressors > < / options > ;
   BY variables:
   FREQ variable:
   ID variables;
   VAR variables;
   WEIGHT variable;
   ADD variables;
   DELETE variables;
   < label: >MTEST < equation, ..., equation > < / options > ;
   OUTPUT < OUT=SAS-data-set >< keyword=names >
                                                     < ... keyword=names > ;
                                 PAINT < condition | ALLOBS >
   RESTRICT equation, . . . , equation;
   REWEIGHT < condition | ALLOBS >

STATUS | UNDO > ;
   PLOT < yvariable*xvariable> < =symbol>
                                            <...yvariable*xvariable> <=symbol> </
         options>;
   PRINT < options > < ANOVA > < MODELDATA > ;
   REFIT:
   RESTRICT equation, ..., equation;
   REWEIGHT < condition | ALLOBS >
                                      /< STATUS / UNDO>;
   < label: >TEST equation, < , . . . , equation > < / option > ;
```

Although there are numerous statements and options available in PROC REG, many analyses use only a few of them. Often you can find the features you need by looking at an example or by scanning this section.

In the preceding list, brackets denote optional specifications, and vertical bars denote a choice of one of the specifications separated by the vertical bars. In all cases, *label* is optional.

The PROC REG statement is required. To fit a model to the data, you must specify the MODEL statement. If you want to use only the options available in the PROC REG statement, you do not need a MODEL statement, but you must use a VAR statement. (See the example in the section "OUTSSCP= Data Sets" on page 5512.) Several MODEL statements can be used. In addition, several MTEST, OUTPUT, PAINT, PLOT, PRINT, RESTRICT, and TEST statements can follow each MODEL statement.

The ADD, DELETE, and REWEIGHT statements are used interactively to change the regression model and the data used in fitting the model. The ADD, DELETE, MTEST, OUTPUT, PLOT, PRINT, RESTRICT, and TEST statements implicitly refit the model; changes made to the model are reflected in the results from these statements. The REFIT statement is used to refit the model explicitly and is most helpful when it follows PAINT and REWEIGHT statements, which do not refit the model.

The BY, FREQ, ID, VAR, and WEIGHT statements are optionally specified once for the entire PROC step, and they must appear before the first RUN statement.

When a TYPE=CORR, TYPE=COV, or TYPE=SSCP data set is used as an input data set to PROC REG, statements and options that require the original data are not available. Specifically, the OUTPUT, PAINT, PLOT, and REWEIGHT statements and the MODEL and PRINT statement options P, R, CLM, CLI, DW, DWPROB, INFLUENCE, PARTIAL, and PARTIALDATA are disabled.

You can specify the following statements with the REG procedure in addition to the PROC REG statement:

ADD adds independent variables to the regression model.

BY specifies variables to define subgroups for the analysis.

DELETE deletes independent variables from the regression model.

FREQ specifies a frequency variable.

ID names a variable to identify observations in the tables.

MODEL specifies the dependent and independent variables in the regression model, re-

quests a model selection method, displays predicted values, and provides details

on the estimates (according to which options are selected).

MTEST performs multivariate tests across multiple dependent variables.

OUTPUT creates an output data set and names the variables to contain predicted values,

residuals, and other diagnostic statistics.

PAINT paints points in scatter plots.

PLOT generates scatter plots.

PRINT displays information about the model and can reset options.

REFIT refits the model.

RESTRICT places linear equality restrictions on the parameter estimates.

REWEIGHT excludes specific observations from analysis or changes the weights of observa-

tions used.

TEST performs an F test on linear functions of the parameters.

VAR lists variables for which crossproducts are to be computed, variables that can be

interactively added to the model, or variables to be used in scatter plots.

WEIGHT declares a variable to weight observations.

PROC REG Statement

PROC REG < options> ;

The PROC REG statement is required. If you want to fit a model to the data, you must also use a MODEL statement. If you want to use only the PROC REG options, you do not need a MODEL statement, but you must use a VAR statement. If you do not use a MODEL statement, then the COVOUT and OUTEST= options are not available.

Table 73.1 lists the options you can use with the PROC REG statement. Note that any option specified in the PROC REG statement applies to all MODEL statements.

Table 73.1 PROC REG Statement Options

Description Data Set Options DATA= names a data set to use for the regression OUTEST= outputs a data set that contains parameter estimates and other model fit summary statistics OUTSSCP= outputs a data set that contains sums of squares and crossproducts COVOUT outputs the covariance matrix for parameter estimates to the OUTEST= data set EDF outputs the number of regressors, the error degrees of freedom, and the model R² to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options <t< th=""><th>PROC</th><th>S REG Statement Options</th></t<>	PROC	S REG Statement Options
DATA= outputs a data set to use for the regression OUTEST= outputs a data set that contains parameter estimates and other model fit summary statistics OUTSSCP= outputs a data set that contains sums of squares and crossproducts outputs the covariance matrix for parameter estimates to the OUTEST= data set EDF outputs the number of regressors, the error degrees of freedom, and the model R² to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set PRESUARE same effect as the EDF option OUTEST= data set RSQUARE same effect as the EDF option OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set Specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	Option	Description
OUTEST= outputs a data set that contains parameter estimates and other model fit summary statistics OUTSSCP= outputs a data set that contains sums of squares and crossproducts outputs the covariance matrix for parameter estimates to the OUTEST= data set EDF outputs the number of regressors, the error degrees of freedom, and the model R² to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	Data Set Option	s
model fit summary statistics OUTSSCP= outputs a data set that contains sums of squares and crossproducts OUTEST= data set EDF outputs the number of regressors, the error degrees of freedom, and the model R² to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set. PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	DATA=	names a data set to use for the regression
OUTSSCP= COVOUT outputs the covariance matrix for parameter estimates to the OUTEST= data set EDF outputs the number of regressors, the error degrees of freedom, and the model R² to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set OUTEST= data set OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE RSQUARE RSQUARE TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= GOUT= specifies an annotation data set specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	OUTEST=	outputs a data set that contains parameter estimates and other
COVOUT outputs the covariance matrix for parameter estimates to the OUTEST= data set EDF outputs the number of regressors, the error degrees of freedom, and the model R² to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set OUTEST= data set OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE RSQUARE RSQUARE same effect as the EDF option Outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and		model fit summary statistics
OUTEST= data set EDF outputs the number of regressors, the error degrees of freedom, and the model R² to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	OUTSSCP=	outputs a data set that contains sums of squares and crossproducts
OUTSEB outputs the number of regressors, the error degrees of freedom, and the model R² to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	COVOUT	*
and the model R^2 to the OUTEST= data set OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set PRESS enerforms ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE RSQUARE TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and		
OUTSEB outputs standard errors of the parameter estimates to the OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	EDF	
OUTEST= data set OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE RSQUARE TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and		
OUTSTB outputs standardized parameter estimates to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option OUTEST= data set Same effect as the EDF option outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	OUTSEB	*
set. Use only with the RIDGE= or PCOMIT= option. OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and		
OUTVIF outputs the variance inflation factors to the OUTEST= data set. Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	OUTSTB	•
Use only with the RIDGE= or PCOMIT= option. PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and		
PCOMIT= performs incomplete principal component analysis and outputs estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	OUTVIF	•
estimates to the OUTEST= data set PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and		•
PRESS outputs the PRESS statistic to the OUTEST= data set RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	PCOMIT=	
RIDGE= performs ridge regression analysis and outputs estimates to the OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	PPEGG	
OUTEST= data set RSQUARE same effect as the EDF option TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and		-
RSQUARE TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	RIDGE=	
TABLEOUT outputs standard errors, confidence limits, and associated test statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	DCOLLABE	
statistics of the parameter estimates to the OUTEST= data set ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	-	
ODS Graphics Options PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	TABLEOUT	•
PLOTS= produces ODS graphical displays Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and		•
Traditional Graphics Options ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	-	
ANNOTATE= specifies an annotation data set GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	PLOTS=	produces ODS graphical displays
GOUT= specifies the graphics catalog in which graphics output is saved Display Options CORR displays correlation matrix for variables listed in MODEL and	Traditional Grap	phics Options
Display Options CORR displays correlation matrix for variables listed in MODEL and	ANNOTATE=	specifies an annotation data set
CORR displays correlation matrix for variables listed in MODEL and	GOUT=	specifies the graphics catalog in which graphics output is saved
CORR displays correlation matrix for variables listed in MODEL and	Display Options	
		VAR statements

Table 73.1 continued

Option	Description
SIMPLE	displays simple statistics for each variable listed in MODEL and
	VAR statements
USCCP	displays uncorrected sums of squares and crossproducts matrix
ALL	displays all statistics (CORR, SIMPLE, and USSCP)
NOPRINT	suppresses output
LINEPRINTER	creates plots requested as line printer plot
Other Options	
ALPHA=	sets significance value for confidence and prediction intervals and
	tests
SINGULAR=	sets criterion for checking for singularity

Following are explanations of the options that you can specify in the PROC REG statement (in alphabetical order).

Note that any option specified in the PROC REG statement applies to all MODEL statements.

ALL

requests the display of many tables. Using the ALL option in the PROC REG statement is equivalent to specifying ALL in every MODEL statement. The ALL option also implies the CORR, SIMPLE, and USSCP options.

ALPHA=number

sets the significance level used for the construction of confidence intervals. The value must be between 0 and 1; the default value of 0.05 results in 95% intervals. This option affects the PROC REG option TABLEOUT; the MODEL options CLB, CLI, and CLM; the OUTPUT statement keywords LCL, LCLM, UCL, and UCLM; the PLOT statement keywords LCL., LCLM., UCL., and UCLM.; and the PLOT statement options CONF and PRED.

ANNOTATE=SAS-data-set

ANNO=SAS-data-set

specifies an input data set containing annotate variables, as described in SAS/GRAPH Software: Reference. You can use this data set to add features to the traditional graphics that you request with the PLOT statement. Features provided in this data set are applied to all plots produced in the current run of PROC REG. To add features to individual plots, use the ANNOTATE= option in the PLOT statement. This option cannot be used if the LINEPRINTER option is specified.

CORR

displays the correlation matrix for all variables listed in the MODEL or VAR statement.

COVOUT

outputs the covariance matrices for the parameter estimates to the OUTEST= data set. This option is valid only if the OUTEST= option is also specified. See the section "OUTEST= Data Set" on page 5506.

DATA=SAS-data-set

names the SAS data set to be used by PROC REG. The data set can be an ordinary SAS data set or a TYPE=CORR, TYPE=COV, or TYPE=SSCP data set. If one of these special TYPE=data sets is used, the OUTPUT, PAINT, PLOT, and REWEIGHT statements, ODS Graphics, and some options in the MODEL and PRINT statements are not available. See Appendix A, "Special SAS Data Sets," for more information about TYPE= data sets. If the DATA= option is not specified, PROC REG uses the most recently created SAS data set.

EDF

outputs the number of regressors in the model excluding and including the intercept, the error degrees of freedom, and the model R^2 to the OUTEST= data set.

GOUT=graphics-catalog

specifies the graphics catalog in which traditional graphics output is saved. The default *graphics-catalog* is WORK.GSEG. The GOUT= option cannot be used if the LINEPRINTER option is specified.

LINEPRINTER | LP

creates plots requested as line printer plots. If you do not specify this option, requested plots are created on a high-resolution graphics device. This option is required if plots are requested and you do not have SAS/GRAPH software.

NOPRINT

suppresses the normal display of results. Note that this option temporarily disables the Output Delivery System (ODS); see Chapter 20, "Using the Output Delivery System," for more information.

OUTEST=SAS-data-set

requests that parameter estimates and optional model fit summary statistics be output to this data set. See the section "OUTEST= Data Set" on page 5506 for details. If you want to create a permanent SAS data set, you must specify a two-level name (refer to the section "SAS Files" in SAS Language Reference: Concepts for more information about permanent SAS data sets).

OUTSEB

outputs the standard errors of the parameter estimates to the OUTEST= data set. The value SEB for the variable _TYPE_ identifies the standard errors. If the RIDGE= or PCOMIT= option is specified, additional observations are included and identified by the values RIDGESEB and IPCSEB, respectively, for the variable _TYPE_. The standard errors for ridge regression estimates and IPC estimates are limited in their usefulness because these estimates are biased. This option is available for all model selection methods except RSQUARE, ADJRSQ, and CP.

OUTSSCP=SAS-data-set

requests that the sums of squares and crossproducts matrix be output to this TYPE=SSCP data set. See the section "OUTSSCP= Data Sets" on page 5512 for details. If you want to create a permanent SAS data set, you must specify a two-level name (refer to the section "SAS Files" in SAS Language Reference: Concepts for more information about permanent SAS data sets).

OUTSTB

outputs the standardized parameter estimates as well as the usual estimates to the OUTEST= data set when the RIDGE= or PCOMIT= option is specified. The values RIDGESTB and IPCSTB for the variable _TYPE_ identify ridge regression estimates and IPC estimates, respectively.

OUTVIF

outputs the variance inflation factors (VIF) to the OUTEST= data set when the RIDGE= or PCOMIT= option is specified. The factors are the diagonal elements of the inverse of the correlation matrix of regressors as adjusted by ridge regression or IPC analysis. These observations are identified in the output data set by the values RIDGEVIF and IPCVIF for the variable _TYPE_.

PCOMIT=list

requests an incomplete principal component (IPC) analysis for each value m in the list. The procedure computes parameter estimates by using all but the last m principal components. Each value of m produces a set of IPC estimates, which are output to the OUTEST= data set. The values of m are saved by the variable _PCOMIT_, and the value of the variable _TYPE_ is set to IPC to identify the estimates. Only nonnegative integers can be specified with the PCOMIT= option.

If you specify the PCOMIT= option, RESTRICT statements are ignored.

```
PLOTS < (global-plot-options) > < = plot-request < (options) > >
```

PLOTS < (global-plot-options) > <= (plot-request < (options) > < ... plot-request < (options) > >) > controls the plots produced through ODS Graphics. When you specify only one plot request, you can omit the parentheses around the plot request. Here are some examples:

```
plots = none
plots = diagnostics(unpack)
plots = (all fit(stats)=none)
plots(label) = (rstudentbyleverage cooksd)
plots(only) = (diagnostics(stats=all) fit(nocli stats=(aic sbc))
```

You must enable ODS Graphics before requesting plots, as shown in the following example. For general information about ODS Graphics, see Chapter 21, "Statistical Graphics Using ODS."

```
ods graphics on;
proc reg;
  model y = x1-x10;
run;
proc reg plots=diagnostics(stats=(default aic sbc));
  model y = x1-x10;
run;
ods graphics off;
```

If you have enabled ODS Graphics but do not specify the PLOTS= option, then PROC REG produces a default set of plots. Table 73.2 lists the default set of plots produced.

Table 73.2 Default ODS Graphics Produced

Plot	Conditional On
DiagnosticsPanel	Unconditional
ResidualPlot	Unconditional
FitPlot	Model with one regressor (excluding intercept)
PartialPlot	PARTIAL option specified in MODEL statement
RidgePanel	RIDGE= option specified in PROC REG or MODEL statement

For models with multiple dependent variables, separate plots are produced for each dependent variable. For jobs with more than one MODEL statement, plots are produced for each model statement.

The *global-options* apply to all plots generated by the REG procedure, unless it is altered by a *specific-plot-option*. The following global plot options are available:

LABEL

specifies that the LABEL option be applied to each plot that supports a LABEL option. See the descriptions of the specific plots for details.

MAXPOINTS=NONE | number

specifies that plots with elements that require processing more than *number* points be suppressed. The default is MAXPOINTS=5000. This cutoff is ignored if you specify MAXPOINTS=NONE.

MODELLABEL

requests that the model label be displayed in the upper-left corner of all plots. This option is useful when you use more than one MODEL statement.

ONLY

suppress the default plots. Only plots specifically requested are displayed.

STATS=ALL | DEFAULT | NONE | (plot-statistics)

requests statistics that are included on the fit plot and diagnostics panel. Table 73.3 lists the statistics that you can request. STATS=ALL requests all these statistics; STATS=NONE suppresses them.

Table 73.3 Statistics Available on Plots

Keyword	Default	Description
ADJRSQ	X	adjusted R-square
AIC		Akaike's information criterion
BIC		Sawa's Bayesian information criterion
CP		Mallows' C_p statistic

Table 73.3 continued

Keyword	Default	Description
COEFFVAR		coefficient of variation
DEPMEAN		mean of dependent
DEFAULT		all default statistics
EDF	X	error degrees of freedom
GMSEP		estimated MSE of prediction, assuming multivariate normality
JP		final prediction error
MSE	X	mean squared error
NOBS	X	number of observations used
NPARM	X	number of parameters in the model (including the intercept)
PC		Amemiya's prediction criterion
RSQUARE	X	R-square
SBC		SBC statistic
SP		SP statistic
SSE		error sum of squares

You request statistics in addition to the default set by including the keyword DEFAULT in the *plot-statistics* list.

UNPACK

suppresses paneling.

USEALL

specifies that predicted values at data points with missing dependent variable(s) be included on appropriate plots. By default, only points used in constructing the SSCP matrix appear on plots.

The following specific plots are available:

ADJRSQ < (adjrsq-options) >

displays the adjusted R-square values for the models examined when you request variable selection with the SELECTION= option in the MODEL statement.

The following *adjrsq-options* are available for models where you request the RSQUARE, ADJRSQ, or CP selection method:

LABEL

requests that the model number corresponding to the one displayed in the "Subset Selection Summary" table be used to label the model with the largest adjusted R-square statistic at each value of the number of parameters.

LABELVARS

requests that the list (excluding the intercept) of the regressors in the relevant model be used to label the model with the largest adjusted R-square statistic at each value of the number of parameters.

AIC < (aic-options) >

displays Akaike's information criterion (AIC) for the models examined when you request variable selection with the SELECTION= option in the MODEL statement.

The following *aic-options* are available for models where you request the RSQUARE, ADJRSQ, or CP selection method:

LABEL

requests that the model number corresponding to the one displayed in the "Subset Selection Summary" table be used to label the model with the smallest AIC statistic at each value of the number of parameters.

LABELVARS

requests that the list (excluding the intercept) of the regressors in the relevant model be used to label the model with the smallest AIC statistic at each value of the number of parameters.

ALL

produces all appropriate plots.

BIC < (bic-options) >

displays Sawa's Bayesian information criterion (BIC) for the models examined when you request variable selection with the SELECTION= option in the MODEL statement.

The following *bic-options* are available for models where you request the RSQUARE, ADJRSQ, or CP selection method:

LABEL

requests that the model number corresponding to the one displayed in the "Subset Selection Summary" table be used to label the model with the smallest BIC statistic at each value of the number of parameters.

LABELVARS

requests that the list (excluding the intercept) of the regressors in the relevant model be used to label the model with the smallest BIC statistic at each value of the number of parameters.

COOKSD <(LABEL)>

plots Cook's D statistic by observation number. Observations whose Cook's D statistic lies above the horizontal reference line at value 4/n, where n is the number of observations used, are deemed to be influential (Rawlings 1998). If you specify the LABEL option, then points deemed as influential are labeled. If you do not specify an ID variable, the observation number within the current BY group is used as the label. If you specify one or more ID variables in one or more ID statements, then the first ID variable you specify is used for the labeling.

CP < (cp-options) >

displays Mallow's C_p statistic for the models examined when you request variable selection with the SELECTION= option in the MODEL statement. For models where you request the RSQUARE, ADJRSQ, or CP selection, reference lines corresponding

to the equations $C_p = p$ and $C_p = 2p - p_{full}$, where p_{full} is the number of parameters in the full model (excluding the intercept) and p is the number of parameters in the subset model (including the intercept), are displayed on the plot of C_p versus p. For the purpose of parameter estimation, Hocking (1976) suggests selecting a model where $C_p \leq 2p - p_{full}$. For the purpose of prediction, Hocking suggests the criterion $C_p \leq p$. Mallows (1973) suggests that all subset models with C_p small and near p be considered for further study.

The following *cp-options* are available for models where you request the RSQUARE, ADJRSQ, or CP selection method:

LABEL

requests that the model number corresponding to the one displayed in the "Subset Selection Summary" table be used to label the model with the smallest C_p statistic at each value of the number of parameters.

LABELVARS

requests that the list (excluding the intercept) of the regressors in the relevant model be used to label the model with the smallest C_p statistic at each value of the number of parameters.

CRITERIA | CRITERIONPANEL < (criteria-options) >

produces a panel of fit criteria for the models examined when you request variable selection with the SELECTION= option in the MODEL statement. The fit criteria displayed are R-square, adjusted R-square, Mallow's C_p , Akaike's information criterion (AIC), Sawa's Bayesian information criterion (BIC), and Schwarz's Bayesian information criterion (SBC). For SELECTION=RSQUARE, SELECTION=ADJRSQ, or SELECTION=CP, scatter plots of these statistics versus the number of parameters (including the intercept) are displayed. For other selection methods, line plots of these statistics as function of the selection step number are displayed.

The following *criteria-options* are available:

LABEL

requests that the model number corresponding to the one displayed in the "Subset Selection Summary" table be used to label the best model at each value of the number of parameters. This option applies only to the RSQUARE, ADJRSQ, and CP selection methods.

LABELVARS

requests that the list (excluding the intercept) of the regressors in the relevant model be used to label the best model at each value of the number of parameters. Since these labels are typically long, LABELVARS is supported only when the panel is unpacked. This option applies only to the RSQUARE, ADJRSQ, and CP selection methods.

UNPACK

suppresses paneling. Separate plots are produced for each of the six fit statistics. For models where you request the RSQUARE, ADJRSQ, or CP selection, two reference lines corresponding to the equations $C_p = p$ and $C_p = 2p - p_{full}$,

where p_{full} is the number of parameters in the full model (excluding the intercept) and p is the number of parameters in the subset model (including the intercept), are displayed on the plot of C_p versus p. For the purpose of parameter estimation, Hocking (1976) suggests selecting a model where $C_p \leq 2p - p_{full}$. For the purpose of prediction, Hocking suggests the criterion $C_p \leq p$. Mallows (1973) suggests that all subset models with C_p small and near p be considered for further study.

DFBETAS < (DFBETAS-options) >

produces panels of DFBETAS by observation number for the regressors in the model. Note that each panel contains at most six plots, and multiple panels are used in the case where there are more than six regressors (including the intercept) in the model. Observations whose DFBETAS' statistics for a regressor are greater in magnitude than $2/\sqrt{n}$, where n is the number of observations used, are deemed to be influential for that regressor (Rawlings 1998).

The following *DFBETAS-options* are available:

COMMONAXES

specifies that the same DFBETAS axis be used in all panels when multiple panels are needed. By default, the DFBETAS axis is chosen independently for each panel. If you also specify the *UNPACK* option, then the same DFBETAS axis is used for each regressor.

LABEL

specifies that observations whose magnitude are greater than $2/\sqrt{n}$ be labeled. If you do not specify an ID variable, the observation number within the current BY group is used as the label. If you specify one or more ID variables on one or more ID statements, then the first ID variable you specify is used for the labeling.

UNPACK

suppresses paneling. The DFBETAS statistics for each regressor are displayed on separate plots.

DFFITS < (LABEL) >

plots the DFFITS statistic by observation number. Observations whose DFFITS' statistic is greater in magnitude than $2\sqrt{p/n}$, where n is the number of observations used and p is the number of regressors, are deemed to be influential (Rawlings 1998). If you specify the LABEL option, then these influential observations are labeled. If you do not specify an ID variable, the observation number within the current BY group is used as the label. If you specify one or more ID variables in one or more ID statements, then the first ID variable you specify is used for the labeling.

DIAGNOSTICS < (diagnostics-options) >

produces a summary panel of fit diagnostics:

- residuals versus the predicted values
- studentized residuals versus the predicted values
- studentized residuals versus the leverage
- normal quantile plot of the residuals
- dependent variable values versus the predicted values
- Cook's D versus observation number
- histogram of the residuals
- "Residual-Fit" (or RF) plot consisting of side-by-side quantile plots of the centered fit and the residuals
- box plot of the residuals if you specify the STATS=NONE suboption

You can specify the following diagnostics-options:

STATS=stats-options

determines which model fit statistics are included in the panel. See the global STATS= suboption for details. The PLOTS= suboption of the DIAGNOSTIC-SPANEL option overrides the global PLOTS= suboption.

UNPACK

produces the eight plots in the panel as individual plots. Note that you can also request individual plots in the panel by name without having to unpack the panel.

FITPLOT | FIT < (fit-options) >

produces a scatter plot of the data overlaid with the regression line, confidence band, and prediction band for models that depend on at most one regressor excluding the intercept.

You can specify the following fit-options:

NOCLI

suppresses the prediction limits.

NOCLM

suppresses the confidence limits.

NOLIMITS

suppresses the confidence and prediction limits.

STATS=stats-options

determines which model fit statistics are included in the panel. See the global STATS= suboption for details. The PLOTS= suboption of the FITPLOT option overrides the global PLOTS= suboption.

OBSERVEDBYPREDICTED < (LABEL) >

plots dependent variable values by the predicted values. If you specify the LABEL option, then points deemed as outliers or influential (see the RSTUDENTBYLEVERAGE option for details) are labeled.

NONE

suppresses all plots.

PARTIAL < (UNPACK) >

produces panels of partial regression plots for each regressor with at most six regressors per panel. If you specify the UNPACK option, then all partial plot panels are unpacked.

PREDICTIONS (X=numeric-variable < prediction-options >)

produces a panel of two plots whose horizontal axis is the variable you specify in the required X= suboption. The upper plot in the panel is a scatter plot of the residuals. The lower plot shows the data overlaid with the regression line, confidence band, and prediction band. This plot is appropriate for models where all regressors are known to be functions of the single variable that you specify in the X= suboption.

You can specify the following *prediction-options*:

NOCLI

suppresses the prediction limits.

NOCLM

suppresses the confidence limits

NOLIMITS

suppresses the confidence and prediction limits

SMOOTH

requests a nonparametric smooth of the residuals as a function of the variable you specify in the X= suboption. This nonparametric fit is a loess fit that uses local linear polynomials, linear interpolation, and a smoothing parameter selected that yields a local minimum of the corrected Akaike information criterion (AICC). See Chapter 50, "The LOESS Procedure," for details. The SMOOTH option is not supported when a FREQ statement is used.

UNPACK

suppresses paneling.

QQPLOT | QQ

produces a normal quantile plot of the residuals.

RESIDUALBOXPLOT | BOXPLOT < (LABEL) >

produces a box plot consisting of the residuals. If you specify label option, points deemed far-outliers are labeled. If you do not specify an ID variable, the observation number within the current BY group is used as the label. If you specify one or more ID variables in one or more ID statements, then the first ID variable you specify is used for the labeling.

RESIDUALBYPREDICTED < (LABEL) >

plots residuals by predicted values. If you specify the LABEL option, then points deemed as outliers or influential (see the RSTUDENTBYLEVERAGE option for details) are labeled.

RESIDUALS < residual-options) >

produces panels of the residuals versus the regressors in the model. Note that each panel contains at most six plots, and multiple panels are used in the case where there are more than six regressors (including the intercept) in the model.

The following *residual-options* are available:

SMOOTH

requests a nonparametric smooth of the residuals for each regressor. Each non-parametric fit is a loess fit that uses local linear polynomials, linear interpolation, and a smoothing parameter selected that yields a local minimum of the corrected Akaike information criterion (AICC). See Chapter 50, "The LOESS Procedure," for details. The SMOOTH option is not supported when a FREQ statement is used.

UNPACK

suppresses paneling.

RESIDUALHISTOGRAM

produces a histogram of the residuals.

RFPLOT | RF

produces a "Residual-Fit" (or RF) plot consisting of side-by-side quantile plots of the centered fit and the residuals. This plot "shows how much variation in the data is explained by the fit and how much remains in the residuals" (Cleveland 1993).

RIDGE | RIDGEPANEL | RIDGEPLOT < (ridge-options) >

creates panels of VIF values and standardized ridge estimates by ridge values for each coefficient. The VIF values for each coefficient are connected by lines and are displayed in the upper plot in each panel. The points corresponding to the standardized estimates of each coefficient are connected by lines and are displayed in the lower plot in each panel. By default, at most 10 coefficients are represented in a panel and multiple panels are produced for models with more than 10 regressors. For ridge estimates to be computed and plotted, the OUTEST= option must be specified in the PROC REG statement, and the RIDGE= list must be specified in either the PROC REG or the MODEL statement. (See Example 73.5.)

The following *ridge-options* are available:

COMMONAXES

specifies that the same VIF axis and the same standardized estimate axis are used in all panels when multiple panels are needed. By default, these axes are chosen independently for the regressors shown in each panel.

RIDGEAXIS=LINEAR | LOG

specifies the axis type used to display the ridge parameters. The default is RIDGEAXIS=LINEAR. Note that the point with the ridge parameter equal to zero is not displayed if you specify RIDGEAXIS=LOG.

UNPACK

suppresses paneling. The traces of the VIF statistics and standardized estimates are shown in separate plots.

VARSPERPLOT=ALL

VARSPERPLOT=number

specifies the maximum number of regressors displayed in each panel or in each plot if you additionally specify the *UNPACK* option. If you specify VARSPER-PLOT=ALL, then the VIF values and ridge traces for all regressors are displayed in a single panel.

VIFAXIS=LINEAR | LOG

specifies the axis type used to display the VIF statistics. The default is VI-FAXIS=LINEAR.

RSQUARE < (rsquare-options) >

displays the R-square values for the models examined when you request variable selection with the SELECTION= option in the MODEL statement.

The following *rsquare-options* are available for models where you request the RSQUARE, ADJRSQ, or CP selection method:

LABEL

requests that the model number corresponding to the one displayed in the "Subset Selection Summary" table be used to label the model with the largest R-square statistic at each value of the number of parameters.

LABELVARS

requests that the list (excluding the intercept) of the regressors in the relevant model be used to label the model with the largest R-square statistic at each value of the number of parameters.

RSTUDENTBYLEVERAGE < (LABEL) >

plots studentized residuals by leverage. Observations whose studentized residuals lie outside the band between the reference lines RSTUDENT $=\pm 2$ are deemed outliers. Observations whose leverage values are greater than the vertical reference LEVERAGE =2p/n, where p is the number of parameters excluding the intercept and n is the number of observations used, are deemed influential (Rawlings 1998). If you specify the LABEL option, then points deemed as outliers or influential are labeled. If you do not specify an ID variable, the observation number within the current BY group is used as the label. If you specify one or more ID variables in one or more ID statements, then the first ID variable you specify is used for the labeling.

RSTUDENTBYPREDICTED < (LABEL) >

plots studentized residuals by predicted values. If you specify the LABEL option, then points deemed as outliers or influential (see the RSTUDENTBYLEVERAGE option for details) are labeled.

SBC < (sbc-options) >

displays Schwarz's Bayesian information criterion (SBC) for the models examined when you request variable selection with the SELECTION= option in the MODEL statement.

The following *sbc-options* are available for models where you request the RSQUARE, ADJRSQ, or CP selection method:

LABEL

requests that the model number corresponding to the one displayed in the "Subset Selection Summary" table be used to label the model with the smallest SBC statistic at each value of the number of parameters.

LABELVARS

requests that the list (excluding the intercept) of the regressors in the relevant model be used to label the model with the smallest SBC statistic at each value of the number of parameters.

PRESS

outputs the PRESS statistic to the OUTEST= data set. The values of this statistic are saved in the variable _PRESS_. This option is available for all model selection methods except RSQUARE, ADJRSQ, and CP.

RIDGE=list

requests a ridge regression analysis and specifies the values of the ridge constant k (see the section "Computations for Ridge Regression and IPC Analysis" on page 5577). Each value of k produces a set of ridge regression estimates that are placed in the OUTEST= data set. The values of k are saved by the variable _RIDGE_, and the value of the variable _TYPE_ is set to RIDGE to identify the estimates.

Only nonnegative numbers can be specified with the RIDGE= option. Example 73.5 illustrates this option.

If ODS Graphics is in effect (see the section "ODS Graphics" on page 5583), then ridge regression plots are automatically produced. These plots consist of panels containing ridge traces for the regressors, with at most eight ridge traces per panel.

If you specify the RIDGE= option, RESTRICT statements are ignored.

RSQUARE

has the same effect as the EDF option.

SIMPLE

displays the sum, mean, variance, standard deviation, and uncorrected sum of squares for each variable used in PROC REG.

SINGULAR=n

tunes the mechanism used to check for singularities. The default value is machine dependent but is approximately 1E-7 on most machines. This option is rarely needed.

Singularity checking is described in the section "Computational Methods" on page 5578.

TABLEOUT

outputs the standard errors and $100(1-\alpha)\%$ confidence limits for the parameter estimates, the t statistics for testing if the estimates are zero, and the associated p-values to the OUTEST= data set. The _TYPE_ variable values STDERR, LnB, UnB, T, and PVALUE, where $n=100(1-\alpha)$, identify these rows in the OUTEST= data set. The α level can be set with the ALPHA= option in the PROC REG or MODEL statement. The OUTEST= option must be specified in the PROC REG statement for this option to take effect.

USSCP

displays the uncorrected sums-of-squares and crossproducts matrix for all variables used in the procedure.

ADD Statement

ADD variables;

The ADD statement adds independent variables to the regression model. Only variables used in the VAR statement or used in MODEL statements before the first RUN statement can be added to the model. You can use the ADD statement interactively to add variables to the model or to include a variable that was previously deleted with a DELETE statement. Each use of the ADD statement modifies the MODEL label.

See the section "Interactive Analysis" on page 5513 for an example.

BY Statement

BY variables;

You can specify a BY statement with PROC REG to obtain separate analyses on observations in groups defined by the BY variables. When a BY statement appears, the procedure expects the input data set to be sorted in the order of the BY variables. The *variables* are one or more variables in the input data set.

If your input data set is not sorted in ascending order, use one of the following alternatives.

- Sort the data by using the SORT procedure with a similar BY statement.
- Specify the BY statement option NOTSORTED or DESCENDING in the BY statement for the REG procedure. The NOTSORTED option does not mean that the data are unsorted but rather that the data are arranged in groups (according to values of the BY variables) and that these groups are not necessarily in alphabetical or increasing numeric order.
- Create an index on the BY variables by using the DATASETS procedure (in Base SAS software).

When a BY statement is used with PROC REG, interactive processing is not possible; that is, once the first RUN statement is encountered, processing proceeds for each BY group in the data set, and no further statements are accepted by the procedure. A BY statement that appears after the first RUN statement is ignored.

For more information about the BY statement, see SAS Language Reference: Contents. For more information about the DATASETS procedure, see the Base SAS Procedures Guide.

DELETE Statement

DELETE variables;

The DELETE statement deletes independent variables from the regression model. The DELETE statement performs the opposite function of the ADD statement and is used in a similar manner. Each use of the DELETE statement modifies the MODEL label.

For an example of how the ADD statement is used (and how the DELETE statement can be used), see the section "Interactive Analysis" on page 5513.

FREQ Statement

FREQ variable;

When a FREQ statement appears, each observation in the input data set is assumed to represent n observations, where n is the value of the FREQ variable. The analysis produced when you use a FREQ statement is the same as an analysis produced by using a data set that contains n observations in place of each observation in the input data set. When the procedure determines degrees of freedom for significance tests, the total number of observations is considered to be equal to the sum of the values of the FREQ variable.

If the value of the FREQ variable is missing or is less than 1, the observation is not used in the analysis. If the value is not an integer, only the integer portion is used.

The FREQ statement must appear before the first RUN statement, or it is ignored.

ID Statement

ID variables;

When one of the MODEL statement options CLI, CLM, P, R, and INFLUENCE is requested, the variables listed in the ID statement are displayed beside each observation. These variables can be used to identify each observation. If the ID statement is omitted, the observation number is used to identify the observations.

Although there are no restrictions on the length of ID variables, PROC REG might truncate ID values to 16 characters for display purposes.

MODEL Statement

< label: > MODEL dependents=< regressors > < / options > ;

After the keyword MODEL, the dependent (response) variables are specified, followed by an equal sign and the regressor variables. Variables specified in the MODEL statement must be numeric variables in the data set being analyzed. For example, if you want to specify a quadratic term for variable *X1* in the model, you cannot use X1*X1 in the MODEL statement but must create a new variable (for example, X1SQUARE=X1*X1) in a DATA step and use this new variable in the MODEL statement. The label in the MODEL statement is optional.

Table 73.4 lists the options available in the MODEL statement. Equations for the statistics available are given in the section "Model Fit and Diagnostic Statistics" on page 5551.

Table 73.4 MODEL Statement Options

Model Selection and SELECTION= BEST=	specifies model selection method specifies maximum number of subset models displayed or output to the OUTEST= data set
	specifies maximum number of subset models displayed or output to the OUTEST= data set
BEST=	put to the OUTEST= data set
DETAILS	produces summary statistics at each step
DETAILS=	specifies the display details for FORWARD, BACKWARD, and STEPWISE methods
GROUPNAMES=	provides names for groups of variables
INCLUDE=	includes first <i>n</i> variables in the model
MAXSTEP=	specifies maximum number of steps that might be performed
NOINT	fits a model without the intercept term
PCOMIT=	performs incomplete principal component analysis and outputs estimates to the OUTEST= data set
RIDGE=	performs ridge regression analysis and outputs estimates to the OUTEST= data set
SLE=	sets criterion for entry into model
SLS=	sets criterion for staying in model
START=	specifies number of variables in model to begin the comparing and switching process
STOP=	stops selection criterion
Statistics	
ADJRSQ	computes adjusted R^2
AIC	computes Akaike's information criterion
В	computes parameter estimates for each model
BIC	computes Sawa's Bayesian information criterion
CP	computes Mallows' C_p statistic

Table 73.4 continued

Option	Description
GMSEP	computes estimated MSE of prediction assuming multivariate
	normality
JP	computes J_p , the final prediction error
MSE	computes MSE for each model
PC	computes Amemiya's prediction criterion
RMSE	displays root MSE for each model
SBC	computes the SBC statistic
SP	computes S_p statistic for each model
SSE	computes error sum of squares for each model
Data Set Options	
EDF	outputs the number of regressors, the error degrees of freedom,
	and the model R^2 to the OUTEST= data set
OUTSEB	outputs standard errors of the parameter estimates to the OUT-
	EST= data set
OUTSTB	outputs standardized parameter estimates to the OUTEST=
	data set. Use only with the RIDGE= or PCOMIT= option.
OUTVIF	outputs the variance inflation factors to the OUTEST= data set.
	Use only with the RIDGE= or PCOMIT= option.
PRESS	outputs the PRESS statistic to the OUTEST= data set
RSQUARE	has same effect as the EDF option
Regression Calcula	
I	displays inverse of sums of squares and crossproducts
XPX	displays sums-of-squares and crossproducts matrix
Details on Estimate	s
ACOV	displays heteroscedasticity- consistent covariance matrix of es-
	timates and heteroscedasticity-consistent standard errors
ACOVMETHOD=	specifies method for computing the asymptotic
	heteroscedasticity-consistent covariance matrix
COLLIN	produces collinearity analysis
COLLINOINT	produces collinearity analysis with intercept adjusted out
CORRB	displays correlation matrix of estimates
COVB	displays covariance matrix of estimates
HCC	displays heteroscedasticity-consistent standard errors
HCCMETHOD=	specifies method for computing the asymptotic
	heteroscedasticity-consistent covariance matrix
LACKFIT	performs lack-of-fit test
PARTIALR2	displays squared semipartial correlation coefficients computed
DCCDD1	using Type I sums of squares
PCORR1	displays squared partial correlation coefficients computed us-
DGOD54	ing Type I sums of squares
PCORR2	displays squared partial correlation coefficients computed us-
	ing Type II sums of squares

Table 73.4 continued

SCORR1 displays squared semipartial correlation coefficients computed using Type I sums of squares displays squared semipartial correlation coefficients computed using Type II sums of squares displays a sequence of parameter estimates during selection process SEQB displays a sequence of parameter estimates during selection process SPEC tests that first and second moments of model are correctly specified displays the sequential sums of squares displays the partial sums of squares displays standardized parameter estimates whitte displays tolerance values for parameter estimates whitte displays heteroscedasticity-consistent standard errors computes variance-inflation factors Predicted and Residual Values CLB computes $100(1-\alpha)\%$ confidence limits for the parameter estimates computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable computes a Durbin-Watson statistic and p-value computes a Durbin-Watson statistic and p-value computes a Durbin-Watson statistic and p-value computes a Durbin-Watson statistic and produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT supresses display of results SIGMA= certain for checking for singularity	Option	Description
SCORR2 displays squared semipartial correlation coefficients computed using Type II sums of squares SEQB displays a sequence of parameter estimates during selection process SPEC tests that first and second moments of model are correctly specified SS1 displays the sequential sums of squares SS2 displays the partial sums of squares STB displays tolerance values for parameter estimates TOL displays tolerance values for parameter estimates WHITE displays heteroscedasticity-consistent standard errors VIF computes variance-inflation factors Predicted and Residual Values CLB computes $100(1-\alpha)\%$ confidence limits for the parameter estimates CLI computes $100(1-\alpha)\%$ confidence limits for an individual predicted value CLM computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p -value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORRI, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	SCORR1	displays squared semipartial correlation coefficients computed
SEQB displays a sequence of parameter estimates during selection process SPEC tests that first and second moments of model are correctly specified displays the sequential sums of squares SS1 displays the partial sums of squares SS2 displays the partial sums of squares STB displays standardized parameter estimates TOL displays tolerance values for parameter estimates WHITE displays heteroscedasticity-consistent standard errors VIF computes variance-inflation factors Predicted and Residual Values CLB computes $100(1-\alpha)\%$ confidence limits for the parameter estimates CLI computes $100(1-\alpha)\%$ confidence limits for an individual predicted value CLM computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p -value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC		using Type I sums of squares
SEQB displays a sequence of parameter estimates during selection process SPEC tests that first and second moments of model are correctly specified SS1 displays the sequential sums of squares SS2 displays the partial sums of squares STB displays standardized parameter estimates TOL displays tolerance values for parameter estimates WHITE displays heteroscedasticity-consistent standard errors VIF computes variance-inflation factors Predicted and Residual Values CLB computes $100(1-\alpha)\%$ confidence limits for the parameter estimates CLI computes $100(1-\alpha)\%$ confidence limits for an individual predicted value CLM computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p -value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	SCORR2	displays squared semipartial correlation coefficients computed
$ \begin{array}{c} \text{process} \\ \text{SPEC} & \text{tests that first and second moments of model are correctly specified} \\ \text{SS1} & \text{displays the sequential sums of squares} \\ \text{SS2} & \text{displays than partial sums of squares} \\ \text{STB} & \text{displays standardized parameter estimates} \\ \text{TOL} & \text{displays tolerance values for parameter estimates} \\ \text{WHITE} & \text{displays heteroscedasticity-consistent standard errors} \\ \text{VIF} & \text{computes variance-inflation factors} \\ \textbf{Predicted and Residual Values} \\ \text{CLB} & \text{computes } 100(1-\alpha)\% \text{ confidence limits for the parameter estimates} \\ \text{CLI} & \text{computes } 100(1-\alpha)\% \text{ confidence limits for an individual predicted value} \\ \text{CLM} & \text{computes } 100(1-\alpha)\% \text{ confidence limits for the expected value} \\ \text{of the dependent variable} \\ \text{DW} & \text{computes a Durbin-Watson statistic} \\ \text{DWPROB} & \text{computes a Durbin-Watson statistic and } p\text{-value} \\ \text{INFLUENCE} & \text{computes influence statistics} \\ \text{P} & \text{computes predicted values} \\ \text{PARTIAL} & \text{displays partial regression plots for each regressor} \\ \text{PARTIALDATA} & \text{displays partial regression plots for each regressor} \\ \text{PARTIALDATA} & \text{displays partial regression data} \\ \text{R} & \text{produces analysis of residuals} \\ \\ \textbf{Display Options and Other Options} \\ \text{ALL} & \text{requests the following options:} \\ & \text{ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX} \\ \text{ALPHA=} & \text{sets significance value for confidence and prediction intervals and tests} \\ \text{NOPRINT} & \text{suppresses display of results} \\ \text{SIGMA=} & \text{specifies the true standard deviation of error term for computing CP and BIC} \\ \end{aligned}$		using Type II sums of squares
spec tests that first and second moments of model are correctly specified sequential sums of squares displays the sequential sums of squares displays the partial sums of squares standardized parameter estimates displays tolerance values for parameter estimates white displays heteroscedasticity-consistent standard errors vife computes variance-inflation factors predicted and Residual Values computes $100(1-\alpha)\%$ confidence limits for the parameter estimates computes $100(1-\alpha)\%$ confidence limits for an individual predicted value computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable computes a Durbin-Watson statistic computes a Durbin-Watson statistic computes and Durbin-Watson statistic and p-value influence statistics computes predicted values computes predicted values displays partial regression plots for each regressor partial displays partial regression data produces analysis of residuals produces analysis of residuals cover analysis of residuals produces analysis of residuals produces analysis of residuals produces analysis of residuals cover and prediction intervals and tests sets significance value for confidence and prediction intervals and tests suppresses display of results specifies the true standard deviation of error term for computing CP and BIC	SEQB	displays a sequence of parameter estimates during selection
ified SS1 displays the sequential sums of squares SS2 displays the partial sums of squares STB displays standardized parameter estimates TOL displays tolerance values for parameter estimates WHITE displays heteroscedasticity-consistent standard errors VIF computes variance-inflation factors Predicted and Residual Values CLB computes 100(1 – α)% confidence limits for the parameter estimates CLI computes 100(1 – α)% confidence limits for an individual predicted value CLM computes 100(1 – α)% confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p-value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC		process
SS1 displays the sequential sums of squares SS2 displays the partial sums of squares STB displays standardized parameter estimates TOL displays tolerance values for parameter estimates WHITE displays heteroscedasticity-consistent standard errors VIF computes variance-inflation factors Predicted and Residual Values CLB computes $100(1-\alpha)\%$ confidence limits for the parameter estimates CLI computes $100(1-\alpha)\%$ confidence limits for an individual predicted value CLM computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p -value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	SPEC	tests that first and second moments of model are correctly spec-
SS2 displays the partial sums of squares STB displays standardized parameter estimates TOL displays tolerance values for parameter estimates WHITE displays heteroscedasticity-consistent standard errors VIF computes variance-inflation factors Predicted and Residual Values CLB computes 100(1 – α)% confidence limits for the parameter estimates CLI computes 100(1 – α)% confidence limits for an individual predicted value CLM computes 100(1 – α)% confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p-value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor DARTIAL displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORRI, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests <tr< td=""><td></td><td>ified</td></tr<>		ified
STB displays standardized parameter estimates TOL displays tolerance values for parameter estimates WHITE displays heteroscedasticity-consistent standard errors VIF computes variance-inflation factors Predicted and Residual Values CLB computes $100(1-\alpha)\%$ confidence limits for the parameter estimates CLI computes $100(1-\alpha)\%$ confidence limits for an individual predicted value CLM computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p -value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	SS1	displays the sequential sums of squares
TOL displays tolerance values for parameter estimates WHITE displays heteroscedasticity-consistent standard errors VIF computes variance-inflation factors Predicted and Residual Values CLB computes $100(1-\alpha)\%$ confidence limits for the parameter estimates CLI computes $100(1-\alpha)\%$ confidence limits for an individual predicted value CLM computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p -value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	SS2	displays the partial sums of squares
WHITEdisplays heteroscedasticity-consistent standard errorsVIFcomputes variance-inflation factorsPredicted and Residual ValuesCLBcomputes $100(1-\alpha)\%$ confidence limits for the parameter estimatesCLIcomputes $100(1-\alpha)\%$ confidence limits for an individual predicted valueCLMcomputes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variableDWcomputes a Durbin-Watson statisticDWPROBcomputes a Durbin-Watson statistic and p -valueINFLUENCEcomputes influence statisticsPcomputes predicted valuesPARTIALdisplays partial regression plots for each regressorPARTIALDATAdisplays partial regression dataRproduces analysis of residualsDisplay Options and Other OptionsALLrequests the following options:ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPXALPHA=sets significance value for confidence and prediction intervals and testsNOPRINTsuppresses display of resultsSIGMA=specifies the true standard deviation of error term for computing CP and BIC	STB	displays standardized parameter estimates
VIFcomputes variance-inflation factorsPredicted and Residual ValuesCLBcomputes $100(1-\alpha)\%$ confidence limits for the parameter estimatesCLIcomputes $100(1-\alpha)\%$ confidence limits for an individual predicted valueCLMcomputes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variableDWcomputes a Durbin-Watson statisticDWPROBcomputes a Durbin-Watson statistic and p -valueINFLUENCEcomputes influence statisticsPcomputes predicted valuesPARTIALdisplays partial regression plots for each regressorPARTIALDATAdisplays partial regression dataRproduces analysis of residualsDisplay Options and Other OptionsALLrequests the following options:ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPXALPHA=sets significance value for confidence and prediction intervals and testsNOPRINTsuppresses display of resultsSIGMA=specifies the true standard deviation of error term for computing CP and BIC	TOL	displays tolerance values for parameter estimates
Predicted and Residual Values CLB computes $100(1-\alpha)\%$ confidence limits for the parameter estimates CLI computes $100(1-\alpha)\%$ confidence limits for an individual predicted value CLM computes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p-value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	WHITE	displays heteroscedasticity-consistent standard errors
CLBcomputes $100(1-\alpha)\%$ confidence limits for the parameter estimatesCLIcomputes $100(1-\alpha)\%$ confidence limits for an individual predicted valueCLMcomputes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variableDWcomputes a Durbin-Watson statisticDWPROBcomputes a Durbin-Watson statistic and p -valueINFLUENCEcomputes influence statisticsPcomputes predicted valuesPARTIALdisplays partial regression plots for each regressorPARTIALDATAdisplays partial regression dataRproduces analysis of residualsDisplay Options and Other OptionsALLrequests the following options:ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPXALPHA=sets significance value for confidence and prediction intervals and testsNOPRINTsuppresses display of resultsSIGMA=specifies the true standard deviation of error term for computing CP and BIC	VIF	computes variance-inflation factors
CLBcomputes $100(1-\alpha)\%$ confidence limits for the parameter estimatesCLIcomputes $100(1-\alpha)\%$ confidence limits for an individual predicted valueCLMcomputes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variableDWcomputes a Durbin-Watson statisticDWPROBcomputes a Durbin-Watson statistic and p -valueINFLUENCEcomputes influence statisticsPcomputes predicted valuesPARTIALdisplays partial regression plots for each regressorPARTIALDATAdisplays partial regression dataRproduces analysis of residualsDisplay Options and Other OptionsALLrequests the following options:ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPXALPHA=sets significance value for confidence and prediction intervals and testsNOPRINTsuppresses display of resultsSIGMA=specifies the true standard deviation of error term for computing CP and BIC	Predicted and Resid	dual Values
timates CLI computes 100(1 – α)% confidence limits for an individual predicted value CLM computes 100(1 – α)% confidence limits for the expected value of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p-value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC		
CLMcomputes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variableDWcomputes a Durbin-Watson statisticDWPROBcomputes a Durbin-Watson statistic and p-valueINFLUENCEcomputes influence statisticsPcomputes predicted valuesPARTIALdisplays partial regression plots for each regressorPARTIALDATAdisplays partial regression dataRproduces analysis of residualsDisplay Options and Other OptionsALLrequests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPXALPHA=sets significance value for confidence and prediction intervals and testsNOPRINTsuppresses display of resultsSIGMA=specifies the true standard deviation of error term for computing CP and BIC		•
CLMcomputes $100(1-\alpha)\%$ confidence limits for the expected value of the dependent variableDWcomputes a Durbin-Watson statisticDWPROBcomputes a Durbin-Watson statistic and p-valueINFLUENCEcomputes influence statisticsPcomputes predicted valuesPARTIALdisplays partial regression plots for each regressorPARTIALDATAdisplays partial regression dataRproduces analysis of residualsDisplay Options and Other OptionsALLrequests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPXALPHA=sets significance value for confidence and prediction intervals and testsNOPRINTsuppresses display of resultsSIGMA=specifies the true standard deviation of error term for computing CP and BIC	CLI	computes $100(1-\alpha)\%$ confidence limits for an individual pre-
of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p-value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC		
of the dependent variable DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p-value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	CLM	computes $100(1-\alpha)\%$ confidence limits for the expected value
DW computes a Durbin-Watson statistic DWPROB computes a Durbin-Watson statistic and p-value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC		
DWPROB computes a Durbin-Watson statistic and p-value INFLUENCE computes influence statistics P computes predicted values PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	DW	
PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	DWPROB	-
PARTIAL displays partial regression plots for each regressor PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options:	INFLUENCE	computes influence statistics
PARTIALDATA displays partial regression data R produces analysis of residuals Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	P	computes predicted values
Display Options and Other Options ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	PARTIAL	displays partial regression plots for each regressor
Display Options and Other Options ALL requests the following options:	PARTIALDATA	displays partial regression data
ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	R	produces analysis of residuals
ALL requests the following options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	Display Options and Other Options	
ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC	- · ·	<u>*</u>
PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results SIGMA= specifies the true standard deviation of error term for computing CP and BIC		
SS1, SS2, STB, TOL, VIF, XPX ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT SIGMA= specifies the true standard deviation of error term for computing CP and BIC		
ALPHA= sets significance value for confidence and prediction intervals and tests NOPRINT suppresses display of results specifies the true standard deviation of error term for computing CP and BIC		
and tests NOPRINT SIGMA= and tests suppresses display of results specifies the true standard deviation of error term for computing CP and BIC	ALPHA=	
SIGMA= specifies the true standard deviation of error term for computing CP and BIC		
SIGMA= specifies the true standard deviation of error term for computing CP and BIC	NOPRINT	
CP and BIC		**
		•
	SINGULAR=	sets criterion for checking for singularity

You can specify the following options in the MODEL statement after a slash (/).

ACOV

displays the estimated asymptotic covariance matrix of the estimates under the hypothesis of heteroscedasticity and heteroscedasticity-consistent standard errors of parameter estimates. See the HCCMETHOD= option and the HCC option and the section "Testing for Heteroscedasticity" on page 5569 for more information.

ACOVMETHOD=0,1,2, or 3

See the HCCMETHOD= option.

ADJRSQ

computes R^2 adjusted for degrees of freedom for each model selected (Darlington 1968; Judge et al. 1980).

AIC

outputs Akaike's information criterion for each model selected (Akaike 1969; Judge et al. 1980) to the OUTEST= data set. If SELECTION=ADJRSQ, SELECTION=RSQUARE, or SELECTION=CP is specified, then the AIC statistic is also added to the SubsetSelSummary table.

ALL

requests all these options: ACOV, CLB, CLI, CLM, CORRB, COVB, HCC, I, P, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, and XPX.

ALPHA=number

sets the significance level used for the construction of confidence intervals for the current MODEL statement. The value must be between 0 and 1; the default value of 0.05 results in 95% intervals. This option affects the MODEL options CLB, CLI, and CLM; the OUTPUT statement keywords LCL, LCLM, UCL, and UCLM; the PLOT statement keywords LCL., LCLM., UCL., and UCLM.; and the PLOT statement options CONF and PRED. If you specify this option in the MODEL statement, it takes precedence over the ALPHA= option in the PROC REG statement.

В

is used with the RSQUARE, ADJRSQ, and CP model-selection methods to compute estimated regression coefficients for each model selected.

BEST=n

is used with the RSQUARE, ADJRSQ, and CP model-selection methods. If SELEC-TION=CP or SELECTION=ADJRSQ is specified, the BEST= option specifies the maximum number of subset models to be displayed or output to the OUTEST= data set. For SELEC-TION=RSQUARE, the BEST= option requests the maximum number of subset models for each size.

If the BEST= option is used without the B option (displaying estimated regression coefficients), the variables in each MODEL are listed in order of inclusion instead of the order in which they appear in the MODEL statement.

If the BEST= option is omitted and the number of regressors is less than 11, all possible subsets are evaluated. If the BEST= option is omitted and the number of regressors is greater

than 10, the number of subsets selected is, at most, equal to the number of regressors. A small value of the BEST= option greatly reduces the CPU time required for large problems.

BIC

outputs Sawa's Bayesian information criterion for each model selected (Sawa 1978; Judge et al. 1980) to the OUTEST= data set. If SELECTION=ADJRSQ, SELECTION=RSQUARE, or SELECTION=CP is specified, then the BIC statistic is also added to the SubsetSelSummary table.

CLB

requests the $100(1-\alpha)\%$ upper and lower confidence limits for the parameter estimates. By default, the 95% limits are computed; the ALPHA= option in the PROC REG or MODEL statement can be used to change the α level. If any of the MODEL statement options ACOV, HCC, or WHITE are in effect, then the CLB option also produces heteroscedasticity-consistent $100(1-\alpha)\%$ upper and lower confidence limits for the parameter estimates.

CLI

requests the $100(1-\alpha)\%$ upper and lower confidence limits for an individual predicted value. By default, the 95% limits are computed; the ALPHA= option in the PROC REG or MODEL statement can be used to change the α level. The confidence limits reflect variation in the error, as well as variation in the parameter estimates. See the section "Predicted and Residual Values" on page 5525 and Chapter 4, "Introduction to Regression Procedures," for more information.

CLM

displays the $100(1-\alpha)\%$ upper and lower confidence limits for the expected value of the dependent variable (mean) for each observation. By default, the 95% limits are computed; the ALPHA= in the PROC REG or MODEL statement can be used to change the α level. This is not a prediction interval (see the CLI option) because it takes into account only the variation in the parameter estimates, not the variation in the error term. See the section "Predicted and Residual Values" on page 5525 and Chapter 4, "Introduction to Regression Procedures," for more information.

COLLIN

requests a detailed analysis of collinearity among the regressors. This includes eigenvalues, condition indices, and decomposition of the variances of the estimates with respect to each eigenvalue. See the section "Collinearity Diagnostics" on page 5549.

COLLINOINT

requests the same analysis as the COLLIN option with the intercept variable adjusted out rather than included in the diagnostics. See the section "Collinearity Diagnostics" on page 5549.

CORRB

displays the correlation matrix of the estimates. This is the $(X'X)^{-1}$ matrix scaled to unit diagonals.

COVB

displays the estimated covariance matrix of the estimates. This matrix is $(\mathbf{X}'\mathbf{X})^{-1}s^2$, where s^2 is the estimated mean squared error.

CP

outputs Mallows' C_p statistic for each model selected (Mallows 1973; Hocking 1976) to the OUTEST= data set. See the section "Criteria Used in Model-Selection Methods" on page 5520 for a discussion of the use of C_p . If SELECTION=ADJRSQ, SELECTION=RSQUARE, or SELECTION=CP is specified, then the C_p statistic is also added to the SubsetSelSummary table.

DETAILS

DETAILS=name

specifies the level of detail produced when the BACKWARD, FORWARD, or STEPWISE method is used, where *name* can be ALL, STEPS, or SUMMARY. The DETAILS or DETAILS=ALL option produces entry and removal statistics for each variable in the model building process, ANOVA and parameter estimates at each step, and a selection summary table. The option DETAILS=STEPS provides the step information and summary table. The option DETAILS=SUMMARY produces only the summary table. The default if the DETAILS option is omitted is DETAILS=STEPS.

DW

calculates a Durbin-Watson statistic to test whether or not the errors have first-order autocorrelation. (This test is appropriate only for time series data.) Note that your data should be sorted by the date/time ID variable before you use this option. The sample autocorrelation of the residuals is also produced. See the section "Autocorrelation in Time Series Data" on page 5575.

DWPROB

calculates a Durbin-Watson statistic and a *p*-value to test whether or not the errors have first-order autocorrelation. Note that it is not necessary to specify the DW option if the DWPROB option is specified. (This test is appropriate only for time series data.) Note that your data should be sorted by the date/time ID variable before you use this option. The sample autocorrelation of the residuals is also produced. See the section "Autocorrelation in Time Series Data" on page 5575.

EDF

outputs the number of regressors in the model excluding and including the intercept, the error degrees of freedom, and the model R^2 to the OUTEST= data set.

GMSEP

outputs the estimated mean square error of prediction assuming that both independent and dependent variables are multivariate normal (Stein 1960; Darlington 1968) to the OUTEST= data set. (Note that Hocking's formula (1976, eq. 4.20) contains a misprint: "n-1" should read "n-2.") If SELECTION=ADJRSQ, SELECTION=RSQUARE, or SELECTION=CP is specified, then the GMSEP statistic is also added to the SubsetSelSummary table.

GROUPNAMES='name1' 'name2' ...

provides names for variable groups. This option is available only in the BACKWARD, FOR-WARD, and STEPWISE methods. The group name can be up to 32 characters. Subsets of independent variables listed in the MODEL statement can be designated as variable groups. This is done by enclosing the appropriate variables in braces. Variables in the same group are entered into or removed from the regression model at the same time. However, if the

tolerance of any variable (see the TOL option on page 5474) in a group is less than the setting of the SINGULAR= option, then the variable is not entered into the model with the rest of its group. If the GROUPNAMES= option is not used, then the names GROUP1, GROUP2, ..., GROUPn are assigned to groups encountered in the MODEL statement. Variables not enclosed by braces are used as groups of a single variable.

For example:

```
model y={x1 x2} x3 / selection=stepwise
    groupnames='x1 x2' 'x3';

Another example:

model y={ht wgt age} bodyfat / selection=forward
    groupnames='htwgtage' 'bodyfat';
```

HCC

requests heteroscedasticity-consistent standard errors of the parameter estimates. You can use the HCCMETHOD= option to specify the method used to compute the heteroscedasticity-consistent covariance matrix.

HCCMETHOD=0,1,2, or 3

specifies the method used to obtain a heteroscedasticity-consistent covariance matrix for use with the ACOV, HCC, or WHITE option in the MODEL statement and for heteroscedasticity-consistent tests with the TEST statement. The default is HCCMETHOD=0. See the section "Testing for Heteroscedasticity" on page 5569 for details.

ı

displays the $(X'X)^{-1}$ matrix. The inverse of the crossproducts matrix is bordered by the parameter estimates and SSE matrices.

INCLUDE=n

forces the first *n* independent variables listed in the MODEL statement to be included in all models. The selection methods are performed on the other variables in the MODEL statement. The INCLUDE= option is not available with SELECTION=NONE.

INFLUENCE

requests a detailed analysis of the influence of each observation on the estimates and the predicted values. See the section "Influence Statistics" on page 5553 for details.

JP

outputs J_p , the estimated mean square error of prediction for each model selected assuming that the values of the regressors are fixed and that the model is correct to the OUTEST= data set. The J_p statistic is also called the final prediction error (FPE) by Akaike (Nicholson 1948; Lord 1950; Mallows 1967; Darlington 1968; Rothman 1968; Akaike 1969; Hocking 1976; Judge et al. 1980). If SELECTION=ADJRSQ, SELECTION=RSQUARE, or SELECTION=CP is specified, then the J_p statistic is also added to the SubsetSelSummary table.

LACKFIT

performs a lack-of-fit test. See the section "Testing for Lack of Fit" on page 5570 for more information. Refer to Draper and Smith (1981) for a discussion of lack-of-fit tests.

MSE

computes the mean square error for each model selected (Darlington 1968).

MAXSTEP=n

specifies the maximum number of steps that are done when SELECTION=FORWARD, SE-LECTION=BACKWARD, or SELECTION=STEPWISE is used. The default value is the number of independent variables in the model for the FORWARD and BACKWARD methods and three times this number for the stepwise method.

NOINT

suppresses the intercept term that is otherwise included in the model.

NOPRINT

suppresses the normal display of regression results. Note that this option temporarily disables the Output Delivery System (ODS); see Chapter 20, "Using the Output Delivery System," for more information.

OUTSEB

outputs the standard errors of the parameter estimates to the OUTEST= data set. The value SEB for the variable _TYPE_ identifies the standard errors. If the RIDGE= or PCOMIT= option is specified, additional observations are included and identified by the values RIDGESEB and IPCSEB, respectively, for the variable _TYPE_. The standard errors for ridge regression estimates and incomplete principal components (IPC) estimates are limited in their usefulness because these estimates are biased. This option is available for all model-selection methods except RSQUARE, ADJRSQ, and CP.

OUTSTB

outputs the standardized parameter estimates as well as the usual estimates to the OUTEST= data set when the RIDGE= or PCOMIT= option is specified. The values RIDGESTB and IPCSTB for the variable _TYPE_ identify ridge regression estimates and IPC estimates, respectively.

OUTVIF

outputs the variance inflation factors (VIF) to the OUTEST= data set when the RIDGE= or PCOMIT= option is specified. The factors are the diagonal elements of the inverse of the correlation matrix of regressors as adjusted by ridge regression or IPC analysis. These observations are identified in the output data set by the values RIDGEVIF and IPCVIF for the variable _TYPE_.

Ρ

calculates predicted values from the input data and the estimated model. The display includes the observation number, the ID variable (if one is specified), the actual and predicted values, and the residual. If the CLI, CLM, or R option is specified, the P option is unnecessary. See the section "Predicted and Residual Values" on page 5525 for more information.

PARTIAL

requests partial regression leverage plots for each regressor. You can use the PARTIALDATA option to obtain a tabular display of the partial regression leverage data. If ODS Graphics is in effect (see the section "ODS Graphics" on page 5583), then these partial plots are produced

in panels with up to six plots per panel. See the section "Influence Statistics" on page 5553 for more information.

PARTIAL DATA

requests partial regression leverage data for each regressor. You can request partial regression leverage plots of these data with the PARTIAL option. See the section "Influence Statistics" on page 5553 for more information.

PARTIALR2 < (< TESTS > < SEQTESTS >) >

See the SCORR1 option.

PC

outputs Amemiya's prediction criterion for each model selected (Amemiya 1976; Judge et al. 1980) to the OUTEST= data set. If SELECTION=ADJRSQ, SELECTION=RSQUARE, or SELECTION=CP is specified, then the PC statistic is also added to the SubsetSelSummary table.

PCOMIT=list

requests an IPC analysis for each value m in the list. The procedure computes parameter estimates by using all but the last m principal components. Each value of m produces a set of IPC estimates, which is output to the OUTEST= data set. The values of m are saved by the variable _PCOMIT_, and the value of the variable _TYPE_ is set to IPC to identify the estimates. Only nonnegative integers can be specified with the PCOMIT= option.

If you specify the PCOMIT= option, RESTRICT statements are ignored. The PCOMIT= option is ignored if you use the SELECTION= option in the MODEL statement.

PCORR1

displays the squared partial correlation coefficients computed using Type I sum of squares (SS). This is calculated as SS/(SS+SSE), where SSE is the error sum of squares.

PCORR2

displays the squared partial correlation coefficients computed using Type II sums of squares. These are calculated the same way as with the PCORR1 option, except that Type II SS are used instead of Type I SS.

PRESS

outputs the PRESS statistic to the OUTEST= data set. The values of this statistic are saved in the variable _PRESS_. This option is available for all model-selection methods except RSQUARE, ADJRSQ, and CP.

R

requests an analysis of the residuals. The results include everything requested by the P option plus the standard errors of the mean predicted and residual values, the studentized residual, and Cook's D statistic to measure the influence of each observation on the parameter estimates. See the section "Predicted and Residual Values" on page 5525 for more information.

RIDGE=list

requests a ridge regression analysis and specifies the values of the ridge constant k (see the section "Computations for Ridge Regression and IPC Analysis" on page 5577). Each value

of k produces a set of ridge regression estimates that are placed in the OUTEST= data set. The values of k are saved by the variable _RIDGE_, and the value of the variable _TYPE_ is set to RIDGE to identify the estimates.

Only nonnegative numbers can be specified with the RIDGE= option. Example 73.5 illustrates this option.

If you specify the RIDGE= option, RESTRICT statements are ignored. The RIDGE= option is ignored if you use the SELECTION= option in the MODEL statement.

RMSE

displays the root mean square error for each model selected.

RSQUARE

has the same effect as the EDF option.

SBC

outputs the SBC statistic for each model selected (Schwarz 1978; Judge et al. 1980) to the OUTEST= data set. If SELECTION=ADJRSQ, SELECTION=RSQUARE, or SELECTION=CP is specified, then the SBC statistic is also added to the SubsetSelSummary table.

SCORR1 < (< TESTS > < SEQTESTS >) >

displays the squared semipartial correlation coefficients computed using Type I sums of squares. This is calculated as SS/SST, where SST is the corrected total SS. If the NOINT option is used, the uncorrected total SS is used in the denominator. The optional arguments TESTS and SEQTESTS request are sequentially added to a model. The *F*-test values are computed as the Type I sum of squares for the variable in question divided by a mean square error. If you specify the TESTS option, the denominator MSE is the residual mean square for the full model specified in the MODEL statement. If you specify the SEQTESTS option, the denominator MSE is the residual mean square for the model containing all the independent variables that have been added to the model up to and including the variable in question. The TESTS and SEQTESTS options are not supported if you specify model selection methods or the RIDGE or PCOMIT options. Note that the PARTIALR2 option is a synonym for the SCORR1 option.

SCORR2 < (TESTS)>

displays the squared semipartial correlation coefficients computed using Type II sums of squares. These are calculated the same way as with the SCORR1 option, except that Type II SS are used instead of Type I SS. The optional TEST argument requests F tests and p-values as variables are sequentially added to a model. The F-test values are computed as the Type II sum of squares for the variable in question divided by the residual mean square for the full model specified in the MODEL statement. The TESTS option is not supported if you specify model selection methods or the RIDGE or PCOMIT options.

SELECTION=name

specifies the method used to select the model, where *name* can be FORWARD (or F), BACK-WARD (or B), STEPWISE, MAXR, MINR, RSQUARE, ADJRSQ, CP, or NONE (use the full model). The default method is NONE. See the section "Model-Selection Methods" on page 5517 for a description of each method.

SEQB

produces a sequence of parameter estimates as each variable is entered into the model. This is displayed as a matrix where each row is a set of parameter estimates.

SIGMA=n

specifies the true standard deviation of the error term to be used in computing the CP and BIC statistics. If the SIGMA= option is not specified, an estimate from the full model is used. This option is available in the RSQUARE, ADJRSQ, and CP model-selection methods only.

SINGULAR=n

tunes the mechanism used to check for singularities. If you specify this option in the MODEL statement, it takes precedence over the SINGULAR= option in the PROC REG statement. The default value is machine dependent but is approximately 1E-7 on most machines. This option is rarely needed. Singularity checking is described in the section "Computational Methods" on page 5578.

SLENTRY=value

SLE=value

specifies the significance level for entry into the model used in the FORWARD and STEP-WISE methods. The defaults are 0.50 for FORWARD and 0.15 for STEPWISE.

SLSTAY=value

SLS=value

specifies the significance level for staying in the model for the BACKWARD and STEPWISE methods. The defaults are 0.10 for BACKWARD and 0.15 for STEPWISE.

SP

outputs the S_p statistic for each model selected (Hocking 1976) to the OUTEST= data set. If SELECTION=ADJRSQ, SELECTION=RSQUARE, or SELECTION=CP is specified, then the SP statistic is also added to the SubsetSelSummary table.

SPEC

performs a test that the first and second moments of the model are correctly specified. See the section "Testing for Heteroscedasticity" on page 5569 for more information.

SS1

displays the sequential sums of squares (Type I SS) along with the parameter estimates for each term in the model. See Chapter 15, "The Four Types of Estimable Functions," for more information about the different types of sums of squares.

SS2

displays the partial sums of squares (Type II SS) along with the parameter estimates for each term in the model. See the SS1 option also.

SSE

computes the error sum of squares for each model selected.

START=s

is used to begin the comparing-and-switching process in the MAXR, MINR, and STEPWISE methods for a model containing the first *s* independent variables in the MODEL statement, where *s* is the START value. For these methods, the default is START=0.

For the RSQUARE, ADJRSQ, and CP methods, START=*s* specifies the smallest number of regressors to be reported in a subset model. For these methods, the default is START=1.

The START= option cannot be used with model-selection methods other than the six described here.

STB

produces standardized regression coefficients. A standardized regression coefficient is computed by dividing a parameter estimate by the ratio of the sample standard deviation of the dependent variable to the sample standard deviation of the regressor.

STOP=s

causes PROC REG to stop when it has found the "best" *s*-variable model, where *s* is the STOP value. For the RSQUARE, ADJRSQ, and CP methods, STOP=*s* specifies the largest number of regressors to be reported in a subset model. For the MAXR and MINR methods, STOP=*s* specifies the largest number of regressors to be included in the model.

The default setting for the STOP= option is the number of variables in the MODEL statement. This option can be used only with the MAXR, MINR, RSQUARE, ADJRSQ, and CP methods.

TOL

produces tolerance values for the estimates. Tolerance for a variable is defined as $1 - R^2$, where R^2 is obtained from the regression of the variable on all other regressors in the model. See the section "Collinearity Diagnostics" on page 5549 for more details.

VIF

produces variance inflation factors with the parameter estimates. Variance inflation is the reciprocal of tolerance. See the section "Collinearity Diagnostics" on page 5549 for more detail.

WHITE

See the HCC option.

XPX

displays the X'X crossproducts matrix for the model. The crossproducts matrix is bordered by the X'Y and Y'Y matrices.

MTEST Statement

```
< label: > MTEST < equation < , ..., equation >> < / options > ;
```

where each *equation* is a linear function composed of coefficients and variable names. The *label* is optional.

The MTEST statement is used to test hypotheses in multivariate regression models where there are several dependent variables fit to the same regressors. If no equations or options are specified, the MTEST statement tests the hypothesis that all estimated parameters except the intercept are zero.

The hypotheses that can be tested with the MTEST statement are of the form

$$(\mathbf{L}\boldsymbol{\beta} - \mathbf{c}\mathbf{j})\mathbf{M} = 0$$

where **L** is a linear function on the regressor side, β is a matrix of parameters, **c** is a column vector of constants, **j** is a row vector of ones, and **M** is a linear function on the dependent side. The special case where the constants are zero is

$$L\beta M = 0$$

See the section "Multivariate Tests" on page 5571 for more details.

Each linear function extends across either the regressor variables or the dependent variables. If the equation is across the dependent variables, then the constant term, if specified, must be zero. The equations for the regressor variables form the L matrix and c vector in the preceding formula; the equations for dependent variables form the M matrix. If no equations for the dependent variables are given, PROC REG uses an identity matrix for M, testing the same hypothesis across all dependent variables. If no equations for the regressor variables are given, PROC REG forms a linear function corresponding to a test that all the nonintercept parameters are zero.

As an example, consider the following statements:

```
model y1 y2 y3=x1 x2 x3;
mtest x1,x2;
mtest y1-y2, y2 -y3, x1;
mtest y1-y2;
```

The first MTEST statement tests the hypothesis that the X1 and X2 parameters are zero for Y1, Y2, and Y3. In addition, the second MTEST statement tests the hypothesis that the X1 parameter is the same for all three dependent variables. For the same model, the third MTEST statement tests the hypothesis that all parameters except the intercept are the same for dependent variables Y1 and Y2.

You can specify the following options in the MTEST statement:

CANPRINT

displays the canonical correlations for the hypothesis combinations and the dependent variable combinations. If you specify

```
mtest / canprint;
```

the canonical correlations between the regressors and the dependent variables are displayed.

DETAILS

displays the M matrix and various intermediate calculations.

MSTAT=FAPPROX

MSTAT=EXACT

specifies the method of evaluating the multivariate test statistics. The default is MSTAT=FAPPROX, which specifies that the multivariate tests are evaluated by using the usual approximations based on the *F* distribution, as discussed in the "Multivariate Tests" section in Chapter 4, "Introduction to Regression Procedures." Alternatively, you can specify MSTAT=EXACT to compute exact *p*-values for three of the four tests (Wilks' lambda, the Hotelling-Lawley trace, and Roy's greatest root) and an improved *F* approximation for the fourth (Pillai's trace). While MSTAT=EXACT provides better control of the significance probability for the tests, especially for Roy's greatest root, computations for the exact *p*-values can be appreciably more demanding, and are in fact infeasible for large problems (many dependent variables). Thus, although MSTAT=EXACT is more accurate for most data, it is not the default method.

PRINT

displays the **H** and **E** matrices.

OUTPUT Statement

OUTPUT < **OUT=**SAS-data-set >< keyword=names> < ...keyword=names> ;

The OUTPUT statement creates a new SAS data set that saves diagnostic measures calculated after fitting the model. The OUTPUT statement refers to the most recent MODEL statement. At least one *keyword=names* specification is required.

All the variables in the original data set are included in the new data set, along with variables created in the OUTPUT statement. These new variables contain the values of a variety of statistics and diagnostic measures that are calculated for each observation in the data set. If you want to create a permanent SAS data set, you must specify a two-level name (for example, *libref.data-set-name*).

For more information about permanent SAS data sets, refer to the section "SAS Files" in SAS Language Reference: Concepts.

The OUTPUT statement cannot be used when a TYPE=CORR, TYPE=COV, or TYPE=SSCP data set is used as the input data set for PROC REG. See the section "Input Data Sets" on page 5502 for more details.

The statistics created in the OUTPUT statement are described in this section. More details are given in the section "Predicted and Residual Values" on page 5525 and the section "Influence Statistics" on page 5553. Also see Chapter 4, "Introduction to Regression Procedures," for definitions of the statistics available from the REG procedure.

You can specify the following options in the OUTPUT statement:

OUT=SAS data set

gives the name of the new data set. By default, the procedure uses the DATAn convention to name the new data set.

kevword=names

specifies the statistics to include in the output data set and names the new variables that contain the statistics. Specify a keyword for each desired statistic (see the following list of keywords), an equal sign, and the variable or variables to contain the statistic.

In the output data set, the first variable listed after a keyword in the OUTPUT statement contains that statistic for the first dependent variable listed in the MODEL statement; the second variable contains the statistic for the second dependent variable in the MODEL statement, and so on. The list of variables following the equal sign can be shorter than the list of dependent variables in the MODEL statement. In this case, the procedure creates the new names in order of the dependent variables in the MODEL statement.

For example, the following SAS statements create an output data set named b:

```
proc reg data=a;
  model y z=x1 x2;
  output out=b
     p=yhat zhat
    r=yresid zresid;
run;
```

In addition to the variables in the input data set, b contains the following variables:

- yhat, with values that are predicted values of the dependent variable y
- zhat, with values that are predicted values of the dependent variable z
- yresid, with values that are the residual values of y
- zresid, with values that are the residual values of z

You can specify the following keywords in the OUTPUT statement. See the section "Model Fit and Diagnostic Statistics" on page 5551 for computational formulas.

Table 73.5 Keywords for OUTPUT Statement

Keyword	Description
COOKD=names	Cook's D influence statistic
COVRATIO=names	standard influence of observation on covariance of betas, as
	discussed in the section "Influence Statistics" on page 5553
DFFITS=names	standard influence of observation on predicted value
H= <i>names</i>	leverage, $x_i(\mathbf{X}'\mathbf{X})^{-1}x_i'$
LCL=names	lower bound of a $100(1-\alpha)\%$ confidence interval for an
	individual prediction. This includes the variance of the
	error, as well as the variance of the parameter estimates.
LCLM=names	lower bound of a $100(1-\alpha)\%$ confidence interval for the
	expected value (mean) of the dependent variable
PREDICTED P=names	predicted values
PRESS=names	<i>i</i> th residual divided by $(1 - h)$, where h is the leverage,
	and where the model has been refit without the i th
	observation
RESIDUAL R=names	residuals, calculated as ACTUAL minus PREDICTED

Table 73.5 continued

Keyword	Description
RSTUDENT=names	a studentized residual with the current observation deleted
STDI=names	standard error of the individual predicted value
STDP=names	standard error of the mean predicted value
STDR=names	standard error of the residual
STUDENT=names	studentized residuals, which are the residuals divided by their standard errors
UCL=names	upper bound of a $100(1 - \alpha)\%$ confidence interval for an individual prediction
UCLM=names	upper bound of a $100(1-\alpha)\%$ confidence interval for the expected value (mean) of the dependent variable

PAINT Statement

PAINT < condition | ALLOBS > < / options > ;
PAINT < STATUS | UNDO > ;

The PAINT statement selects observations to be *painted* or highlighted in a scatter plot on line printer output; the PAINT statement is ignored if the LINEPRINTER option is not specified in the PROC REG statement.

All observations that satisfy *condition* are painted using some specific symbol. The PAINT statement does not generate a scatter plot and must be followed by a PLOT statement, which does generate a scatter plot. Several PAINT statements can be used before a PLOT statement, and all prior PAINT statement requests are applied to all later PLOT statements.

The PAINT statement lists the observation numbers of the observations selected, the total number of observations selected, and the plotting symbol used to paint the points.

On a plot, paint symbols take precedence over all other symbols. If any position contains more than one painted point, the paint symbol for the observation plotted last is used.

The PAINT statement cannot be used when a TYPE=CORR, TYPE=COV, or TYPE=SSCP data set is used as the input data set for PROC REG. Also, the PAINT statement cannot be used for models with more than one dependent variable. Note that the syntax for the PAINT statement is the same as the syntax for the REWEIGHT statement.

For detailed examples of painting scatter plots, see the section "Painting Scatter Plots" on page 5537.

Specifying Condition

Condition is used to select observations to be painted. The syntax of condition is

variable compare value

or

variable compare value logical variable compare value

where

variable is one of the following:

- a variable name in the input data set
- OBS., which is the observation number
- *keyword*., where *keyword* is a keyword for a statistic requested in the OUTPUT statement

compare

is an operator that compares *variable* to *value*. *Compare* can be any one of the following: <, <=, >, >=, =, ^ =. The operators LT, LE, GT, GE, EQ, and NE, respectively, can be used instead of the preceding symbols. Refer to the "Expressions" section in *SAS Language Reference: Concepts* for more information about comparison operators.

value

gives an unformatted value of *variable*. Observations are selected to be painted if they satisfy the condition created by *variable compare value*. *Value* can be a number or a character string. If *value* is a character string, it must be eight characters or less and must be enclosed in quotes. In addition, *value* is case-sensitive. In other words, the statements

```
paint name='henry';
and

paint name='Henry';
are not the same.
```

logical

is one of two logical operators. Either AND or OR can be used. To specify AND, use AND or the symbol &. To specify OR, use OR or the symbol |.

Here are some examples of the *variable compare value* form:

```
paint name='Henry';
paint residual.>=20;
paint obs.=99;
```

Here are some examples of the variable compare value logical variable compare value form:

```
paint name='Henry'|name='Mary';
paint residual.>=20 or residual.<=10;
paint obs.>=11 and residual.<=20;</pre>
```

Using ALLOBS

Instead of specifying *condition*, the ALLOBS option can be used to select all observations. This is most useful when you want to unpaint all observations. For example,

```
paint allobs / reset;
```

resets the symbols for all observations.

Options in the PAINT Statement

The following options can be used when either a condition is specified, the ALLOBS option is specified, or nothing is specified before the slash. If only an option is listed, the option applies to the observations selected in the previous PAINT statement, *not* to the observations selected by reapplying the condition from the previous PAINT statement. For example, in the statements

```
paint r.>0 / symbol='a';
reweight r.>0;
refit;
paint / symbol='b';
```

the second PAINT statement paints only those observations selected in the first PAINT statement. No additional observations are painted even if, after refitting the model, there are new observations that meet the condition in the first PAINT statement.

NOTE: Options are not available when either the UNDO or STATUS option is used.

You can specify the following options after a slash (/).

NOLIST

suppresses the display of the selected observation numbers. If the NOLIST option is not specified, a list of observations selected is written to the log. The list includes the observation numbers and painting symbol used to paint the points. The total number of observations selected to be painted is also shown.

RESET

changes the painting symbol to the current default symbol, effectively unpainting the observations selected. If you set the default symbol by using the SYMBOL= option in the PLOT statement, the RESET option in the PAINT statement changes the painting symbol to the symbol you specified. Otherwise, the default symbol of '1' is used.

SYMBOL='character'

specifies a painting symbol. If the SYMBOL= option is omitted, the painting symbol is either the one used in the most recent PAINT statement or, if there are no previous PAINT statements, the symbol '@'. For example,

```
paint / symbol='#';
```

changes the painting symbol for the observations selected by the most recent PAINT statement to '#'. As another example,

```
paint temp lt 22 / symbol='c';
```

changes the painting symbol to 'c' for all observations with TEMP<22. In general, the numbers 1, 2, ..., 9 and the asterisk are not recommended as painting symbols. These symbols are used as default symbols in the PLOT statement, where they represent the number of replicates at a point. If SYMBOL=" is used, no painting is done in the current plot. If SYMBOL=" is used, observations are painted with a blank and are no longer seen on the plot.

STATUS and UNDO

Instead of specifying *condition* or the ALLOBS option, you can use the STATUS or UNDO option as follows:

STATUS

lists (in the log) the observation number and plotting symbol of all currently painted observations.

UNDO

undoes changes made by the most recent PAINT statement. Observations might be, but are not necessarily, unpainted. For example:

```
paint obs. <=10 / symbol='a';
\Codecomment{...other interactive statements}
paint obs.=1 / symbol='b';
\Codecomment{...other interactive statements}
paint undo;</pre>
```

The last PAINT statement changes the plotting symbol used for observation 1 back to 'a'. If the statement

```
paint / reset;
```

is used instead, observation 1 is unpainted.

PLOT Statement

```
PLOT < yvariable*xvariable> <=symbol> <...yvariable*xvariable> <=symbol> </ options>;
```

The PLOT statement in PROC REG displays scatter plots with *yvariable* on the vertical axis and *xvariable* on the horizontal axis. Line printer plots are generated if the LINEPRINTER option is specified in the PROC REG statement; otherwise, the traditional graphics are created. Points in line printer plots can be marked with *symbols*, while global graphics statements such as GOPTIONS and SYMBOL are used to enhance the traditional graphics. Note that the plots you request by using the PLOT statement are independent of the ODS graphical displays (see the section "ODS Graphics" on page 5583) that are now available in PROC REG.

As with most other interactive statements, the PLOT statement implicitly refits the model. For example, if a PLOT statement is preceded by a REWEIGHT statement, the model is recomputed, and the plot reflects the new model.

If there are multiple MODEL statements preceding a PLOT statement, then the PLOT statement refers to the latest MODEL statement.

The PLOT statement cannot be used when a TYPE=CORR, TYPE=COV, or TYPE=SSCP data set is used as input to PROC REG.

You can specify several PLOT statements for each MODEL statement, and you can specify more than one plot in each PLOT statement.

For detailed examples of using the PLOT statement and its options, see the section "Producing Scatter Plots" on page 5529.

Specifying Yvariables, Xvariables, and Symbol

More than one *yvariable*xvariable* pair can be specified to request multiple plots. The *yvariables* and *xvariables* can be as follows:

- any variables specified in the VAR or MODEL statement before the first RUN statement
- *keyword*., where *keyword* is a regression diagnostic statistic available in the OUTPUT statement (see Table 73.6). For example,

```
plot predicted.*residual.;
```

generates one plot of the predicted values by the residuals for each dependent variable in the MODEL statement. These statistics can also be plotted against any of the variables in the VAR or MODEL statements.

- the keyword OBS. (the observation number), which can be plotted against any of the preceding variables
- the keyword NPP. or NQQ., which can be used with any of the preceding variables to construct normal P-P or Q-Q plots, respectively (see the section "Construction of Q-Q and P-P Plots" on page 5577 and "Traditional Normal Quantile and Normal Probability Plots" on page 5545 for more information)
- keywords for model fit summary statistics available in the OUTEST= data set with _TYPE_= PARMS (see Table 73.6). A SELECTION= method (other than NONE) must be requested in the MODEL statement for these variables to be plotted. If one member of a *yvariable*xvariable* pair is from the OUTEST= data set, the other member must also be from the OUTEST= data set.

The OUTPUT statement and the OUTEST= option are not required when their keywords are specified in the PLOT statement.

The *yvariable* and *xvariable* specifications can be replaced by a set of variables and statistics enclosed in parentheses. When this occurs, all possible combinations of *yvariable* and *xvariable* are generated. For example, the following two statements are equivalent:

```
plot (y1 y2)*(x1 x2);
plot y1*x1 y1*x2 y2*x1 y2*x2;
```

The statement

plot;

is equivalent to respecifying the most recent PLOT statement without any options. However, the line printer options COLLECT, HPLOTS=, SYMBOL=, and VPLOTS=, described in the section "Line Printer Plots" on page 5491, apply across PLOT statements and remain in effect if they have been previously specified.

Options used for the traditional graphics are described in the following section; see "Line Printer Plots" on page 5491 for more information.

Traditional Graphics

The display of traditional graphics is described in the following paragraphs, the options are summarized in Table 73.6 and described in the section "Dictionary of PLOT Statement Options" on page 5487, and the section "Traditional Graphics" on page 5541 contains several examples of the graphics output.

Several line printer statements and options are not supported for the traditional graphics. In particular the PAINT statement is disabled, as are the PLOT statement options CLEAR, COLLECT, HPLOTS=, NOCOLLECT, SYMBOL=, and VPLOTS=. To display more than one plot per page or to collect plots from multiple PLOT statements, use the PROC GREPLAY statement (refer to SAS/GRAPH Software: Reference). Also note that traditional graphics options are not recognized for line printer plots.

The fitted model equation and a label are displayed in the top margin of the plot; this display can be suppressed with the NOMODEL option. If the label is requested but cannot fit on one line, it is not displayed. The equation and label are displayed on one line when possible; if more lines are required, the label is displayed in the first line with the model equation in successive lines. If displaying the entire equation causes the plot to be unacceptably small, the equation is truncated. Table 73.7 lists options to control the display of the equation. The section "Traditional Graphics for Simple Linear Regression" on page 5541 illustrates the display of the model equation.

Four statistics are displayed by default in the right margin: the number of observations, R^2 , the adjusted R^2 , and the root mean square error. (See Figure 73.43.) The display of these statistics can be suppressed with the NOSTAT option. You can specify other options to request the display of various statistics in the right margin; see Table 73.7.

A default reference line at zero is displayed if residuals are plotted. If the dependent variable is plotted against the independent variable in a simple linear regression model, the fitted regression line is displayed by default. (See Figure 73.42.) Default reference lines can be suppressed with the NOLINE option; the lines are not displayed if the OVERLAY option is specified.

Specialized plots are requested with special options. For each coefficient, the RIDGEPLOT option plots the ridge estimates against the ridge values k; see the description of the RIDGEPLOT option in the section "Dictionary of PLOT Statement Options" on page 5487 for more details. The CONF option plots $100(1-\alpha)\%$ confidence intervals for the mean while the PRED option plots $100(1-\alpha)\%$ prediction intervals; see the description of these options in the section "Dictionary of PLOT Statement Options" on page 5487 for more details.

If a SELECTION= method is requested, the fitted model equation and the statistics displayed in the margin correspond to the selected model. For the ADJRSQ and CP methods, the selected model is treated as a submodel of the full model. If a CP.*NP. plot is requested, the CHOCKING= and CMALLOWS= options display model selection reference lines; see the descriptions of these options in the section "Dictionary of PLOT Statement Options" on page 5487 and "Traditional Graphics for Variable Selection" on page 5544 for more details.

PLOT Statement variable Keywords

The following table lists the keywords available as PLOT statement *xvariables* and *yvariables*. All keywords have a trailing dot; for example, "*COOKD*." requests Cook's *D* statistic. Neither the OUTEST= option needs to be specified.

Table 73.6 Keywords for PLOT Statement xvariables

Keyword	Description
Diagnostic Statistics	
COOKD.	Cook's D influence statistics
COVRATIO.	standard influence of observation on covariance of betas
DFFITS.	standard influence of observation on predicted value
H.	leverage
LCL.	lower bound of $100(1 - \alpha)\%$ confidence interval for individual prediction
LCLM.	lower bound of $100(1 - \alpha)\%$ confidence interval for the mean of the dependent variable
PREDICTED.	predicted values
PRED. P.	
PRESS.	residuals from refitting the model with current observation deleted
RESIDUAL. R.	residuals
RSTUDENT.	studentized residuals with the current observation deleted
STDI.	standard error of the individual predicted value
STDP.	standard error of the mean predicted value
STDR.	standard error of the residual
STUDENT.	residuals divided by their standard errors
UCL.	upper bound of $100(1-\alpha)\%$ confidence interval for individual prediction
UCLM.	upper bound of $100(1 - \alpha)\%$ confidence interval for the mean of the dependent variables
Other Keywords Used	with Diagnostic Statistics
NPP.	normal probability-probability plot
NQQ.	normal quantile-quantile plot

Table 73.6 continued

Keyword	Description
OBS.	observation number (cannot plot against OUTEST= statistics)
Model Fit Summary Statistics	
ADJRSQ.	adjusted R-square
AIC.	Akaike's information criterion
BIC.	Sawa's Bayesian information criterion
CP.	Mallows' C_p statistic
EDF.	error degrees of freedom
GMSEP.	estimated MSE of prediction, assuming multivariate normality
IN.	number of regressors in the model not including the intercept
JP.	final prediction error
MSE.	mean squared error
NP.	number of parameters in the model (including the intercept)
PC.	Amemiya's prediction criterion
RMSE.	root MSE
RSQ.	R-square
SBC.	SBC statistic
SP.	SP statistic
SSE.	error sum of squares

Summary of PLOT Statement Graphics Options

The following table lists the PLOT statement *options* by function. These *options* are available unless the LINEPRINTER option is specified in the PROC REG statement. For complete descriptions, see the section "Dictionary of PLOT Statement Options" on page 5487.

Table 73.7 Traditional Graphics Options

0.4	D 14
Option	Description
General Graphics Opt	ions
ANNOTATE=	specifies the annotate data set
SAS-data-set	
CHOCKING=color	requests a reference line for C_p model selection criteria
CMALLOWS=color	requests a reference line for the C_p model selection criterion
CONF	requests plots of $100(1-\alpha)\%$ confidence intervals for the mean
DESCRIPTION=	specifies a description for graphics catalog member
'string'	
NAME='string'	names the plot in the graphics catalog
OVERLAY	overlays plots from the same model
PRED	requests plots of $100(1-\alpha)\%$ prediction intervals for individual
	responses
RIDGEPLOT	requests the ridge trace for ridge regression
Axis and Legend Options	
LEGEND=LEGENDn	specifies LEGEND statement to be used
HAXIS=values	specifies tick mark values for horizontal axis
VAXIS=values	specifies tick mark values for vertical axis

Table 73.7 continued

	D 1.0		
Option	Description		
Reference Line Option	Reference Line Options		
HREF=values	specifies reference lines perpendicular to horizontal axis		
LHREF=linetype	specifies line style for HREF= lines		
LLINE=linetype	specifies line style for lines displayed by default		
LVREF=linetype	specifies line style for VREF= lines		
NOLINE	suppresses display of any default reference line		
VREF=values	specifies reference lines perpendicular to vertical axis		
Color Options			
CAXIS=color	specifies color for axis line and tick marks		
CFRAME=color	specifies color for frame		
CHREF=color	specifies color for HREF= lines		
CLINE=color	specifies color for lines displayed by default		
CTEXT=color	specifies color for text		
CVREF=color	specifies color for VREF= lines		
Options for Displaying	the Fitted Model Equation		
MODELFONT=font	specifies font of model equation and model label		
MODELHT=value	specifies text height of model equation and model label		
MODELLAB='label'	specifies model label		
NOMODEL	suppresses display of the fitted model and the label		
Options for Displaying	Statistics in the Plot Margin		
AIC	displays Akaike's information criterion		
BIC	displays Sawa's Bayesian information criterion		
CP	displays Mallows' C_p statistic		
EDF	displays the error degrees of freedom		
GMSEP	displays the estimated MSE of prediction assuming		
	multivariate normality		
IN	displays the number of regressors in the model not including		
	the intercept		
JP	displays the J_p statistic		
MSE	displays the mean squared error		
NOSTAT	suppresses display of the default statistics: the number of		
	observations, R-square, adjusted R-square, and		
	root mean square error		
NP	displays the number of parameters in the model including the		
	intercept, if any		
PC	displays the PC statistic		
SBC	displays the SBC statistic		
SP	displays the S_p statistic		
SSE	displays the error sum of squares		
STATFONT=font	specifies font of text displayed in the margin		
STATHT=value	specifies height of text displayed in the margin		

Dictionary of PLOT Statement Options

The following entries describe the PLOT statement *options* in detail. Note that these *options* are available unless you specify the LINEPRINTER option in the PROC REG statement.

AIC

displays Akaike's information criterion in the plot margin.

ANNOTATE=SAS-data-set

ANNO=SAS-data-set

specifies an input data set that contains appropriate variables for annotation. This applies only to displays created with the current PLOT statement. Refer to SAS/GRAPH Software: Reference for more information.

BIC

displays Sawa's Bayesian information criterion in the plot margin.

CAXIS=color

CAXES=color

CA=color

specifies the color for the axes, frame, and tick marks.

CFRAME=color

CFR=color

specifies the color for filling the area enclosed by the axes and the frame.

CHOCKING=color

requests reference lines corresponding to the equations $C_p = p$ and $C_p = 2p - p_{full}$, where p_{full} is the number of parameters in the full model (excluding the intercept) and p is the number of parameters in the subset model (including the intercept). The *color* must be specified; the $C_p = p$ line is solid and the $C_p = 2p - p_{full}$ line is dashed. Only PLOT statements of the form PLOT CP.*NP. produce these lines.

For the purpose of parameter estimation, Hocking (1976) suggests selecting a model where $C_p \leq 2p - p_{full}$. For the purpose of prediction, Hocking suggests the criterion $C_p \leq p$. You can request the single reference line $C_p = p$ with the CMALLOWS= option. If, for example, you specify both CHOCKING=RED and CMALLOWS=BLUE, then the $C_p = 2p - p_{full}$ line is red and the $C_p = p$ line is blue (see Figure 73.45).

CHREF=color

CH=color

specifies the color for lines requested with the HREF= option.

CLINE=color

CL=color

specifies the color for lines displayed by default. See the NOLINE option for details.

CMALLOWS=color

requests a $C_p = p$ reference line, where p is the number of parameters (including the intercept) in the subset model. The *color* must be specified; the line is solid. Only PLOT statements of the form PLOT CP.*NP. produce this line.

Mallows (1973) suggests that all subset models with C_p small and near p be considered for further study. See the CHOCKING= option for related model-selection criteria.

CONF

is a keyword used as a shorthand option to request plots that include $(100 - \alpha)\%$ confidence intervals for the mean response (see Figure 73.44). The ALPHA= option in the PROC REG or MODEL statement selects the significance level α , which is 0.05 by default. The CONF option is valid for simple regression models only, and is ignored for plots where confidence intervals are inappropriate. The CONF option replaces the CONF95 option; however, the CONF95 option is still supported when the ALPHA= option is not specified. The OVERLAY option is ignored when the CONF option is specified.

CP

displays Mallows' C_p statistic in the plot margin.

CTEXT=color

CT=color

specifies the color for text including tick mark labels, axis labels, the fitted model label and equation, the statistics displayed in the margin, and legends.

CVREF=color

CV=color

specifies the color for lines requested with the VREF= option.

DESCRIPTION='string'

DESC='string'

specifies a descriptive string, up to 40 characters, that appears in the description field of the PROC GREPLAY master menu.

EDF

displays the error degrees of freedom in the plot margin.

GMSEP

displays the estimated mean square error of prediction in the plot margin. Note that the estimate is calculated under the assumption that both independent and dependent variables have a multivariate normal distribution.

HAXIS=values

HA=values

specifies tick mark values for the horizontal axis.

HREF=values

specifies where reference lines perpendicular to the horizontal axis are to appear.

IN

displays the number of regressors in the model (not including the intercept) in the plot margin.

JP

displays the J_p statistic in the plot margin.

LEGEND=LEGENDn

specifies the LEGEND*n* statement to be used. The LEGEND*n* statement is a global graphics statement; refer to *SAS/GRAPH Software: Reference* for more information.

LHREF=linetype

LH=linetype

specifies the line style for lines requested with the HREF= option. The default *linetype* is 2. Note that LHREF=1 requests a solid line. Refer to *SAS/GRAPH Software: Reference* for a table of available line types.

LLINE=linetype

LL=linetype

specifies the line style for reference lines displayed by default; see the NOLINE option for details. The default *linetype* is 2. Note that LLINE=1 requests a solid line.

LVREF=linetype

LV=linetype

specifies the line style for lines requested with the VREF= option. The default *linetype* is 2. Note that LVREF=1 requests a solid line.

MODELFONT=font

specifies the font used for displaying the fitted model label and the fitted model equation. Refer to SAS/GRAPH Software: Reference for tables of software fonts.

MODELHT=height

specifies the text height for the fitted model label and the fitted model equation.

MODELLAB='label'

specifies the label to be displayed with the fitted model equation. By default, no label is displayed. If the label does not fit on one line, it is not displayed. See the section "Traditional Graphics" on page 5483 for more information.

MSE

displays the mean squared error in the plot margin.

NAME='string'

specifies a descriptive string, up to eight characters, that appears in the name field of the PROC GREPLAY master menu. The default *string* is REG.

NOLINE

suppresses the display of default reference lines. A default reference line at zero is displayed if residuals are plotted. If the dependent variable is plotted against the independent variable in a simple regression model, then the fitted regression line is displayed by default. Default reference lines are not displayed if the OVERLAY option is specified.

NOMODEL

suppresses the display of the fitted model equation.

NOSTAT

suppresses the display of statistics in the plot margin. By default, the number of observations, R-square, adjusted R-square, and root MSE are displayed.

NP

displays the number of regressors in the model including the intercept, if any, in the plot margin.

OVERLAY

overlays all plots specified in the PLOT statement from the same model on one set of axes. The variables for the first plot label the axes. The procedure automatically scales the axes to fit all of the variables unless the HAXIS= or VAXIS= option is used. Default reference lines are not displayed. A default legend is produced; the LEGEND= option can be used to customize the legend.

PC

displays the PC statistic in the plot margin.

PRED

is a keyword used as a shorthand option to request plots that include $(100 - \alpha)\%$ prediction intervals for individual responses (see Figure 73.44). The ALPHA= option in the PROC REG or MODEL statement selects the significance level α , which is 0.05 by default. The PRED option is valid for simple regression models only, and is ignored for plots where prediction intervals are inappropriate. The PRED option replaces the PRED95 option; however, the PRED95 option is still supported when the ALPHA= option is not specified. The OVERLAY option is ignored when the PRED option is specified.

RIDGEPLOT

creates overlaid plots of ridge estimates against ridge values for each coefficient. The points corresponding to the estimates of each coefficient in the plot are connected by lines. For ridge estimates to be computed and plotted, the OUTEST= option must be specified in the PROC REG statement, and the RIDGE=list must be specified in either the PROC REG or MODEL statement.

SBC

displays the SBC statistic in the plot margin.

SP

displays the S_p statistic in the plot margin.

SSE

displays the error sum of squares in the plot margin.

STATFONT=font

specifies the font used for displaying the statistics that appear in the plot margin. Refer to SAS/GRAPH Software: Reference for tables of software fonts.

STATHT=height

specifies the text height of the statistics that appear in the plot margin.

USEALL

specifies that predicted values at data points with missing dependent variable(s) be included on appropriate plots. By default, only points used in constructing the SSCP matrix appear on plots.

VAXIS=values

VA=values

specifies tick mark values for the vertical axis.

VREF=values

specifies where reference lines perpendicular to the vertical axis are to appear.

Line Printer Plots

Line printer plots are requested with the LINEPRINTER option in the PROC REG statement. Points in line printer plots can be marked with *symbols*, which can be specified as a single character enclosed in quotes or the name of any variable in the input data set.

If a character variable is used for the symbol, the first (leftmost) nonblank character in the formatted value of the variable is used as the plotting symbol. If a character in quotes is specified, that character becomes the plotting symbol. If a character is used as the plotting symbol, and if there are different plotting symbols needed at the same point, the symbol '?' is used at that point.

If an unformatted numeric variable is used for the symbol, the symbols '1', '2', ..., '9' are used for variable values 1, 2, ..., 9. For noninteger values, only the integer portion is used as the plotting symbol. For values of 10 or greater, the symbol '*' is used. For negative values, a '?' is used. If a numeric variable is used, and if there is more than one plotting symbol needed at the same point, the sum of the variable values is used at that point. If the sum exceeds 9, the symbol '*' is used.

If a symbol is not specified, the number of replicates at the point is displayed. The symbol '*' is used if there are 10 or more replicates.

If the LINEPRINTER option is used, you can specify the following options in the PLOT statement after a slash (/):

CLEAR

clears any collected scatter plots before plotting begins but does not turn off the COLLECT option. Use this option when you want to begin a new collection with the plots in the current PLOT statement. For more information about collecting plots, see the COLLECT and NOCOLLECT options in this section.

COLLECT

specifies that plots begin to be collected from one PLOT statement to the next and that subsequent plots show an overlay of all collected plots. This option enables you to overlay plots before and after changes to the model or to the data used to fit the model. Plots collected before changes are unaffected by the changes and can be overlaid on later plots. You can request more than one plot with this option, and you do not need to request the same number of plots in subsequent PLOT statements. If you specify an unequal number of plots, plots in corresponding positions are overlaid. For example, the statements

```
plot residual.*predicted. y*x / collect;
run;
produce two plots. If these statements are then followed by
   plot residual.*x;
run;
```

two plots are again produced. The first plot shows residual against X values overlaid on residual against predicted values. The second plot is the same as that produced by the first PLOT statement.

Axes are scaled for the first plot or plots collected. The axes are not rescaled as more plots are collected.

Once specified, the COLLECT option remains in effect until the NOCOLLECT option is specified.

HPLOTS=number

sets the number of scatter plots that can be displayed across the page. The procedure begins with one plot per page. The value of the HPLOTS= option remains in effect until you change it in a later PLOT statement. See the VPLOTS= option for an example.

NOCOLLECT

specifies that the collection of scatter plots ends after adding the plots in the current PLOT statement. PROC REG starts with the NOCOLLECT option in effect. After you specify the NOCOLLECT option, any following PLOT statement produces a new plot that contains only the plots requested by that PLOT statement.

For more information, see the COLLECT option.

OVERLAY

enables requested scatter plots to be superimposed. The axes are scaled so that points on all plots are shown. If the HPLOTS= or VPLOTS= option is set to more than one, the overlaid plot occupies the first position on the page. The OVERLAY option is similar to the COLLECT option in that both options produce superimposed plots. However, OVERLAY superimposes only the plots in the associated PLOT statement; COLLECT superimposes plots across PLOT statements. The OVERLAY option can be used when the COLLECT option is in effect.

SYMBOL='character'

changes the default plotting symbol used for all scatter plots produced in the current and in subsequent PLOT statements. Both SYMBOL=' and SYMBOL=' are allowed.

If the SYMBOL= option has not been specified, the default symbol is '1' for positions with one observation, '2' for positions with two observations, and so on. For positions with more than 9 observations, '*' is used. The SYMBOL= option (or a plotting symbol) is needed to avoid any confusion caused by this default convention. Specifying a particular symbol is especially important when either the OVERLAY or COLLECT option is being used.

If you specify the SYMBOL= option and use a number for *character*, that number is used for all points in the plot. For example, the statement

```
plot y*x / symbol='1';
```

produces a plot with the symbol '1' used for all points.

If you specify a plotting symbol and the SYMBOL= option, the plotting symbol overrides the SYMBOL= option. For example, in the statements

```
plot y*x y*v='.' / symbol='*';
```

the symbol used for the plot of Y against X is '*', and a '.' is used for the plot of Y against V.

If a paint symbol is defined with a PAINT statement, the paint symbol takes precedence over both the SYMBOL= option and the default plotting symbol for the PLOT statement.

VPLOTS=number

sets the number of scatter plots that can be displayed down the page. The procedure begins with one plot per page. The value of the VPLOTS= option remains in effect until you change it in a later PLOT statement.

For example, to specify a total of six plots per page, with two rows of three plots, use the HPLOTS= and VPLOTS= options as follows:

PRINT Statement

```
PRINT < options > < ANOVA > < MODELDATA > ;
```

The PRINT statement enables you to interactively display the results of MODEL statement options, produce an ANOVA table, display the data for variables used in the current model, or redisplay the options specified in a MODEL or a previous PRINT statement. In addition, like most other interactive statements in PROC REG, the PRINT statement implicitly refits the model; thus, effects of REWEIGHT statements are seen in the resulting tables. If ODS Graphics is in effect (see the section "ODS Graphics" on page 5583), the PRINT statement also requests the use of the ODS graphical displays associated with the current model.

The following specifications can appear in the PRINT statement:

options

interactively displays the results of MODEL statement options, where *options* is one or more of the following: ACOV, ALL, CLI, CLM, COLLIN, COLLINOINT, CORRB, COVB, DW, I, INFLUENCE, P, PARTIAL, PCORR1, PCORR2, R, SCORR1, SCORR2, SEQB, SPEC, SS1, SS2, STB, TOL, VIF, or XPX. See the section "MODEL Statement" on page 5463 for a description of these options.

ANOVA

produces the ANOVA table associated with the current model. This is either the model specified in the last MODEL statement or the model that incorporates changes made by ADD, DELETE, or REWEIGHT statements after the last MODEL statement.

MODELDATA

displays the data for variables used in the current model.

Use the statement

```
print;
```

to reprint options in the most recently specified PRINT or MODEL statement.

Options that require original data values, such as R or INFLUENCE, cannot be used when a TYPE=CORR, TYPE=COV, or TYPE=SSCP data set is used as the input data set to PROC REG. See the section "Input Data Sets" on page 5502 for more detail.

REFIT Statement

REFIT:

The REFIT statement causes the current model and corresponding statistics to be recomputed immediately. No output is generated by this statement. The REFIT statement is needed after one or more REWEIGHT statements to cause them to take effect before subsequent PAINT or REWEIGHT statements. This is sometimes necessary when you are using statistical conditions in REWEIGHT statements. For example, consider the following statements:

```
paint student.>2;
plot student.*p.;
reweight student.>2;
refit;
paint student.>2;
plot student.*p.;
```

The second PAINT statement paints any additional observations that meet the condition after deleting observations and refitting the model. The REFIT statement is used because the REWEIGHT statement does not cause the model to be recomputed. In this particular example, the same effect could be achieved by replacing the REFIT statement with a PLOT statement.

Most interactive statements can be used to implicitly refit the model; any plots or statistics produced by these statements reflect changes made to the model and changes made to the data used to compute the model. The two exceptions are the PAINT and REWEIGHT statements, which do not cause the model to be recomputed.

RESTRICT Statement

```
RESTRICT equation < , . . . , equation > ;
```

A RESTRICT statement is used to place restrictions on the parameter estimates in the MODEL preceding it. More than one RESTRICT statement can follow each MODEL statement. Each RE-

STRICT statement replaces any previous RESTRICT statement. To lift all restrictions on a model, submit a new MODEL statement. If there are several restrictions, separate them with commas. The statement

```
restrict equation1=equation2=equation3;
```

is equivalent to imposing the two restrictions

```
restrict equation1=equation2;
restrict equation2=equation3;
```

Each restriction is written as a linear equation and can be written as

equation

or

```
equation = equation
```

The form of each equation is

```
c_1 \times variable_1 \pm c_2 \times variable_2 \pm \cdots \pm c_n \times variable_n
```

where the c_i 's are constants and the *variable*_i's are any regressor variables.

When no equal sign appears, the linear combination is set equal to zero. Each variable name mentioned must be a variable in the MODEL statement to which the RESTRICT statement refers. The keyword INTERCEPT can also be used as a variable name, and it refers to the intercept parameter in the regression model.

Note that the parameters associated with the variables are restricted, not the variables themselves. Restrictions should be consistent and not redundant.

Examples of valid RESTRICT statements include the following:

```
restrict x1;
restrict a+b=1;
restrict a=b=c;
restrict a=b, b=c;
restrict 2*f=g+h, intercept+f=0;
restrict f=g=h=intercept;
```

The third and fourth statements in this list produce identical restrictions. You cannot specify

```
restrict f-g=0,
    f-intercept=0,
    g-intercept=1;
```

because the three restrictions are not consistent. If these restrictions are included in a RESTRICT statement, one of the restrict parameters is set to zero and has zero degrees of freedom, indicating that PROC REG is unable to apply a restriction.

The restrictions usually operate even if the model is not of full rank. Check to ensure that DF = -1 for each restriction. In addition, the model DF should decrease by 1 for each restriction.

The parameter estimates are those that minimize the quadratic criterion (SSE) subject to the restrictions. If a restriction cannot be applied, its parameter value and degrees of freedom are listed as zero.

The method used for restricting the parameter estimates is to introduce a Lagrangian parameter for each restriction (Pringle and Rayner 1971). The estimates of these parameters are displayed with test statistics. Note that the t statistic reported for the Lagrangian parameters does not follow a Student's t distribution, but its square follows a beta distribution (LaMotte 1994). The p-value for these parameters is computed using the beta distribution.

The Lagrangian parameter γ measures the sensitivity of the SSE to the restriction constant. If the restriction constant is changed by a small amount ϵ , the SSE is changed by $2\gamma\epsilon$. The t ratio tests the significance of the restrictions. If γ is zero, the restricted estimates are the same as the unrestricted estimates, and a change in the restriction constant in either direction increases the SSE.

RESTRICT statements are ignored if the PCOMIT= or RIDGE= option is specified in the PROC REG statement.

REWEIGHT Statement

```
REWEIGHT < condition | ALLOBS > < / options > ;
REWEIGHT < STATUS | UNDO > ;
```

The REWEIGHT statement interactively changes the weights of observations that are used in computing the regression equation. The REWEIGHT statement can change observation weights, or set them to zero, which causes selected observations to be excluded from the analysis. When a REWEIGHT statement sets observation weights to zero, the observations are not deleted from the data set. More than one REWEIGHT statement can be used. The requests from all REWEIGHT statements are applied to the subsequent statements. Each use of the REWEIGHT statement modifies the MODEL label.

The model and corresponding statistics are not recomputed after a REWEIGHT statement. For example, consider the following statements:

```
reweight r.>0;
reweight r.>0;
```

The second REWEIGHT statement does not exclude any additional observations since the model is not recomputed after the first REWEIGHT statement. Either use a REFIT statement to explicitly refit the model, or implicitly refit the model by following the REWEIGHT statement with any other interactive statement except a PAINT statement or another REWEIGHT statement.

The REWEIGHT statement cannot be used if a TYPE=CORR, TYPE=COV, or TYPE=SSCP data set is used as an input data set to PROC REG. Note that the syntax used in the REWEIGHT statement is the same as the syntax in the PAINT statement.

The syntax of the REWEIGHT statement is described in the following sections.

For detailed examples of using this statement, see the section "Reweighting Observations in an Analysis" on page 5563.

Specifying Condition

Condition is used to find observations to be reweighted. The syntax of condition is

variable compare value

or

variable compare value logical variable compare value

where

variable

is one of the following:

- a variable name in the input data set
- OBS., which is the observation number
- keyword., where keyword is a keyword for a statistic requested in the OUTPUT statement. The keyword specification is applied to all dependent variables in the model.

compare

is an operator that compares *variable* to *value*. *Compare* can be any one of the following: <, <=, >, >=, =, ^ =. The operators LT, LE, GT, GE, EQ, and NE, respectively, can be used instead of the preceding symbols. Refer to the "Expressions" chapter in *SAS Language Reference: Concepts* for more information about comparison operators.

value

gives an unformatted value of *variable*. Observations are selected to be reweighted if they satisfy the condition created by *variable compare value*. *Value* can be a number or a character string. If *value* is a character string, it must be eight characters or less and must be enclosed in quotes. In addition, *value* is case-sensitive. In other words, the following two statements are not the same:

```
reweight name='steve';
reweight name='Steve';
```

logical

is one of two logical operators. Either AND or OR can be used. To specify AND, use AND or the symbol &. To specify OR, use OR or the symbol |.

Here are some examples of the variable compare value form:

```
reweight obs. le 10;
reweight temp=55;
reweight type='new';
```

Here are some example of the variable compare value logical variable compare value form:

```
reweight obs.<=10 and residual.<2;
reweight student.<-2 or student.>2;
reweight name='Mary' | name='Susan';
```

Using ALLOBS

Instead of specifying *condition*, you can use the ALLOBS option to select all observations. This is most useful when you want to restore the original weights of all observations. For example,

```
reweight allobs / reset;
```

resets weights for all observations and uses all observations in the subsequent analysis. Note that reweight allobs;

specifies that all observations be excluded from analysis. Consequently, using ALLOBS is useful only if you also use one of the options discussed in the following section.

Options in the REWEIGHT Statement

The following options can be used when either a condition, ALLOBS, or nothing is specified before the slash. If only an option is listed, the option applies to the observations selected in the previous REWEIGHT statement, not to the observations selected by reapplying the condition from the previous REWEIGHT statement. For example, consider the following statements:

```
reweight r.>0 / weight=0.1;
refit;
reweight;
```

The second REWEIGHT statement excludes from the analysis only those observations selected in the first REWEIGHT statement. No additional observations are excluded even if there are new observations that meet the condition in the first REWEIGHT statement.

NOTE: Options are not available when either the UNDO or STATUS option is used.

NOLIST

suppresses the display of the selected observation numbers. If you omit the NOLIST option, a list of observations selected is written to the log.

RESET

resets the observation weights to their original values as defined by the WEIGHT statement or to WEIGHT=1 if no WEIGHT statement is specified. For example,

```
reweight / reset;
```

resets observation weights to the original weights in the data set. If previous REWEIGHT statements have been submitted, this REWEIGHT statement applies only to the observations selected by the previous REWEIGHT statement. Note that, although the RESET option does reset observation weights to their original values, it does not cause the model and corresponding statistics to be recomputed.

WEIGHT=value

changes observation weights to the specified nonnegative real number. If you omit the WEIGHT= option, the observation weights are set to zero, and observations are excluded from the analysis. For example:

```
reweight name='Alan';
\Codecomment{...other interactive statements}
reweight / weight=0.5;
```

The first REWEIGHT statement changes weights to zero for all observations with name='Alan', effectively deleting these observations. The subsequent analysis does not include these observations. The second REWEIGHT statement applies only to those observations selected by the previous REWEIGHT statement, and it changes the weights to 0.5 for all the observations with NAME='Alan'. Thus, the next analysis includes all original observations; however, those observations with NAME='Alan' have their weights set to 0.5.

STATUS and UNDO

If you omit *condition* and the ALLOBS options, you can specify one of the following options.

STATUS

writes to the log the observation's number and the weight of all reweighted observations. If an observation's weight has been set to zero, it is reported as deleted. However, the observation is not deleted from the data set, only from the analysis.

UNDO

undoes the changes made by the most recent REWEIGHT statement. Weights might be, but are not necessarily, reset. For example, consider the following statements:

```
reweight student.>2 / weight=0.1;
reweight;
reweight undo;
```

The first REWEIGHT statement sets the weights of observations that satisfy the condition to 0.1. The second REWEIGHT statement sets the weights of the same observations to zero. The third REWEIGHT statement undoes the second, changing the weights back to 0.1.

TEST Statement

```
< label: > TEST equation, < , . . . , equation > < / option > ;
```

The TEST statement tests hypotheses about the parameters estimated in the preceding MODEL statement. It has the same syntax as the RESTRICT statement except that it supports an option. Each equation specifies a linear hypothesis to be tested. The rows of the hypothesis are separated by commas.

Variable names must correspond to regressors, and each variable name represents the coefficient of the corresponding variable in the model. An optional label is useful to identify each test with a name. The keyword INTERCEPT can be used instead of a variable name to refer to the model's intercept.

The REG procedure performs an F test for the joint hypotheses specified in a single TEST statement. More than one TEST statement can accompany a MODEL statement. The numerator is the usual quadratic form of the estimates; the denominator is the mean squared error. If hypotheses can be represented by

$$L\beta = c$$

then the numerator of the F test is

$$Q = (Lb - c)'(L(X'X)^{-}L')^{-1}(Lb - c)$$

divided by degrees of freedom, where **b** is the estimate of β . For example:

```
model y=a1 a2 b1 b2;
aplus: test a1+a2=1;
b1: test b1=0, b2=0;
b2: test b1, b2;
```

The last two statements are equivalent; since no constant is specified, zero is assumed.

Note that, when the ACOV, HCC, or WHITE option is specified in the MODEL statement, tests are recomputed using the heteroscedasticity-consistent covariance matrix specified with the HCCMETHOD= option in the MODEL statement (see the section "Testing for Heteroscedasticity" on page 5569).

One option can be specified in the TEST statement after a slash (/):

PRINT

```
displays intermediate calculations. This includes L(X'X)^-L' bordered by Lb - c, and (L(X'X)^-L')^{-1} bordered by (L(X'X)^-L')^{-1}(Lb - c).
```

VAR Statement

VAR variables;

The VAR statement is used to include numeric variables in the crossproducts matrix that are not specified in the first MODEL statement.

Variables not listed in MODEL statements before the first RUN statement must be listed in the VAR statement if you want the ability to add them interactively to the model with an ADD statement, to include them in a new MODEL statement, or to plot them in a scatter plot with the PLOT statement.

In addition, if you want to use options in the PROC REG statement and do not want to fit a model to the data (with a MODEL statement), you must use a VAR statement.

WEIGHT Statement

WEIGHT variable;

A WEIGHT statement names a variable in the input data set with values that are relative weights for a weighted least squares fit. If the weight value is proportional to the reciprocal of the variance for each observation, then the weighted estimates are the best linear unbiased estimates (BLUE).

Values of the weight variable must be nonnegative. If an observation's weight is zero, the observation is deleted from the analysis. If a weight is negative or missing, it is set to zero, and the observation is excluded from the analysis. A more complete description of the WEIGHT statement can be found in Chapter 39, "The GLM Procedure."

Observation weights can be changed interactively with the REWEIGHT statement.

Details: REG Procedure

Missing Values

PROC REG constructs only one crossproducts matrix for the variables in all regressions. If any variable needed for any regression is missing, the observation is excluded from all estimates. If you include variables with missing values in the VAR statement, the corresponding observations are excluded from all analyses, even if you never include the variables in a model. PROC REG assumes that you might want to include these variables after the first RUN statement and deletes observations with missing values.

Input Data Sets

PROC REG does not compute new regressors. For example, if you want a quadratic term in your model, you should create a new variable when you prepare the input data. For example, the statement

```
model y=x1 x1*x1;
```

is not valid. Note that this MODEL statement is valid in the GLM procedure.

The input data set for most applications of PROC REG contains standard rectangular data, but special TYPE=CORR, TYPE=COV, and TYPE=SSCP data sets can also be used. TYPE=CORR and TYPE=COV data sets created by the CORR procedure contain means and standard deviations. In addition, TYPE=CORR data sets contain correlations and TYPE=COV data sets contain covariances. TYPE=SSCP data sets created in previous runs of PROC REG that used the OUTSSCP= option contain the sums of squares and crossproducts of the variables.

See Appendix A, "Special SAS Data Sets," and the "SAS Files" section in SAS Language Reference: Concepts for more information about special SAS data sets.

These summary files save CPU time. It takes nk^2 operations (where n=number of observations and k=number of variables) to calculate crossproducts; the regressions are of the order k^3 . When n is in the thousands and k is less than 10, you can save 99% of the CPU time by reusing the SSCP matrix rather than recomputing it.

When you want to use a special SAS data set as input, PROC REG must determine the TYPE for the data set. PROC CORR and PROC REG automatically set the type for their output data sets. However, if you create the data set by some other means (such as a DATA step), you must specify its type with the TYPE= data set option. If the TYPE for the data set is not specified when the data set is created, you can specify TYPE= as a data set option in the DATA= option in the PROC REG statement. For example:

```
proc reg data=a(type=corr);
```

When a TYPE=CORR, TYPE=COV, or TYPE=SSCP data set is used with PROC REG, statements and options that require the original data values have no effect. The OUTPUT, PAINT, PLOT, and REWEIGHT statements and the MODEL and PRINT statement options P, R, CLM, CLI, DW, IN-FLUENCE, and PARTIAL are disabled since the original observations needed to calculate predicted and residual values are not present.

Example Using TYPE=CORR Data Set

The following statements use PROC CORR to produce an input data set for PROC REG. The fitness data for this analysis can be found in Example 73.2.

```
proc corr data=fitness outp=r noprint;
   var Oxygen RunTime Age Weight RunPulse MaxPulse RestPulse;
proc print data=r;
proc reg data=r;
```

model Oxygen=RunTime Age Weight;
run;

Since the OUTP= data set from PROC CORR is automatically set to TYPE=CORR, the TYPE=data set option is not required in this example. The data set containing the correlation matrix is displayed by the PRINT procedure as shown in Figure 73.14. Figure 73.15 shows results from the regression that uses the TYPE=CORR data as an input data set.

Figure 73.14 TYPE=CORR Data Set Created by PROC CORR

									R
							R	M	e
				R			u	a	s
	_	_	0	u		W	n	x	t
	T	N	x	n		e	P	P	P
	Y	A	y	T		i	u	u	u
0	P	M	g	i	A	g	1	1	1
b	E	E	е	m	g	h	s	s	s
s	_	_	n	e	e	t	е	е	e
1	MEAN		47.3758	10.5861	47.6774	77.4445	169.645	173.774	53.4516
2	STD		5.3272	1.3874	5.2114	8.3286	10.252	9.164	7.6194
3	N		31.0000	31.0000	31.0000	31.0000	31.000	31.000	31.0000
4	CORR	Oxygen	1.0000	-0.8622	-0.3046	-0.1628	-0.398	-0.237	-0.3994
5	CORR	RunTime	-0.8622	1.0000	0.1887	0.1435	0.314	0.226	0.4504
6	CORR	Age	-0.3046	0.1887	1.0000	-0.2335	-0.338	-0.433	-0.1641
7	CORR	Weight	-0.1628	0.1435	-0.2335	1.0000	0.182	0.249	0.0440
8	CORR	RunPulse	-0.3980	0.3136	-0.3379	0.1815	1.000	0.930	0.3525
9	CORR	MaxPulse	-0.2367	0.2261	-0.4329	0.2494	0.930	1.000	0.3051
10	CORR	RestPulse	-0.3994	0.4504	-0.1641	0.0440	0.352	0.305	1.0000

Figure 73.15 Regression on TYPE=CORR Data Set

			e REG Proce				
			nt Variable				
		Ana	lysis of Va	riance			
			Sum of		Mean		
Source		DF	Squares	Sc	quare I	7 Value	Pr > F
Model		3	656.27095	218.7	5698	30.27	<.0001
Error		27	195.11060	7.2	2632		
Corrected Total		30	851.38154				
Dep	t MSE endent Me ff Var	ean	2.68818 47.37581 5.67416	R-Squar Adj R-S		7708 7454	
		Par	ameter Esti	mates			
		Parame	ter S	tandard			
Variable	DF	Estim	ate	Error	t Value	Pr >	t
Intercept	1	93.12	615	7.55916	12.32	<.0	001
RunTime	1	-3.14	039	0.36738	-8.55	<.0	001
Age	1	-0.17	388	0.09955	-1.75	0.0	921
90							

The following example uses the saved crossproducts matrix:

```
proc reg data=fitness outsscp=sscp noprint;
    model Oxygen=RunTime Age Weight RunPulse MaxPulse RestPulse;
proc print data=sscp;
proc reg data=sscp;
    model Oxygen=RunTime Age Weight;
run;
```

First, all variables are used to fit the data and create the SSCP data set. Figure 73.16 shows the PROC PRINT display of the SSCP data set. The SSCP data set is then used as the input data set for PROC REG, and a reduced model is fit to the data.

Figure 73.16 TYPE=SSCP Data Set Created by PROC REG

Obs	_TYPE_	_NAME_	Intercept	RunTime	Age	Weight
1	SSCP	Intercept	31.00	328.17	1478.00	2400.78
2	SSCP	RunTime	328.17	3531.80	15687.24	25464.71
3	SSCP	Age	1478.00	15687.24	71282.00	114158.90
4	SSCP	Weight	2400.78	25464.71	114158.90	188008.20
5	SSCP	RunPulse	5259.00	55806.29	250194.00	407745.67
6	SSCP	MaxPulse	5387.00	57113.72	256218.00	417764.62
7	SSCP	RestPulse	1657.00	17684.05	78806.00	128409.28
8	SSCP	Oxygen	1468.65	15356.14	69767.75	113522.26
9	N		31.00	31.00	31.00	31.00
Obs	RunPulse	MaxPulse	RestPulse	Ожуде	en	
1	5259.00	5387.00	1657.00	1468.6	55	
2	55806.29	57113.72	17684.05	15356.1	.4	
3	250194.00	256218.00	78806.00	69767.7	15	
4	407745.67	417764.62	128409.28	113522.2	26	
5	895317.00	916499.00	281928.00	248497.3	31	
6	916499.00	938641.00	288583.00	254866.7	75	
7	281928.00	288583.00	90311.00	78015.4	11	
8	248497.31	254866.75	78015.41	70429.8	36	
9	31.00	31.00	31.00	31.0	00	

Figure 73.17 also shows the PROC REG results for the reduced model. (For the PROC REG results for the full model, see Figure 73.29.)

Figure 73.17 Regression on TYPE=SSCP Data Set

		The REG F				
	1	Model. Dependent Vari				
		•				
		Analysis o	of Variance			
		Sum	n of	Mean		
Source	1	DF Squa	ires S	Square F	Value Pr	> F
Model		3 656.27	7095 218	. 75698	30.27 <.0	001
Error	:	27 195.11	.060 7	. 22632		
Corrected Total	:	30 851.38	3154			
	endent Mea	an 47.37 5.67		-Sq 0.74	154	
		Parameter	Estimates			
		Parameter	Standard			
Variable	DF	Estimate	Error	t Value	Pr > t	
Intercept	1	93.12615	7.55916	12.32	<.0001	
RunTime	1	-3.14039	0.36738	-8.55	<.0001	
Age	1	-0.17388	0.09955	-1.75	0.0921	
Weight	1	-0.05444	0.06181	-0.88	0.3862	

In the preceding example, the TYPE= data set option is not required since PROC REG sets the OUTSSCP= data set to TYPE=SSCP.

Output Data Sets

OUTEST= Data Set

The OUTEST= specification produces a TYPE=EST output SAS data set containing estimates and optional statistics from the regression models. For each BY group on each dependent variable occurring in each MODEL statement, PROC REG outputs an observation to the OUTEST= data set. The variables output to the data set are as follows:

- the BY variables, if any
- _MODEL_, a character variable containing the label of the corresponding MODEL statement, or MODELn if no label is specified, where n is 1 for the first MODEL statement, 2 for the second model statement, and so on
- _TYPE_, a character variable with the value 'PARMS' for every observation

- DEPVAR, the name of the dependent variable
- _RMSE_, the root mean squared error or the estimate of the standard deviation of the error term
- Intercept, the estimated intercept, unless the NOINT option is specified
- all the variables listed in any MODEL or VAR statement. Values of these variables are the estimated regression coefficients for the model. A variable that does not appear in the model corresponding to a given observation has a missing value in that observation. The dependent variable in each model is given a value of -1.

If you specify the COVOUT option, the covariance matrix of the estimates is output after the estimates; the _TYPE_ variable is set to the value 'COV' and the names of the rows are identified by the character variable, _NAME_.

If you specify the TABLEOUT option, the following statistics listed by _TYPE_ are added after the estimates:

- STDERR, the standard error of the estimate
- T, the t statistic for testing if the estimate is zero
- PVALUE, the associated *p*-value
- LnB, the $100(1-\alpha)$ lower confidence limit for the estimate, where n is the nearest integer to $100(1-\alpha)$ and α defaults to 0.05 or is set by using the ALPHA= option in the PROC REG or MODEL statement
- UnB, the $100(1-\alpha)$ upper confidence limit for the estimate

Specifying the option ADJRSQ, AIC, BIC, CP, EDF, GMSEP, JP, MSE, PC, RSQUARE, SBC, SP, or SSE in the PROC REG or MODEL statement automatically outputs these statistics and the model R^2 for each model selected, regardless of the model selection method. Additional variables, in order of occurrence, are as follows:

- _IN_, the number of regressors in the model not including the intercept
- P, the number of parameters in the model including the intercept, if any
- EDF, the error degrees of freedom
- _SSE_, the error sum of squares, if the SSE option is specified
- MSE, the mean squared error, if the MSE option is specified
- RSQ, the R^2 statistic
- ADJRSQ, the adjusted R^2 , if the ADJRSQ option is specified
- $_{\text{CP}}$, the C_p statistic, if the CP option is specified

- \bullet _SP_, the S_p statistic, if the SP option is specified
- \bullet _JP_, the J_p statistic, if the JP option is specified
- _PC_, the PC statistic, if the PC option is specified
- _GMSEP_, the GMSEP statistic, if the GMSEP option is specified
- _AIC_, the AIC statistic, if the AIC option is specified
- _BIC_, the BIC statistic, if the BIC option is specified
- _SBC_, the SBC statistic, if the SBC option is specified

The following statements produce and display the OUTEST= data set. This example uses the population data given in the section "Polynomial Regression" on page 5434. Figure 73.18 through Figure 73.20 show the regression equations and the resulting OUTEST= data set.

```
proc reg data=USPopulation outest=est;
   m1: model Population=Year;
   m2: model Population=Year YearSq;
proc print data=est;
run;
```

Figure 73.18 Regression Output for Model M1

		The REG Proced	ure		
		Model: m1			
	Depende	nt Variable: F	opulation		
	A	nalysis of Var	riance		
		Sum of	Mea	n	
Source	DF	Squares	Squar	e F Value	Pr > F
Model	1	146869	14686	9 228.92	<.0001
Error	20	12832	641.5816	0	
Corrected Total	21	159700			
Roc	ot MSE	25.32946	R-Square	0.9197	
Dep	endent Mean	94.64800	Adj R-Sq	0.9156	
Coe	eff Var	26.76175			
	P	arameter Estin	nates		
	Para	meter St	andard		
Variable	DF Est	imate	Error t	Value Pr >	t
Intercept	1 -2345.	85498 161	39279 -	.14.54 <.0	0001
Year			0.08512	15.13 <.0	0001

Figure 73.19 Regression Output for Model M2

		Ana	lysis of Va	ariance			
			Sum of		Mean		
Source		DF	Squares	s	quare	F Value	e Pr > I
Model		2	159529		79765	8864.19	<.0001
Error		19	170.97193	8.	99852		
Corrected Tot	al	21	159700				
	Root MSE		2.99975	R-Squa	re	0.9989	
	Dependent	Mean	94.64800	Adj R-	Sq	0.9988	
	Coeff Var		3.16938				
		Par	ameter Est	imates			
		Parame	ter :	Standard			
Variable	DF	Estim	ate	Error	t Val	lue Pr	> t
Intercept	. 1	21	.631 63	39.50181	33.	.82	<.0001
Year	1	-24.04	581	0.67547	-35.	.60	<.0001
YearSq	1	0.00	668 0.0	00017820	37.	.51	<.0001

Figure 73.20 OUTEST= Data Set

Obs	s _MODEL_	_TYPE_	_DEPVAR_	_RMSE_	Intercept	Year	Population	YearSq
1	m1	PARMS	Population	25.3295	-2345.85	1.2879	-1	
2	m2	PARMS	Population	2.9998	21630.89	-24.0458	-1	.006684346

The following modification of the previous example uses the TABLEOUT and ALPHA= options to obtain additional information in the OUTEST= data set:

```
proc reg data=USPopulation outest=est tableout alpha=0.1;
   m1: model Population=Year/noprint;
   m2: model Population=Year YearSq/noprint;
proc print data=est;
run;
```

Notice that the TABLEOUT option causes standard errors, t statistics, p-values, and confidence limits for the estimates to be added to the OUTEST= data set. Also note that the ALPHA= option is used to set the confidence level at 90%. The OUTEST= data set is shown in Figure 73.21.

Figure 73.21 The OUTEST= Data Set When TABLEOUT Is Specified

Obs	_MODEL_	_TYPE_	_DEPVAR_	_RMSE_	Intercept	Year	Population	YearSq
1	m1	PARMS	Population	25.3295	-2345.85	1.2879	-1	
2	m1	STDERR	Population	25.3295	161.39	0.0851		
3	m1	T	Population	25.3295	-14.54	15.1300		
4	m1	PVALUE	Population	25.3295	0.00	0.0000		
5	m1	L90B	Population	25.3295	-2624.21	1.1411		
6	m1	U90B	Population	25.3295	-2067.50	1.4347		
7	m2	PARMS	Population	2.9998	21630.89	-24.0458	-1	0.0067
8	m2	STDERR	Population	2.9998	639.50	0.6755	•	0.0002
9	m2	T	Population	2.9998	33.82	-35.5988	•	37.5096
10	m2	PVALUE	Population	2.9998	0.00	0.0000	•	0.0000
11	m2	L90B	Population	2.9998	20525.11	-25.2138	•	0.0064
12	m2	U90B	Population	2.9998	22736.68	-22.8778	•	0.0070

A slightly different OUTEST= data set is created when you use the RSQUARE selection method. The following statements request only the "best" model for each subset size but ask for a variety of model selection statistics, as well as the estimated regression coefficients. An OUTEST= data set is created and displayed. See Figure 73.22 and Figure 73.23 for the results.

```
proc reg data=fitness outest=est;
  model Oxygen=Age Weight RunTime RunPulse RestPulse MaxPulse
      / selection=rsquare mse jp gmsep cp aic bic sbc b best=1;
proc print data=est;
run;
```

Figure 73.22 PROC REG Output for Physical Fitness Data: Best Models

				EG Procedu: el: MODEL1	re		
			Dependent '	Variable: 0	xygen		
			R-Square	Selection N	l ethod		
Number in	5 6	G(1)	170	27.0	Estimated		
Model	R-Square	C (p)	AIC	віс	of Predict	10n J(p)	MSE
1	0.7434	13.6988 	64.5341	65.4673 	8.0	546 8.0199 	7.53384
2	0.7642	12.3894	63.9050	64.8212	7.9	478 7.8621	7.16842
3	0.8111	6.9596	59.0373	61.3127	6.8	583 6.7253	5.95669
4	0.8368	4.8800	56.4995	60.3996	6.3	984 6.2053	5.34346
5	0.8480	5.1063	56.2986	61.5667	6.4	565 6.1782	5.17634
6	0.8487	7.0000	58.1616	64.0748	6.9	870 6.5804	5.36825
Number in					Parameter	Estimates	
Model	R-Square	SBC	Inter	cept	Age	Weight	RunTime
1	0.7434	67.40210	82.4	2177			-3.31056
2	0.7642	68.20695	88.4	 6229	-0.15037		-3.20395
3	0.8111	64.77326	111.7	 1806	-0.25640		-2.82538
4	0.8368	63.66941	98.1	 4789	-0.19773		-2.76758
5	0.8480	64.90250	102.2	 0428	-0.21962	-0.07230	-2.68252
6	0.8487	68.19952	102.9	 3448	-0.22697	-0.07418	-2.62865
Number in		Р	arameter E	stimates			
Model	R-Square	RunPulse	RestPu	lse Ma	xPulse		
1	0.7434						
2	0.7642	·					
3	0.8111	-0.13091					
4	0.8368				0.27051		
5	0.8480	-0.37340			0.30491		
 6	0.8487	 -0.36963	-0.0	 2153	0.30322		

Obs MODEL TYPE DEPVAR RMSE Intercept Age Weight 2.74478 1 MODEL1 PARMS Oxygen 82.422 2 MODEL1 2.67739 PARMS Oxygen 88.462 -0.15037-0.25640 3 MODEL1 2.44063 111.718 PARMS Oxygen 98.148 MODEL1 -0.19773 4 PARMS Oxygen 2.31159 5 MODEL1 PARMS Oxygen 2.27516 102.204 -0.21962 -0.072302 6 MODEL1 PARMS Oxygen 2.31695 102.934 -0.22697 -0.074177Max RunTime RunPulse RestPulse Oxygen _IN_ _P_ _EDF_ MSE Obs Pulse 2 29 7.53384 1 -3.31056-1 1 2 -3.20395 -1 2 3 28 7.16842 -2.82538 -0.13091 . 3 -1 3 4 27 5.95669 0.27051 -2.76758 -0.34811 . 5 4 -1 26 5.34346 5 -2.68252 -0.37340 0.30491 -1 5 6 25 5.17634 -2.62865 -0.36963 -0.021534 0.30322 7 -1 6 24 5.36825 Obs _RSQ_ _CP_ _JP_ GMSEP _AIC_ _BIC_ _SBC_ 13.6988 8.01990 65.4673 67.4021 1 0.74338 8.05462 64.5341 2 0.76425 12.3894 7.86214 7.94778 63.9050 64.8212 68.2069 3 0.81109 6.9596 6.72530 6.85833 59.0373 61.3127 64.7733 4 0.83682 4.8800 6.20531 6.39837 56.4995 60.3996 63.6694 5 0.84800 5.1063 6.17821 6.45651 56.2986 61.5667 64.9025 0.84867 7.0000 6.58043 6.98700 58.1616 64.0748 68.1995

Figure 73.23 PROC PRINT Output for Physical Fitness Data: OUTEST= Data Set

OUTSSCP= Data Sets

The OUTSSCP= option produces a TYPE=SSCP output SAS data set containing sums of squares and crossproducts. A special row (observation) and column (variable) of the matrix called Intercept contain the number of observations and sums. Observations are identified by the character variable _NAME_. The data set contains all variables used in MODEL statements. You can specify additional variables that you want included in the crossproducts matrix with a VAR statement.

The SSCP data set is used when a large number of observations are explored in many different runs. The SSCP data set can be saved and used for subsequent runs, which are much less expensive since PROC REG never reads the original data again. If you run PROC REG once to create only a SSCP data set, you should list all the variables that you might need in a VAR statement or include all the variables that you might need in a MODEL statement.

The following statements use the fitness data from Example 73.2 to produce an output data set with the OUTSSCP= option. The resulting output is shown in Figure 73.24.

```
proc reg data=fitness outsscp=sscp;
  var Oxygen RunTime Age Weight RestPulse RunPulse MaxPulse;
proc print data=sscp;
run;
```

Since a model is not fit to the data and since the only request is to create the SSCP data set, a MODEL statement is not required in this example. However, since the MODEL statement is not used, the VAR statement is required.

Figure 73.24	SSCP Data Set	Created with	OUTSSCP= O	ption: REG Procedure
---------------------	---------------	--------------	------------	----------------------

Obs	_TYPE_	_NAME_	Intercept	Oxygen	RunTime	Age
1	SSCP	Intercept	31.00	1468.65	328.17	1478.00
2	SSCP	Oxygen	1468.65	70429.86	15356.14	69767.75
3	SSCP	RunTime	328.17	15356.14	3531.80	15687.24
4	SSCP	Age	1478.00	69767.75	15687.24	71282.00
5	SSCP	Weight	2400.78	113522.26	25464.71	114158.90
6	SSCP	RestPulse	1657.00	78015.41	17684.05	78806.00
7	SSCP	RunPulse	5259.00	248497.31	55806.29	250194.00
8	SSCP	MaxPulse	5387.00	254866.75	57113.72	256218.00
9	N		31.00	31.00	31.00	31.00
Obs	Weight	RestPulse	RunPulse	MaxPulse		
1	2400.78	1657.00	5259.00	5387.00		
2	113522.26	78015.41	248497.31	254866.75		
3	25464.71	17684.05	55806.29	57113.72		
4	114158.90	78806.00	250194.00	256218.00		
5	188008.20	128409.28	407745.67	417764.62		
6	128409.28	90311.00	281928.00	288583.00		
7	407745.67	281928.00	895317.00	916499.00		
8	417764.62	288583.00	916499.00	938641.00		
9	31.00	31.00	31.00	31.00		

Interactive Analysis

PROC REG enables you to change interactively both the model and the data used to compute the model, and to produce and highlight scatter plots. See the section "Using PROC REG Interactively" on page 5444 for an overview of interactive analysis that uses PROC REG. The following statements can be used interactively (without reinvoking PROC REG): ADD, DELETE, MODEL, MTEST, OUTPUT, PAINT, PLOT, PRINT, REFIT, RESTRICT, REWEIGHT, and TEST. All interactive features are disabled if there is a BY statement.

The ADD, DELETE, and REWEIGHT statements can be used to modify the current MODEL. Every use of an ADD, DELETE, or REWEIGHT statement causes the model label to be modified by attaching an additional number to it. This number is the cumulative total of the number of ADD, DELETE, or REWEIGHT statements following the current MODEL statement.

A more detailed explanation of changing the data used to compute the model is given in the section "Reweighting Observations in an Analysis" on page 5563. Extra features for line printer scatter plots are discussed in the section "Line Printer Scatter Plot Features" on page 5528.

The following statements illustrate the usefulness of the interactive features. First, the full regression model is fit to the Class data (see the section "Getting Started: REG Procedure" on page 5430), and Figure 73.25 is produced.

```
ods graphics on;
proc reg data=Class plots(modelLabel only)=ResidualByPredicted;
  model Weight=Age Height;
run;
```

Figure 73.25 Interactive Analysis: Full Model

		T	he REG Pro	cedure				
			Model: MOI	EL1				
		Depend	ent Variab	Le: Weig	ht			
		An	alysis of \	/ariance				
			Sum of	Ē	Mean			
Source		DF	Squares	5	Square	F Va	lue	Pr > F
Model		2	7215.63710	36	07.81855	27	.23	<.000
Error		16	2120.09974	1 1	32.50623			
Corrected Total		18	9335.73684	1				
Pee	t MSE		11.51114	1 D.C		0.7729		
	endent Me				quare R-Sq			
-	ff Var	Ean	11.5081		K-54	0.7443	,	
				-				
		Pa	rameter Est	imates				
		Param	eter	Standar	d			
Variable	DF	Esti	mate	Erro	r t Va	lue	Pr >	tl
Intercept	1	-141.2	2376	33.3830	9 –4	. 23	0.00	06
Age	1	1.2	7839	3.1101	0 0	.41	0.68	65
Height	1	3.5	9703	0.9054	6 3	. 97	0.00	11

Next, the regression model is reduced by the following statements, and Figure 73.26 is produced.

```
delete age;
print;
run;
```

Figure 73.26 Interactive Analysis: Reduced Model

		1	Analysis of	Variance				
			Sum	of	Mean			
Source		DF	Squar	es	Square	F	Value	Pr > F
Model		1	7193.249	719	3.24912		57.08	<.0001
Error		17	2142.487	772 12	6.02869			
Corrected Total		18	9335.736	584				
Roc	t MSE		11.226	525 R-Sq	quare	0.77	05	
Dep	endent	Mean	100.026	32 Adj	R-Sq	0.75	70	
Coe	ff Var		11.223	330				
		I	Parameter E	Estimates				
		Para	ameter	Standard	L			
Variable	DF	Est	cimate	Error	t Va	lue	Pr >	t
Intercept	1	-143	. 02692	32.27459	-4	.43	0.0	004
Height	1	3	. 89903	0.51609	7	. 55	<.0	001

Note that the MODEL label has been changed from MODEL1 to MODEL1.1, since the original MODEL has been changed by the delete statement.

When ODS Graphics is enabled, updated plots are produced whenever a PRINT statement is used. The option

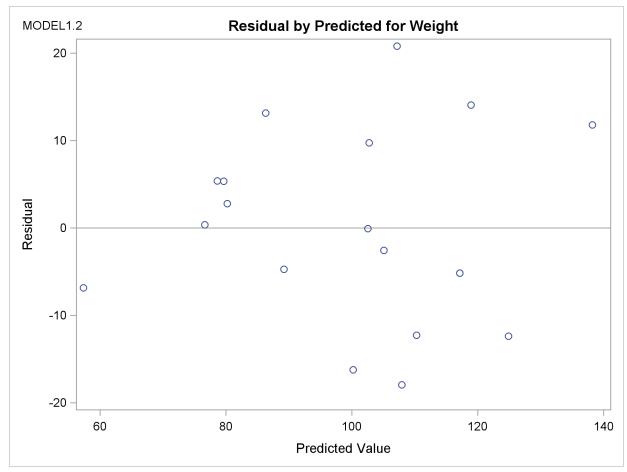
plots(modelLabel only) = Residual By Predicted

in the PROC REG statement specifies that the only plot produced is a scatter plot of residuals by predicted values. The MODELLABEL option specifies that the current model label is added to the plot.

The following statements generate a scatter plot of the residuals against the predicted values from the full model. Figure 73.27 is produced, and the scatter plot shows a possible outlier.

add age;
print;
run;

Figure 73.27 Interactive Analysis: Scatter Plot



The following statements delete the observation with the largest residual, refit the regression model, and produce a scatter plot of residuals against predicted values for the refitted model. Figure 73.28 shows the new scatter plot.

```
reweight r.>20;
print;
run;
ods graphics off;
```

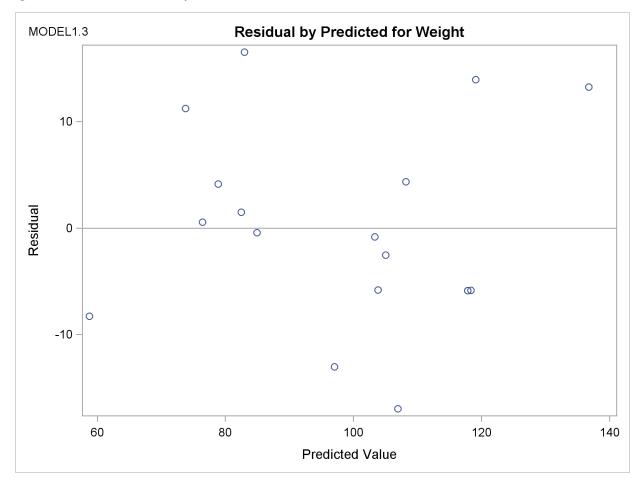


Figure 73.28 Interactive Analysis: Scatter Plot

Model-Selection Methods

The nine methods of model selection implemented in PROC REG are specified with the SELEC-TION= option in the MODEL statement. Each method is discussed in this section.

Full Model Fitted (NONE)

This method is the default and provides no model selection capability. The complete model specified in the MODEL statement is used to fit the model. For many regression analyses, this might be the only method you need.

Forward Selection (FORWARD)

The forward-selection technique begins with no variables in the model. For each of the independent variables, the FORWARD method calculates F statistics that reflect the variable's contribution to the model if it is included. The p-values for these F statistics are compared to the SLENTRY=

value that is specified in the MODEL statement (or to 0.50 if the SLENTRY= option is omitted). If no F statistic has a significance level greater than the SLENTRY= value, the FORWARD selection stops. Otherwise, the FORWARD method adds the variable that has the largest F statistic to the model. The FORWARD method then calculates F statistics again for the variables still remaining outside the model, and the evaluation process is repeated. Thus, variables are added one by one to the model until no remaining variable produces a significant F statistic. Once a variable is in the model, it stays.

Backward Elimination (BACKWARD)

The backward elimination technique begins by calculating F statistics for a model, including all of the independent variables. Then the variables are deleted from the model one by one until all the variables remaining in the model produce F statistics significant at the SLSTAY= level specified in the MODEL statement (or at the 0.10 level if the SLSTAY= option is omitted). At each step, the variable showing the smallest contribution to the model is deleted.

Stepwise (STEPWISE)

The stepwise method is a modification of the forward-selection technique and differs in that variables already in the model do not necessarily stay there. As in the forward-selection method, variables are added one by one to the model, and the F statistic for a variable to be added must be significant at the SLENTRY= level. After a variable is added, however, the stepwise method looks at all the variables already included in the model and deletes any variable that does not produce an F statistic significant at the SLSTAY= level. Only after this check is made and the necessary deletions are accomplished can another variable be added to the model. The stepwise process ends when none of the variables outside the model has an F statistic significant at the SLENTRY= level and every variable in the model is significant at the SLSTAY= level, or when the variable to be added to the model is the one just deleted from it.

Maximum R² Improvement (MAXR)

The maximum R^2 improvement technique does not settle on a single model. Instead, it tries to find the "best" one-variable model, the "best" two-variable model, and so forth, although it is not guaranteed to find the model with the largest R^2 for each size.

The MAXR method begins by finding the one-variable model producing the highest R^2 . Then another variable, the one that yields the greatest increase in R^2 , is added. Once the two-variable model is obtained, each of the variables in the model is compared to each variable not in the model. For each comparison, the MAXR method determines if removing one variable and replacing it with the other variable increases R^2 . After comparing all possible switches, the MAXR method makes the switch that produces the largest increase in R^2 . Comparisons begin again, and the process continues until the MAXR method finds that no switch could increase R^2 . Thus, the two-variable model achieved is considered the "best" two-variable model the technique can find. Another variable is then added to the model, and the comparing-and-switching process is repeated to find the "best" three-variable model, and so forth.

The difference between the STEPWISE method and the MAXR method is that all switches are evaluated before any switch is made in the MAXR method. In the STEPWISE method, the "worst" variable might be removed without considering what adding the "best" remaining variable might accomplish. The MAXR method might require much more computer time than the STEPWISE method.

Minimum R² (MINR) Improvement

The MINR method closely resembles the MAXR method, but the switch chosen is the one that produces the smallest increase in R^2 . For a given number of variables in the model, the MAXR and MINR methods usually produce the same "best" model, but the MINR method considers more models of each size.

R² Selection (RSQUARE)

The RSQUARE method finds subsets of independent variables that best predict a dependent variable by linear regression in the given sample. You can specify the largest and smallest number of independent variables to appear in a subset and the number of subsets of each size to be selected. The RSQUARE method can efficiently perform all possible subset regressions and display the models in decreasing order of R^2 magnitude within each subset size. Other statistics are available for comparing subsets of different sizes. These statistics, as well as estimated regression coefficients, can be displayed or output to a SAS data set.

The subset models selected by the RSQUARE method are optimal in terms of R^2 for the given sample, but they are not necessarily optimal for the population from which the sample is drawn or for any other sample for which you might want to make predictions. If a subset model is selected on the basis of a large R^2 value or any other criterion commonly used for model selection, then all regression statistics computed for that model under the assumption that the model is given a priori, including all statistics computed by PROC REG, are biased.

While the RSQUARE method is a useful tool for exploratory model building, no statistical method can be relied on to identify the "true" model. Effective model building requires substantive theory to suggest relevant predictors and plausible functional forms for the model.

The RSQUARE method differs from the other selection methods in that RSQUARE always identifies the model with the largest R^2 for each number of variables considered. The other selection methods are not guaranteed to find the model with the largest R^2 . The RSQUARE method requires much more computer time than the other selection methods, so a different selection method such as the STEPWISE method is a good choice when there are many independent variables to consider.

Adjusted R² Selection (ADJRSQ)

This method is similar to the RSQUARE method, except that the adjusted R^2 statistic is used as the criterion for selecting models, and the method finds the models with the highest adjusted R^2 within the range of sizes.

Mallows' C_D Selection (CP)

This method is similar to the ADJRSQ method, except that Mallows' C_p statistic is used as the criterion for model selection. Models are listed in ascending order of C_p .

Additional Information about Model-Selection Methods

If the RSQUARE or STEPWISE procedure (as documented in SAS User's Guide: Statistics, Version 5 Edition) is requested, PROC REG with the appropriate model-selection method is actually used.

Reviews of model-selection methods by Hocking (1976) and Judge et al. (1980) describe these and other variable-selection methods.

Criteria Used in Model-Selection Methods

When many significance tests are performed, each at a level of, for example, 5%, the overall probability of rejecting at least one true null hypothesis is much larger than 5%. If you want to guard against including any variables that do not contribute to the predictive power of the model in the population, you should specify a very small SLE= significance level for the FORWARD and STEP-WISE methods and a very small SLS= significance level for the BACKWARD and STEPWISE methods.

In most applications, many of the variables considered have some predictive power, however small. If you want to choose the model that provides the best prediction computed using the sample estimates, you need only to guard against estimating more parameters than can be reliably estimated with the given sample size, so you should use a moderate significance level, perhaps in the range of 10% to 25%.

In addition to \mathbb{R}^2 , the \mathbb{C}_p statistic is displayed for each model generated in the model-selection methods. The \mathbb{C}_p statistic is proposed by Mallows (1973) as a criterion for selecting a model. It is a measure of total squared error defined as

$$C_p = \frac{SSE_p}{s^2} - (N - 2p)$$

where s^2 is the MSE for the full model, and SSE_p is the sum-of-squares error for a model with p parameters including the intercept, if any. If C_p is plotted against p, Mallows recommends the model where C_p first approaches p. When the right model is chosen, the parameter estimates are unbiased, and this is reflected in C_p near p. For further discussion, refer to Daniel and Wood (1980).

The adjusted R^2 statistic is an alternative to R^2 that is adjusted for the number of parameters in the model. The adjusted R^2 statistic is calculated as

ADJRSQ =
$$1 - \frac{(n-i)(1-R^2)}{n-p}$$

where n is the number of observations used in fitting the model, and i is an indicator variable that is 1 if the model includes an intercept, and 0 otherwise.

Limitations in Model-Selection Methods

The use of model-selection methods can be time-consuming in some cases because there is no built-in limit on the number of independent variables, and the calculations for a large number of independent variables can be lengthy. The recommended limit on the number of independent variables for the MINR method is 20 + i, where i is the value of the INCLUDE= option.

For the RSQUARE, ADJRSQ, or CP method, with a large value of the BEST= option, adding one more variable to the list from which regressors are selected might significantly increase the CPU time. Also, the time required for the analysis is highly dependent on the data and on the values of the BEST=, START=, and STOP= options.

Parameter Estimates and Associated Statistics

The following example uses the fitness data from Example 73.2. Figure 73.30 shows the parameter estimates and the tables from the SS1, SS2, STB, CLB, COVB, and CORRB options:

```
proc reg data=fitness;
  model Oxygen=RunTime Age Weight RunPulse MaxPulse RestPulse
      / ss1 ss2 stb clb covb corrb;
run;
```

The procedure first displays an analysis of variance table (Figure 73.29). The F statistic for the overall model is significant, indicating that the model explains a significant portion of the variation in the data.

Figure 73.29 ANOVA Table

	Depen	The REG Proced Model: MODEL dent Variable:	.1		
	A	malysis of Var	ciance		
		Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > F
Model	6	722.54361	120.42393	22.43	<.0001
Error	24	128.83794	5.36825		
Corrected Total	30	851.38154			
Root MS	E	2.31695	R-Square	0.8487	
Depende	nt Mean	47.37581	Adj R-Sq	0.8108	
Coeff V	ar	4.89057	- -		

The procedure next displays parameter estimates and some associated statistics (Figure 73.30). First, the estimates are shown, followed by their standard errors. The next two columns of the table contain the t statistics and the corresponding probabilities for testing the null hypothesis that the parameter is not significantly different from zero. These probabilities are usually referred to as p-values. For example, the Intercept term in the model is estimated to be 102.9 and is significantly different from zero. The next two columns of the table are the result of requesting the SS1 and SS2 options, and they show sequential and partial sums of squares (SS) associated with each variable. The standardized estimates (produced by the STB option) are the parameter estimates that result when all variables are standardized to a mean of 0 and a variance of 1. These estimates are computed by multiplying the original estimates by the standard deviation of the regressor (independent) variable and then dividing by the standard deviation of the dependent variable. The CLB option adds the upper and lower 95% confidence limits for the parameter estimates; the α level can be changed by specifying the ALPHA= option in the PROC REG or MODEL statement.

Figure 73.30 SS1, SS2, STB, CLB, COVB, and CORRB Options: Parameter Estimates

		Pa	rameter Estin	nates		
		Parameter	Standard			
Variable	DF	Estimate	Error	t Value	Pr > t	Type I SS
Intercept	1	102.93448	12.40326	8.30	<.0001	69578
RunTime	1	-2.62865	0.38456	-6.84	<.0001	632.90010
Age	1	-0.22697	0.09984	-2.27	0.0322	17.76563
Weight	1	-0.07418	0.05459	-1.36	0.1869	5.60522
RunPulse	1	-0.36963	0.11985	-3.08	0.0051	38.87574
MaxPulse	1	0.30322	0.13650	2.22	0.0360	26.82640
RestPulse	1	-0.02153	0.06605	-0.33	0.7473	0.57051
		Pa	rameter Estin			
Variable			Standardi: Estima		95% Confiden	
variable	DF	Type II SS	ESTIMA	ate	95% Confiden	ice Limits
Intercept	1	369.72831		0	77.33541	128.53355
RunTime	1	250.82210	-0.68	460	-3.42235	-1.83496
Age	1	27.74577	-0.22	204	-0.43303	-0.02092
Weight	1	9.91059	-0.11	597	-0.18685	0.03850
RunPulse	1	51.05806	-0.71	133	-0.61699	-0.12226
MaxPulse	1	26.49142	0.52	L61	0.02150	0.58493
RestPulse	1	0.57051	-0.030	080	-0.15786	0.11480

The final two tables are produced as a result of requesting the COVB and CORRB options (Figure 73.31). These tables show the estimated covariance matrix of the parameter estimates, and the estimated correlation matrix of the estimates.

Figure 73.31 SS1, SS2, STB, CLB, COVB, and CORRB Options: Covariances and Correlations

		Covariance o	of Estimates		
Variable	Intercept	Rur	Time	Age	Weight
Intercept	153.84081152	0.767837	/3769 – 0.9	02049478	-0.178237818
RunTime	0.7678373769	0.147888	0839 -0.0	14191688	-0.004417672
Age	-0.902049478	-0.01419	0.0	09967521	0.0010219105
Weight	-0.178237818	-0.00441	.7672 0.00	10219105	0.0029804131
RunPulse	0.280796516	-0.00904	7784 -0.0	01203914	0.0009644683
MaxPulse	exPulse -0.832761667		9498 0.00	35823843	-0.001372241
RestPulse	-0.147954715	-0.01091	.5224 0.00	14897532	0.0003799295
		Covariance o	of Estimates		
Vari	iable R	unPulse	MaxPulse	Re	estPulse
Inte	ercept 0.28	0796516	-0.832761667	-0.1	47954715
Run'	Time -0.00	9047784	0.0046249498	-0.0	10915224
Age	-0.00	1203914	0.0035823843	0.00	14897532
Weig	ght 0.000	9644683	-0.001372241	0.00	03799295
RunI	Pulse 0.014	3647273	-0.014952457	-0.0	00764507
Max	Pulse -0.01	4952457	0.0186309364		03425724
Rest	Pulse -0.00	0764507	0.0003425724 0		43631674
Variable	C Intercept	orrelation o	of Estimates	Age	Weight
Variable	Intercept	i.u.	. I I I I I	ngc	wergine
Intercept	1.0000	0.	1610	-0.7285	-0.2632
RunTime	0.1610	1.	0000	-0.3696	-0.2104
Age	-0.7285	-0.	3696	1.0000	0.1875
Weight	-0.2632		2104	0.1875	1.0000
RunPulse	0.1889		1963	-0.1006	0.1474
MaxPulse	-0.4919		0881	0.2629	-0.1842
RestPulse	-0.1806	-0.	4297	0.2259	0.1054
		Correlation	of Estimates		
Vari	iable R	unPulse	MaxPulse	Re	estPulse
	ercept	0.1889	-0.4919		-0.1806
Run'		-0.1963	0.0881		-0.4297
		-0.1006	0.2629		0.2259
Age		0.1474	-0.1842		0.1054
Weig					
Weig Runl	Pulse	1.0000	-0.9140		-0.0966
Weiq Run! Max!	Pulse Pulse		-0.9140 1.0000 0.0380		-0.0966 0.0380 1.0000

For further discussion of the parameters and statistics, see the section "Displayed Output" on page 5578, and Chapter 4, "Introduction to Regression Procedures."

Predicted and Residual Values

The display of the predicted values and residuals is controlled by the P, R, CLM, and CLI options in the MODEL statement. The P option causes PROC REG to display the observation number, the ID value (if an ID statement is used), the actual value, the predicted value, and the residual. The R, CLI, and CLM options also produce the items under the P option. Thus, P is unnecessary if you use one of the other options.

The R option requests more detail, especially about the residuals. The standard errors of the mean predicted value and the residual are displayed. The studentized residual, which is the residual divided by its standard error, is both displayed and plotted. A measure of influence, Cook's D, is displayed. Cook's D measures the change to the estimates that results from deleting each observation (Cook 1977, 1979). This statistic is very similar to DFFITS.

The CLM option requests that PROC REG display the $100(1-\alpha)\%$ lower and upper confidence limits for the mean predicted values. This accounts for the variation due to estimating the parameters only. If you want a $100(1-\alpha)\%$ confidence interval for observed values, then you can use the CLI option, which adds in the variability of the error term. The α level can be specified with the ALPHA= option in the PROC REG or MODEL statement.

You can use these statistics in PLOT and PAINT statements. This is useful in performing a variety of regression diagnostics. For definitions of the statistics produced by these options, see Chapter 4, "Introduction to Regression Procedures."

The following statements use the U.S. population data found in the section "Polynomial Regression" on page 5434. The results are shown in Figure 73.32 and Figure 73.33.

```
data USPop2;
   input Year @@;
   YearSq=Year*Year;
   datalines;
2010 2020 2030
;
data USPop2;
   set USPopulation USPop2;

proc reg data=USPop2;
   id Year;
   model Population=Year YearSq / r cli clm;
run;
```

Figure 73.32 Regression Using the R, CLI, and CLM Options

			REG Proce				
	_		MODE:		_		
	D	ependent	Variable: 1	Populatio	n		
		Anal	ysis of Va	riance			
			Sum of		Mean		
Source		DF	Squares	s	quare	F Value	Pr > F
Model		2	159529		79765	8864.19	<.0001
Error		19	170.97193	8.	99852		
Corrected Total		21	159700				
Ro	ot MSE		2.99975	R-Squa	re 0.	9989	
De	pendent M	ean	94.64800	Adj R-	Sq 0.	9988	
Co	eff Var		3.16938				
		Para	meter Estir	mates			
		Paramet	er St	tandard			
Variable	DF	Estima	ite	Error	t Value	Pr >	t
Intercept	1	216	631	9.50181	33.82	. <.0	001
Year	1	-24.045	81 (0.67547	-35.60	<.0	001
YearSq	1	0.006	68 0.00	0017820	37.51	<.0	001

Figure 73.33 Regression Using the R, CLI, and CLM Options

The REG Procedure

Model: MODEL1

Dependent Variable: Population

Output Statistics

		Dependent	Predicted	Std Error				
Obs	Year	Variable	Value	Mean Predict	95% CI	L Mean	95% CL I	Predict
	1500		6 0107	4 8565	0 5060		1 0601	10 1001
1	1790	3.9290	6.2127	1.7565	2.5362	9.8892	-1.0631	13.4884
2	1800	5.3080	5.7226	1.4560	2.6751	8.7701	-1.2565	12.7017
3	1810	7.2390	6.5694	1.2118	4.0331	9.1057	-0.2021	13.3409
4	1820	9.6380	8.7531	1.0305	6.5963	10.9100	2.1144	15.3918
5	1830	12.8660	12.2737	0.9163	10.3558	14.1916	5.7087	18.8386
6	1840	17.0690	17.1311	0.8650	15.3207	18.9415	10.5968	23.6655
7	1850	23.1910	23.3254	0.8613	21.5227	25.1281	16.7932	29.8576
8	1860	31.4430	30.8566	0.8846	29.0051	32.7080	24.3107	37.4024
9	1870	39.8180	39.7246	0.9163	37.8067	41.6425	33.1597	46.2896
10	1880	50.1550	49.9295	0.9436	47.9545	51.9046	43.3476	56.5114
11	1890	62.9470	61.4713	0.9590	59.4641	63.4785	54.8797	68.0629
12	1900	75.9940	74.3499	0.9590	72.3427	76.3571	67.7583	80.9415
13	1910	91.9720	88.5655	0.9436	86.5904	90.5405	81.9836	95.1473
14	1920	105.7100	104.1178	0.9163	102.2000	106.0357	97.5529	110.6828
15	1930	122.7750	121.0071	0.8846	119.1556	122.8585	114.4612	127.5529
16	1940	131.6690	139.2332	0.8613	137.4305	141.0359	132.7010	145.7654
17	1950	151.3250	158.7962	0.8650	156.9858	160.6066	152.2618	165.3306
18	1960	179.3230	179.6961	0.9163	177.7782	181.6139	173.1311	186.2610
19	1970	203.2110	201.9328	1.0305	199.7759	204.0896	195.2941	208.5715
20	1980	226.5420	225.5064	1.2118	222.9701	228.0427	218.7349	232.2779
21	1990	248.7100	250.4168	1.4560	247.3693	253.4644	243.4378	257.3959
22	2000	281.4220	276.6642	1.7565	272.9877	280.3407	269.3884	283.9400
23	2010		304.2484	2.1073	299.8377	308.6591	296.5754	311.9214
24	2020		333.1695	2.5040	327.9285	338.4104	324.9910	341.3479
25	2030		363.4274	2.9435	357.2665	369.5883	354.6310	372.2238
	_000	•	303.12/4	2.5255	202000	203.0005	201.0010	2.2.220

Output Statistics

Obs	Year	Residual	Std Error Residual	Student Residual	-2	2-1 0 1	2	Cook's
1	1790	-2.2837	2.432	-0.939	1	*	1	0.153
2	1800	-0.4146	2.623	-0.158	1	1	1	0.003
3	1810	0.6696	2.744	0.244	1	1	1	0.004
4	1820	0.8849	2.817	0.314	1	1	1	0.004
5	1830	0.5923	2.856	0.207	1	1	1	0.001
6	1840	-0.0621	2.872	-0.0216	1	1	1	0.000
7	1850	-0.1344	2.873	-0.0468	1	1	1	0.000
8	1860	0.5864	2.866	0.205	1	1	1	0.001
9	1870	0.0934	2.856	0.0327	1	1	1	0.000
10	1880	0.2255	2.847	0.0792	1	I	1	0.000

Figure 73.33 continued

			The REG P					
			Model:					
		Dep	endent Variab	le: Populati	.on			
			Output S	tatistics				
			Std Error	Student				Cook's
Obs	Year	Residual	Residual	Residual	-2	-1 0 1 2		D
11	1890	1.4757	2.842	0.519	ı	*	ı	0.010
12	1900	1.6441	2.842	0.578	1	*	ı	0.013
13	1910	3.4065	2.847	1.196	- 1	**	ı	0.052
14	1920	1.5922	2.856	0.557	1	*	ı	0.011
15	1930	1.7679	2.866	0.617	ı	*	1	0.012
16	1940	-7.5642	2.873	-2.632	**	***	ı	0.208
17	1950	-7.4712	2.872	-2.601	**	***	ı	0.205
18	1960	-0.3731	2.856	-0.131	- 1	1	ı	0.001
19	1970	1.2782	2.817	0.454	- 1	1	ı	0.009
20	1980	1.0356	2.744	0.377	- 1	1	ı	0.009
21	1990	-1.7068	2.623	-0.651	- 1	*	- 1	0.044
22	2000	4.7578	2.432	1.957	ı	***	1	0.666
23	2010	•		•				
24	2020	•		•				
25	2030							

After producing the usual analysis of variance and parameter estimates tables (Figure 73.32), the procedure displays the results of requesting the options for predicted and residual values (Figure 73.33). For each observation, the requested information is shown. Note that the ID variable is used to identify each observation. Also note that, for observations with missing dependent variables, the predicted value, standard error of the predicted value, and confidence intervals for the predicted value are still available.

The columnar print plot of studentized residuals and Cook's *D* statistics are displayed as a result of requesting the R option. In the plot of studentized residuals, the large number of observations with absolute values greater than two indicates an inadequate model. You can use ODS Graphics to obtain high-resolution plots of studentized residuals by predicted values or leverage; see Example 73.1 for a similar example.

Line Printer Scatter Plot Features

This section discusses the special options available with line printer scatter plots. Detailed examples of traditional graphics and options are given in the section "Traditional Graphics" on page 5541.

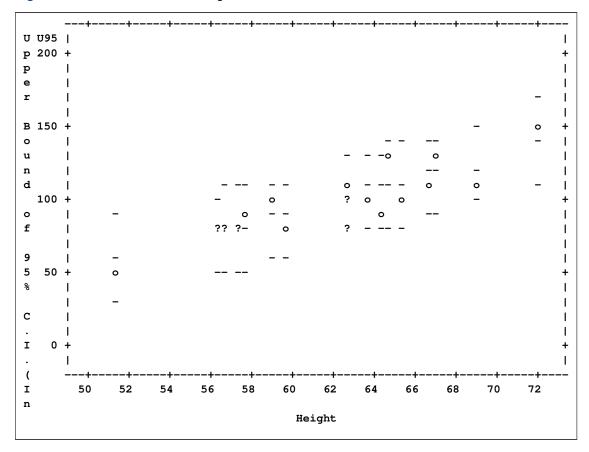
Producing Scatter Plots

The interactive PLOT statement available in PROC REG enables you to look at scatter plots of data and diagnostic statistics. These plots can help you to evaluate the model and detect outliers in your data. Several options enable you to place multiple plots on a single page, superimpose plots, and collect plots to be overlaid by later plots. The PAINT statement can be used to highlight points on a plot. See the section "Painting Scatter Plots" on page 5537 for more information about painting.

The Class data set introduced in the section "Simple Linear Regression" on page 5430 is used in the following examples.

You can superimpose several plots with the OVERLAY option. With the following statements, a plot of Weight against Height is overlaid with plots of the predicted values and the 95% prediction intervals. The model on which the statistics are based is the full model including Height and Age. These statements produce the plot in Figure 73.34:

Figure 73.34 Scatter Plot Showing Data, Predicted Values, and Confidence Limits



In this plot, the data values are marked with the symbol 'o' and the predicted values and prediction interval limits are labeled with the symbol '-'. The plot is scaled to accommodate the points from all plots. This is an important difference from the COLLECT option, which does not rescale plots after the first plot or plots are collected. You could separate the overlaid plots by using the following statements:

```
plot;
run;

This places each of the four plots on a separate page, while the statements
plot / overlay;
run;

repeat the previous overlaid plot. In general, the statement
plot;
```

is equivalent to respecifying the most recent PLOT statement without any options. However, the COLLECT, HPLOTS=, SYMBOL=, and VPLOTS= options apply across PLOT statements and remain in effect.

The next example shows how you can overlay plots of statistics before and after a change in the model. For the full model involving Height and Age, the ordinary residuals and the studentized residuals are plotted against the predicted values. The COLLECT option causes these plots to be collected or retained for redisplay later. The option HPLOTS=2 enables the two plots to appear side by side on one page. The symbol 'f' is used on these plots to identify them as resulting from the full model. These statements produce Figure 73.35:

```
plot r.*p. student.*p. / collect hplots=2 symbol='f';
run;
```

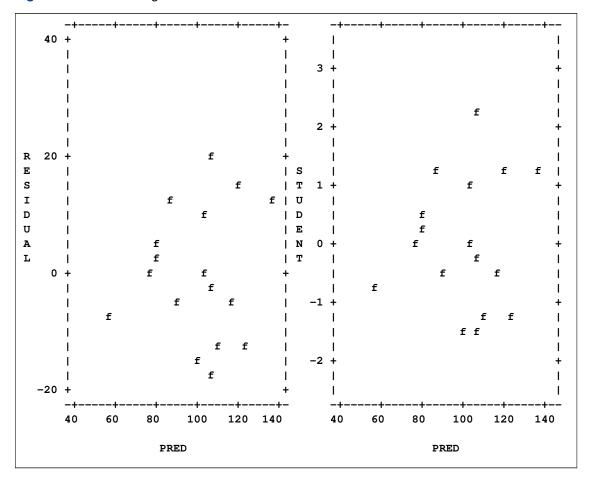


Figure 73.35 Collecting Residual Plots for the Full Model

Note that these plots are not overlaid. The COLLECT option does not overlay the plots in one PLOT statement but retains them so that they can be overlaid by later plots. When the COLLECT option appears in a PLOT statement, the plots in that statement become the first plots in the collection.

Next, the model is reduced by deleting the Age variable. The PLOT statement requests the same plots as before but labels the points with the symbol 'r' denoting the reduced model. The following statements produce Figure 73.36:

```
delete Age;
plot r.*p. student.*p. / symbol='r';
run;
```

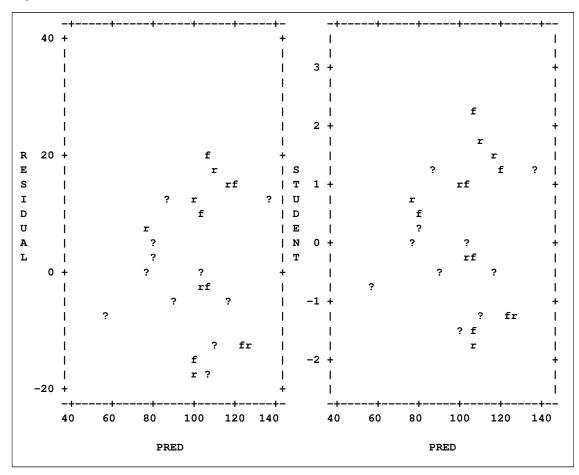


Figure 73.36 Overlaid Residual Plots for Full and Reduced Models

Notice that the COLLECT option causes the corresponding plots to be overlaid. Also notice that the DELETE statement causes the model label to be changed from MODEL1 to MODEL1.1. The points labeled 'f' are from the full model, and the points labeled 'r' are from the reduced model. Positions labeled '?' contain at least one point from each model. In this example, the OVERLAY option cannot be used because all of the plots to be overlaid cannot be specified in one PLOT statement. With the COLLECT option, any changes to the model or the data used to fit the model do not affect plots collected before the changes. Collected plots are always reproduced exactly as they first appear. (Similarly, a PAINT statement does not affect plots collected before the PAINT statement is issued.)

The previous example overlays the residual plots for two different models. You might prefer to see them side by side on the same page. This can also be done with the COLLECT option by using a blank plot. Continuing from the last example, the COLLECT, HPLOTS=2, and SYMBOL='r' options are still in effect. In the following PLOT statement, the CLEAR option deletes the collected plots and enables the specified plot to begin a new collection. The plot created is the residual plot for the reduced model. These statements produce Figure 73.37:

```
plot r.*p. / clear;
run;
```

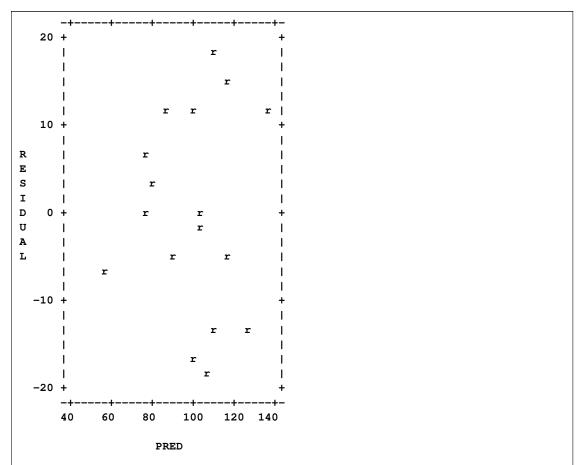


Figure 73.37 Residual Plot for Reduced Model Only

The next statements add the variable AGE to the model and place the residual plot for the full model next to the plot for the reduced model. Notice that a blank plot is created in the first plot request by placing nothing between the quotes. Since the COLLECT option is in effect, this plot is superimposed on the residual plot for the reduced model. The residual plot for the full model is created by the second request. The result is the desired side-by-side plots. The NOCOLLECT option turns off the collection process after the specified plots are added and displayed. Any PLOT statements that follow show only the newly specified plots. These statements produce Figure 73.38:

```
add Age;
plot r.*p.='' r.*p.='f' / nocollect;
run;
```

Figure 73.38 Side-by-Side Residual Plots for the Full and Reduced Models

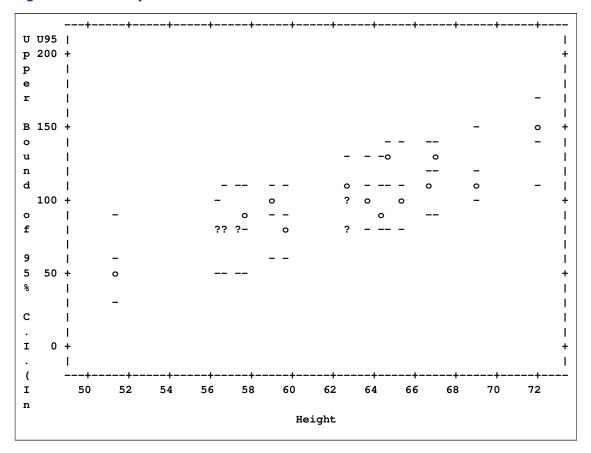


Figure 73.38 continued

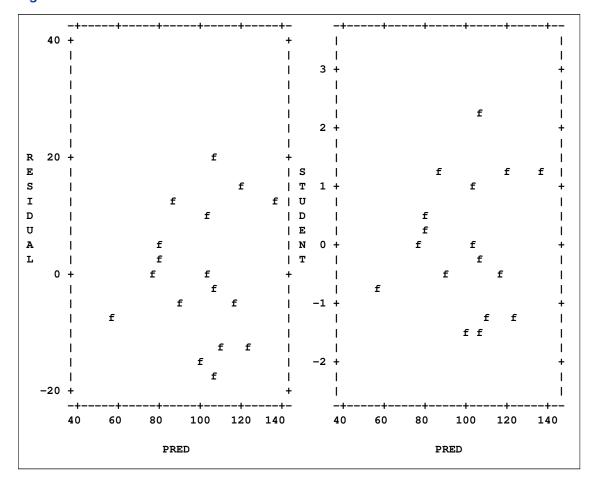


Figure 73.38 continued

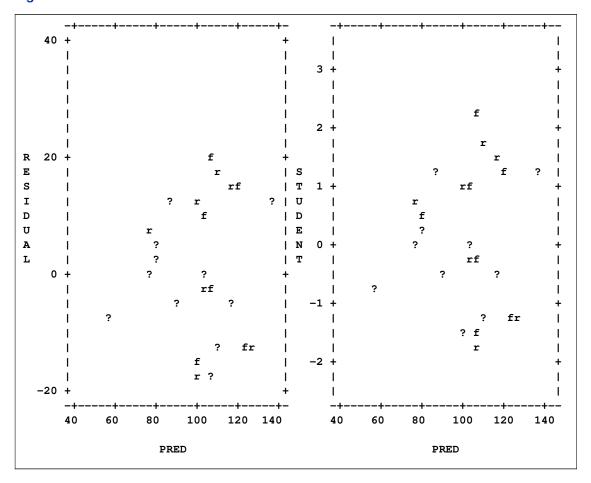
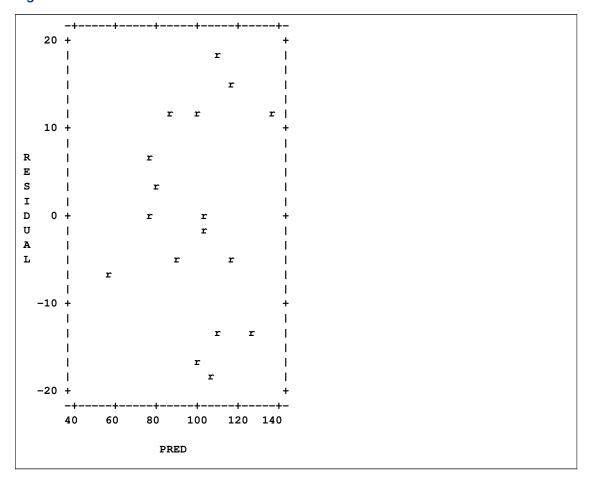


Figure 73.38 continued



Frequently, when the COLLECT option is in effect, you want the current and following PLOT statements to show only the specified plots. To do this, use both the CLEAR and NOCOLLECT options in the current PLOT statement.

Painting Scatter Plots

Painting scatter plots is a useful interactive tool that enables you to mark points of interest in scatter plots. Painting can be used to identify extreme points in scatter plots or to reveal the relationship between two scatter plots. The Class data (from the section "Simple Linear Regression" on page 5430) is used to illustrate some of these applications.

The following statements produce the scatter plot of the studentized residuals against the predicted values in Figure 73.39.

```
proc reg data=Class lineprinter;
  model Weight=Age Height / noprint;
  plot student.*p.;
run;
```

-2 +

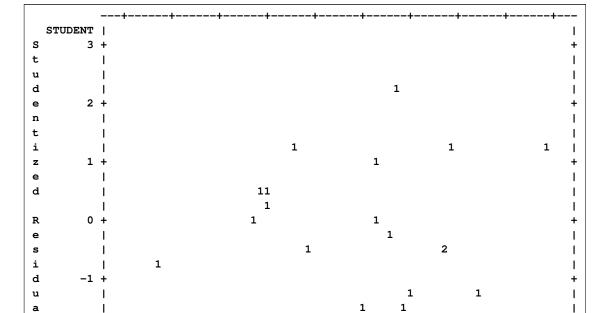


Figure 73.39 Plotting Studentized Residuals against Predicted Values

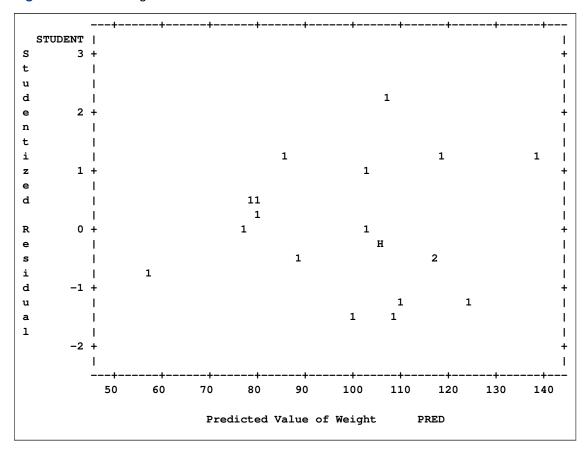
Then, the following statements identify the observation 'Henry' in the scatter plot and produce the plot in Figure 73.40:

Predicted Value of Weight

PRED

```
paint Name='Henry' / symbol = 'H';
plot;
run;
```



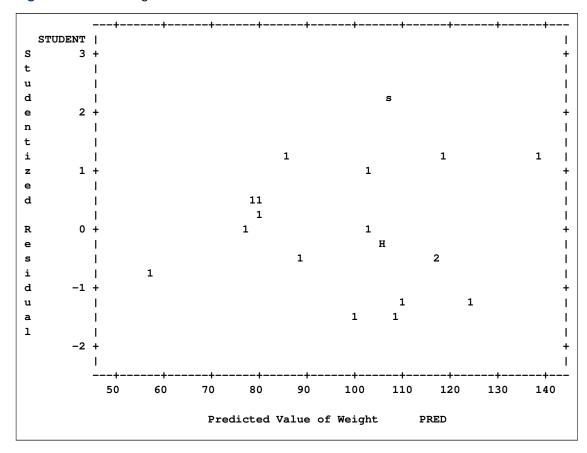


Next, the following statements identify observations with large absolute residuals:

```
paint student.>=2 or student.<=-2 / symbol='s';
plot;
run;</pre>
```

The log shows the observation numbers found with these conditions and gives the painting symbol and the number of observations found. Note that the previous PAINT statement is also used in the PLOT statement. Figure 73.41 shows the scatter plot produced by the preceding statements.

Figure 73.41 Painting Several Observations



The following statements relate two different scatter plots. These statements produce the plot in Figure 73.42.

```
paint student.>=1 / symbol='p';
paint student.<1 and student.>-1 / symbol='s';
paint student.<=-1 / symbol='n';
plot student. * p. cookd. * h. / hplots=2;
run;</pre>
```

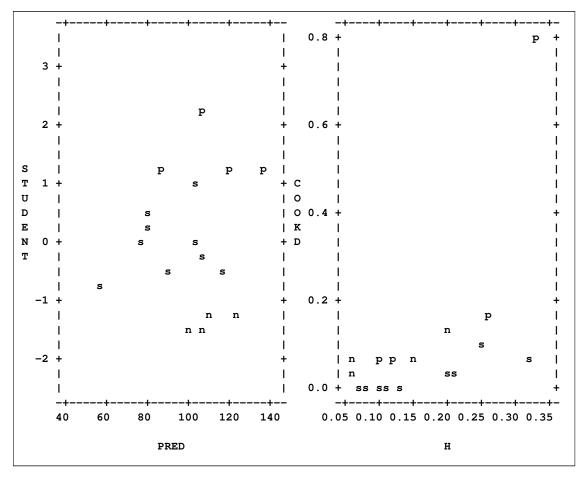


Figure 73.42 Painting Observations on More Than One Plot

Traditional Graphics

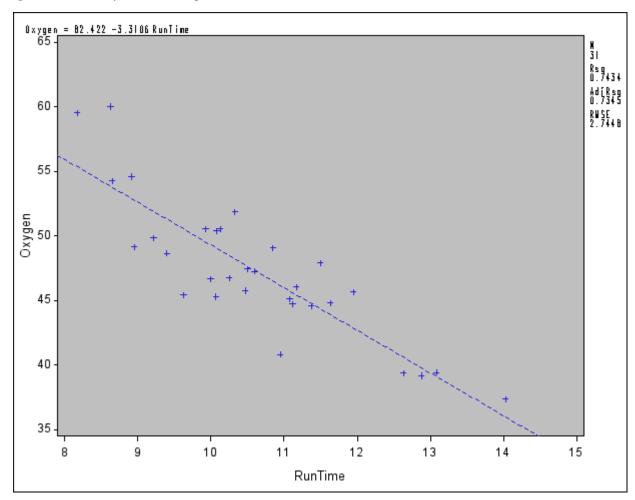
This section provides examples of using options available with the traditional graphics that you request with the PLOT statement. An alternative is to use ODS Graphics to obtain plots relevant to the analysis. See Example 73.1, Example 73.2, and Example 73.5 for examples of obtaining graphical displays with ODS Graphics. Examples in this section use the Fitness data set that is described in Example 73.2.

Traditional Graphics for Simple Linear Regression

The following statements introduce the basic PLOT statement graphics syntax. A simple linear regression of Oxygen on RunTime is performed, and a plot of Oxygen*RunTime is requested. The fitted model, the regression line, and the four default statistics are also displayed in Figure 73.43.

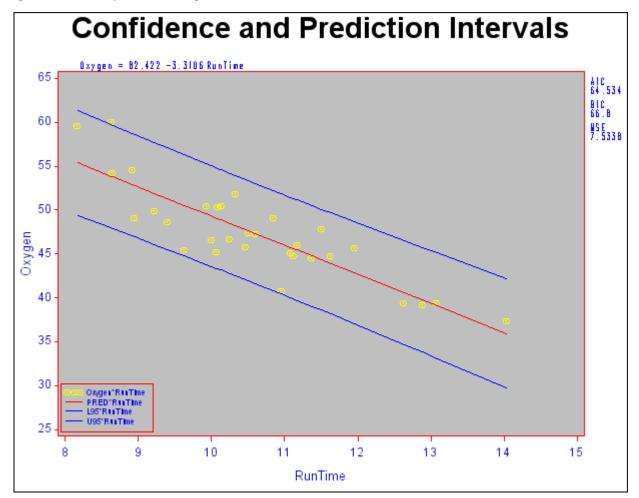
```
proc reg data=fitness;
  model Oxygen=RunTime;
  plot Oxygen*RunTime / cframe=ligr;
run;
```

Figure 73.43 Simple Linear Regression



You can use shorthand commands to plot the dependent variable, the predicted value, and the 95% confidence or prediction intervals against a regressor. The following statements use the CONF and PRED options to create a plot with confidence and prediction intervals. Results are displayed in Figure 73.44. Note that the statistics displayed by default in the margin are suppressed while three other statistics are exhibited. Furthermore, global graphics LEGEND and SYMBOL statements and PLOT statement options are used to control the appearance of the plot. For more information about the global graphics statements, see *SAS/GRAPH Software: Reference*.

Figure 73.44 Simple Linear Regression



Traditional Graphics for Variable Selection

When you use the SELECTION= option in the MODEL statement, you can produce plots showing model fit summary statistics for the models examined. The following statements produce the plot shown in Figure 73.45 of the C_p statistic for model selection plotted against the number of parameters in the model; the CHOCKING= and CMALLOWS= options draw useful reference lines.

In the GOPTIONS statement,

BORDER frames the entire display.

CBACK= specifies the background color.

CTEXT= selects the default color for the border and all text, including titles, footnotes, and

notes.

CTITLE= specifies the title, footnote, note, and border color.

HTEXT= specifies the height for all text in the display.

HTITLE= specifies the height for the first title line.

FTEXT= selects the default font for all text, including titles, footnotes, notes, the model

label and equation, the statistics, the axis labels, the tick values, and the legend.

FTITLE= specifies the first title font.

For more information about the GOPTIONS statement and other global graphics statements, see *SAS/GRAPH Software: Reference*.

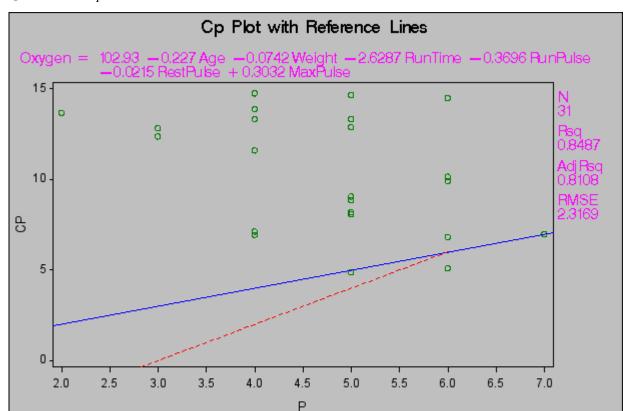


Figure 73.45 C_p Plot with Reference Lines

Traditional Normal Quantile and Normal Probability Plots

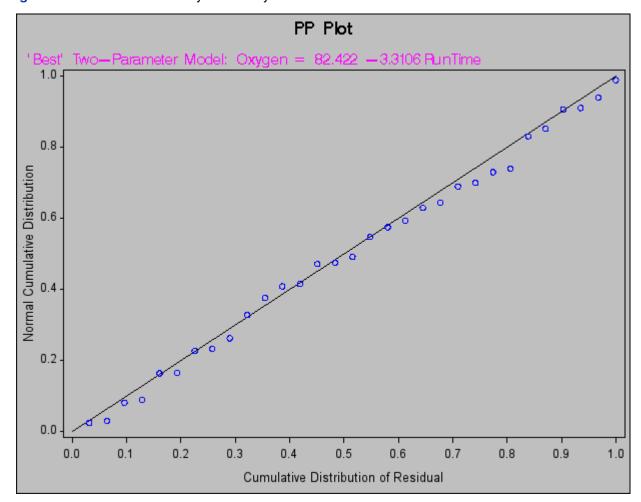
DOG CD#D

The following statements create probability-probability plots and quantile-quantile plots of the residuals (Figure 73.46 and Figure 73.47, respectively). An annotation data set is created to produce the (0,0)–(1,1) reference line for the P-P plot. Note that the NOSTAT option for the P-P plot suppresses the statistics that would be displayed in the margin.

2P - (P for full model) + 1

```
data annote1;
  length function color $8;
  retain ysys xsys '2' color 'black';
  function='move';
    x=0;
    y=0;
    output;
  function='draw';
    x=1;
    y=1;
    output;
run;
```

Figure 73.46 Normal Probability-Probability Plot for the Residuals



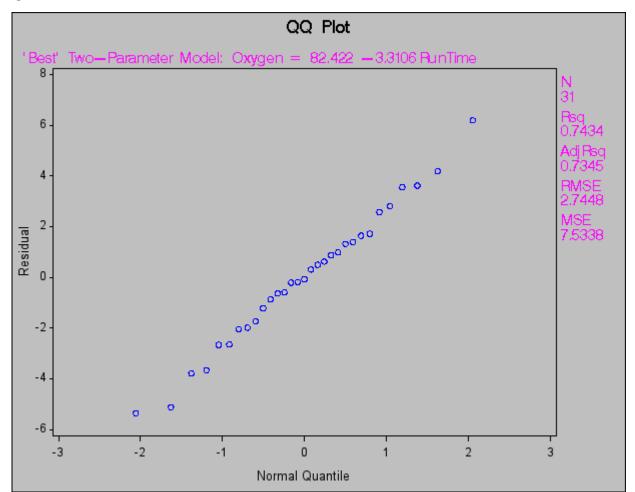


Figure 73.47 Normal Quantile-Quantile Plot for the Residuals

Models of Less Than Full Rank

If the model is not full rank, there are an infinite number of least squares solutions for the estimates. PROC REG chooses a nonzero solution for all variables that are linearly independent of previous variables and a zero solution for other variables. This solution corresponds to using a generalized inverse in the normal equations, and the expected values of the estimates are the Hermite normal form of **X** multiplied by the true parameters:

$$E(\mathbf{b}) = (\mathbf{X}'\mathbf{X})^{-}(\mathbf{X}'\mathbf{X})\boldsymbol{\beta}$$

Degrees of freedom for the zeroed estimates are reported as zero. The hypotheses that are not testable have t tests reported as missing. The message that the model is not full rank includes a display of the relations that exist in the matrix.

The following statements use the fitness data from Example 73.2. The variable Dif=RunPulse—RestPulse is created. When this variable is included in the model along with RunPulse and RestPulse, there is a linear dependency (or exact collinearity) between the independent variables. Figure 73.48 shows how this problem is diagnosed.

```
data fit2;
    set fitness; Dif=RunPulse-RestPulse;
proc reg data=fit2;
    model Oxygen=RunTime Age Weight RunPulse MaxPulse RestPulse Dif;
run;
```

Figure 73.48 Model That Is Not Full Rank: REG Procedure

			The REG E Model:		-				
		Depen	dent Vari	iable:	Oxygen				
		A	nalysis o	of Vari	iance				
			Sun	n of		Mean			
Source		DF	Squa	ares	s	quare	F V	Value	Pr > F
Model		6	722.54	1361	120.	42393	2	22.43	<.0001
Error		24	128.83	3794	5.	36825			
Corrected Total		30	851.38	3154					
Roc	t MSE		2.31	L695	R-Squa	re	0.848	87	
Dep	endent	Mean	47.37	7581	Adj R-		0.81	08	
Coe	ff Var		4.89	9057					
		P	arameter	Estima	ates				
		Para	meter	Sta	andard				
Variable	DF	Est	imate		Error	t Va	lue	Pr >	t
Intercept	1	102.	93448	12	. 40326	8	. 30	<.0	001
RunTime	1	-2.	62865	0	. 38456	-6	.84	<.0	001
Age	1	-0.	22697	0	.09984	-2	. 27	0.0	322
Weight	1	-0.	07418	0	. 05459	-1	.36	0.1	869
RunPulse	В	-0.	36963	0	.11985	-3	.08	0.0	051
MaxPulse	1	0.	30322	0	.13650	2	.22	0.0	360
RestPulse	В	-0.	02153	0	. 06605	-0	.33	0.7	473
Dif	0		0						

PROC REG produces a message informing you that the model is less than full rank. Parameters with DF=0 are not estimated, and parameters with DF=B are biased. In addition, the form of the linear dependency among the regressors is displayed.

Collinearity Diagnostics

When a regressor is nearly a linear combination of other regressors in the model, the affected estimates are unstable and have high standard errors. This problem is called *collinearity* or *multi-collinearity*. It is a good idea to find out which variables are nearly collinear with which other variables. The approach in PROC REG follows that of Belsley, Kuh, and Welsch (1980). PROC REG provides several methods for detecting collinearity with the COLLIN, COLLINOINT, TOL, and VIF options.

The COLLIN option in the MODEL statement requests that a collinearity analysis be performed. First, X'X is scaled to have 1s on the diagonal. If you specify the COLLINOINT option, the intercept variable is adjusted out first. Then the eigenvalues and eigenvectors are extracted. The analysis in PROC REG is reported with eigenvalues of X'X rather than singular values of X. The eigenvalues of X'X are the squares of the singular values of X.

The condition indices are the square roots of the ratio of the largest eigenvalue to each individual eigenvalue. The largest condition index is the condition number of the scaled X matrix. Belsey, Kuh, and Welsch (1980) suggest that, when this number is around 10, weak dependencies might be starting to affect the regression estimates. When this number is larger than 100, the estimates might have a fair amount of numerical error (although the statistical standard error almost always is much greater than the numerical error).

For each variable, PROC REG produces the proportion of the variance of the estimate accounted for by each principal component. A collinearity problem occurs when a component associated with a high condition index contributes strongly (variance proportion greater than about 0.5) to the variance of two or more variables.

The VIF option in the MODEL statement provides the variance inflation factors (VIF). These factors measure the inflation in the variances of the parameter estimates due to collinearities that exist among the regressor (independent) variables. There are no formal criteria for deciding if a VIF is large enough to affect the predicted values.

The TOL option requests the tolerance values for the parameter estimates. The tolerance is defined as 1/VIF.

For a complete discussion of the preceding methods, refer to Belsley, Kuh, and Welsch (1980). For a more detailed explanation of using the methods with PROC REG, refer to Freund and Littell (1986).

This example uses the COLLIN option on the fitness data found in Example 73.2. The following statements produce Figure 73.49.

Figure 73.49 Regression Using the TOL, VIF, and COLLIN Options

		•	The REG Proc	edure		
			Model: MOD	EL1		
		Depen	dent Variabl	e: Oxygen		
		A	nalysis of V	ariance		
			g	•		
a			Sum of		lean	
Source		DF	Squares	Squ	are F Val	lue Pr > F
Model		6	722.54361	120.42	393 22	.43 <.0001
Error		24	128.83794	5.36	825	
Corrected '	Total	30	851.38154			
		t MSE	2.31695	-		
	-	endent Mean	47.37581		0.8108	
	Coe	ff Var	4.89057			
		Pa	arameter Est	imates		
		Parameter	Standard			
Variable	DF	Estimate	Error	t Value	Pr > t	Tolerance
Intercept	1	102.93448	12.40326	8.30	<.0001	
RunTime	1	-2.62865	0.38456	-6.84	<.0001	0.62859
Age	1	-0.22697	0.09984	-2.27	0.0322	0.66101
Weight	1	-0.07418	0.05459	-1.36	0.1869	0.86555
RunPulse	1	-0.36963	0.11985	-3.08	0.0051	0.11852
MaxPulse	1	0.30322	0.13650	2.22	0.0360	0.11437
RestPulse	1	-0.02153	0.06605	-0.33	0.7473	0.70642
		Pa	arameter Est	imates		
				••		
				Variance		
		Varia	ole DF	Inflation		
		Inter	cept 1	0		
		RunTi	me 1	1.59087		
		Age	1	1.51284		
		Weigh	t 1	1.15533		
		RunPu	lse 1	8.43727		
		MaxPu	lse 1	8.74385		
		RestP	ulse 1	1.41559		

			Collineari	ty Diagn	ostics			
			Condition		Propor	tion of	Varia	tion
Number	Eig	envalue	Index	Inte	rcept	Run	Time	Ag
1		6.94991	1.00000	0.000	02326	0.0002	1086	0.0001545
2	(0.01868	19.29087	0.	00218	0.0	2522	0.1463
3	(0.01503	21.50072	0.000	61541	0.1	2858	0.1501
4	(0.00911	27.62115	0.	00638	0.6	0897	0.0318
5	(0.00607	33.82918	0.	00133	0.1	2501	0.1128
6	(0.00102	82.63757	0.	79966	0.0	9746	0.4966
7	0.0	0017947	196.78560	0.	18981	0.0	1455	0.0621
			Prop	ortion o	of Variat	ion		
Num	ber	Weig	_	Pulse		ulse		tPulse
	1	0.000196	551 0.000	00862	0.0000	0634	0.00	027850
	2	0.010	0.000	00244	0.0000	0743	0	.39064
	3	0.235	571 0.	00119	0.0	0125	0	.02809
	4	0.183	313 0.	00149	0.0	0123	0	.19030
	5	0.444	42 0.	01506	0.0	0833	0	.36475
	6	0.103	30 0.	06948	0.0	0561	0	.02026
	7	0.022	.83 0.	91277	0.9	8357	0	.00568

Model Fit and Diagnostic Statistics

Figure 73.49 continued

This section gathers the formulas for the statistics available in the MODEL, PLOT, and OUTPUT statements. The model to be fit is $\mathbf{Y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\epsilon}$, and the parameter estimate is denoted by $\mathbf{b} = (\mathbf{X}'\mathbf{X})^{-}\mathbf{X}'\mathbf{Y}$. The subscript i denotes values for the ith observation, the parenthetical subscript (i) means that the statistic is computed by using all observations except the ith observation, and the subscript jj indicates the jth diagonal matrix entry. The ALPHA= option in the PROC REG or MODEL statement is used to set the α value for the t statistics.

Table 73.8 contains the summary statistics for assessing the fit of the model.

Table 73.8 Formulas and Definitions for Model Fit Summary Statistics

MODEL Option or Statistic	Definition or Formula
n	the number of observations
p	the number of parameters including the intercept
i	1 if there is an intercept, 0 otherwise
$\hat{\sigma}^2$	the estimate of pure error variance from the SIGMA=
	option or from fitting the full model
SST ₀	the uncorrected total sum of squares for the dependent variable

Table 73.8 continued

MODEL Option or Statistic	Definition or Formula
SST ₁	the total sum of squares corrected for the mean for the
	dependent variable
SSE	the error sum of squares
MSE	$\frac{\text{SSE}}{n-p}$
R^2	$1 - \frac{\text{SSE}}{\text{SST}_i}$
ADJRSQ	$1 - \frac{(n-i)(1-R^2)}{n-p}$
AIC	$n \ln \left(\frac{\text{SSE}}{n} \right) + 2p$
BIC	$n \ln \left(\frac{\text{SSE}}{n} \right) + 2(p+2)q - 2q^2 \text{ where } q = \frac{n\hat{\sigma}^2}{\text{SSE}}$
$\mathrm{CP}\left(C_{p}\right)$	$\frac{\text{SSE}}{\hat{\sigma}^2} + 2p - n$
GMSEP	$\frac{\text{MSE}(n+1)(n-2)}{n(n-p-1)} = \frac{1}{n} S_p(n+1)(n-2)$
$\mathrm{JP}\left(J_{p} ight)$	$\frac{n+p}{n}$ MSE
PC	$\frac{n+p}{n-p}(1-R^2) = J_p\left(\frac{n}{SST_i}\right)$
PRESS	the sum of squares of $predr_i$ (see Table 73.9)
RMSE	$\sqrt{\text{MSE}}$
SBC	$n\ln\left(\frac{\mathrm{SSE}}{n}\right) + p\ln(n)$
$SP(S_p)$	$\frac{\text{MSE}}{n-p-1}$

Table 73.9 contains the diagnostic statistics and their formulas; these formulas and further information can be found in Chapter 4, "Introduction to Regression Procedures," and in the section "Influence Statistics" on page 5553. Each statistic is computed for each observation.

 Table 73.9
 Formulas and Definitions for Diagnostic Statistics

MODEL Option or Statistic	Formula
PRED $(\widehat{\mathbf{Y}}_i)$ RES (r_i) H (h_i)	$egin{aligned} \mathbf{X}_i \mathbf{b} \ \mathbf{Y}_i - \widehat{\mathbf{Y}}_i \ \mathbf{x}_i (\mathbf{X}'\mathbf{X})^- \mathbf{x}_i' \end{aligned}$
STDP	$\sqrt{h_i\widehat{\sigma}^2}$

Table 73.9 continued

MODEL Option or Statistic	Formula
STDI	$\sqrt{(1+h_i)\widehat{\sigma}^2}$
STDR	$\sqrt{(1-h_i)\widehat{\sigma}^2}$
LCL	$\widehat{Y}_i - t_{\frac{\alpha}{2}}$ STDI
LCLM	$\widehat{Y}_i - t_{\frac{\alpha}{2}}^2 \text{STDP}$
UCL	$\widehat{Y}_i + t_{\frac{\alpha}{2}}$ STDI
UCLM	$\widehat{Y}_i + t_{\frac{\alpha}{2}}^2 STDP$
STUDENT	$\frac{r_i}{\mathrm{STDR}_i}$
RSTUDENT	$\frac{r_i}{\hat{\sigma}_{(i)}\sqrt{1-h_i}}$
COOKD	$\frac{1}{p} \frac{\text{STDP}^2}{\text{STDR}^2}$ $\det(\hat{\sigma}_{(i)}^2(\mathbf{x}_{(i)}'\mathbf{x}_{(i)})^{-1}$
COVRATIO	$\frac{\det(\hat{\sigma}_{(i)}^2(\mathbf{x}_{(i)}'\mathbf{x}_{(i)})^{-1}}{\det(\hat{\sigma}_{(i)}^2(\mathbf{X}'\mathbf{X})^{-1})}$
DFFITS	$\frac{(\widehat{\mathbf{Y}}_i - \widehat{\mathbf{Y}}_{(i)})}{(\widehat{\sigma}_{(i)}\sqrt{h_i})}$
$DFBETAS_j$	$\frac{\mathbf{b}_{j} - \mathbf{b}_{(i)j}}{\hat{\sigma}_{(i)}\sqrt{(\mathbf{X}'\mathbf{X})_{jj}}}$
$PRESS(predr_i)$	$\frac{r_i}{1-h_i}$

Influence Statistics

This section discusses the INFLUENCE option, which produces several influence statistics, and the PARTIAL option, which produces partial regression leverage plots.

The INFLUENCE Option

The INFLUENCE option (in the MODEL statement) requests the statistics proposed by Belsley, Kuh, and Welsch (1980) to measure the influence of each observation on the estimates. Influential observations are those that, according to various criteria, appear to have a large influence on the parameter estimates.

Let $\mathbf{b}(i)$ be the parameter estimates after deleting the *i*th observation; let $s(i)^2$ be the variance estimate after deleting the *i*th observation; let $\mathbf{X}(i)$ be the \mathbf{X} matrix without the *i*th observation; let $\hat{y}(i)$ be the *i*th value predicted without using the *i*th observation; let $r_i = y_i - \hat{y}_i$ be the *i*th

residual; and let h_i be the *i*th diagonal of the projection matrix for the predictor space, also called the *hat matrix*:

$$h_i = \mathbf{x}_i (\mathbf{X}'\mathbf{X})^{-1} \mathbf{x}_i'$$

Belsley, Kuh, and Welsch (1980) propose a cutoff of 2p/n, where n is the number of observations used to fit the model and p is the number of parameters in the model. Observations with h_i values above this cutoff should be investigated.

For each observation, PROC REG first displays the residual, the studentized residual (RSTUDENT), and the h_i . The studentized residual RSTUDENT differs slightly from STUDENT since the error variance is estimated by $s_{(i)}^2$ without the ith observation, not by s^2 . For example,

$$RSTUDENT = \frac{r_i}{s_{(i)}\sqrt{(1-h_i)}}$$

Observations with RSTUDENT larger than 2 in absolute value might need some attention.

The COVRATIO statistic measures the change in the determinant of the covariance matrix of the estimates by deleting the *i*th observation:

$$\text{COVRATIO} = \frac{\det \left(s^2(i) (\mathbf{X}'_{(i)} \mathbf{X}_{(i)})^{-1} \right)}{\det \left(s^2 (\mathbf{X}' \mathbf{X})^{-1} \right)}$$

Belsley, Kuh, and Welsch (1980) suggest that observations with

$$|COVRATIO - 1| \ge \frac{3p}{n}$$

where p is the number of parameters in the model and n is the number of observations used to fit the model, are worth investigation.

The DFFITS statistic is a scaled measure of the change in the predicted value for the ith observation and is calculated by deleting the ith observation. A large value indicates that the observation is very influential in its neighborhood of the \mathbf{X} space.

DFFITS =
$$\frac{\hat{y}_i - \hat{y}_{(i)}}{s_{(i)}\sqrt{h_{(i)}}}$$

Large values of DFFITS indicate influential observations. A general cutoff to consider is 2; a size-adjusted cutoff recommended by Belsley, Kuh, and Welsch (1980) is $2\sqrt{p/n}$, where n and p are as defined previously.

The DFFITS statistic is very similar to Cook's D, defined in the section "Predicted and Residual Values" on page 5525.

The DFBETAS statistics are the scaled measures of the change in each parameter estimate and are calculated by deleting the ith observation:

DFBETAS_j =
$$\frac{b_j - b_{(i)j}}{s_{(i)} \sqrt{(\mathbf{X}'\mathbf{X})_{jj}}}$$

where $(\mathbf{X}'\mathbf{X})_{jj}$ is the (j, j)th element of $(\mathbf{X}'\mathbf{X})^{-1}$.

In general, large values of DFBETAS indicate observations that are influential in estimating a given parameter. Belsley, Kuh, and Welsch (1980) recommend 2 as a general cutoff value to indicate influential observations and $2/\sqrt{n}$ as a size-adjusted cutoff.

The following statements use the population example in the section "Polynomial Regression" on page 5434. See Figure 73.32 for the fitted regression equation. The INFLUENCE option produces the tables shown in Figure 73.50 and Figure 73.51.

```
proc reg data=USPopulation;
  model Population=Year YearSq / influence;
run;
```

Figure 73.50 Regression Using the INFLUENCE Option

		The REG Pr	ocedure		
		Model: M			
	Depe	ndent Variabl	e: Populatio	on	
		Output St	atistics		
		oucput be	aciscies		
			Hat Diag	Cov	
Obs	Residual	RStudent	Н	Ratio	DFFITS
1	-2.2837	-0.9361	0.3429	1.5519	-0.6762
2	-0.4146	-0.1540	0.2356	1.5325	-0.0855
3	0.6696	0.2379	0.1632	1.3923	0.1050
4	0.8849	0.3065	0.1180	1.3128	0.1121
5	0.5923	0.2021	0.0933	1.2883	0.0648
6	-0.0621	-0.0210	0.0831	1.2827	-0.0063
7	-0.1344	-0.0455	0.0824	1.2813	-0.0136
8	0.5864	0.1994	0.0870	1.2796	0.0615
9	0.0934	0.0318	0.0933	1.2969	0.0102
10	0.0354	0.0310	0.0990	1.3040	0.0102
11	1.4757	0.5090	0.1022	1.2550	0.0233
				1.2420	0.1717
12	1.6441	0.5680	0.1022		
13	3.4065	1.2109	0.0990	1.0320	0.4013
14	1.5922	0.5470	0.0933	1.2345	0.1755
15	1.7679	0.6064	0.0870	1.2123	0.1871
16	-7.5642	-3.2147	0.0824	0.3286	-0.9636
17	-7.4712	-3.1550	0.0831	0.3425	
18	-0.3731	-0.1272	0.0933	1.2936	-0.0408
19	1.2782	0.4440	0.1180	1.2906	0.1624
20	1.0356	0.3687	0.1632	1.3741	0.1628
21	-1.7068	-0.6406	0.2356	1.4380	-0.3557
22	4.7578	2.1312	0.3429	0.9113	1.5395
		Output Sta	tistics		
			-DFBETAS		
	Obs	Intercept	Year	YearSq	
	1	0.4024	0 4963	0.4802	
	1		0.4862		
	2	-0.0540	0.0531	-0.0523	
	3	0.0517	-0.0505	0.0494	
	4	0.0335	-0.0322	0.0310	
	5	0.0040	-0.0032	0.0025	
	6	0.0012	-0.0012	0.0013	
	7	0.0054	-0.0055	0.0056	
	8	-0.0339	0.0343	-0.0347	
	9	-0.0067	0.0067	-0.0068	
	10	-0.0182	0.0183	-0.0183	
	11	-0.1272	0.1275	-0.1276	
	12	-0.1426	0.1426	-0.1424	
	13	-0.2895	0.2889	-0.2880	
	14	-0.1173	0.1167	-0.1160	
	15	-0.1076	0.1067	-0.1056	
	16	0.4130	-0.4063	0.3987	
		0 0101	-0.2048	0.1957	
	17	0.2131			
	17 18	-0.0007	0.0012	-0.0016	
			0.0012 -0.0432	-0.0016 0.0449	
	18	-0.0007 0.0415	-0.0432		
	18 19	-0.0007		0.0449	

Figure 73.51 Residual Statistics

```
Sum of Residuals -4.7569E-11
Sum of Squared Residuals 170.97193
Predicted Residual SS (PRESS) 237.71229
```

In Figure 73.50, observations 16, 17, and 19 exceed the cutoff value of 2 for RSTUDENT. None of the observations exceeds the general cutoff of 2 for DFFITS or the DFBETAS, but observations 16, 17, and 19 exceed at least one of the size-adjusted cutoffs for these statistics. Observations 1 and 19 exceed the cutoff for the hat diagonals, and observations 1, 2, 16, 17, and 18 exceed the cutoffs for COVRATIO. Taken together, these statistics indicate that you should look first at observations 16, 17, and 19 and then perhaps investigate the other observations that exceeded a cutoff.

When you enable ODS Graphics, you can request influence diagnostic plots by using the PLOTS= option in the PROC REG statement as shown in the following statements:

```
ods graphics on;
proc reg data=USPopulation
        plots(label)=(CooksD RStudentByLeverage DFFITS DFBETAS);
   id Year;
   model Population=Year YearSq;
run;
ods graphics off;
```

The LABEL suboption specified in the PLOTS(LABEL)= option requests that observations that exceed the relevant cutoffs for the statistics being plotted are labeled. Since Year has been named in an ID statement, the value of Year is used for the labels. The requested plots are shown in Figure 73.52.

Figure 73.52 Influence Diagnostics

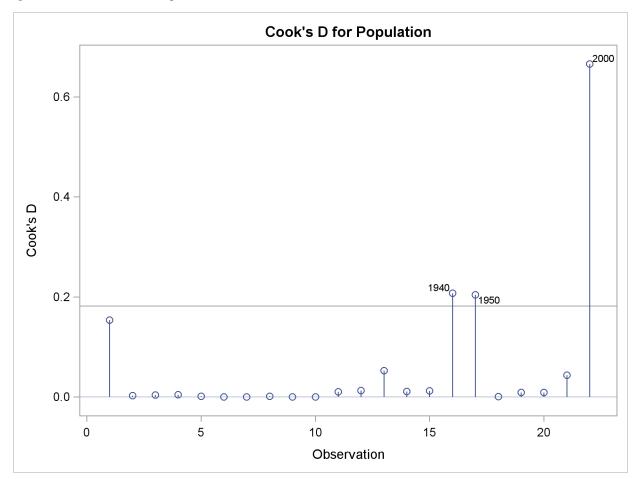


Figure 73.52 continued

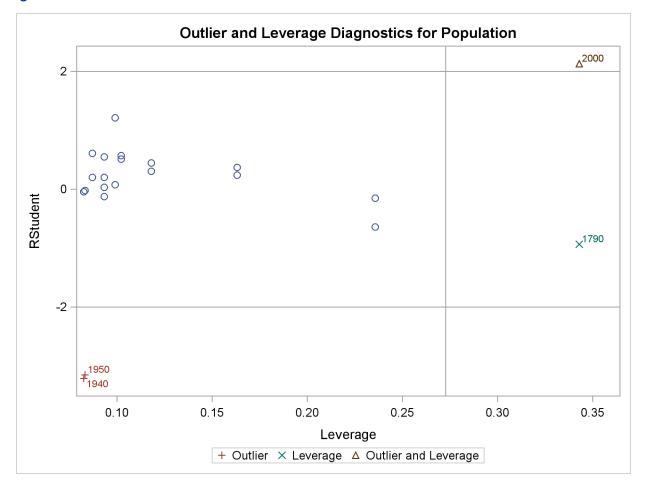


Figure 73.52 continued

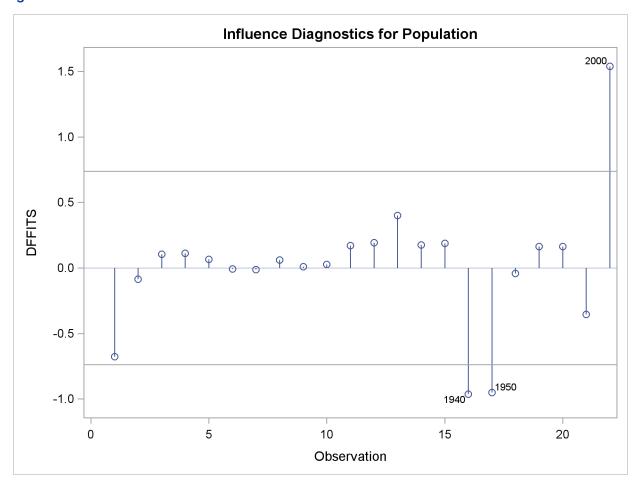
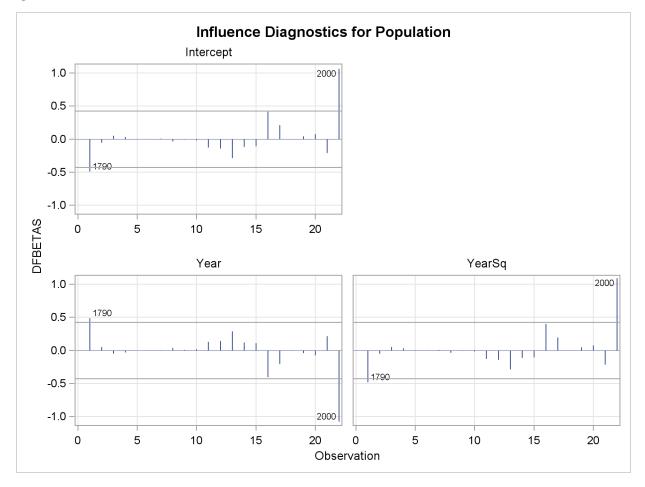


Figure 73.52 continued



The PARTIAL and PARTIALDATA Options

The PARTIAL option in the MODEL statement produces partial regression leverage plots. If ODS Graphics is not in effect, this option requires the use of the LINEPRINTER option in the PROC REG statement. One plot is created for each regressor in the current full model. For example, plots are produced for regressors included by using ADD statements; plots are not produced for interim models in the various model-selection methods but only for the full model. If you use a model-selection method and the final model contains only a subset of the original regressors, the PARTIAL option still produces plots for all regressors in the full model. If ODS Graphics is in effect, these plots are produced as high-resolution graphics, in panels with a maximum of six partial regression leverage plots per panel. Multiple panels are displayed for models with more than six regressors.

For a given regressor, the partial regression leverage plot is the plot of the dependent variable and the regressor after they have been made orthogonal to the other regressors in the model. These can be obtained by plotting the residuals for the dependent variable against the residuals for the selected regressor, where the residuals for the dependent variable are calculated with the selected regressor omitted, and the residuals for the selected regressor are calculated from a model where the selected regressor is regressed on the remaining regressors. A line fit to the points has a slope equal to the parameter estimate in the full model.

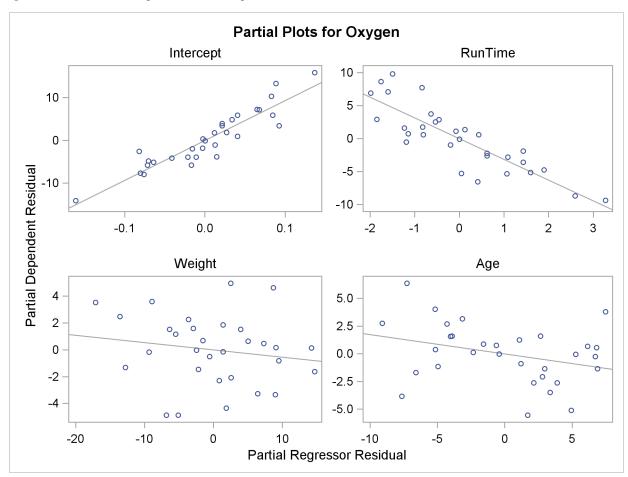
When ODS Graphics is not in effect, points in the plot are marked by the number of replicates appearing at one position. The symbol '*' is used if there are 10 or more replicates. If an ID statement is specified, the leftmost nonblank character in the value of the ID variable is used as the plotting symbol.

The PARTIALDATA option in the MODEL statement produces a table that contains the partial regression data that are displayed in the partial regression leverage plots. You can request partial regression data even if you do not requests plots with the PARTIAL option.

The following statements use the fitness data in Example 73.2 with the PARTIAL option and the ODS GRAPHICS statement to produce the partial regression leverage plots. The plots are shown in Figure 73.53.

```
ods graphics on;
proc reg data=fitness;
  model Oxygen=RunTime Weight Age / partial;
run;
ods graphics off;
```

Figure 73.53 Partial Regression Leverage Plots



Reweighting Observations in an Analysis

Reweighting observations is an interactive feature of PROC REG that enables you to change the weights of observations used in computing the regression equation. Observations can also be deleted from the analysis (not from the data set) by changing their weights to zero. In the following statements, the Class data (in the section "Getting Started: REG Procedure" on page 5430) are used to illustrate some of the features of the REWEIGHT statement. First, the full model is fit, and the residuals are displayed in Figure 73.54.

```
proc reg data=Class;
  model Weight=Age Height / p;
  id Name;
run;
```

Figure 73.54 Full Model for Class Data, Residuals Shown

		Model: MODEI	_	
	Depend	lent Variable:	Weight	
	C	output Statist	ics	
		Dependent	Predicted	
Obs	Name	Variable	Value	Residual
1	Alfred	112.5000	124.8686	-12.3686
2	Alice	84.0000	78.6273	5.3727
3	Barbara	98.0000	110.2812	-12.2812
4	Carol	102.5000	102.5670	-0.0670
5	Henry	102.5000	105.0849	-2.5849
6	James	83.0000	80.2266	2.7734
7	Jane	84.5000	89.2191	-4.7191
8	Janet	112.5000	102.7663	9.7337
9	Jeffrey	84.0000	100.2095	-16.2095
10	John	99.5000	86.3415	13.1585
11	Joyce	50.5000	57.3660	-6.8660
12	Judy	90.0000	107.9625	-17.9625
13	Louise	77.0000	76.6295	0.3705
14	Mary	112.0000	117.1544	-5.1544
15	Philip	150.0000	138.2164	11.7836
16	Robert	128.0000	107.2043	20.7957
17	Ronald	133.0000	118.9529	14.0471
18	Thomas	85.0000	79.6676	5.3324
19	William	112.0000	117.1544	-5.1544
Sı	ım of Residua	ıls		0
	ım of Squared	-	2120.0	9974
	-	dual SS (PRES		

Upon examining the data and residuals, you realize that observation 17 (Ronald) was mistakenly included in the analysis. Also, you would like to examine the effect of reweighting to 0.5 those observations with residuals that have absolute values greater than or equal to 17. The following statements show how you request this reweighting:

```
reweight obs.=17;
reweight r. le -17 or r. ge 17 / weight=0.5;
print p;
run;
```

At this point, a message appears (in the log) that tells you which observations have been reweighted and what the new weights are. Figure 73.55 is produced.

Figure 73.55 Model with Reweighted Observations

		mha DEC	Duagaduna		
			Procedure MODEL1.2		
	_			_	
	L	Dependent Var	iabie: weigh	ıc	
		Output	Statistics		
		Weight	Dependent	Predicted	
Obs	Name	Variable	Variable	Value	Residual
1	Alfred	1.0000	112.5000	121.6250	-9.1250
2	Alice	1.0000	84.0000	79.9296	4.0704
3	Barbara	1.0000	98.0000	107.5484	-9.5484
4	Carol	1.0000	102.5000	102.1663	0.3337
5	Henry	1.0000	102.5000	104.3632	-1.8632
6	James	1.0000	83.0000	79.9762	3.0238
7	Jane	1.0000	84.5000	87.8225	-3.3225
8	Janet	1.0000	112.5000	103.6889	8.8111
9	Jeffrey	1.0000	84.0000	98.7606	-14.7606
10	John	1.0000	99.5000	85.3117	14.1883
11	Joyce	1.0000	50.5000	58.6811	-8.1811
12	Judy	0.5000	90.0000	106.8740	-16.8740
13	Louise	1.0000	77.0000	76.8377	0.1623
14	Mary	1.0000	112.0000	116.2429	-4.2429
15	Philip	1.0000	150.0000	135.9688	14.0312
16	Robert	0.5000	128.0000	103.5150	24.4850
17	Ronald	0	133.0000	117.8121	15.1879
18	Thomas	1.0000	85.0000	78.1398	6.8602
19	William	1.0000	112.0000	116.2429	-4.2429
	Sum of Re	esiduals		0	
	Sum of So	quared Residu	als	1500.61194	
		d Residual SS		2287.57621	
			,,	2	

The first REWEIGHT statement excludes observation 17, and the second REWEIGHT statement reweights observations 12 and 16 to 0.5. An important feature to note from this example is that the model is not refit until after the PRINT statement. REWEIGHT statements do not cause the model to be refit. This is so that multiple REWEIGHT statements can be applied to a subsequent model.

In this example, since the intent is to reweight observations with large residuals, the observation that was mistakenly included in the analysis should be deleted; then the model should be fit for those remaining observations, and the observations with large residuals should be reweighted. To accomplish this, use the REFIT statement. Note that the model label has been changed from MODEL1 to MODEL1.2 since two REWEIGHT statements have been used. The following statements produce Figure 73.56:

```
reweight allobs / weight=1.0;
reweight obs.=17;
refit;
reweight r. le -17 or r. ge 17 / weight=.5;
print;
run;
```

Figure 73.56 Observations Excluded from Analysis, Model Refitted, and Observations Reweighted

			Procedure MODEL1.5		
	,	Model. Dependent Var		+	
		bependent var	Table. Weigh		
		Output	Statistics		
		Weight	Dependent	Predicted	
Obs	Name	Variable	Variable	Value	Residual
1	Alfred	1.0000	112.5000	120.9716	-8.4716
2	Alice	1.0000	84.0000	79.5342	4.4658
3	Barbara	1.0000	98.0000	107.0746	-9.0746
4	Carol	1.0000	102.5000	101.5681	0.9319
5	Henry	1.0000	102.5000	103.7588	-1.2588
6	James	1.0000	83.0000	79.7204	3.2796
7	Jane	1.0000	84.5000	87.5443	-3.0443
8	Janet	1.0000	112.5000	102.9467	9.5533
9	Jeffrey	1.0000	84.0000	98.3117	-14.3117
10	John	1.0000	99.5000	85.0407	14.4593
11	Joyce	1.0000	50.5000	58.6253	-8.1253
12	Judy	1.0000	90.0000	106.2625	-16.2625
13	Louise	1.0000	77.0000	76.5908	0.4092
14	Mary	1.0000	112.0000	115.4651	-3.4651
15	Philip	1.0000	150.0000	134.9953	15.0047
16	Robert	0.5000	128.0000	103.1923	24.8077
17	Ronald	0	133.0000	117.0299	15.9701
18	Thomas	1.0000	85.0000	78.0288	6.9712
19	William	1.0000	112.0000	115.4651	-3.4651
	Sum of R	esiduals		0	
	Sum of S	quared Residu	als	1637.81879	
	Predicte	d Residual SS	(PRESS)	2473.87984	

Notice that this results in a slightly different model than the previous set of statements: only observation 16 is reweighted to 0.5. Also note that the model label is now MODEL1.5 since five REWEIGHT statements have been used for this model.

Another important feature of the REWEIGHT statement is the ability to nullify the effect of a previous or all REWEIGHT statements. First, assume that you have several REWEIGHT statements in effect and you want to restore the original weights of all the observations. The following REWEIGHT statement accomplishes this and produces Figure 73.57:

```
reweight allobs / reset;
print;
run;
```

Figure 73.57 Restoring Weights of All Observations

	7	The REG Proced Model: MODEL1	-	
	Depend	lent Variable:		
	c	Output Statist	ics	
		Dependent	Predicted	
Obs	Name	Variable	Value	Residual
1	Alfred	112.5000	124.8686	-12.3686
2	Alice	84.0000	78.6273	5.3727
3	Barbara	98.0000	110.2812	-12.2812
4	Carol	102.5000	102.5670	-0.0670
5	Henry	102.5000	105.0849	-2.5849
6	James	83.0000	80.2266	2.7734
7	Jane	84.5000	89.2191	-4.7191
8	Janet	112.5000	102.7663	9.7337
9	Jeffrey	84.0000	100.2095	-16.2095
10	John	99.5000	86.3415	13.1585
11	Joyce	50.5000	57.3660	-6.8660
12	Judy	90.0000	107.9625	-17.9625
13	Louise	77.0000	76.6295	0.3705
14	Mary	112.0000	117.1544	-5.1544
15	Philip	150.0000	138.2164	11.7836
16	Robert	128.0000	107.2043	20.7957
17	Ronald	133.0000	118.9529	14.0471
18	Thomas	85.0000	79.6676	5.3324
19	William	112.0000	117.1544	-5.1544
Su	m of Residua	ıls		0
Su	m of Squared	l Residuals	2120.09	9974
Pr	edicted Resi	dual SS (PRES	s) 3272.72	2186

The resulting model is identical to the original model specified at the beginning of this section. Notice that the model label is now MODEL1.6. Note that the Weight column does not appear, since all observations have been reweighted to have weight=1.

Now suppose you want only to undo the changes made by the most recent REWEIGHT statement. Use REWEIGHT UNDO for this. The following statements produce Figure 73.58:

```
reweight r. le -12 or r. ge 12 / weight=.75;
reweight r. le -17 or r. ge 17 / weight=.5;
reweight undo;
print;
run;
```

Figure 73.58 Example of UNDO in REWEIGHT Statement

			Procedure MODEL1.9		
				_	
	1	Dependent Var	iabie: weign	.τ	
		Output	Statistics		
		Weight	Dependent	Predicted	
Obs	Name	Variable	Variable	Value	Residual
1	Alfred	0.7500	112.5000	125.1152	-12.6152
2	Alice	1.0000	84.0000	78.7691	5.2309
3	Barbara	0.7500	98.0000	110.3236	-12.3236
4	Carol	1.0000	102.5000	102.8836	-0.3836
5	Henry	1.0000	102.5000	105.3936	-2.8936
6	James	1.0000	83.0000	80.1133	2.8867
7	Jane	1.0000	84.5000	89.0776	-4.5776
8	Janet	1.0000	112.5000	103.3322	9.1678
9	Jeffrey	0.7500	84.0000	100.2835	-16.2835
10	John	0.7500	99.5000	86.2090	13.2910
11	Joyce	1.0000	50.5000	57.0745	-6.5745
12	Judy	0.7500	90.0000	108.2622	-18.2622
13	Louise	1.0000	77.0000	76.5275	0.4725
14	Mary	1.0000	112.0000	117.6752	-5.6752
15	Philip	1.0000	150.0000	138.9211	11.0789
16	Robert	0.7500	128.0000	107.0063	20.9937
17	Ronald	0.7500	133.0000	119.4681	13.5319
18	Thomas	1.0000	85.0000	79.3061	5.6939
19	William	1.0000	112.0000	117.6752	-5.6752
	Sum of Residuals			0	
	Sum of S	quared Residu	1694.87114		
	Predicted	d Residual SS	2547.22751		

The resulting model reflects changes made only by the first REWEIGHT statement since the third REWEIGHT statement negates the effect of the second REWEIGHT statement. Observations 1, 3, 9, 10, 12, 16, and 17 have their weights changed to 0.75. Note that the label MODEL1.9 reflects the use of nine REWEIGHT statements for the current model.

Now suppose you want to reset the observations selected by the most recent REWEIGHT statement to their original weights. Use the REWEIGHT statement with the RESET option to do this. The following statements produce Figure 73.59:

```
reweight r. le -12 or r. ge 12 / weight=.75;
reweight r. le -17 or r. ge 17 / weight=.5;
reweight / reset;
print;
run;
```

Figure 73.59 REWEIGHT Statement with RESET option

			Procedure				
	_		MODEL1.12				
	I	Dependent Var	iable: Weigh	t			
Output Statistics							
		Weight	Dependent	Predicted			
Obs	Name	Variable	Variable	Value	Residual		
1	Alfred	0.7500	112.5000	126.0076	-13.5076		
2	Alice	1.0000	84.0000	77.8727	6.1273		
3	Barbara	0.7500	98.0000	111.2805	-13.2805		
4	Carol	1.0000	102.5000	102.4703	0.0297		
5	Henry	1.0000	102.5000	105.1278	-2.6278		
6	James	1.0000	83.0000	80.2290	2.7710		
7	Jane	1.0000	84.5000	89.7199	-5.2199		
8	Janet	1.0000	112.5000	102.0122	10.4878		
9	Jeffrey	0.7500	84.0000	100.6507	-16.6507		
10	John	0.7500	99.5000	86.6828	12.8172		
11	Joyce	1.0000	50.5000	56.7703	-6.2703		
12	Judy	1.0000	90.0000	108.1649	-18.1649		
13	Louise	1.0000	77.0000	76.4327	0.5673		
14	Mary	1.0000	112.0000	117.1975	-5.1975		
15	Philip	1.0000	150.0000	138.7581	11.2419		
16	Robert	1.0000	128.0000	108.7016	19.2984		
17	Ronald	0.7500	133.0000	119.0957	13.9043		
18	Thomas	1.0000	85.0000	80.3076	4.6924		
19	William	1.0000	112.0000	117.1975	-5.1975		
	Sum of Residuals			0			
	Sum of So	quared Residu	1879.08980				
	Predicted	d Residual SS	2959.57279				

Note that observations that meet the condition of the second REWEIGHT statement (residuals with an absolute value greater than or equal to 17) now have weights reset to their original value of 1. Observations 1, 3, 9, 10, and 17 have weights of 0.75, but observations 12 and 16 (which meet the condition of the second REWEIGHT statement) have their weights reset to 1.

Notice how the last three examples show three ways to change weights back to a previous value. In the first example, ALLOBS and the RESET option are used to change weights for all observations back to their original values. In the second example, the UNDO option is used to negate the effect of a previous REWEIGHT statement, thus changing weights for observations selected in the previous REWEIGHT statement to the weights specified in still another REWEIGHT statement. In the third example, the RESET option is used to change weights for observations selected in a pre-

vious REWEIGHT statement back to their original values. Finally, note that the label MODEL1.12 indicates that 12 REWEIGHT statements have been applied to the original model.

Testing for Heteroscedasticity

The regression model is specified as $y_i = \mathbf{x}_i \boldsymbol{\beta} + \epsilon_i$, where the ϵ_i 's are identically and independently distributed: $E(\epsilon) = 0$ and $E(\epsilon' \epsilon) = \sigma^2 \mathbf{I}$. If the ϵ_i 's are not independent or their variances are not constant, the parameter estimates are unbiased, but the estimate of the covariance matrix is inconsistent.

In the case of heteroscedasticity, if the regression data are from a simple random sample, then White (1980), showed that matrix

$$HC_0 = (X'X)^{-1}(X'\text{diag}(e_i^2)X)(X'X)^{-1}$$

where

$$e_i = y_i - \mathbf{x}_i \mathbf{b}$$

is an asymptotically consistent estimate of the covariance matrix. MacKinnon and White (1985) introduced three alternative heteroscedasticity-consistent covariance matrix estimators that are all asymptotically equivalent to the estimator HC_0 but that typically have better small sample behavior. These estimators labeled HC_1 , HC_2 , and HC_3 are defined as follows:

$$HC_1 = \frac{n}{n-p}HC_0$$

where n is the number of observations and p is the number of regressors including the intercept.

$$HC_2 = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\operatorname{diag}(\frac{e_i^2}{1 - h_{ii}})\mathbf{X}(\mathbf{X}'\mathbf{X})^{-1}$$

where

$$h_{ii} = \mathbf{x}_i (\mathbf{X}'\mathbf{X})^{-1} \mathbf{x}_i'$$

is the leverage of the ith observation.

$$HC_3 = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\operatorname{diag}(\frac{e_i^2}{(1 - h_{ii})^2})\mathbf{X}(\mathbf{X}'\mathbf{X})^{-1}$$

Long and Ervin (2000) studied the performance of these estimators and recommend using the HC₃ estimator if the sample size is less than 250.

You can use the HCCMETHOD=0,1,2, or 3 in the MODEL statement to select a heteroscedasticity-consistent covariance matrix estimator, with HC₀ being the default. The ACOV option in the MODEL statement displays the heteroscedasticity-consistent covariance matrix estimator in effect and adds heteroscedasticity-consistent standard errors, also known as White standard errors, to the parameter estimates table. If you specify the HCC or WHITE option in the MODEL statement, but do not also specify the ACOV option, then the heteroscedasticity-consistent standard errors are added to the parameter estimates table but the heteroscedasticity- consistent covariance matrix is not displayed.

The SPEC option performs a model specification test. The null hypothesis for this test maintains that the errors are homoscedastic and independent of the regressors and that several technical assumptions about the model specification are valid. For details, see theorem 2 and assumptions 1–7 of White (1980). When the model is correctly specified and the errors are independent of the regressors, the rejection of this null hypothesis is evidence of heteroscedasticity. In implementing this test, an estimator of the average covariance matrix (White 1980, p. 822) is constructed and inverted. The nonsingularity of this matrix is one of the assumptions in the null hypothesis about the model specification. When PROC REG determines this matrix to be numerically singular, a generalized inverse is used and a note to this effect is written to the log. In such cases, care should be taken in interpreting the results of this test.

When you specify the SPEC, ACOV, HCC, or WHITE option in the MODEL statement, tests listed in the TEST statement are performed with both the usual covariance matrix and the heteroscedasticity-consistent covariance matrix requested with the HCCMETHOD= option. Tests performed with the consistent covariance matrix are asymptotic. For more information, refer to White (1980).

Both the ACOV and SPEC options can be specified in a MODEL or PRINT statement.

Testing for Lack of Fit

The test for lack of fit compares the variation around the model with "pure" variation within replicated observations. This measures the adequacy of the specified model. In particular, if there are n_i replicated observations Y_{i1}, \ldots, Y_{in_i} of the response all at the same values \mathbf{x}_i of the regressors, then you can predict the true response at \mathbf{x}_i either by using the predicted value \hat{Y}_i based on the model or by using the mean \bar{Y}_i of the replicated values. The test for lack of fit decomposes the residual error into a component due to the variation of the replications around their mean value (the "pure" error) and a component due to the variation of the mean values around the model prediction (the "bias" error):

$$\sum_{i} \sum_{j=1}^{n_i} (Y_{ij} - \hat{Y}_i)^2 = \sum_{i} \sum_{j=1}^{n_i} (Y_{ij} - \bar{Y}_i)^2 + \sum_{i} n_i (\bar{Y}_i - \hat{Y}_i)^2$$

If the model is adequate, then both components estimate the nominal level of error; however, if the bias component of error is much larger than the pure error, then this constitutes evidence that there is significant lack of fit.

If some observations in your design are replicated, you can test for lack of fit by specifying the LACKFIT option in the MODEL statement (see Example 73.6). Note that, since all other tests use total error rather than pure error, you might want to hand-calculate the tests with respect to pure error if the lack of fit is significant. On the other hand, significant lack of fit indicates that the specified model is inadequate, so if this is a problem you can also try to refine the model.

Multivariate Tests

The MTEST statement described in the section "MTEST Statement" on page 5474 can test hypotheses involving several dependent variables in the form

$$(\mathbf{L}\boldsymbol{\beta} - \mathbf{c}\mathbf{j})\mathbf{M} = 0$$

where **L** is a linear function on the regressor side, β is a matrix of parameters, **c** is a column vector of constants, **j** is a row vector of ones, and **M** is a linear function on the dependent side. The special case where the constants are zero is

$$\mathbf{L}\boldsymbol{\beta}\mathbf{M} = 0$$

To test this hypothesis, PROC REG constructs two matrices called \mathbf{H} and \mathbf{E} that correspond to the numerator and denominator of a univariate F test:

$$H = M'(LB - cj)'(L(X'X)^{-}L')^{-1}(LB - cj)M$$

$$\mathbf{E} = \mathbf{M}'(\mathbf{Y}'\mathbf{Y} - \mathbf{B}'(\mathbf{X}'\mathbf{X})\mathbf{B})\mathbf{M}$$

These matrices are displayed for each MTEST statement if the PRINT option is specified.

Four test statistics based on the eigenvalues of $\mathbf{E}^{-1}\mathbf{H}$ or $(\mathbf{E} + \mathbf{H})^{-1}\mathbf{H}$ are formed. These are Wilks' lambda, Pillai's trace, the Hotelling-Lawley trace, and Roy's greatest root. These test statistics are discussed in Chapter 4, "Introduction to Regression Procedures."

The following code creates MANOVA data from Morrison (1976):

```
* Manova Data from Morrison (1976, 190);
data a;
input sex $ drug $ @;
do rep=1 to 4;
   input y1 y2 @;
   sexcode=(sex='m')-(sex='f');
  drug1=(drug='a')-(drug='c');
  drug2=(drug='b')-(drug='c');
  sexdrug1=sexcode*drug1;
  sexdrug2=sexcode*drug2;
   output;
end;
datalines;
ma 5 6 5 4 9 9 7 6
m b 7 6 7 7 9 12 6 8
m c 21 15 14 11 17 12 12 10
fa 7 10 6 6 9 7 8 10
f b 10 13 8 7 7 6 6 9
f c 16 12 14 9 14 8 10 5
```

The following statements perform a multivariate analysis of variance and produce Figure 73.60 through Figure 73.63:

```
proc reg;
  model y1 y2=sexcode drug1 drug2 sexdrug1 sexdrug2;
  y1y2drug: mtest y1=y2, drug1,drug2;
  drugshow: mtest drug1, drug2 / print canprint;
run;
```

Figure 73.60 Multivariate Analysis of Variance: REG Procedure

		The REG Proced Model: MODEL	-		
	Dep	endent Variabl	.e: y1		
	A	analysis of Var	riance		
		Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > F
Model	5	316.00000	63.20000	12.04	<.0001
Error	18	94.50000	5.25000		
Corrected Total	23	410.50000			
Root MS	SE	2.29129	R-Square	0.7698	
Depende	ent Mean	9.75000	Adj R-Sq	0.7058	
Coeff V	/ar	23.50039			

Figure 73.60 continued

Parameter Estimates								
		Parameter	Standard					
Variable	DF	Estimate	Error	t Value	Pr > t			
Intercept	1	9.75000	0.46771	20.85	<.0001			
sexcode	1	0.16667	0.46771	0.36	0.7257			
drug1	1	-2.75000	0.66144	-4.16	0.0006			
drug2	1	-2.25000	0.66144	-3.40	0.0032			
sexdrug1	1	-0.66667	0.66144	-1.01	0.3269			
sexdrug2	1	-0.41667	0.66144	-0.63	0.5366			

Figure 73.61 Multivariate Analysis of Variance: REG Procedure

		A	nalysis of	f Varia	nce				
			Sum	of	1	Mean			
Source		DF	Squar	res	Squ	uare	F	Value	Pr > I
Model		5	69.333	333	13.86	6667		2.19	0.1008
Error		18	114.000	000	6.33	3333			
Corrected Total		23	183.33	333					
Roc	t MSE		2.51	661	R-Square	e	0.3	782	
Dep	endent 1	l ean	8.66	667 .	Adj R-S	a	0.2	055	
Coe	ff Var		29.03	782					
		P	arameter 1	Estimat	es				
		Para	meter	Stan	dard				
Variable	DF	Est	imate	E	rror	t Va	lue	Pr >	t
Intercept	1	8.	66667	0.5	1370	16	. 87	<.0	0001
sexcode	1	0.	16667	0.5	1370	0	. 32	0.	7493
drug1	1	-1.	41667	0.7	2648	-1	. 95	0.0	0669
drug2	1	-0.	16667	0.7	2648	-0	. 23	0.8	8211
sexdrug1	1	-1.	16667	0.7	2648	-1	. 61	0.3	1257
sexdrug2	1	-0.	41667	0.7	2648	-0	. 57	0.	5734

Figure 73.62 Multivariate Analysis of Variance: First Test

The REG Procedure Model: MODEL1 Multivariate Test: y1y2drug Multivariate Statistics and Exact F Statistics M=0S=1 N=8 Value F Value Statistic Num DF Den DF Pr > F23.08
23.08
23.08
Hotelling-Lawley Trace 2.56456456 23.08
Roy's Greatest Root 2.56456456 23.08 Wilks' Lambda Pillai's Trace Wilks' Lambda 0.28053917 23.08 2 18 <.0001 2 2 2 18 <.0001 18 <.0001 2 18 <.0001

The four multivariate test statistics are all highly significant, giving strong evidence that the coefficients of drug1 and drug2 are not the same across dependent variables y1 and y2.

Figure 73.63 Multivariate Analysis of Variance: Second Test

Figure 73.63 continued

		Adju	sted	Approxim	ate		Squa	red
Canon				Stand	ard	Ca	anoni	cal
Correla	tion	Correlat	tion	Er	ror	Cor	relat	ion
0.90	5903	0.89	9927	0.040	101	(0.820	661
0.24	4371			0.210	254	(0.059	717
		Eigen [,]	values	of Inv(E)	*H			
		-						
Eigen	value	Differ	ence	Proporti	on	Cumu	lative	e
1 4	.5760	4.!	5125	0.98	63	(0.986	3
2 0	.0635			0.01	37	:	1.000	0
Test of	HO: Th	ne canonio	cal cor	relations	in t	the		
						-		
Likelih	ood	Approxima	ate					
Ra	tio	F Va	lue	Num DF	Den	DF	Pr >	F
0.16862	952	12	. 20	4		34	<.000	01
0.94028	273	1	. 14	1		18	0.29	91
Multivar	iate St	atistics	and F	Approxima	tions	5		
	S=2	M=-0.	5 N=	7.5				
		Value	F Val	ue Num	DF	Den	DF	Pr > 1
	0.16	862952	12.	20	4		34	<.000
•	0.88	3037810	7.	08	4		36	0.000
ey Trace	4.63	3953666	19.	40	4	19.4	407	<.000
Root	4.57	1602675	41.	18	2		18	<.000
	Correla 0.90 0.24 Eigen 1 4 2 0 Test of curre Likelih Ra 0.16862 0.94028 Multivar	0.905903 0.244371 Eigenvalue 1	Canonical Canonical Correlation O.905903	Correlation Correlation 0.905903	Canonical Canonical Stand Correlation Correlation Er 0.905903	Canonical Canonical Standard Correlation Correlation Error 0.905903 0.899927 0.040101 0.244371 . 0.210254 Eigenvalues of Inv(E)*H = CanRsq/(1-CanRsq) Eigenvalue Difference Proportion 1 4.5760 4.5125 0.9863 2 0.0635 0.0137 Test of H0: The canonical correlations in current row and all that follow are zero Likelihood Approximate Ratio F Value Num DF Den 0.16862952 12.20 4 0.94028273 1.14 1 Multivariate Statistics and F Approximations S=2 M=-0.5 N=7.5 Value F Value Num DF 0.16862952 12.20 4 0.88037810 7.08 4 ey Trace 4.63953666 19.40 4	Canonical Canonical Standard Carcelation Correlation Error Correlation Error Correlation Error Correlation Error Correlation 0.905903 0.899927 0.040101 0.210254 0.00101 0.244371 0.210254 0.00101 0.210254 0.00101 0.244371 0.210254 0.00101 0.210254 0.00101 0.210254 0.00101 0.210254 0.00101 0.01010101	Canonical Canonical Standard Canonical Correlation Correlation Error Correlat: 0.905903 0.899927 0.040101 0.8200 0.244371

The four multivariate test statistics are all highly significant, giving strong evidence that the coefficients of drug1 and drug2 are not zero for both dependent variables.

Autocorrelation in Time Series Data

When regression is performed on time series data, the errors might not be independent. Often errors are autocorrelated; that is, each error is correlated with the error immediately before it. Autocorrelation is also a symptom of systematic lack of fit. The DW option provides the Durbin-Watson d statistic to test that the autocorrelation is zero:

$$d = \frac{\sum_{i=2}^{n} (e_i - e_{i-1})^2}{\sum_{i=1}^{n} e_i^2}$$

The value of d is close to 2 if the errors are uncorrelated. The distribution of d is reported by Durbin and Watson (1951). Tables of the distribution are found in most econometrics textbooks, such as Johnston (1972) and Pindyck and Rubinfeld (1981).

The sample autocorrelation estimate is displayed after the Durbin-Watson statistic. The sample is computed as

$$r = \frac{\sum_{i=2}^{n} e_i e_{i-1}}{\sum_{i=1}^{n} e_i^2}$$

This autocorrelation of the residuals might not be a very good estimate of the autocorrelation of the true errors, especially if there are few observations and the independent variables have certain patterns. If there are missing observations in the regression, these measures are computed as though the missing observations did not exist.

Positive autocorrelation of the errors generally tends to make the estimate of the error variance too small, so confidence intervals are too narrow and true null hypotheses are rejected with a higher probability than the stated significance level. Negative autocorrelation of the errors generally tends to make the estimate of the error variance too large, so confidence intervals are too wide and the power of significance tests is reduced. With either positive or negative autocorrelation, least squares parameter estimates are usually not as efficient as generalized least squares parameter estimates. For more details, refer to Judge et al. (1985, Chapter 8) and the SAS/ETS User's Guide.

The following SAS statements request the DWPROB option for the U.S. population data (see Figure 73.64). If you use the DW option instead of the DWPROB option, then *p*-values are not produced.

```
proc reg data=USPopulation;
  model Population=Year YearSq / dwProb;
run;
```

Figure 73.64 Regression Using DW Option

```
The REG Procedure

Model: MODEL1

Dependent Variable: Population

Durbin-Watson D 1.191

Pr < DW 0.0050

Pr > DW 0.9950

Number of Observations 22

1st Order Autocorrelation 0.323
```

Computations for Ridge Regression and IPC Analysis

In ridge regression analysis, the crossproduct matrix for the independent variables is centered (the NOINT option is ignored if it is specified) and scaled to one on the diagonal elements. The ridge constant k (specified with the RIDGE= option) is then added to each diagonal element of the crossproduct matrix. The ridge regression estimates are the least squares estimates obtained by using the new crossproduct matrix.

Let **X** be an $n \times p$ matrix of the independent variables after centering the data, and let **Y** be an $n \times 1$ vector corresponding to the dependent variable. Let **D** be a $p \times p$ diagonal matrix with diagonal elements as in **X'X**. The ridge regression estimate corresponding to the ridge constant k can be computed as

$$\mathbf{D}^{-\frac{1}{2}}(\mathbf{Z}'\mathbf{Z} + k\mathbf{I}_p)^{-1}\mathbf{Z}'\mathbf{Y}$$

where $\mathbf{Z} = \mathbf{X}\mathbf{D}^{-\frac{1}{2}}$ and \mathbf{I}_p is a $p \times p$ identity matrix.

For IPC analysis, the smallest m eigenvalues of $\mathbf{Z}'\mathbf{Z}$ (where m is specified with the PCOMIT= option) are omitted to form the estimates.

For information about ridge regression and IPC standardized parameter estimates, parameter estimate standard errors, and variance inflation factors, refer to Rawlings (1988), Neter, Wasserman, and Kutner (1990), and Marquardt and Snee (1975). Unlike Rawlings (1988), the REG procedure uses the mean squared errors of the submodels instead of the full model MSE to compute the standard errors of the parameter estimates.

Construction of Q-Q and P-P Plots

If a normal probability-probability or quantile-quantile plot for the variable x is requested, the n nonmissing values of x are first ordered from smallest to largest:

$$x_{(1)} \le x_{(2)} \le \cdots \le x_{(n)}$$

If a Q-Q plot is requested (with a PLOT statement of the form PLOT *yvariable**NQQ.), the *i*th-ordered value $x_{(i)}$ is represented by a point with *y*-coordinate $x_{(i)}$ and *x*-coordinate $\Phi^{-1}\left(\frac{i-0.375}{n+0.25}\right)$, where $\Phi(\cdot)$ is the standard normal distribution.

If a P-P plot is requested (with a PLOT statement of the form PLOT yvariable*NPP.), the ith-ordered value $x_{(i)}$ is represented by a point with y-coordinate $\frac{i}{n}$ and x-coordinate $\Phi\left(\frac{x_{(i)}-\mu}{\sigma}\right)$, where μ is the mean of the nonmissing x-values and σ is the standard deviation. If an x-value has multiplicity k (that is, $x_{(i)} = \cdots = x_{(i+k-1)}$), then only the point $\left(\Phi\left(\frac{x_{(i)}-\mu}{\sigma}\right), \frac{i+k-1}{n}\right)$ is displayed.

Computational Methods

The REG procedure first composes a crossproducts matrix. The matrix can be calculated from input data, reformed from an input correlation matrix, or read in from an SSCP data set. For each model, the procedure selects the appropriate crossproducts from the main matrix. The normal equations formed from the crossproducts are solved by using a sweep algorithm (Goodnight 1979). The method is accurate for data that are reasonably scaled and not too collinear.

The mechanism that PROC REG uses to check for singularity involves the diagonal (pivot) elements of **X'X** as it is being swept. If a pivot is less than SINGULAR*CSS, then a singularity is declared and the pivot is not swept (where CSS is the corrected sum of squares for the regressor and SINGULAR is machine dependent but is approximately 1E–7 on most machines or reset in the PROC REG statement).

The sweep algorithm is also used in many places in the model-selection methods. The RSQUARE method uses the leaps-and-bounds algorithm by Furnival and Wilson (1974).

Computer Resources in Regression Analysis

The REG procedure is efficient for ordinary regression; however, requests for optional features can greatly increase the amount of time required.

The major computational expense in the regression analysis is the collection of the crossproducts matrix. For p variables and n observations, the time required is proportional to np^2 . For each model run, PROC REG needs time roughly proportional to k^3 , where k is the number of regressors in the model. Include an additional nk^2 for the R, CLM, or CLI option and another nk^2 for the INFLUENCE option.

Most of the memory that PROC REG needs to solve large problems is used for crossproducts matrices. PROC REG requires $4p^2$ bytes for the main crossproducts matrix plus $4k^2$ bytes for the largest model. If several output data sets are requested, memory is also needed for buffers.

See the section "Input Data Sets" on page 5502 for information about how to use TYPE=SSCP data sets to reduce computing time.

Displayed Output

Many of the more specialized tables are described in detail in previous sections. Most of the formulas for the statistics are in Chapter 4, "Introduction to Regression Procedures," while other formulas can be found in the section "Model Fit and Diagnostic Statistics" on page 5551 and the section "Influence Statistics" on page 5553.

The analysis-of-variance table includes the following:

- the Source of the variation, Model for the fitted regression, Error for the residual error, and C Total for the total variation after correcting for the mean. The Uncorrected Total Variation is produced when the NOINT option is used.
- the degrees of freedom (DF) associated with the source
- the Sum of Squares for the term
- the Mean Square, the sum of squares divided by the degrees of freedom
- the F Value for testing the hypothesis that all parameters are zero except for the intercept. This is formed by dividing the mean square for Model by the mean square for Error.
- the Prob>F, the probability of getting a greater F statistic than that observed if the hypothesis is true. This is the significance probability.

Other statistics displayed include the following:

- Root MSE is an estimate of the standard deviation of the error term. It is calculated as the square root of the mean square error.
- Dep Mean is the sample mean of the dependent variable.
- C.V. is the coefficient of variation, computed as 100 times Root MSE divided by Dep Mean. This expresses the variation in unitless values.
- R-square is a measure between 0 and 1 that indicates the portion of the (corrected) total variation that is attributed to the fit rather than left to residual error. It is calculated as SS(Model) divided by SS(Total). It is also called the *coefficient of determination*. It is the square of the multiple correlation—in other words, the square of the correlation between the dependent variable and the predicted values.
- Adj R-square, the adjusted R^2 , is a version of R^2 that has been adjusted for degrees of freedom. It is calculated as

$$\bar{R}^2 = 1 - \frac{(n-i)(1-R^2)}{n-p}$$

where i is equal to 1 if there is an intercept and 0 otherwise, n is the number of observations used to fit the model, and p is the number of parameters in the model.

The parameter estimates and associated statistics are then displayed, and they include the following:

- the Variable used as the regressor, including the name Intercept to represent the estimate of the intercept parameter
- the degrees of freedom (DF) for the variable. There is one degree of freedom unless the model is not full rank.

- the Parameter Estimate
- the Standard Error, the estimate of the standard deviation of the parameter estimate
- T for H0: Parameter=0, the *t* test that the parameter is zero. This is computed as the Parameter Estimate divided by the Standard Error.
- the Prob > |T|, the probability that a t statistic would obtain a greater absolute value than that observed given that the true parameter is zero. This is the two-tailed significance probability.

If model-selection methods other than NONE, RSQUARE, ADJRSQ, and CP are used, the analysis-of-variance table and the parameter estimates with associated statistics are produced at each step. Also displayed are the following:

- C(p), which is Mallows' C_p statistic
- bounds on the condition number of the correlation matrix for the variables in the model (Berk 1977)

After statistics for the final model are produced, the following is displayed when the method chosen is FORWARD, BACKWARD, or STEPWISE:

• a Summary table listing Step number, Variable Entered or Removed, Partial and Model R-square, and C(p) and F statistics

The RSQUARE method displays its results beginning with the model containing the fewest independent variables and producing the largest R^2 . Results for other models with the same number of variables are then shown in order of decreasing R^2 , and so on, for models with larger numbers of variables. The ADJRSQ and CP methods group models of all sizes together and display results beginning with the model having the optimal value of adjusted R^2 and C_p , respectively.

For each model considered, the RSQUARE, ADJRSQ, and CP methods display the following:

- Number in Model or IN, the number of independent variables used in each model
- R-square or RSQ, the squared multiple correlation coefficient

If the B option is specified, the RSQUARE, ADJRSQ, and CP methods produce the following:

• Parameter Estimates, the estimated regression coefficients

If the B option is not specified, the RSQUARE, ADJRSQ, and CP methods display the following:

Variables in Model, the names of the independent variables included in the model

ODS Table Names

PROC REG assigns a name to each table it creates. You can use these names to reference the table when using the Output Delivery System (ODS) to select tables and create output data sets. These names are listed in the following table. For more information about ODS, see Chapter 20, "Using the Output Delivery System."

Table 73.10 ODS Tables Produced by PROC REG

ODS Table Name	Description	Statement	Option
ACovEst	Consistent covariance of estimates matrix	MODEL	ALL, ACOV
ACovTestANOVA	Test ANOVA using ACOV estimates	TEST	ACOV (MODEL statement)
ANOVA	Model ANOVA table	MODEL	default
CanCorr	Canonical correlations for hypothesis combinations	MTEST	CANPRINT
CollinDiag	Collinearity Diagnostics table	MODEL	COLLIN
CollinDiagNoInt	Collinearity Diagnostics for no intercept model	MODEL	COLLINOINT
ConditionBounds	Bounds on condition number	MODEL	(SELECTION=BACKWARD FORWARD STEPWISE MAXR MINR) and DETAILS
Corr	Correlation matrix for analysis variables	PROC	ALL, CORR
CorrB	Correlation of estimates	MODEL	CORRB
CovB	Covariance of estimates	MODEL	COVB
CrossProducts	Bordered model X'X matrix	MODEL	ALL, XPX
DWStatistic	Durbin-Watson statistic	MODEL	ALL, DW
DependenceEquations	Linear dependence equations	MODEL	default if needed
Eigenvalues	MTest eigenvalues	MTEST	CANPRINT
Eigenvectors	MTest eigenvectors	MTEST	CANPRINT
EntryStatistics	Entry statistics for selection methods	MODEL	(SELECTION=BACKWARD FORWARD STEPWISE MAXR MINR) and DETAILS
ErrorPlusHypothesis	MTest error plus hypothesis matrix H + E	MTEST	PRINT
ErrorSSCP	MTest error matrix E	MTEST	PRINT
FitStatistics	Model fit statistics	MODEL	default
HypothesisSSCP	MTest hypothesis matrix	MTEST	PRINT
InvMTestCov	Inv(L Ginv(X'X) L') and Inv(Lb-c)	MTEST	DETAILS

Table 73.10 continued

ODS Table Name	Description	Statement	Option
InvTestCov	Inv(L Ginv(X'X) L') and Inv(Lb-c)	TEST	PRINT
InvXPX	Bordered X'X inverse matrix	MODEL	I
MTestCov	L Ginv(X'X) L' and Lb-c	MTEST	DETAILS
MTransform	MTest matrix M , across dependents	MTEST	DETAILS
MultStat	Multivariate test statistics	MTEST	default
NObs	Number of observations		default
OutputStatistics	Output statistics table	MODEL	ALL, CLI, CLM, INFLUENCE, P, R
PartialData	Partial regression leverage data	MODEL	PARTIALDATA
ParameterEstimates	Model parameter estimates	MODEL	default
RemovalStatistics	Removal statistics for selection methods	MODEL	(SELECTION=BACKWARD STEPWISE MAXR MINR) and DETAILS
ResidualStatistics	Residual statistics and PRESS statistic	MODEL	ALL, CLI, CLM, INFLUENCE, P, R
SelParmEst	Parameter estimates for selection methods	MODEL	SELECTION=BACKWARD FORWARD STEPWISE MAXR MINR
SelectionSummary	Selection summary for FORWARD, BACKWARD, and STEPWISE methods	MODEL	SELECTION=BACKWARD FORWARD STEPWISE
SeqParmEst	Sequential parameter estimates	MODEL	SEQB
SimpleStatistics	Simple statistics for analysis variables	PROC	ALL, SIMPLE
SpecTest	White's heteroscedasticity test	MODEL	ALL, SPEC
SubsetSelSummary	Selection summary for R-square, Adj-RSq, and Cp methods	MODEL	SELECTION=RSQUARE ADJRSQ CP
TestANOVA	Test ANOVA table	TEST	default
TestCov	L Ginv(X'X) L' and Lb-c	TEST	PRINT
USSCP	Uncorrected SSCP matrix for analysis variables	PROC	ALL, USSCP

ODS Graphics

This section describes the use of ODS for creating statistical graphs with the REG procedure. To request these graphs you must specify the ODS GRAPHICS statement. For more information about the ODS GRAPHICS statement, see Chapter 21, "Statistical Graphics Using ODS." The following sections describe the ODS graphical displays produced by PROC REG.

Diagnostics Panel

The "Diagnostics Panel" provides a display that you can use to get an overall assessment of your model. See Figure 73.8 for an example.

The panel contains the following plots:

- residuals versus the predicted values
- externally studentized residuals (RSTUDENT) versus the predicted values
- externally studentized residuals versus the leverage
- normal quantile-quantile plot (Q-Q plot) of the residuals
- dependent variable values versus the predicted values
- Cook's D versus observation number
- histogram of the residuals
- "Residual-Fit" (or RF) plot consisting of side-by-side quantile plots of the centered fit and the residuals
- box plot of the residuals if you specify the STATS=NONE suboption

Patterns in the plots of residuals or studentized residuals versus the predicted values, or spread of the residuals being greater than the spread of the centered fit in the RF plot, are indications of an inadequate model. Patterns in the spread about the 45-degree reference line in the plot of the dependent variable values versus the predicted values are also indications of an inadequate model.

The Q-Q plot, residual histogram, and box plot of the residuals are useful for diagnosing violations of the normality and homoscedasticity assumptions. If the data in a Q-Q plot come from a normal distribution, the points will cluster tightly around the reference line. A normal density is overlaid on the residual histogram to help in detecting departures form normality.

Following Rawlings (1998), reference lines are shown on the relevant plots to identify observations deemed outliers or influential. Observations whose externally studentized residual magnitudes exceed 2 are deemed outliers. Observations whose leverage value exceeds 2p/n or whose Cook's D value exceeds 4/n are deemed influential (p is the number of regressors including the intercept, and n is the number of observations used in the analysis). If you specify the LABEL suboption of

the PLOTS=DIAGNOSTICS option, then the points deemed outliers or influential are labeled on the appropriate plots.

Fit statistics are shown in the lower right of the plot and can be customized or suppressed by using the STATS= suboption of the PLOTS=DIAGNOSTICS option.

Residuals by Regressor Plots

Panels of plots of the residuals versus each of the regressors in the model are produced by default. Patterns in these plots are indications of an inadequate model. To help in detecting patterns, you can use the SMOOTH= suboption of the PLOTS=RESIDUALS option to add loess fits to these residual plots. See Figure 73.1.6 for an example.

Fit and Prediction Plots

A fit plot consisting of a scatter plot of the data overlaid with the regression line, as well as confidence and prediction limits, is produced for models depending on a single regressor. Fit statistics are shown to the right of the plot and can be customized or suppressed by using the STATS= suboption of the PLOTS=FIT option.

When a model contains more than one regressor, a fit plot is not appropriate. However, if all the regressors in the model are transformations of a single variable in the input data set, then you can request a scatter plot of the dependent variable overlaid with a fit line and confidence and prediction limits versus this variable. You can also plot residuals versus this variable. You request these plots, shown in a panel, with the PLOTS=PREDICTION option. See Figure 73.13 for an example.

Influence Plots

In addition to the "Cook's D Plot" and the "RStudent By Leverage Plot," you can request plots of the DFBETAS and DFFITS statistics versus observation number by using the PLOTS=DFBETAS and PLOTS=DFFITS options. You can also obtain partial regression leverage plots by using the PLOTS=PARTIAL option. See the section "Influence Statistics" on page 5553 for examples of these plots and details about their interpretation.

Ridge and VIF Plots

When you use ridge regression, you can request plots of the variance inflation factor (VIF) values and standardized ridge estimates by ridge values for each coefficient with the PLOTS=RIDGE option. See Example 73.5 for examples.

Variable Selection Plots

When you request variable selection by using the SELECTION= option in the MODEL statement, you can request plots of fit criteria for the models examined by using the PLOTS=CRITERIA

option. The fit criteria are displayed versus the step number for the FORWARD, BACKWARD, and STEPWISE selection methods and the step at which the optimal value of each criterion is obtained is indicated using a "Star" marker. For the all-subset-based selection methods (SELEC-TION=RSQUARE|ADJRSQ|CP), the fit criteria are displayed versus the number of observations in the model.

The criteria are shown in a panel, but you can use the UNPACK suboption of the PLOTS=CRITERIA option to obtain separate plots for each criterion. You can also use the LABEL suboption of the PLOTS=CRITERIA option to request that optimal models be labeled on the plots. Example 73.2 provides several examples.

ODS Graph Names

PROC REG assigns a name to each graph it creates using ODS. You can use these names to reference the graphs when using ODS. The names are listed in Table 73.11.

To request these graphs you must specify the ODS GRAPHICS statement. For more information about the ODS GRAPHICS statement, see Chapter 21, "Statistical Graphics Using ODS."

Table 73.11 ODS Graphical Displays Produced by PROC REG

ODS Graph Name	Plot Description	PLOTS Option
AdjrsqPlot	Adjusted R-square statistic for models examined doing variable selection	ADJRSQ
AICPlot	AIC statistic for models examined doing variable selection	AIC
BICPlot	BIC statistic for models examined doing variable selection	BIC
CooksDPlot	Cook's <i>D</i> statistic versus observation number	COOKSD
CPPlot	C_p statistic for models examined doing variable selection	СР
DFFITSPlot	DFFITS statistics versus observa- tion number	DFFITS
DFBETASPanel	Panel of DFBETAS statistics versus observation number	DFBETAS
DFBETASPlot	DFBETAS statistics versus observa- tion number	DFBETAS(UNPACK)
DiagnosticsPanel	Panel of fit diagnostics	DIAGNOSTICS
FitPlot	Regression line, confidence limits, and prediction limits overlaid on scatter plot of data	FIT
ObservedByPredicted	Dependent variable versus predicted values	OBSERVEDBYPREDICTED
PartialPlot	Partial regression plot	PARTIAL
PredictionPanel	Panel of residuals and fit versus specified variable	PREDICTIONS

Table 73.11 continued

ODS Graph Name	Plot Description	PLOTS Option
PredictionPlot	Regression line, confidence limits, and prediction limits versus specified variable	PREDICTIONS(UNPACK)
PredictionResidualPlot	Residuals versus specified variable	PREDICTIONS(UNPACK)
QQPlot	Normal quantile plot of residuals	QQ
ResidualBoxPlot	Box plot of residuals	BOXPLOT
ResidualByPredicted	Residuals versus predicted values	RESIDUALBYPREDICTED
ResidualHistogram	Histogram of fit residuals	RESIDUALHISTOGRAM
ResidualPlot	Plot of residuals versus regressor	RESIDUALS
RFPlot	Side-by-side plots of quantiles of centered fit and residuals	RF
RidgePanel	Plot of VIF and ridge traces	RIDGE
RidgePlot	Plot of ridge traces	RIDGE(UNPACK)
RSquarePlot	R-square statistic for models examined doing variable selection	RSQUARE
RStudentByLeverage	Studentized residuals versus leverage	RSTUDENTBYLEVERAGE
RStudentByPredicted	Studentized residuals versus predicted values	RSTUDENTBYPREDITED
SBCPlot	SBC statistic for models examined doing variable selection	SBC
SelectionCriterionPanel	Panel of fit statistics for models examined doing variable selection	CRITERIA
VIFPlot	Plot of VIF traces	RIDGE(UNPACK)

Examples: REG Procedure

Example 73.1: Modeling Salaries of Major League Baseball Players

This example features the use of ODS Graphics in the process of building models by using the REG procedure and highlights the use of fit and influence diagnostics.

The following data set contains salary and performance information for Major League Baseball players who played at least one game in both the 1986 and 1987 seasons, excluding pitchers. The salaries (*Sports Illustrated*, April 20, 1987) are for the 1987 season and the performance measures are from 1986 (Collier Books, *The 1987 Baseball Encyclopedia Update*).

```
data baseball;
   length name $ 18;
   length team $ 12;
   input name $ 1-18 no_atbat no_hits no_home no_runs no_rbi no_bb yr_major
         cr_atbat cr_hits cr_home cr_runs cr_rbi cr_bb league $
         division $ team $ position $ no_outs no_assts no_error salary;
   logSalary = log10(salary);
   label name="Player's Name"
      no_hits="Hits in 1986"
      no runs="Runs in 1986"
      no_rbi="RBIs in 1986"
      no bb="Walks in 1986"
      yr_major="Years in MLB"
      cr_hits="Career Hits"
      salary="1987 Salary in $ Thousands"
      logSalary = "log10(Salary)";
   datalines;
Allanson, Andy
                      293
                             66
                                    1
                                         30
                                                29
                                                      14
                        1
                            293
                                   66
                                          1
                                                30
                                                      29
                                                            14
                    American East Cleveland C 446 33 20 .
                      315
                             81
                                    7
                                         24
                                                38
                                                      39
Ashby, Alan
                       14 3449
                                  835
                                         69
                                               321
                                                     414
                                                           375
                    National West Houston C 632 43 10 475
Davis, Alan
                      479
                            130
                                   18
                                         66
                                                72
                                                      76
                        3 1624
                                               224
                                                     266
                                  457
                                         63
                                                           263
                    American West Seattle 1B 880 82 14 480
                                                      37
                      496
                            141
                                   20
                                         65
                                                78
Dawson, Andre
                                               828
                                                     838
                       11 5628 1575
                                        225
                    National East Montreal RF 200 11 3 500
                      321
                             87
                                   10
                                         39
                                                42
                                                      30
Galarraga, Andres
                        2
                            396
                                  101
                                         12
                                                48
                                                      46
                                                            33
                    National East Montreal 1B 805 40 4 91.5
Griffin, Alfredo
                      594
                            169
                                    4
                                         74
                                                51
                                                      35
                      11 4408 1133
                                         19
                                               501
                                                     336
                                                           194
... more lines ...
                      631
                            170
                                    9
                                         77
                                                44
                                                      31
Wilson, Willie
                       11 4908 1457
                                         30
                                               775
                                                     357
                    American West KansasCity CF 408 4 3 1000
;
```

Suppose you want to investigate whether you can model the players' salaries for the 1987 season based on batting statistics for the previous season and lifetime batting performance. Since the variation in salaries is much greater for higher salaries, it is appropriate to apply a log transformation for this analysis. The following statements begin the analysis:

```
ods graphics on;
proc reg data=baseball;
  id name team league;
  model logSalary = no_hits no_runs no_rbi no_bb yr_major cr_hits;
run;
```

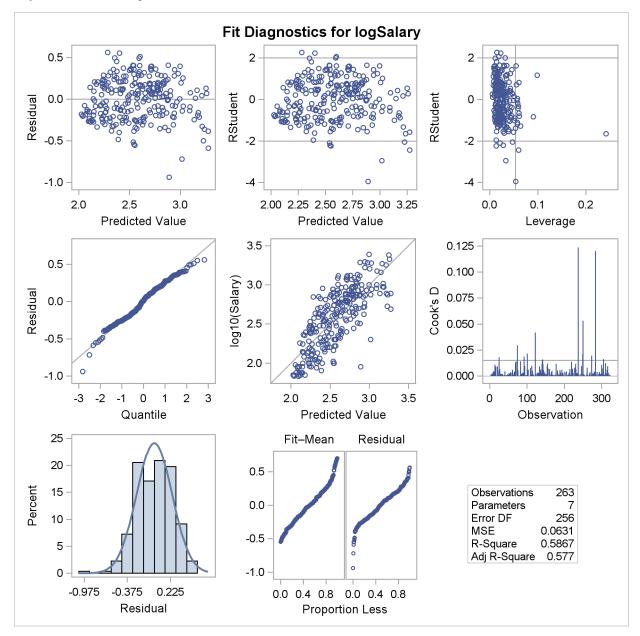
Output 73.1.1 shows the default output produced by PROC REG. The number of observations table shows that 59 observations are excluded because they have missing values for at least one of the variables used in the analysis. The analysis of variance and parameter estimates tables provide details about the fitted model.

Output 73.1.1 Default Output from PROC REG

		Т	he REG Proced	ure		
		_	Model: MODEL			
	Dependen	t Vari	able: logSala	ry log10(Salar	y)	
	Number of Obs				322	
	Number of Obs				263	
	Number of Obs	ervati	ons with Miss	ing Values	59	
		An	alysis of Var	iance		
			Sum of	Mean		
Source		DF	Squares	Square	F Value	Pr > F
Model		6	22.92208	3.82035	60.56	<.0001
Error	2	56	16.14954	0.06308		
Corrected	Total 2	62	39.07162			
	Root MSE		0.25117	R-Square	0.5867	
	Dependent Me	an	2.57416	Adj R-Sq	0.5770	
	Coeff Var		9.75719			
		Pa	rameter Estima	ates		
			Parameter	Standard		
Variable	Label	DF	Estimate	Error	t Value	Pr > t
Intercept	Intercept	1	1.80065	0.05912	30.46	<.0001
no_hits	Hits in 1986	1	0.00288	0.00091244	3.15	0.0018
no_runs	Runs in 1986	1	0.00008638	0.00173	0.05	0.9602
no_rbi	RBIs in 1986	1	0.00054382	0.00102	0.53	0.5947
no_bb	Walks in 1986	1	0.00292	0.00104	2.81	0.0054
<pre>yr_major</pre>	Years in MLB	1	0.03087	0.00836	3.69	0.0003
cr_hits	Career Hits	1	0.00010384	0.00006328	1.64	0.1020
Intercept no_hits no_runs no_rbi no_bb yr_major	Intercept Hits in 1986 Runs in 1986 RBIs in 1986 Walks in 1986 Years in MLB	1 1 1 1 1	1.80065 0.00288 0.0008638 0.00054382 0.00292 0.03087	0.05912 0.00091244 0.00173 0.00102 0.00104 0.00836	30.46 3.15 0.05 0.53 2.81 3.69	<.00 0.00 0.96 0.59 0.00

Before you accept a regression model, it is important to examine influence and fit diagnostics to see whether the model might be unduly influenced by a few observations and whether the data support the assumptions that underlie the linear regression. To facilitate such investigations, you can obtain diagnostic plots by enabling ODS Graphics.

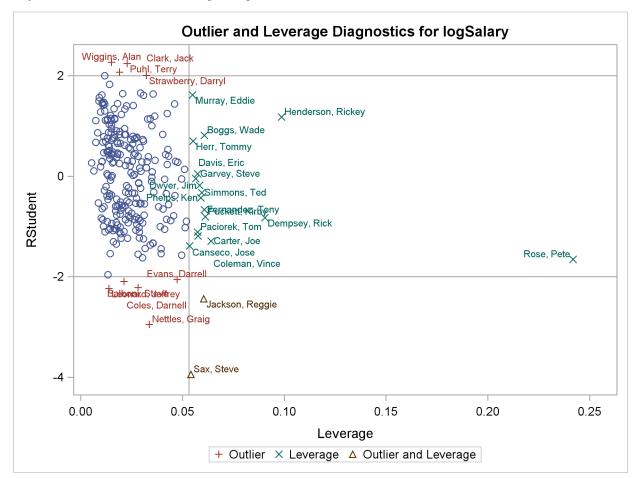
Output 73.1.2 Fit Diagnostics



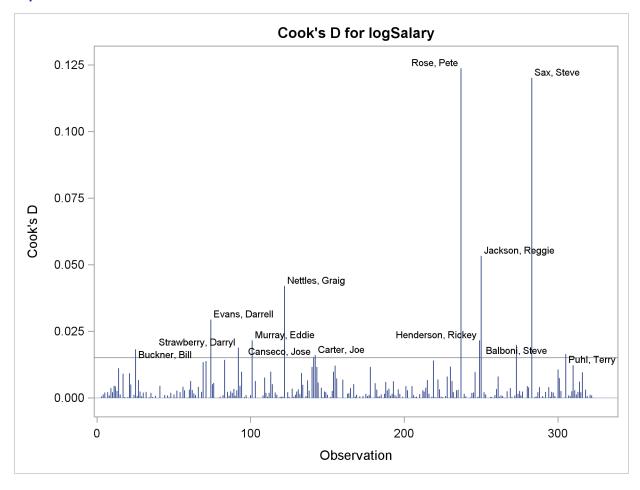
Output 73.1.2 shows a panel of diagnostic plots. The plot of externally studentized residuals (RStudent) by leverage values reveals that there is one observation with very high leverage that might be overly influencing the fit produced. The plot of Cook's *D* by observation also indicates two highly influential observations. To investigate further, you can use the PLOTS= option in the PROC REG statement as follows to produce labeled versions of these plots:

Output 73.1.3 and Output 73.1.4 reveal that Pete Rose is the highly influential observation. You might obtain a better fit to the remaining data if you omit his statistics when building the model.

Output 73.1.3 Outlier and Leverage Diagnostics



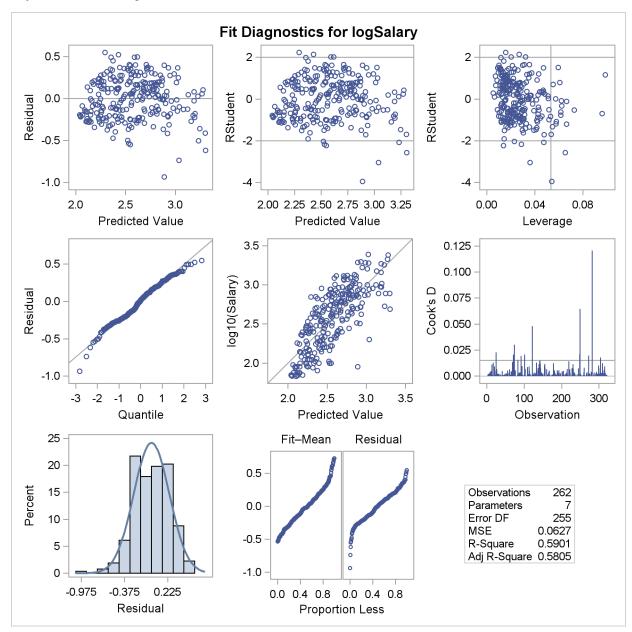
Output 73.1.4 Cook's *D*



The following statements use a WHERE statement to omit Pete Rose's statistics when building the model. An alternative way to do this within PROC REG is to use a REWEIGHT statement. See "Reweighting Observations in an Analysis" on page 5563 for details about reweighting.

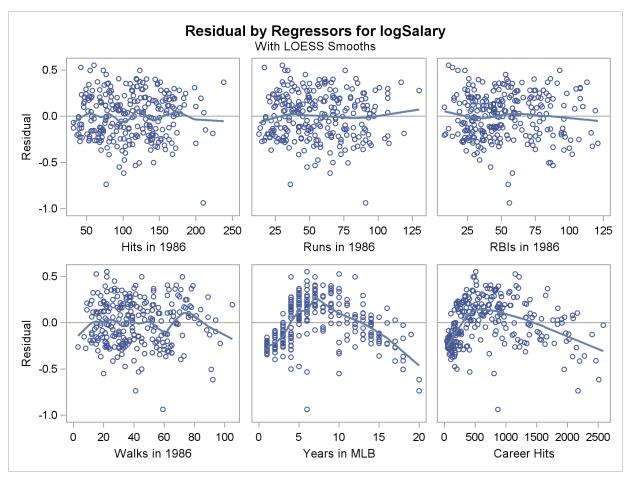
Output 73.1.5 shows the new fit diagnostics panel. You can see that there are still several influential and outlying observations. One possible reason for observing outliers is that the linear model specified is not appropriate to capture the variation in this data. You can often see evidence of an inappropriate model by observing patterns in plots of residuals.

Output 73.1.5 Fit Diagnostics



Output 73.1.6 shows plots of the residuals by the regressors in the model. When you specify the RESIDUALS(SMOOTH) suboption of the PLOTS option in the PROC REG statement, a loess fit is overlaid on each of these plots. You can see the same clear pattern in the residual plots for yr_major and cr_hits. Players near the start of their careers and players near the end of their careers get paid less than the model predicts.





You can address this lack of fit by using polynomials of degree 2 for these two variables as shown in the following statements:

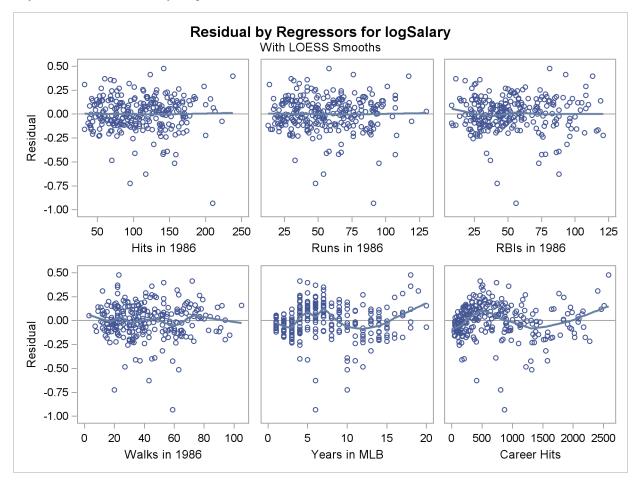
Output 73.1.7 shows the analysis of variance and parameter estimates for this model. Note that the R-square value of 0.787 for this model is considerably larger than the R-square value of 0.587 for the initial model shown in Output 73.1.1.

Output 73.1.7 Output from PROC REG

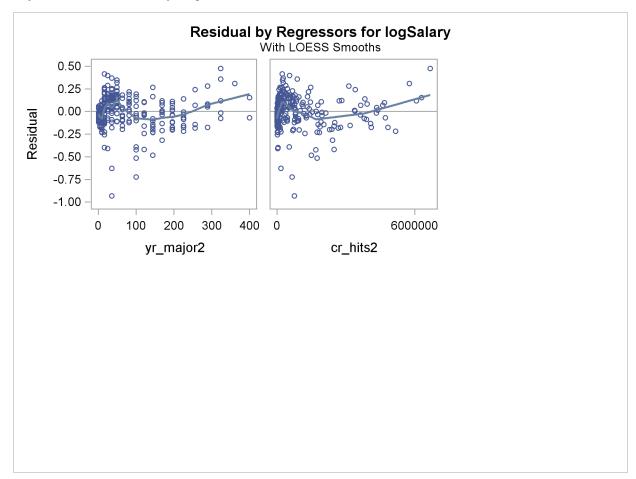
			The REG Proced	-		
			Model: MODEL:			
	Dependen	t Var	iable: logSala:	ry log10(Salar	у)	
		A	nalysis of Var	iance		
			Sum of	Mean		
Source		DF	Squares	Square	F Value	Pr > F
Model		8	30.69367	3.83671	117.13	<.0001
Error	2	53	8.28706	0.03276		
Corrected	Total 2	61	38.98073			
	Root MSE		0.18098	R-Square	0.7874	
	Dependent Me	an	2.57301	Adj R-Sq	0.7807	
	Coeff Var		7.03393			
		P	arameter Estima	ates		
			Parameter	Standard		
Variable	Label	DF	Estimate	Error	t Value	Pr > t
Intercept	Intercept	1	1.64564	0.05030	32.72	<.0001
no_hits	Hits in 1986	1	-0.00005539	0.00069200	-0.08	0.9363
no_runs	Runs in 1986	1	0.00093586	0.00125	0.75	0.4549
no_rbi	RBIs in 1986	1	0.00187	0.00074649	2.51	0.0127
no_bb	Walks in 1986	1	0.00218	0.00075057	2.90	0.0040
${\tt yr_major}$	Years in MLB	1	0.10383	0.01495	6.94	<.0001
cr_hits	Career Hits	1	0.00073955	0.00011970	6.18	<.0001
<pre>yr_major2</pre>		1	-0.00625	0.00071687	-8.73	<.0001
cr_hits2		1	-1.44072E-7	4.348471E-8	-3.31	0.0011

The plots of residuals by regressors in Output 73.1.8 and Output 73.1.9 show that the strong pattern in the plots for cr_majors and cr_hits has been reduced, although there is still some indication of a pattern remaining in these residuals. This suggests that a quadratic function might be insufficient to capture dependence of salary on these regressors.

Output 73.1.8 Residuals by Regressors

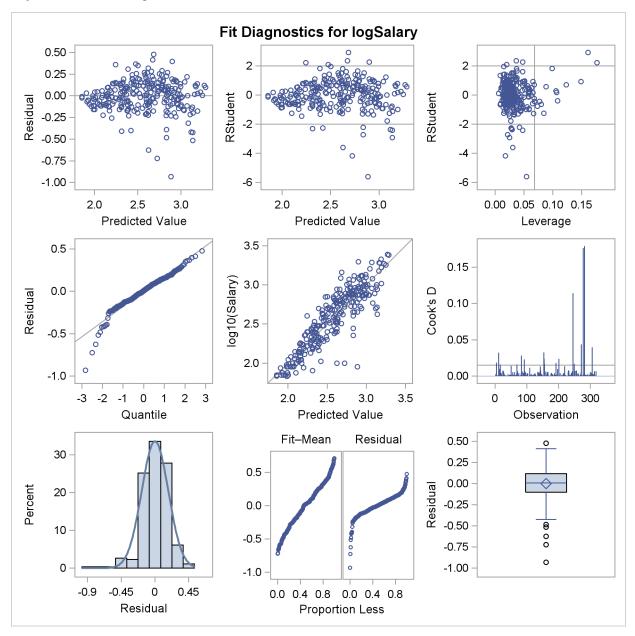


Output 73.1.9 Residuals by Regressors

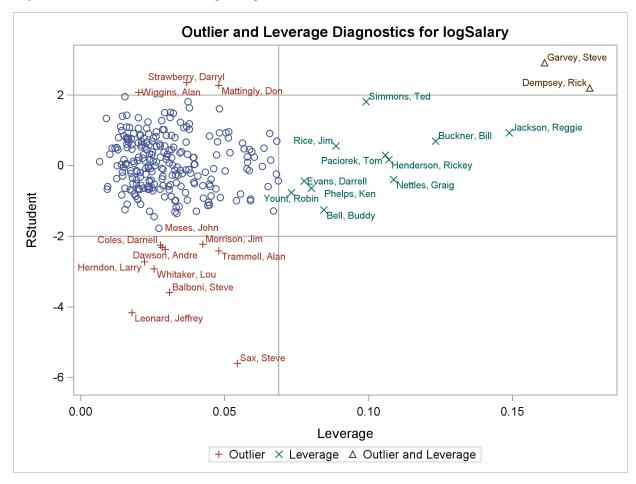


Output 73.1.10 show the diagnostics plots; three of the plots, with points of interest labeled, are shown individually in Output 73.1.11, Output 73.1.12, and Output 73.1.13. The STATS=NONE suboption specified in the PLOTS=DIAGNOSTICS option replaces the inset of statistics with a box plot of the residuals in the fit diagnostics panel. The observed by predicted value plot reveals a reasonably successful model for explaining the variation in salary for most of the players. However, the model tends to overpredict the salaries of several players near the lower end of the salary range. This bias can also be seen in the distribution of the residuals that you can see in the histogram, Q-Q plot, and box plot in Output 73.1.10.

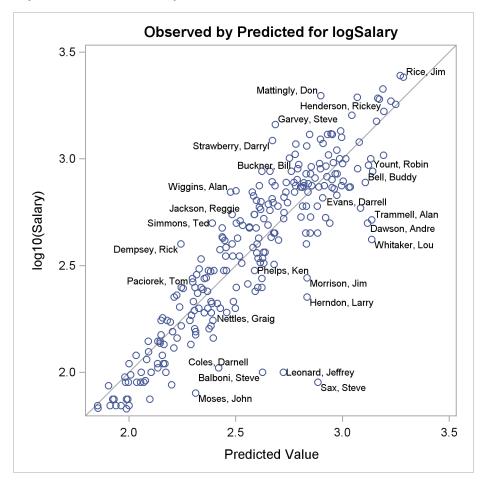
Output 73.1.10 Fit Diagnostics



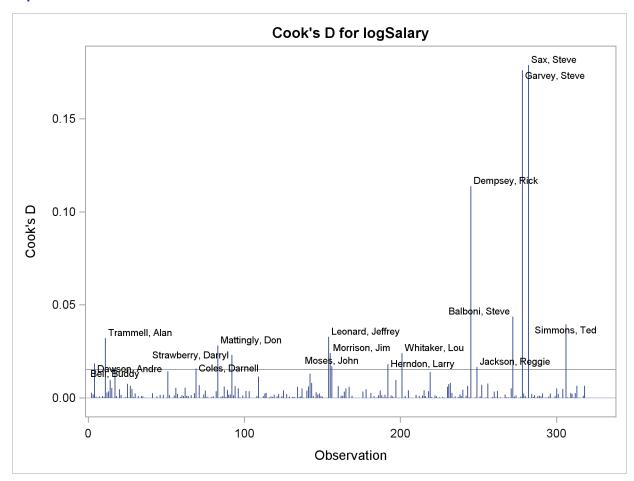
Output 73.1.11 Outlier and Leverage Diagnostics



Output 73.1.12 Observed by Predicted Values

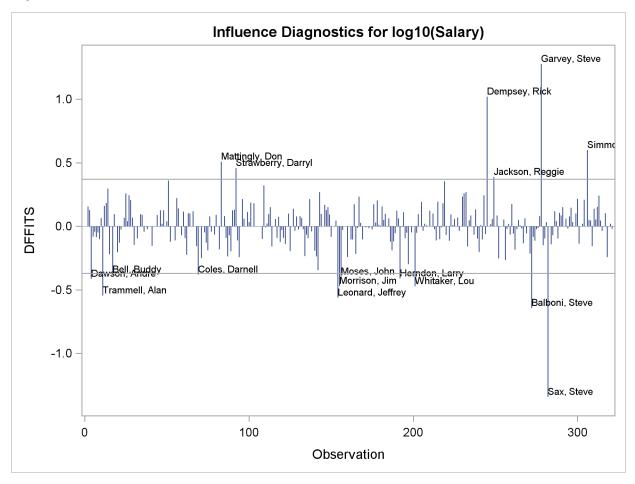


Output 73.1.13 Cook's D

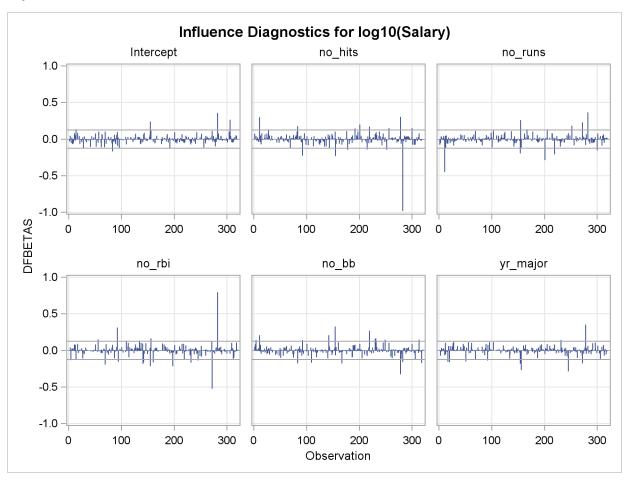


The RStudent by leverage plot in Output 73.1.11 and the Cook's *D* plot in Output 73.1.13 show that there are still a number of influential observations. By specifying the DFFITS and DFBE-TAS suboptions of the PLOTS= option, you obtain additional influence diagnostics plots shown in Output 73.1.14 and Output 73.1.15. See "Influence Statistics" on page 5553 for details about the interpretation DFFITS and DFBETAS statistics.

Output 73.1.14 DFFITS



Output 73.1.15 DFBETAS



You can continue this analysis by investigating how the influential observations identified in the various influence plots affect the fit. You can also use PROC ROBUSTREG to obtain a fit that is resistant to the presence of high leverage points and outliers.

Example 73.2: Aerobic Fitness Prediction

Aerobic fitness (measured by the ability to consume oxygen) is fit to some simple exercise tests. The goal is to develop an equation to predict fitness based on the exercise tests rather than on expensive and cumbersome oxygen consumption measurements. Three model-selection methods are used: forward selection, backward selection, and MAXR selection. Here are the data:

```
*-----*
| These measurements were made on men involved in a physical
| fitness course at N.C.State Univ. The variables are Age
| (years), Weight (kg), Oxygen intake rate (ml per kg body
| weight per minute), time to run 1.5 miles (minutes), heart
| rate while resting, heart rate while running (same time
| Oxygen rate measured), and maximum heart rate recorded while |
| running.
| ***Certain values of MaxPulse were changed for this analysis.|
*-----;
data fitness;
  input Age Weight Oxygen RunTime RestPulse RunPulse MaxPulse @@;
datalines:
44 89.47 44.609 11.37 62 178 182 40 75.07 45.313 10.07 62 185 185
44 85.84 54.297 8.65 45 156 168 42 68.15 59.571 8.17 40 166 172
38 89.02 49.874 9.22 55 178 180 47 77.45 44.811 11.63 58 176 176
40 75.98 45.681 11.95 70 176 180 43 81.19 49.091 10.85 64 162 170
44 81.42 39.442 13.08 63 174 176 38 81.87 60.055 8.63 48 170 186
44 73.03 50.541 10.13 45 168 168 45 87.66 37.388 14.03 56 186 192
45 66.45 44.754 11.12 51 176 176 47 79.15 47.273 10.60 47 162 164
54 83.12 51.855 10.33 50 166 170 49 81.42 49.156 8.95 44 180 185
51 69.63 40.836 10.95 57 168 172 51 77.91 46.672 10.00 48 162 168
48 91.63 46.774 10.25 48 162 164 49 73.37 50.388 10.08 67 168 168
57 73.37 39.407 12.63 58 174 176 54 79.38 46.080 11.17 62 156 165
52 76.32 45.441 9.63 48 164 166 50 70.87 54.625 8.92 48 146 155
51 67.25 45.118 11.08 48 172 172 54 91.63 39.203 12.88 44 168 172
51 73.71 45.790 10.47 59 186 188 57 59.08 50.545 9.93 49 148 155
49 76.32 48.673 9.40 56 186 188 48 61.24 47.920 11.50 52 170 176
52 82.78 47.467 10.50 53 170 172
```

The following statements demonstrate the FORWARD, BACKWARD, and MAXR model selection methods:

```
proc reg data=fitness;
  model Oxygen=Age Weight RunTime RunPulse RestPulse MaxPulse
      / selection=forward;
  model Oxygen=Age Weight RunTime RunPulse RestPulse MaxPulse
      / selection=backward;
  model Oxygen=Age Weight RunTime RunPulse RestPulse MaxPulse
      / selection=maxr;
run;
```

Output 73.2.1 shows the sequence of models produced by the FORWARD model-selection method.

Output 73.2.1 Forward Selection Method: PROC REG

The REG Procedure
Model: MODEL1
Dependent Variable: Oxygen

Forward Selection: Step 1

Variable RunTime Entered: R-Square = 0.7434 and C(p) = 13.6988

Analysis of Variance

Source	DF	Sum of Squares	Me Squa		alue	Pr > F
Model	1	632.90010	632.900	10 8	4.01	<.0001
Error	29	218.48144	7.533	84		
Corrected Total	30	851.38154				
	Parameter	Standard				
Variable	Estimate	Error	Type II SS	F Value	Pr > F	
Intercept	82.42177	3.85530	3443.36654	457.05	<.0001	
RunTime	-3.31056	0.36119	632.90010	84.01	<.0001	

Bounds on condition number: 1, 1

Forward Selection: Step 2

Variable Age Entered: R-Square = 0.7642 and C(p) = 12.3894

Analysis of Variance

Source	DF	Sum of Squares	Me Squa	an ire FV	alue	Pr > F
		_	_			
Model	2	650.66573	325.332	87 4	5.38	<.0001
Error	28	200.71581	7.168	42		
Corrected Total	30	851.38154				
	Parameter	Standard				
Variable	Estimate	Error	Type II SS	F Value	Pr > F	
Intercept	88.46229	5.37264	1943.41071	271.11	<.0001	
Age	-0.15037	0.09551	17.76563	2.48	0.1267	
RunTime	-3.20395	0.35877	571.67751	79.75	<.0001	

Output 73.2.1 continued

Bounds on condition number: 1.0369, 4.1478

Forward Selection: Step 3

Variable RunPulse Entered: R-Square = 0.8111 and C(p) = 6.9596

Analysis of Variance

		Sum of	Mea	an		
Source	DF	Squares	Squar	re F V	/alue	Pr > F
Model	3	690.55086	230.183	62 3	38.64	<.0001
Error	27	160.83069	5.956	69		
Corrected Total	30	851.38154				
	Parameter	Standard				
Variable	Estimate	Error	Type II SS	F Value	Pr > F	
Intercept	111.71806	10.23509	709.69014	119.14	<.0001	
Age	-0.25640	0.09623	42.28867	7.10	0.0129	
RunTime	-2.82538	0.35828	370.43529	62.19	<.0001	
RunPulse	-0.13091	0.05059	39.88512	6.70	0.0154	

Bounds on condition number: 1.3548, 11.597

Forward Selection: Step 4

Variable MaxPulse Entered: R-Square = 0.8368 and C(p) = 4.8800

Source	DF	Sum of Squares	Mean Square	F V	alue	Pr > F
Model	4	712.45153	178.11288	3	3.33	<.0001
Error	26	138.93002	5.34346			
Corrected Total	30	851.38154				
Variable	Parameter Estimate	Standard Error	Type II SS F	Value	Pr > F	
Intercept	98.14789	11.78569	370.57373	69.35	<.0001	
Age	-0.19773	0.09564	22.84231	4.27	0.0488	
RunTime	-2.76758	0.34054	352.93570	66.05	<.0001	
RunPulse	-0.34811	0.11750	46.90089	8.78	0.0064	
MaxPulse	0.27051	0.13362	21.90067	4.10	0.0533	

Output 73.2.1 continued

	Forwa	ard Selection	: Step 5			
Variab	le Weight Enter	ed: R-Square	= 0.8480 and C	(p) =	5.1063	
	A	nalysis of Va	riance			
		Sum of	Mean			
Source	DF	Squares	Square	F	Value	Pr > 1
Model	5	721.97309	144.39462		27.90	<.000
Error	25	129.40845	5.17634			
Corrected Total	30	851.38154				
	Parameter	Standard				
Variable	Estimate	Error	Type II SS F	Value	Pr > F	
Intercept	102.20428	11.97929	376.78935	72.79	<.0001	
Age	-0.21962	0.09550	27.37429	5.29	0.0301	
Weight	-0.07230	0.05331	9.52157	1.84	0.1871	
RunTime	-2.68252	0.34099	320.35968	61.89	<.0001	
RunPulse	-0.37340					
MaxPulse	0.30491	0.13394	26.82640	5.18	0.0316	

The final variable available to add to the model, RestPulse, is not added since it does not meet the 50% (the default value of the SLE option is 0.5 for FORWARD selection) significance-level criterion for entry into the model.

The BACKWARD model-selection method begins with the full model. Output 73.2.2 shows the steps of the BACKWARD method. RestPulse is the first variable deleted, followed by Weight. No other variables are deleted from the model since the variables remaining (Age, RunTime, RunPulse, and MaxPulse) are all significant at the 10% (the default value of the SLS option is 0.1 for the BACKWARD elimination method) significance level.

Output 73.2.2 Backward Selection Method: PROC REG

Backward Elimination: Step 0	Backward	Elimination:	Step 0
------------------------------	----------	--------------	--------

All Variables Entered: R-Square = 0.8487 and C(p) = 7.0000

Analysis of Variance

		Sum of	Mean			
Source	DF	Squares	Square	F V	alue	Pr > F
Model	6	722.54361	120.42393	2	2.43	<.0001
Error	24	128.83794	5.36825			
Corrected Total	30	851.38154				
	Parameter	Standard				
Variable	Estimate	Error	Type II SS F	Value	Pr > F	
Intercept	102.93448	12.40326	369.72831	68.87	<.0001	
Age	-0.22697	0.09984	27.74577	5.17	0.0322	
Weight	-0.07418	0.05459	9.91059	1.85	0.1869	
RunTime	-2.62865	0.38456	250.82210	46.72	<.0001	
RunPulse	-0.36963	0.11985	51.05806	9.51	0.0051	
RestPulse	-0.02153	0.06605	0.57051	0.11	0.7473	
MaxPulse	0.30322	0.13650	26.49142	4.93	0.0360	

Bounds on condition number: 8.7438, 137.13

Backward Elimination: Step 1

Variable RestPulse Removed: R-Square = 0.8480 and C(p) = 5.1063

		Sum of	Mean	ı		
Source	DF	Squares	Square	FV	alue	Pr > F
Model	5	721.97309	144.39462	2	7.90	<.0001
Error	25	129.40845	5.17634			
Corrected Total	30	851.38154				
	Parameter	Standard				
Variable	Estimate	Error	Type II SS F	Value	Pr > F	
Intercept	102.20428	11.97929	376.78935	72.79	<.0001	
Age	-0.21962	0.09550	27.37429	5.29	0.0301	
Weight	-0.07230	0.05331	9.52157	1.84	0.1871	
RunTime	-2.68252	0.34099	320.35968	61.89	<.0001	
RunPulse	-0.37340	0.11714	52.59624	10.16	0.0038	
MaxPulse	0.30491	0.13394	26.82640	5.18	0.0316	

Output 73.2.2 continued

	Backwa	ard Eliminati	on: Step 2		
Variable	e Weight Remove	ed: R-Square	= 0.8368 and C	(p) = 4.8800	
	Aı	nalysis of Va	riance		
		Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > F
Model	4	712.45153	178.11288	33.33	<.0001
Error	26	138.93002	5.34346		
Corrected Total	30	851.38154			
	Parameter	Standard			
Variable	Estimate	Error	Type II SS F	Value Pr >	F
Intercept	98.14789	11.78569	370.57373	69.35 <.000	01
Age	-0.19773	0.09564	22.84231	4.27 0.048	88
RunTime	-2.76758	0.34054	352.93570	66.05 <.000	01
RunPulse	-0.34811	0.11750	46.90089	8.78 0.000	64
MaxPulse	0.27051	0.13362	21.90067	4.10 0.053	33

The MAXR method tries to find the "best" one-variable model, the "best" two-variable model, and so on. Output 73.2.3 shows that the one-variable model contains RunTime; the two-variable model contains RunTime and Age; the three-variable model contains RunTime, Age, and RunPulse; the four-variable model contains Age, RunTime, RunPulse, and MaxPulse; the five-variable model contains Age, Weight, RunTime, RunPulse, and MaxPulse; and finally, the six-variable model contains all the variables in the MODEL statement.

Output 73.2.3 Maximum R-Square Improvement Selection Method: PROC REG

	Maximum R	-Square Improve	ment: Step 1		
Variable Run	Time Enter	ed: R-Square =	0.7434 and C(p	o) = 13.6988	3
	A	nalysis of Vari	ance		
		Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > I
Model	1	632.90010	632.90010	84.01	<.000
T	29	218.48144	7.53384		
Error					

Output 73.2.3 continued

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	82.42177	3.85530	3443.36654	457.05	<.0001
RunTime	-3.31056	0.36119	632.90010	84.01	<.0001
	Bounds o	on condition	number: 1, 1		

The above model is the best 1-variable model found.

Maximum R-Square Improvement: Step 2

Variable Age Entered: R-Square = 0.7642 and C(p) = 12.3894

Analysis of Variance

Source	DF	Sum of Squares	Mea Squar		alue	Pr > F
Model	2	650.66573	325.3328	87 4	5.38	<.0001
Error	28	200.71581	7.1684	42		
Corrected Total	30	851.38154				
	Parameter	Standard				
Variable	Estimate	Error	Type II SS	F Value	Pr > F	
Intercept	88.46229	5.37264	1943.41071	271.11	<.0001	
Age	-0.15037	0.09551	17.76563	2.48	0.1267	
RunTime	-3.20395	0.35877	571.67751	79.75	<.0001	

Bounds on condition number: 1.0369, 4.1478

The above model is the best 2-variable model found.

Maximum R-Square Improvement: Step 3

Variable RunPulse Entered: R-Square = 0.8111 and C(p) = 6.9596

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	3	690.55086	230.18362	38.64	<.0001
Error	27	160.83069	5.95669		
Corrected Total	30	851.38154			

Output 73.2.3 continued

Variable	Parameter Estimate	Standard Error	Type II SS	F Value	Pr > F
Intercept	111.71806	10.23509	709.69014	119.14	<.0001
Age	-0.25640	0.09623	42.28867	7.10	0.0129
RunTime	-2.82538	0.35828	370.43529	62.19	<.0001
RunPulse	-0.13091	0.05059	39.88512	6.70	0.0154

Bounds on condition number: 1.3548, 11.597

The above model is the best 3-variable model found.

 ${\tt Maximum} \ {\tt R-Square} \ {\tt Improvement:} \ {\tt Step} \ {\tt 4}$

Variable MaxPulse Entered: R-Square = 0.8368 and C(p) = 4.8800

Source	DF	Sum of Squares	Mean Square		alue	Pr > F
Model	4	712.45153	178.11288	3	3.33	<.0001
Error	26	138.93002	5.34346			
Corrected Total	30	851.38154				
	Parameter	Standard				
Variable	Estimate	Error	Type II SS F	Value	Pr > F	
Intercept	98.14789	11.78569	370.57373	69.35	<.0001	
Age	-0.19773	0.09564	22.84231	4.27	0.0488	
RunTime	-2.76758	0.34054	352.93570	66.05	<.0001	
RunPulse	-0.34811	0.11750	46.90089	8.78	0.0064	
MaxPulse	0.27051	0.13362	21.90067	4.10	0.0533	

Output 73.2.3 continued

Bounds on condition number: 8.4182, 76.851

The above model is the best 4-variable model found.

Maximum R-Square Improvement: Step 5

Variable Weight Entered: R-Square = 0.8480 and C(p) = 5.1063

Analysis of Variance

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model Error	5 25	721.97309 129.40845	144.39462 5.17634	27.90	<.0001
Corrected Total	30	851.38154	3.17034		
Variable	Parameter Estimate	Standard Error	Type II SS F	Value Pr > F	
Intercept Age Weight	102.20428 -0.21962 -0.07230	11.97929 0.09550 0.05331	376.78935 27.37429 9.52157	72.79 <.0001 5.29 0.0301 1.84 0.1871	
RunTime RunPulse MaxPulse	-2.68252 -0.37340 0.30491	0.34099 0.11714 0.13394	320.35968 52.59624 26.82640	61.89 <.0001 10.16 0.0038 5.18 0.0316	

Bounds on condition number: 8.7312, 104.83

The above model is the best 5-variable model found.

Maximum R-Square Improvement: Step 6

Variable RestPulse Entered: R-Square = 0.8487 and C(p) = 7.0000

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	6	722.54361	120.42393	22.43	<.0001
Error	24	128.83794	5.36825		
Corrected Total	30	851.38154			

Output 73.2.3 continued

Variable	Estimate	Error	Type II SS	F Value	Pr > F
Intercept	102.93448	12.40326	369.72831	68.87	<.0001
Age	-0.22697	0.09984	27.74577	5.17	0.0322
Weight	-0.07418	0.05459	9.91059	1.85	0.1869
RunTime	-2.62865	0.38456	250.82210	46.72	<.0001
RunPulse	-0.36963	0.11985	51.05806	9.51	0.0051
RestPulse	-0.02153	0.06605	0.57051	0.11	0.7473
MaxPulse	0.30322	0.13650	26.49142	4.93	0.0360

Note that for all three of these methods, RestPulse contributes least to the model. In the case of forward selection, it is not added to the model. In the case of backward selection, it is the first variable to be removed from the model. In the case of MAXR selection, RestPulse is included only for the full model.

For the STEPWISE, BACKWARD, and FORWARD selection methods, you can control the amount of detail displayed by using the DETAILS option, and you can use ODS Graphics to produce plots that show how selection criteria progress as the selection proceeds. For example, the following statements display only the selection summary table for the FORWARD selection method (Output 73.2.4) and produce the plots shown in Output 73.2.5 and Output 73.2.6.

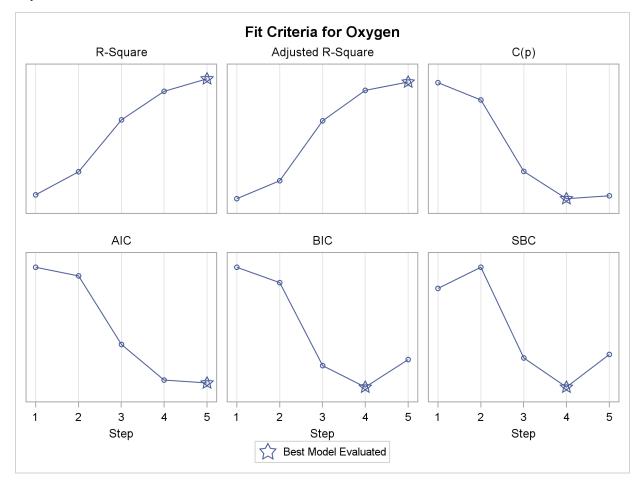
```
ods graphics on;
proc reg data=fitness plots=(criteria sbc);
  model Oxygen=Age Weight RunTime RunPulse RestPulse MaxPulse
      / selection=forward details=summary;
run;
```

Output 73.2.4 Forward Selection Summary

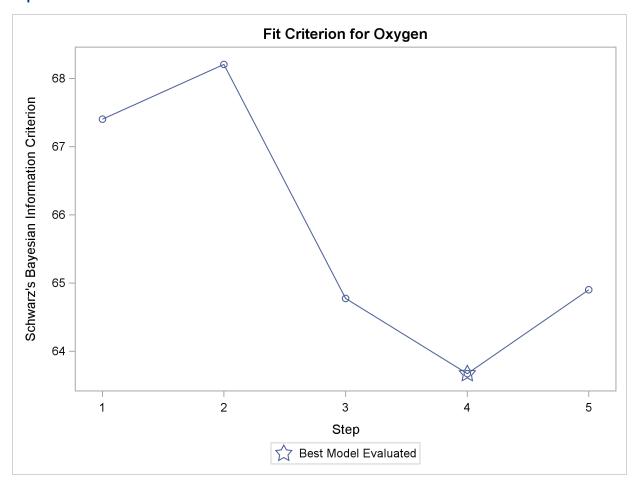
		Dej	Model: pendent Var:		en		
		Sum	mary of For	ward Select:	ion		
	Variable	Number	Partial	Model			
Step	Entered	Vars In	R-Square	R-Square	C(p)	F Value	Pr > F
1	RunTime	1	0.7434	0.7434	13.6988	84.01	<.0001
2	Age	2	0.0209	0.7642	12.3894	2.48	0.1267
	RunPulse	3	0.0468	0.8111	6.9596	6.70	0.0154
3		4	0.0257	0.8368	4.8800	4.10	0.0533
3 4	${ t MaxPulse}$	-					

Output 73.2.5 show how six fit criteria progress as the forward selection proceeds. The step at which each criterion achieves its best value is indicated. For example, the BIC criterion achieves its minimum value for the model at step 4. Note that this does not mean that the model at step 4 achieves the smallest BIC criterion among all possible models that use a subset of the regressors; the model at step 4 yields the smallest BIC statistic among the models at each step of the forward selection. Output 73.2.6 show the progression of the SBC statistic in its own plot. If you want to see six of the selection criteria in individual plots, you can specify the UNPACK suboption of the PLOTS=CRITERIA option in the PROC REG statement.

Output 73.2.5 Fit Criteria



Output 73.2.6 SBC Criterion



Next, the RSQUARE model-selection method is used to request R^2 and C_p statistics for all possible combinations of the six independent variables. The following statements produce Output 73.2.7:

```
proc reg data=fitness plots=(criteria(label) cp);
  model Oxygen=Age Weight RunTime RunPulse RestPulse MaxPulse
     / selection=rsquare cp;
  title 'Physical fitness data: all models';
run;
```

Output 73.2.7 All Models by the RSQUARE Method: PROC REG

Physical fitness data: all models

The REG Procedure

Model: MODEL1

Dependent Variable: Oxygen

		R-S	Square Sele	ection Method
Model	Number in			
Index	Model	R-Square	C(p)	Variables in Model
1	1	0.7434		RunTime
2	1	0.1595		RestPulse
3	1	0.1584		RunPulse
4	1	0.0928		
5	1	0.0560		
6	1	0.0265	127.3948	Weight
7	2	0.7642	12.3894	Age RunTime
8	2	0.7614	12.8372	RunTime RunPulse
9	2	0.7452	15.4069	RunTime MaxPulse
10	2	0.7449	15.4523	Weight RunTime
11	2	0.7435	15.6746	RunTime RestPulse
12	2	0.3760	73.9645	Age RunPulse
13	2	0.3003	85.9742	Age RestPulse
14	2	0.2894	87.6951	RunPulse MaxPulse
15	2	0.2600	92.3638	Age MaxPulse
16	2	0.2350		RunPulse RestPulse
17	2	0.1806	104.9523	Weight RestPulse
18	2		105.9939	RestPulse MaxPulse
19	2	0.1669		-
20	2	0.1506		
21	2	0.0675	122.8881	Weight MaxPulse
22	3	0.8111	6.9596	Age RunTime RunPulse
23	3	0.8100	7.1350	RunTime RunPulse MaxPulse
24	3	0.7817	11.6167	Age RunTime MaxPulse
25	3	0.7708	13.3453	Age Weight RunTime
26	3	0.7673	13.8974	Age RunTime RestPulse
27	3	0.7619	14.7619	RunTime RunPulse RestPulse
28	3	0.7618	14.7729	Weight RunTime RunPulse
29	3	0.7462	17.2588	Weight RunTime MaxPulse
30	3	0.7452	17.4060	RunTime RestPulse MaxPulse
31	3	0.7451		-
32	3	0.4666		
33	3	0.4223		
34	3	0.4091		
35	3	0.3900		-
36	3	0.3568		
37	3	0.3538	79.4891	RunPulse RestPulse MaxPulse

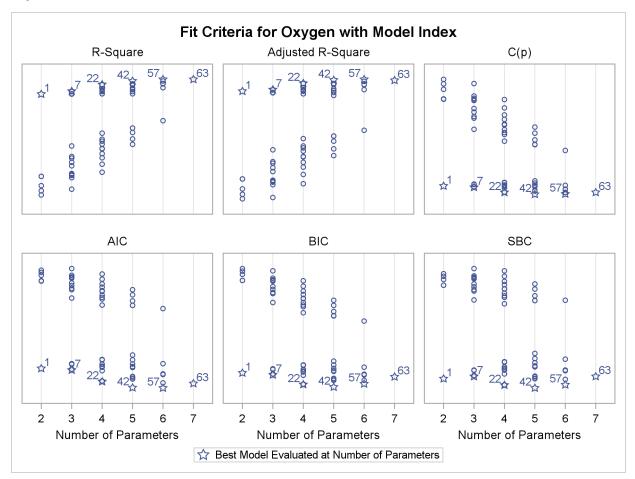
Output 73.2.7 continued

			m1									
			The REG P									
		D	Model:									
		рере	endent vari	able: Oxygen								
R-Square Selection Method												
Model	Number in											
Index	Model	R-Square	C(p)	Variables in Model								
38	3	0.3208	84.7216	Weight RunPulse MaxPulse								
39	3	0.2902	89.5693	Age Weight MaxPulse								
40	3	0.2447	96.7952									
41	3	0.1882		Weight RestPulse MaxPulse								
 42	4	0.8368	4.8800	Age RunTime RunPulse MaxPulse								
43	4	0.8165	8.1035	Age Weight RunTime RunPulse								
44	4	0.8158	8.2056	Weight RunTime RunPulse MaxPulse								
45	4	0.8117	8.8683	Age RunTime RunPulse RestPulse								
46	4	0.8104	9.0697	RunTime RunPulse RestPulse MaxPulse								
47	4	0.7862	12.9039	Age Weight RunTime MaxPulse								
48	4	0.7834	13.3468	Age RunTime RestPulse MaxPulse								
49	4	0.7750	14.6788	Age Weight RunTime RestPulse								
50	4	0.7623	16.7058	Weight RunTime RunPulse RestPulse								
51	4	0.7462	19.2550	Weight RunTime RestPulse MaxPulse								
52	4	0.5034	57.7590	Age Weight RunPulse RestPulse								
53	4	0.5025	57.9092	Age RunPulse RestPulse MaxPulse								
54	4	0.4717	62.7830	Age Weight RunPulse MaxPulse								
55	4	0.4256	70.0963	Age Weight RestPulse MaxPulse								
56	4	0.3858	76.4100	Weight RunPulse RestPulse MaxPulse								
57	5	0.8480	5.1063	Age Weight RunTime RunPulse MaxPulse								
58	5	0.8370	6.8461	Age RunTime RunPulse RestPulse MaxPul								
59	5	0.8176	9.9348	Age Weight RunTime RunPulse RestPulse								
60	5	0.8161	10.1685	Weight RunTime RunPulse RestPulse MaxPulse								
61	5	0.7887	14.5111									
62	5	0.5541	51.7233	Age Weight RunPulse RestPulse MaxPuls								
63	6	0.8487	7.0000	Age Weight RunTime RunPulse RestPulse MaxPulse								

The models in Output 73.2.7 are arranged first by the number of variables in the model and then by the magnitude of R^2 for the model.

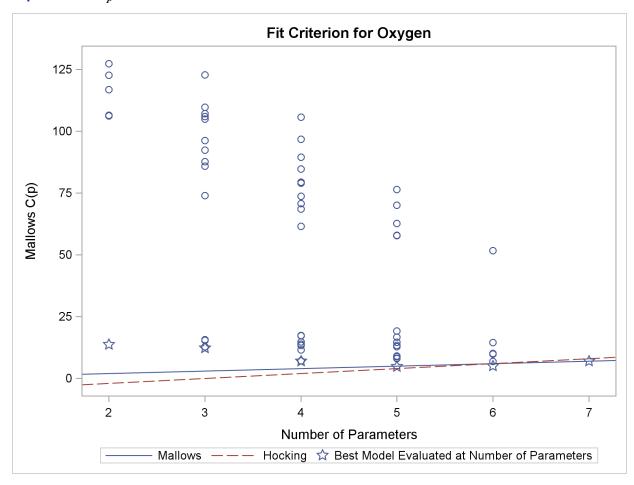
Output 73.2.8 shows the panel of fit criteria for the RSQUARE selection method. The best models (based on the R-square statistic) for each subset size are indicated on the plots. The LABEL suboption specifies that these models are labeled by the model number that appears in the summary table shown in Output 73.2.7.

Output 73.2.8 Fit Criteria



Output 73.2.9 shows the plot of the C_p criterion by number of regressors in the model. Useful reference lines suggested by Mallows (1973) and Hocking (1976) are included on the plot. However, because all possible subset models are included on this plot, the better models are all compressed near the bottom of the plot.

Output 73.2.9 C_p Criterion



The following statements use the BEST=20 option in the model statement and SELECTION=CP to restrict attention to the models that yield the 20 smallest values of the C_p statistic:

Output 73.2.10 shows the summary table listing the regressors in the 20 models that yield the smallest C_p values, and Output 73.2.11 presents the results graphically. Reference lines $C_p = 2p - p_{full}$ and $C_p = p$ are shown on this plot. See the PLOTS=CP option on page 5453 for interpretations of these lines. For the Fitness data, these lines indicate that a six-variable model is a reasonable choice for doing parameter estimation, while a five-variable model might be suitable for doing prediction.

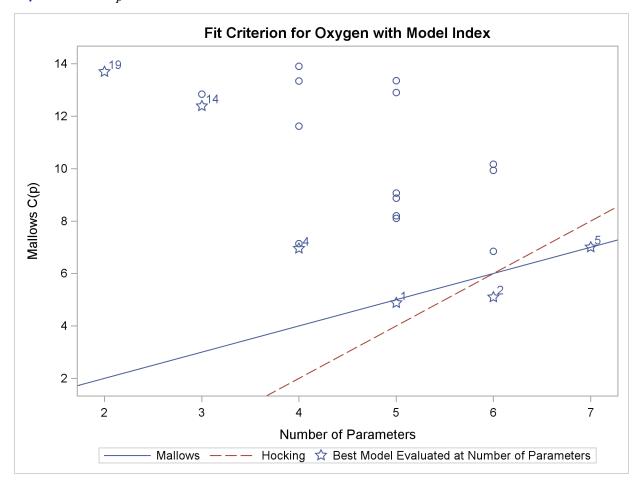
Output 73.2.10 C_p Selection Summary: PROC REG

The REG Procedure
Model: MODEL1
Dependent Variable: Oxygen

C(p) Selection Method

Model	Number in			
Index	Model	C(p)	R-Square	Variables in Model
1	4	4.8800	0.8368	Age RunTime RunPulse MaxPulse
2	5	5.1063	0.8480	Age Weight RunTime RunPulse MaxPulse
3	5	6.8461	0.8370	Age RunTime RunPulse RestPulse MaxPulse
4	3	6.9596	0.8111	-
5	6	7.0000	0.8487	
				MaxPulse
6	3	7.1350	0.8100	RunTime RunPulse MaxPulse
7	4	8.1035	0.8165	Age Weight RunTime RunPulse
8	4	8.2056	0.8158	Weight RunTime RunPulse MaxPulse
9	4	8.8683	0.8117	Age RunTime RunPulse RestPulse
10	4	9.0697	0.8104	RunTime RunPulse RestPulse MaxPulse
11	5	9.9348	0.8176	Age Weight RunTime RunPulse RestPulse
12	5	10.1685	0.8161	Weight RunTime RunPulse RestPulse
				MaxPulse
13	3	11.6167	0.7817	Age RunTime MaxPulse
14	2	12.3894	0.7642	Age RunTime
15	2	12.8372	0.7614	RunTime RunPulse
16	4	12.9039	0.7862	Age Weight RunTime MaxPulse
17	3	13.3453	0.7708	Age Weight RunTime
18	4	13.3468	0.7834	Age RunTime RestPulse MaxPulse
19	1	13.6988	0.7434	RunTime
20	3	13.8974	0.7673	Age RunTime RestPulse

Output 73.2.11 C_p Criterion



Before making a final decision about which model to use, you would want to perform collinearity diagnostics. Note that, since many different models have been fit and the choice of a final model is based on \mathbb{R}^2 , the statistics are biased and the p-values for the parameter estimates are not valid.

Example 73.3: Predicting Weight by Height and Age

In this example, the weights of schoolchildren are modeled as a function of their heights and ages. The example shows the use of a BY statement with PROC REG, multiple MODEL statements, and the OUTEST= and OUTSSCP= options, which create data sets. Here are the data:

Modeling is performed separately for boys and girls. Since the BY statement is used, interactive processing is not possible in this example; no statements can appear after the first RUN statement.

The following statements produce Output 73.3.1 through Output 73.3.4:

```
proc reg outest=est1 outsscp=sscp1 rsquare;
  by sex;
  eq1: model weight=height;
  eq2: model weight=height age;

proc print data=sscp1;
  title2 'SSCP type data set';

proc print data=est1;
  title2 'EST type data set';

run;
```

Output 73.3.1 Height and Weight Data: Submodel for Female Children

		sex=i			
	r	he REG Proced	lure		
		Model: eq1			
	Depend	lent Variable:	weight		
	Ar	alysis of Var	ciance		
		Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > F
Model	1	21507	21507	141.09	<.0001
Error	109	16615	152.42739		
Corrected Total	110	38121			
Root	MSE	12.34615	R-Square	0.5642	
Deper	ndent Mean	98.87838	Adj R-Sq	0.5602	
Coef	f Var	12.48620			
	Pa	rameter Estim	nates		
	Param	neter St	andard		
Variable	DF Esti	mate	Error t V	alue Pr >	t
Intercept	1 -153.1	.2891 21	24814 -	7.21 <.	0001
height	1 4.1	.6361 0	1.35052	1.88 <.	0001

Output 73.3.2 Height and Weight Data: Full Model for Female Children

		sex=f			
		The REG Proced	ure		
		Model: eq2			
	Depen	dent Variable:	weight		
	A	nalysis of Var	iance		
		Sum of	Mea	n	
Source	DF	Squares	Squar	e F Value	Pr > F
Model	2	22432	1121	6 77.21	<.0001
Error	108	15689	145.2670	0	
Corrected Total	110	38121			
Roc	t MSE	12.05268	R-Square	0.5884	
Dep	endent Mean	98.87838	Adj R-Sq	0.5808	
Coe	ff Var	12.18939			
	_				
	P	arameter Estin	ates		
			andard		
Variable	DF Est	imate	Error t	Value Pr >	t
Intercept	1 -150.	59698 20	.76730	-7.25 <.	0001
height	1 3.	60378 0	.40777	8.84 <.	0001
age	1 1.	90703	.75543	2.52 0.	0130

Output 73.3.3 Height and Weight Data: Submodel for Male Children

			The REG Pro	cedure			
			Model:	eq1			
		Depen	ndent Variab	le: weigh	t		
		A	analysis of	Variance			
			Sum o	f	Mean		
Source		DF	Square	s	Square	F Value	Pr > 1
Model		1	3112	6	31126	206.24	<.000
Error		124	1871	4 15	0.92222		
Corrected Tota	1	125	4984	0			
R	oot MSE		12.2850	4 R-Sq	uare	0.6245	
D	ependent	Mean	103.4484	-	R-Sq		
	oeff Var		11.8755	-	•		
		F	arameter Es	timates			
		Para	meter	Standard			
Variable	DF	Est	imate	Error	t Va	alue Pr	> t
Intercept	1	-125.	69807	15.99362	-7	7.86 <	.0001
height	1	3.	68977	0.25693	14	1.36 <	.0001

Output 73.3.4 Height and Weight Data: Full Model for Male Children

			sex=	m					
		7	he REG Pr	ocedure					
			Model:	eq2					
		Depend	lent Varia	ble: we	ight				
		Ar	nalysis of	Varian	ce				
			Sum	of	ı	Mean			
Source		DF	Squar	es	Sqı	are	F Va	lue	Pr > F
Model		2	329	75	16	6487	120	0.24	<.0001
Error		123	168	66	137.11	1922			
Corrected Total		125	498	40					
Roc	t MSE		11.709	79 R	-Square	a	0.661	5	
Dep	endent	Mean	103.448	41 A	dj R-So	7	0.6563	L	
Coe	ff Var		11.319	45	-	_			
		Pa	arameter E	stimate	s				
		Paran	meter	Stand	ard				
Variable	DF		mate		ror	t Val	ue	Pr >	t
Intercept	1	-113.7	1346	15.59	021	-7.	29	<.0	001
height	1	2.6	8075	0.36	809	7.	28	<.0	001
age	1	3.0	8167	0.83	927	3.	67	0.0	004

For both female and male children, the overall F statistics for both models are significant, indicating that the model explains a significant portion of the variation in the data. For females, the full model is

weight =
$$-150.57 + 3.60 \times \text{height} + 1.91 \times \text{age}$$

and for males, the full model is

weight =
$$-113.71 + 2.68 \times \text{height} + 3.08 \times \text{age}$$

The OUTSSCP= data set is shown in Output 73.3.5. Note how the BY groups are separated. Observations with _TYPE_='N' contain the number of observations in the associated BY group. Observations with _TYPE_='SSCP' contain the rows of the uncorrected sums of squares and crossproducts matrix. The observations with _NAME_='Intercept' contain crossproducts for the intercept.

Output 73.3.5 SSCP Matrix

Obs	sex	_TYPE_	_NAME_	Intercept	height	weight	age
1	f	SSCP	Intercept	111.0	6718.40	10975.50	1824.90
2	f	SSCP	height	6718.4	407879.32	669469.85	110818.32
3	f	SSCP	weight	10975.5	669469.85	1123360.75	182444.95
4	f	SSCP	age	1824.9	110818.32	182444.95	30363.81
5	f	N		111.0	111.00	111.00	111.00
6	m	SSCP	Intercept	126.0	7825.00	13034.50	2072.10
7	m	SSCP	height	7825.0	488243.60	817919.60	129432.57
8	m	SSCP	weight	13034.5	817919.60	1398238.75	217717.45
9	m	SSCP	age	2072.1	129432.57	217717.45	34515.95
10	m	N		126.0	126.00	126.00	126.00

The OUTEST= data set is displayed in Output 73.3.6; again, the BY groups are separated. The _MODEL_ column contains the labels for models from the MODEL statements. If no labels are specified, the defaults MODEL1 and MODEL2 would appear as values for _MODEL_. Note that _TYPE_='PARMS' for all observations, indicating that all observations contain parameter estimates. The _DEPVAR_ column displays the dependent variable, and the _RMSE_ column gives the root mean square error for the associated model. The Intercept column gives the estimate for the intercept for the associated model, and variables with the same name as variables in the original data set (height, age) give parameter estimates for those variables. The dependent variable, weight, is shown with a value of -1. The _IN_ column contains the number of regressors in the model not including the intercept; _P_ contains the number of parameters in the model; _EDF_ contains the error degrees of freedom; and _RSQ_ contains the R² statistic. Finally, note that the _IN_, _P_, _EDF_, and _RSQ_ columns appear in the OUTEST= data set since the RSQUARE option is specified in the PROC REG statement.

Output 73.3.6 OUTEST Data Set

```
I
                                n
               D
                                t
    М
               E
         Т
    0
               Ρ
                       R
    D
         Y
               v
                       М
                                С
    E
         Ρ
               Α
                       s
                                                             D
                                                                   s
                                е
                                        g
                                              g
    L
         E
               R
                       Е
                                                        ΝP
                                        h
                                              h
                                                                   Q
                                р
1 f eq1 PARMS weight 12.3461 -153.129 4.16361 -1 .
                                                        1 2 109 0.56416
2 f eq2 PARMS weight 12.0527 -150.597 3.60378 -1 1.90703 2 3 108 0.58845
3 m eq1 PARMS weight 12.2850 -125.698 3.68977 -1 .
                                                        1 2 124 0.62451
4 m eq2 PARMS weight 11.7098 -113.713 2.68075 -1 3.08167 2 3 123 0.66161
```

Example 73.4: Regression with Quantitative and Qualitative Variables

At times it is desirable to have independent variables in the model that are qualitative rather than quantitative. This is easily handled in a regression framework. Regression uses qualitative variables to distinguish between populations. There are two main advantages of fitting both populations in one model. You gain the ability to test for different slopes or intercepts in the populations, and more degrees of freedom are available for the analysis.

Regression with qualitative variables is different from analysis of variance and analysis of covariance. Analysis of variance uses qualitative independent variables only. Analysis of covariance uses quantitative variables in addition to the qualitative variables in order to account for correlation in the data and reduce MSE; however, the quantitative variables are not of primary interest and merely improve the precision of the analysis.

Consider the case where Y_i is the dependent variable, $\mathbf{X1}_i$ is a quantitative variable, $\mathbf{X2}_i$ is a qualitative variable taking on values 0 or 1, and $\mathbf{X1}_i\mathbf{X2}_i$ is the interaction. The variable $\mathbf{X2}_i$ is called a dummy, binary, or indicator variable. With values 0 or 1, it distinguishes between two populations. The model is of the form

$$\mathbf{Y}_i = \beta_0 + \beta_1 \mathbf{X} \mathbf{1}_i + \beta_2 \mathbf{X} \mathbf{2}_i + \beta_3 \mathbf{X} \mathbf{1}_i \mathbf{X} \mathbf{2}_i + \boldsymbol{\epsilon}_i$$

for the observations i = 1, 2, ..., n. The parameters to be estimated are β_0 , β_1 , β_2 , and β_3 . The number of dummy variables used is one less than the number of qualitative levels. This yields a nonsingular X'X matrix. See Chapter 10 of Neter, Wasserman, and Kutner (1990) for more details.

An example from Neter, Wasserman, and Kutner (1990) follows. An economist is investigating the relationship between the size of an insurance firm and the speed at which it implements new insurance innovations. He believes that the type of firm might affect this relationship and suspects that there might be some interaction between the size and type of firm. The dummy variable in the model enables the two firms to have different intercepts. The interaction term enables the firms to have different slopes as well.

In this study, \mathbf{Y}_i is the number of months from the time the first firm implemented the innovation to the time it was implemented by the *i*th firm. The variable $\mathbf{X}\mathbf{1}_i$ is the size of the firm, measured in total assets of the firm. The variable $\mathbf{X}\mathbf{2}_i$ denotes the firm type; it is 0 if the firm is a mutual fund company and 1 if the firm is a stock company. The dummy variable enables each firm type to have a different intercept and slope.

The previous model can be broken down into a model for each firm type by plugging in the values for $\mathbf{X2}_i$. If $\mathbf{X2}_i = 0$, the model is

$$\mathbf{Y}_i = \beta_0 + \beta_1 \mathbf{X} \mathbf{1}_i + \boldsymbol{\epsilon}_i$$

This is the model for a mutual company. If $X2_i = 1$, the model for a stock firm is

$$\mathbf{Y}_i = (\beta_0 + \beta_2) + (\beta_1 + \beta_3)\mathbf{X}\mathbf{1}_i + \boldsymbol{\epsilon}_i$$

This model has intercept $\beta_0 + \beta_2$ and slope $\beta_1 + \beta_3$.

The data¹ follow. Note that the interaction term is created in the DATA step since polynomial effects such as size*type are not allowed in the MODEL statement in the REG procedure.

```
title 'Regression With Quantitative and Qualitative Variables';
data insurance;
  input time size type @@;
  sizetype=size*type;
  datalines;
17 151 0  26 92 0  21 175 0  30  31 0  22 104 0
  0 277 0  12 210 0  19 120 0  4 290 0  16 238 0
28 164 1  15 272 1  11 295 1  38 68 1  31 85 1
21 224 1  20 166 1  13 305 1  30 124 1  14 246 1
;
run;
```

The following statements begin the analysis:

```
proc reg data=insurance;
  model time = size type sizetype;
run;
```

The ANOVA table is displayed in Output 73.4.1.

Output 73.4.1 ANOVA Table and Parameter Estimates

				ariables					
		The REG Proced	lure						
		Model: MODEL	.1						
	Depe	endent Variable	e: time						
Analysis of Variance									
		Sum of	Mean						
Source	DF	Squares	Square	F Value	Pr > F				
Model	3	1504.41904	501.47301	45.49	<.0001				
Error	16	176.38096	11.02381						
Corrected Total	19	1680.80000							
Root	MSE	3.32021	R-Square	0.8951					
Deper	ndent Mean	19.40000	Adj R-Sq	0.8754					
Coef	f Var	17.11450	_						

¹From Neter, J., et al., *Applied Linear Statistical Models*, Third Edition, Copyright (c) 1990, Richard D. Irwin. Reprinted with permission of The McGraw-Hill Companies.

Output 73.4.1 continued

Parameter Estimates								
		Parameter	Standard					
Variable	DF	Estimate	Error	t Value	Pr > t			
Intercept	1	33.83837	2.44065	13.86	<.0001			
size	1	-0.10153	0.01305	-7.78	<.0001			
type	1	8.13125	3.65405	2.23	0.0408			
sizetype	1	-0.00041714	0.01833	-0.02	0.9821			

The overall F statistic is significant (F=45.490, p<0.0001). The interaction term is not significant (t=-0.023, p=0.9821). Hence, this term should be removed and the model refitted, as shown in the following statements:

```
delete sizetype;
  print;
run;
```

The DELETE statement removes the interaction term (sizetype) from the model. The new ANOVA and parameter estimates tables are shown in Output 73.4.2.

Output 73.4.2 ANOVA Table and Parameter Estimates

		1	Analysis o	f Variance	1			
			Sum	of	Mean			
Source		DF	Squa	res	Square	F	Value	Pr > 1
Model		2	1504.41	333 7	52.20667		72.50	<.000
Error		17	176.38	667	10.37569			
Corrected Total		19	1680.80	000				
Ro	ot MSE		3.22	113 R-S	quare	0.89	51	
De	pendent	Mean	19.40	000 Ad	R-Sq	0.88	27	
Co	eff Var		16.60	377				
		I	Parameter 1	Estimates				
		Para	ameter	Standar	d			
Variable	DF	Est	cimate	Erro	or t V	alue	Pr >	t
Intercept	1	33	.87407	1.8138	6 1	8.68	<.0	001
size	1	-0	.10174	0.0088	9 -1	1.44	<.0	001
type	1	8	. 05547	1.4591	.1	5.52	<.0	001

The overall F statistic is still significant (F=72.497, p<0.0001). The intercept and the coefficients associated with size and type are significantly different from zero (t=18.675, p<0.0001; t=-11.443, p<0.0001; t=5.521, p<0.0001, respectively). Notice that the R^2 did not change with the omission of the interaction term.

The fitted model is

time =
$$33.87 - 0.102 \times \text{size} + 8.055 \times \text{type}$$

The fitted model for a mutual fund company $(X2_i = 0)$ is

$$time = 33.87 - 0.102 \times size$$

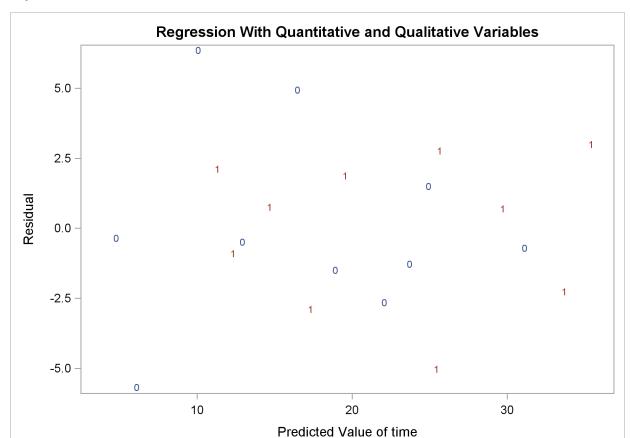
and the fitted model for a stock company $(X2_i = 1)$ is

time =
$$(33.87 + 8.055) - 0.102 \times \text{size}$$

So the two models have different intercepts but the same slope.

The following statements first use an OUTPUT statement to save the residuals and predicted values from the new model in the OUT= data set. Next PROC SGPLOT is used to produce Output 73.4.3, which plots residuals versus predicted values. The firm type is used as the plot symbol; this can be useful in determining if the firm types have different residual patterns.

```
output out=out r=r p=p;
run;
proc sgplot data=out;
   scatter x=p y=r / markerchar=type group=type;
run;
```



Output 73.4.3 Plot of Residual vs. Predicted Values

The residuals show no major trend. Neither firm type by itself shows a trend either. This indicates that the model is satisfactory.

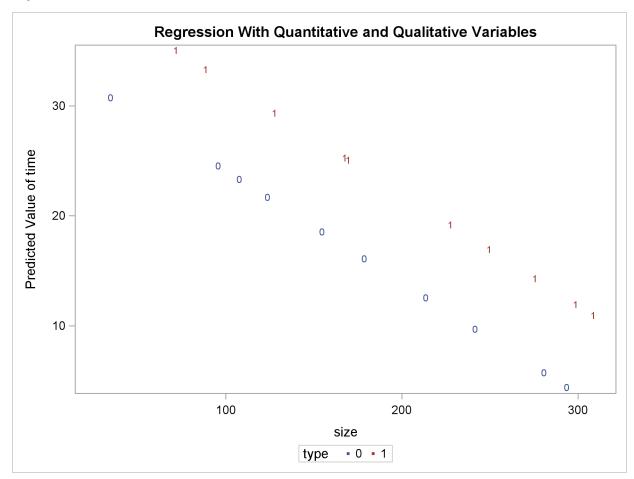
type

• 0 • 1

The following statements produce the plot of the predicted values versus size that appears in Output 73.4.4, where the firm type is again used as the plotting symbol:

```
proc sgplot data=out;
   scatter x=size y=p / markerchar=type group=type;
run;
```

Output 73.4.4 Plot of Predicted vs. Size



The different intercepts are very evident in this plot.

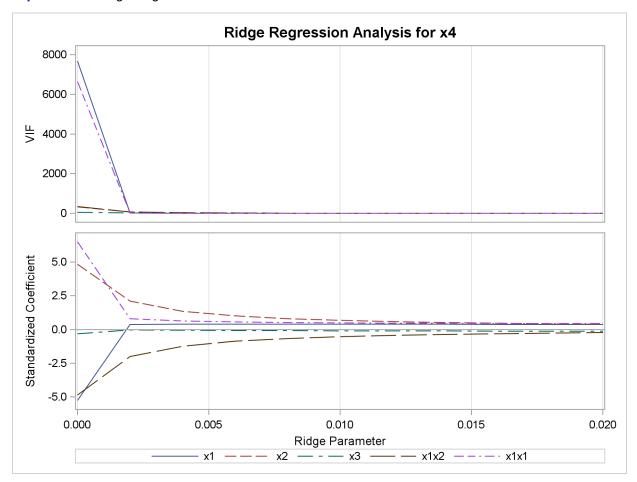
Example 73.5: Ridge Regression for Acetylene Data

This example uses the acetylene data in Marquardt and Snee (1975) to illustrate the RIDGEPLOT and OUTVIF options. Here are the data:

```
1300 7.5 .012 49
                    1300 9
                              .012 50.2 1300 11 .0115 50.5
                              .0135 47.5 1300 23 .012
1300 13.5 .013 48.5 1300 17
1200 5.3 .04
               28
                    1200 7.5 .038
                                    31.5 1200 11 .032
                                                       34.5
1200 13.5 .026 35
                    1200 17
                              .034
                                    38
                                         1200 23 .041
                                                       38.5
1100 5.3 .084 15
                    1100 7.5 .098
                                    17
                                         1100 11 .092 20.5
          .086 29.5
1100 17
ods graphics on;
proc reg data=acetyl outvif
         outest=b ridge=0 to 0.02 by .002;
  model x4=x1 x2 x3 x1x2 x1x1;
run;
proc print data=b;
run;
```

When you enable ODS Graphics and you request ridge regression by using the RIDGE= option in the PROC REG statement, PROC REG produces a panel showing variance inflation factors (VIF) in the upper plot in the panel and ridge traces in the lower plot. This panel is shown in Output 73.5.1.

Output 73.5.1 Ridge Regression and VIF Traces



The OUTVIF option outputs the variance inflation factors to the OUTEST= data set that is shown in Output 73.5.2.

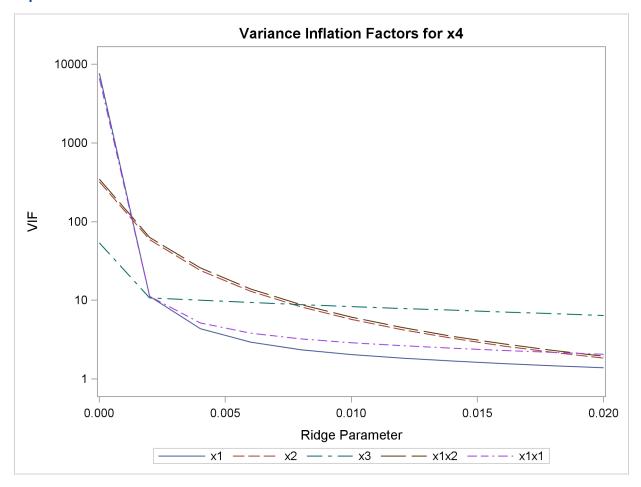
Output 73.5.2 OUTEST Data Set Showing VIF Values

Obs	_MODEL_	_TYPE_	_DEPVAR_	_RIDGE_	_PCOMIT_	_RMSE_	Intercept
1	MODEL1	PARMS	x 4	•	•	1.15596	390.538
2	MODEL1	RIDGEVIF	x4	0.000	•	•	•
3	MODEL1	RIDGE	x4	0.000	•	1.15596	390.538
4	MODEL1	RIDGEVIF	x4	0.002	•		
5	MODEL1	RIDGE	x4	0.002	•	2.69721	-103.388
6	MODEL1	RIDGEVIF	x 4	0.004		•	
7	MODEL1	RIDGE	x 4	0.004		3.22340	-93.797
8	MODEL1	RIDGEVIF	×4	0.006		•	
9	MODEL1	RIDGE	x 4	0.006		3.47752	-87.687
10	MODEL1	RIDGEVIF	x4	0.008			
11	MODEL1	RIDGE	x4	0.008		3.62677	-83.593
12	MODEL1	RIDGEVIF	x4	0.010		•	•
13	MODEL1	RIDGE	×4	0.010		3.72505	-80.603
14	MODEL1	RIDGEVIF	×4	0.012		•	
15	MODEL1	RIDGE	×4	0.012		3.79477	-78.276
16	MODEL1	RIDGEVIF	×4	0.014		•	
17	MODEL1	RIDGE	x4	0.014		3.84693	-76.381
18	MODEL1	RIDGEVIF	x4	0.016			
19	MODEL1	RIDGE	x4	0.016		3.88750	-74.785
20	MODEL1	RIDGEVIF	x4	0.018			
21	MODEL1	RIDGE	x4	0.018		3.92004	-73.407
22	MODEL1	RIDGEVIF	x4	0.020			
23	MODEL1	RIDGE	x4	0.020	•	3.94679	-72.193
Obs	ж1	x 2	x 3	ж1	Lx2 x	1x1 x4	
1	-0.78	10.174	-121.626	-0.0	0 800	.00 -1	
2	7682.37				6643	.32 –1	
3	-0.78	10.174	-121.626	-0.0	0 800	.00 -1	
4	11.18	58.731	10.744	63.2	208 11	.22 –1	
5	0.05	4.404	-9.065	-0.0	003 0	.00 -1	
6	4.36	23.939	9.996	25.7	744 5	.15 –1	
7	0.06	2.839	-21.338			.00 -1	
8	2.93	13.011	9.383	13.9	976 3	.81 -1	
9	0.06	2.110	-28.447	-0.0	001 0	.00 -1	
10	2.36	8.224				.23 –1	
11	0.06	1.689				.00 -1	
12	2.04	5.709	8.343			.89 –1	
13	0.06	1.414	-37.177	-0.0	001 0	.00 -1	
14	1.84	4.226	7.891	4.5		.65 -1	
15	0.06	1.221	-40.297	-0.0		.00 -1	
16	1.69	3.279	7.476	3.4		.46 -1	
17	0.06	1.078	-42.965	-0.0		.00 -1	
18	1.57	2.637	7.094	2.8		.31 –1	
19	0.06	0.968	-45.309	-0.0		.00 -1	
20	1.47	2.182	6.741	2.3		.18 –1	
21	0.06	0.880	-47.407	-0.0		.00 -1	
22	1.39	1.847	6.415			.06 -1	
23	0.06	0.809	-49.310	-0.0		.00 -1	

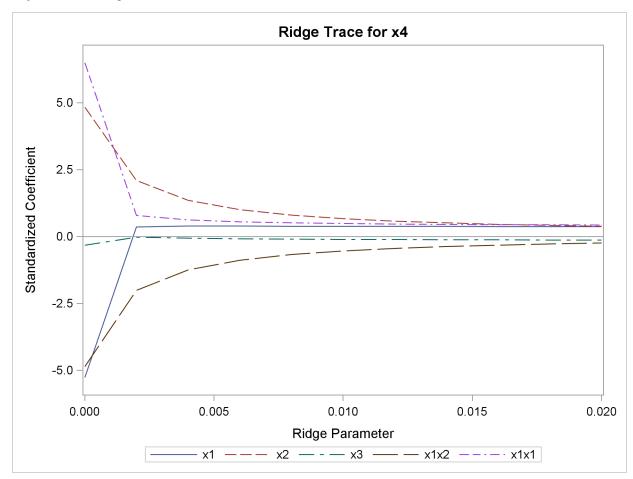
If you want to obtain separate plots containing the ridge traces and VIF traces, you can specify the UNPACK suboption in the PLOTS=RIDGE option. You can also request that one or both of the VIF axis and ridge parameter axis be displayed on a logarithmic scale. You can see in Output 73.5.1 that the VIF traces for several of the parameters are nearly indistinguishable when displayed on a linear scale. The following code illustrates how you obtain separate VIF and ridge traces with the VIF values displayed on a logarithmic scale. Note that you can obtain plots of VIF values even though you do not specify the OUTVIF option in the PROC REG statement.

The requested plots are shown in Output 73.5.3 and Output 73.5.4.

Output 73.5.3 VIF Traces



Output 73.5.4 Ridge Traces



Example 73.6: Chemical Reaction Response

This example shows how you can use lack-of-fit tests with the REG procedure. See the section "Testing for Lack of Fit" on page 5570 for details about lack-of-fit tests.

In a study of the percentage of raw material that responds in a reaction, researchers identified the following five factors:

- the feed rate of the chemicals (FeedRate), ranging from 10 to 15 liters per minute
- the percentage of the catalyst (Catalyst), ranging from 1% to 2%
- the agitation rate of the reactor (AgitRate), ranging from 100 to 120 revolutions per minute
- the temperature (Temperature), ranging from 140 to 180 degrees Celsius
- the concentration (Concentration), ranging from 3% to 6%

The following data set contains the results of an experiment designed to estimate main effects for all factors:

```
data reaction;
 input FeedRate Catalyst AgitRate Temperature
       Concentration ReactionPercentage;
datalines;
10.0
      1.0 100
              140 6.0
                          37.5
10.0
      1.0 120 180 3.0
                          28.5
10.0
      2.0 100
               180 3.0
                          40.4
     2.0 120 140 6.0
10.0
                          48.2
15.0
      1.0 100 180 6.0
                          50.7
      1.0 120 140 3.0
                          28.9
15.0
15.0
      2.0 100 140 3.0
                          43.5
15.0
    2.0 120 180 6.0
                        64.5
12.5
     1.5 110 160 4.5
                          39.0
12.5
      1.5 110
               160 4.5
                          40.3
                160 4.5
12.5
      1.5 110
                          38.7
12.5
      1.5 110
                160 4.5
                          39.7
```

The first eight runs of this experiment enable orthogonal estimation of the main effects for all factors. The last four comprise four replicates of the centerpoint.

The following statements fit a linear model. Because this experiment includes replications, you can test for lack of fit by using the LACKFIT option in the MODEL statement.

Output 73.6.1 shows that the lack of fit for the linear model is significant, indicating that a more complex model is required. Models that include interactions should be investigated. In this case, this will require additional experimentation to obtain appropriate data for estimating the effects.

Output 73.6.1 Analysis of Variance

		Model: MODEI	-		
	Dependent '	Variable: React	ionPercentage		
	1	Analysis of Var	iance		
		Sum of	Mean		
Source	DF	Squares	Square	F Value	Pr > F
Model	5	990.27000	198.05400	33.29	0.0003
Error	6	35.69917	5.94986		
Lack of Fit	3	34.15167	11.38389	22.07	0.0151
Pure Error	3	1.54750	0.51583		
Corrected Total	11	1025.96917			
Roc	ot MSE	2.43923	R-Square	0.9652	
Der	pendent Mean	41.65833	Adj R-Sq	0.9362	
Coe	eff Var	5.85533	_		

References

Akaike, H. (1969), "Fitting Autoregressive Models for Prediction," *Annals of the Institute of Statistical Mathematics*, 21, 243–247.

Allen, D. M. (1971), "Mean Square Error of Prediction as a Criterion for Selecting Variables," *Technometrics*, 13, 469–475.

Allen, D. M. and Cady, F. B. (1982), *Analyzing Experimental Data by Regression*, Belmont, CA: Lifetime Learning Publications.

Amemiya, T. (1976), "Selection of Regressors," Technical Report No. 225, Stanford, CA: Stanford University.

Belsley, D. A., Kuh, E., and Welsch, R. E. (1980), *Regression Diagnostics*, New York: John Wiley & Sons.

Berk, K. N. (1977), "Tolerance and Condition in Regression Computations," *Journal of the American Statistical Association*, 72, 863–866.

Bock, R. D. (1975), *Multivariate Statistical Methods in Behavioral Research*, New York: McGraw-Hill.

Box, G. E. P. (1966), "The Use and Abuse of Regression," Technometrics, 8, 625–629.

Cleveland, W. S. (1993), Visualizing Data, Summit, NJ: Hobart Press.

Collier Books (1987), The 1987 Baseball Encyclopedia Update, New York: Macmillan.

Cook, R. D. (1977), "Detection of Influential Observations in Linear Regression," *Technometrics*, 19, 15–18.

Cook, R. D. (1979), "Influential Observations in Linear Regression," *Journal of the American Statistical Association*, 74, 169–174.

Daniel, C. and Wood, F. (1980), *Fitting Equations to Data*, Revised Edition, New York: John Wiley & Sons.

Darlington, R. B. (1968), "Multiple Regression in Psychological Research and Practice," *Psychological Bulletin*, 69, 161–182.

Draper, N. and Smith, H. (1981), *Applied Regression Analysis*, Second Edition, New York: John Wiley & Sons.

Durbin, J. and Watson, G. S. (1951), "Testing for Serial Correlation in Least Squares Regression," *Biometrika*, 37, 409–428.

Freund, R. J. and Littell, R. C. (1986), SAS System for Regression, 1986 Edition, Cary, NC: SAS Institute Inc.

Furnival, G. M. and Wilson, R. W. (1974), "Regression by Leaps and Bounds," *Technometrics*, 16, 499–511.

Goodnight, J. H. (1979), "A Tutorial on the SWEEP Operator," *The American Statistician*, 33, 149–158. (Also available as *The Sweep Operator: Its Importance in Statistical Computing*, SAS Technical Report R-106.)

Hocking, R. R. (1976), "The Analysis and Selection of Variables in Linear Regression," *Biometrics*, 32, 1–50.

Johnston, J. (1972), Econometric Methods, New York: McGraw-Hill.

Judge, G. G., Griffiths, W. E., Hill, R. C., and Lee, T. (1980), *The Theory and Practice of Econometrics*, New York: John Wiley & Sons.

Judge, G. G., Griffiths, W. E., Hill, R. C., Lutkepohl, H., and Lee, T. C. (1985), *The Theory and Practice of Econometrics*, Second Edition, New York: John Wiley & Sons.

Kennedy, W. J. and Gentle, J. E. (1980), Statistical Computing, New York: Marcel Dekker.

LaMotte, L. R. (1994), "A Note on the Role of Independence in t Statistics Constructed from Linear Statistics in Regression Models," *The American Statistician*, 48, 238–240.

Lewis, T. and Taylor, L. R. (1967), *Introduction to Experimental Ecology*, New York: Academic Press.

Long, J. S. and Ervin, L. H.(2000), "Correcting for Heteroscedasticity with Heteroscedasticity Consistent Standard Errors in the Linear Regression Model: Small Sample Considerations," *The American Statistician*, 54, 217–224.

Lord, F. M. (1950), "Efficiency of Prediction When a Progression Equation from One Sample Is Used in a New Sample," Research Bulletin No. 50-40, Princeton, NJ: Educational Testing Service.

MacKinnon, J. G. and White, H. (1985), "Some Heteroskedasticity Consistent Covariance matrix Estimators with Improved Finite Sample Properties," *Journal of Econometrics*, 29, 53–57.

Mallows, C. L. (1967), "Choosing a Subset Regression," unpublished report, Bell Telephone Laboratories.

Mallows, C. L. (1973), "Some Comments on C_p ," Technometrics, 15, 661–675.

Mardia, K. V., Kent, J. T., and Bibby, J. M. (1979), Multivariate Analysis, London: Academic Press.

Marquardt, D. W. and Snee, R. D. (1975), "Ridge Regression in Practice," *American Statistician*, 29 (1), 3–20.

Morrison, D. F. (1976), Multivariate Statistical Methods, Second Edition, New York: McGraw-Hill.

Mosteller, F. and Tukey, J. W. (1977), *Data Analysis and Regression*, Reading, MA: Addison-Wesley.

Neter, J., Wasserman, W., and Kutner, M. H. (1990), Applied Linear Statistical Models, Third

Edition, Homewood, IL: Irwin.

Nicholson, G. E., Jr. (1948), "The Application of a Regression Equation to a New Sample," unpublished Ph.D. dissertation, University of North Carolina at Chapel Hill.

Pillai, K. C. S. (1960), *Statistical Table for Tests of Multivariate Hypotheses*, Manila: The Statistical Center, University of the Philippines.

Pindyck, R. S. and Rubinfeld, D. L. (1981), *Econometric Models and Econometric Forecasts*, Second Edition, New York: McGraw-Hill.

Pringle, R. M. and Rayner, A. A. (1971), *Generalized Inverse Matrices with Applications to Statistics*, New York: Hafner Publishing.

Rao, C. R. (1973), *Linear Statistical Inference and Its Applications*, Second Edition, New York: John Wiley & Sons.

Rawlings, J. O. (1988), Applied Regression Analysis: A Research Tool, Belmont, CA: Wadsworth.

Rothman, D. (1968), letter to the editor, *Technometrics*, 10, 432.

Sall, J. P. (1981), SAS Regression Applications, Revised Edition, SAS Technical Report A-102, Cary, NC: SAS Institute Inc.

Sawa, T. (1978), "Information Criteria for Discriminating among Alternative Regression Models," *Econometrica*, 46, 1273–1282.

Schwarz, G. (1978), "Estimating the Dimension of a Model," Annals of Statistics, 6, 461–464.

Sports Illustrated, April 20, 1987.

Stein, C. (1960), "Multiple Regression," in *Contributions to Probability and Statistics*, eds. I. Olkin et al., Stanford, CA: Stanford University Press.

Timm, N. H. (1975), *Multivariate Analysis with Applications in Education and Psychology*, Monterey, CA: Brooks-Cole.

Weisberg, S. (1980), Applied Linear Regression, New York: John Wiley & Sons.

White, H. (1980), "A Heteroskedasticity-Consistent Covariance Matrix Estimator and a Direct Test for Heteroskedasticity," *Econometrics*, 48, 817–838.

Subject Index

adjusted R ² selection (REG), 5519	REG procedure, 5450, 5471
alpha level	influence diagnostics
REG procedure, 5448	examples (REG), 5586
annotate	influence statistics
global data set (REG), 5448	REG procedure, 5553
local data set (REG), 5487	IPC analysis
autocorrelation	REG procedure, 5450, 5471, 5577
REG procedure, 5575	
	lack of fit
backward elimination	examples (REG), 5636
REG procedure, 5429, 5518	lack-of-fit
***	testing (REG), 5570
collinearity	line printer plots
REG procedure, 5549	REG procedure, 5491, 5528
correlation	LMSELECT procedure
matrix (REG), 5448	ODS Graphics, 5450
covariance matrix	
REG procedure, 5448	Mallows' C_p selection
COVRATIO statistic, 5554	REG procedure, 5520
crossproducts matrix	model
REG procedure, 5578	fit summary (REG), 5551
delete veriables (DEC) 5462	model building
delete variables (REG), 5462 deleting observations	examples (REG), 5586
REG procedure, 5563	model selection
DFBETAS statistic (REG), 5555	examples (REG), 5602
DFFITS statistic (REG), 3333	REG procedure, 5429, 5517, 5520, 5521
REG procedure, 5554	multicollinearity
diagnostic statistics	REG procedure, 5549
REG procedure, 5551, 5552	multivariate tests
REG procedure, 3331, 3332	REG procedure, 5571
fit diagnostics	non-full-rank models
examples (REG), 5586	REG procedure, 5547
forward selection	REG procedure, 3347
REG procedure, 5429, 5517	ODS graph names
Table procedure, 6 125, 6617	REG procedure, 5585
graphics	ODS GRAPHICS
keywords (REG), 5484	examples (REG), 5586
options (REG), 5485	ODS Graphics
traditional plots (REG), 5483	LMSELECT procedure, 5450
•	Embedder procedure, eneo
hat matrix, 5554	P-P plots
heteroscedasticity	REG procedure, 5577
testing (REG), 5569	painting line-printer plots
hypothesis tests	REG procedure, 5537
multivariate (REG), 5571	parameter estimates
REG procedure, 5474, 5500	example (REG), 5521
	REG procedure, 5579
incomplete principal components	partial regression leverage plots
	· · · · · · · · · · · · · · · · · · ·

REG procedure, 5561	IPC analysis, 5450, 5471, 5577
plots	lack of fit, 5636
keywords (REG), 5484	lack-of-fit, testing, 5570
line printer (REG), 5491, 5528	line printer plots, 5491, 5528
options (REG), 5485, 5487	Mallows' C_p selection, 5520
traditional (REG), 5483, 5541	missing values, 5501
polynomial regression	model building, 5586
REG procedure, 5434	model fit summary statistics, 5551
predicted values	model selection, 5429, 5517, 5520, 5521,
REG procedure, 5520, 5525	5602
prediction	multicollinearity, 5549
example (REG), 5602	multivariate tests, 5571
(1123), c 002	new regressors, 5502
Q-Q plots	non-full-rank models, 5547
REG procedure, 5577	ODS graph names, 5585
qualitative variables	ODS GRAPHICS, 5586
REG procedure, 5627	ODS table names, 5581
ribo procedure, co2/	output data sets, 5506, 5512
R ² improvement	<u> </u>
REG procedure, 5518, 5519	P-P plots, 5577
R ² selection	painting line-printer plots, 5537
REG procedure, 5519	parameter estimates, 5521, 5579
refitting models	partial regression leverage plots, 5561
REG procedure, 5564	plot keywords and options, 5484, 5485,
REG procedure	5487
adding variables, 5461	plots, traditional, 5483
adjusted R ² selection, 5519	polynomial regression, 5434
alpha level, 5448	predicted values, 5520, 5525, 5602
annotations, 5448, 5487	Q-Q plots, 5577
ANOVA table, 5578	qualitative variables, 5627
	R ² improvement, 5518, 5519
autocorrelation, 5575	R ² selection, 5519
backward elimination, 5429, 5518	refitting models, 5564
collinearity, 5549	residual values, 5525
computational methods, 5578	restoring weights, 5565
correlation matrix, 5448	reweighting observations, 5563
covariance matrix, 5448	ridge regression, 5460, 5471, 5490, 5577
crossproducts matrix, 5578	5632
delete variables, 5462	singularities, 5578
deleting observations, 5563	stepwise selection, 5429, 5518
diagnostic statistics, 5551, 5552	summary statistics, 5551
dictionary of options, 5487	sweep algorithm, 5578
fit diagnostics, 5586	time series data, 5575
forward selection, 5429, 5517	traditional graphics, 5541
graphics keywords and options, 5484, 5485	variance inflation factors (VIF), 5450
graphics plots, traditional, 5483	regression
heteroscedasticity, testing, 5569	analysis (REG), 5428
hypothesis tests, 5474, 5500	residuals
incomplete principal components, 5450,	REG procedure, 5525
5471	restoring weights
influence diagnostics, 5586	REG procedure, 5565
influence statistics, 5553	reweighting observations
input data sets, 5502	REG procedure, 5563
interactive analysis, 5444, 5513	ridge regression
introductory example, 5430	riage regression

```
REG procedure, 5460, 5471, 5490, 5577,
         5632
singularities
    REG procedure, 5578
stepwise selection
    REG procedure, 5429, 5518
studentized residual, 5554
summary statistics
    REG procedure, 5551
sweep algorithm
    REG procedure, 5578
time series data
    REG procedure, 5575
traditional graphics
    REG procedure, 5541
variance inflation factors (VIF)
     REG procedure, 5450
VIF, see variance inflation factors
```

Syntax Index

ACOV option	CLINE= option
MODEL statement (REG), 5466	PLOT statement (REG), 5487
ACOVMETHOD= option	CLM option
MODEL statement (REG), 5466	MODEL statement (REG), 5467
ADD statement, REG procedure, 5461	CMALLOWS= option
ADJRSQ option	PLOT statement (REG), 5488
MODEL statement (REG), 5466	COLLECT option
AIC option	PLOT statement (REG), 5491
MODEL statement (REG), 5466	COLLIN option
PLOT statement (REG), 5487	MODEL statement (REG), 5467
ALL option	COLLINOINT option
MODEL statement (REG), 5466	MODEL statement (REG), 5467
PROC REG statement, 5448	CONF option
,	<u>-</u>
ALLOBS option PAINT statement (REC) 5480	PLOT statement (REG), 5488
PAINT statement (REG), 5480	CORR option
REWEIGHT statement (REG), 5498	PROC REG statement, 5448
ALPHA= option	CORRB option
MODEL statement (REG), 5466	MODEL statement (REG), 5467
PROC REG statement, 5448	COVB option
ANNOTATE= option	MODEL statement (REG), 5467
PLOT statement (REG), 5487	COVOUT option
PROC REG statement, 5448	PROC REG statement, 5448
D. and an	CP option
B option	MODEL statement (REG), 5468
MODEL statement (REG), 5466	PLOT statement (REG), 5488
BEST= option	CTEXT= option
MODEL statement (REG), 5466	PLOT statement (REG), 5488
BIC option	CVREF= option
MODEL statement (REG), 5467	PLOT statement (REG), 5488
PLOT statement (REG), 5487	
BY statement	DATA= option
REG procedure, 5461	PROC REG statement, 5449
	DELETE statement, REG procedure, 5462
CANPRINT option	DESCRIPTION= option
MTEST statement (REG), 5475	PLOT statement (REG), 5488
CAXIS= option	DETAILS option
PLOT statement (REG), 5487	MODEL statement (REG), 5468
CFRAME= option	MTEST statement (REG), 5475
PLOT statement (REG), 5487	DW option
CHOCKING= option	MODEL statement (REG), 5468
PLOT statement (REG), 5487	DWPROB option
CHREF= option	MODEL statement (REG), 5468
PLOT statement (REG), 5487	Mobble statement (RES), 5 100
CLB option	EDF option
MODEL statement (REG), 5467	MODEL statement (REG), 5468
CLEAR option	PLOT statement (REG), 5488
PLOT statement (REG), 5491	PROC REG statement, 5449
CLI option	The critical statement, 5 (1)
MODEL statement (REG), 5467	FREQ statement
(= // = = -	

REG procedure, 5462	REG procedure, 5463
	MODELFONT option
GMSEP option	PLOT statement (REG), 5489
MODEL statement (REG), 5468	MODELHT option
PLOT statement (REG), 5488	PLOT statement (REG), 5489
GOUT= option	MODELLAB option
PROC REG statement, 5449	PLOT statement (REG), 5489
GROUPNAMES= option	MSE option
MODEL statement (REG), 5468	MODEL statement (REG), 5470
` ''	PLOT statement (REG), 5489
HAXIS= option	MSTAT= option
PLOT statement (REG), 5488	MTEST statement (REG), 5476
HCC option	MTEST statement (REG), 5470
MODEL statement (REG), 5469	
HCCMETHOD= option	REG procedure, 5474
MODEL statement (REG), 5469	NAME= option
HPLOTS= option	PLOT statement (REG), 5489
PLOT statement (REG), 5492	
HREF= option	NOCOLLECT option
PLOT statement (REG), 5488	PLOT statement (REG), 5492
r LOT statement (RLO), 5468	NOINT option
I option	MODEL statement (REG), 5470
MODEL statement (REG), 5469	NOLINE option
ID statement	PLOT statement (REG), 5489
REG procedure, 5462	NOLIST option
	PAINT statement (REG), 5480
IN option	REWEIGHT statement (REG), 5498
PLOT statement (REG), 5489	NOMODEL option
INCLUDE= option	PLOT statement (REG), 5490
MODEL statement (REG), 5469	NOPRINT option
INFLUENCE option	MODEL statement (REG), 5470
MODEL statement (REG), 5469	PROC REG statement, 5449
ID and an	NOSTAT option
JP option	PLOT statement (REG), 5490
MODEL statement (REG), 5469	NP option
PLOT statement (REG), 5489	PLOT statement (REG), 5490
1	
keyword= option	OUT= option
OUTPUT statement (REG), 5477	OUTPUT statement (REG), 5476
I ACVEIT antion	OUTEST= option
LACKFIT option MODEL statement (REC) 5460	PROC REG statement, 5449
MODEL statement (REG), 5469	OUTPUT statement
LEGEND= option	REG procedure, 5476
PLOT statement (REG), 5489	OUTSEB option
LHREF= option	MODEL statement (REG), 5470
PLOT statement (REG), 5489	PROC REG statement, 5449
LINEPRINTER option	OUTSSCP= option
PROC REG statement, 5449	PROC REG statement, 5449
LLINE= option	•
PLOT statement (REG), 5489	OUTSTB option
LVREF= option	MODEL statement (REG), 5470
PLOT statement (REG), 5489	PROC REG statement, 5450
	OUTVIF option
MAXSTEP option	MODEL statement (REG), 5470
MODEL statement (REG), 5470	PROC REG statement, 5450
MODEL statement	OVERLAY option

PLOT statement (REG), 5490, 5492	ALL option, 5466
	ALPHA= option, 5466
P option	B option, 5466
MODEL statement (REG), 5470	BEST= option, 5466
PAINT statement	BIC option, 5467
REG procedure, 5478	CLB option, 5467
PARTIAL option	CLI option, 5467
MODEL statement (REG), 5470	CLM option, 5467
PARTIALDATA option	COLLIN option, 5467
MODEL statement (REG), 5471	COLLINOINT option, 5467
PARTIALR2 option	CORRB option, 5467
MODEL statement (REG), 5471	COVB option, 5467
PC option	CP option, 5468
MODEL statement (REG), 5471	DETAILS option, 5468
PLOT statement (REG), 5490	DW option, 5468
PCOMIT= option	DWPROB option, 5468
MODEL statement (REG), 5471	EDF option, 5468
PROC REG statement, 5450	GMSEP option, 5468
PCORR1 option	GROUPNAMES= option, 5468
MODEL statement (REG), 5471	HCC option, 5469
PCORR2 option	HCCMETHOD= option, 5469
MODEL statement (REG), 5471	I option, 5469
PLOT option	<u>*</u>
PROC REG statement, 5450	INCLUDE= option, 5469
PLOT statement	INFLUENCE option, 5469
REG procedure, 5481	JP option, 5469
<u> -</u>	LACKFIT option, 5469
PLOTS option PROCEREC statement, 5450	MAXSTEP option, 5470
PROC REG statement, 5450	MSE option, 5470
PRED option	NOINT option, 5470
PLOT statement (REG), 5490	NOPRINT option, 5470
PRESS option	OUTSEB option, 5470
MODEL statement (REG), 5471	OUTSTB option, 5470
PROC REG statement, 5460	OUTVIF option, 5470
PRINT option	P option, 5470
MTEST statement (REG), 5476	PARTIAL option, 5470
TEST statement (REG), 5500	PARTIALDATA option, 5471
PRINT statement, REG procedure, 5493	PARTIALR2 option, 5471
PROC REG statement, see REG procedure	PC option, 5471
	PCOMIT= option, 5471
R option	PCORR1 option, 5471
MODEL statement (REG), 5471	PCORR2 option, 5471
REFIT statement, REG procedure, 5494	PRESS option, 5471
REG procedure	R option, 5471
syntax, 5445	RIDGE= option, 5471
REG procedure, ADD statement, 5461	RMSE option, 5472
REG procedure, BY statement, 5461	RSQUARE option, 5472
REG procedure, DELETE statement, 5462	SBC option, 5472
REG procedure, FREQ statement, 5462	SCORR1 option, 5472
REG procedure, ID statement, 5462	SCORR2 option, 5472
REG procedure, MODEL statement, 5463	SELECTION= option, 5429, 5472
ACOV option, 5466	SEQB option, 5473
ACOVMETHOD= option, 5466	SIGMA= option, 5473
ADJRSQ option, 5466	SINGULAR= option, 5473
AIC option, 5466	SLENTRY= option, 5473
<u>*</u>	OLABANIS I — ODUUH. 14/1

SLSTAY= option, 5473	LLINE= option, 5489
SP option, 5473	LVREF= option, 5489
SPEC option, 5473	MODELFONT option, 5489
SS1 option, 5473	MODELHT option, 5489
SS2 option, 5473	MODELLAB option, 5489
SSE option, 5473	MSE option, 5489
START= option, 5474	NAME= option, 5489
STB option, 5474	NOCOLLECT option, 5492
STOP= option, 5474	NOLINE option, 5489
TOL option, 5474	NOMODEL option, 5490
VIF option, 5474	NOSTAT option, 5490
WHITE option, 5474	NP option, 5490
XPX option, 5474	OVERLAY option, 5490, 5492
REG procedure, MTEST statement, 5474	PC option, 5490
CANPRINT option, 5475	PRED option, 5490
DETAILS option, 5475	RIDGEPLOT option, 5490
MSTAT= option, 5476	SBC option, 5490
PRINT option, 5476	SP option, 5490
REG procedure, OUTPUT statement, 5476	SSE option, 5490
keyword= option, 5477	STATFONT option, 5490
OUT= option, 5476	STATHT option, 5491
REG procedure, PAINT statement, 5478	summary of options, 5484, 5485
ALLOBS option, 5480	SYMBOL= option, 5492
NOLIST option, 5480	USEALL option, 5491
RESET option, 5480	VAXIS= option, 5491
STATUS option, 5481	VPLOTS= option, 5493
SYMBOL= option, 5480	VREF= option, 5491
5 I MDOL- Option, 5460	VKET - Option, 5491
LINDO option 5481	DEC procedure DDINT statement 5403
UNDO option, 5481	REG procedure, PRINT statement, 5493
REG procedure, PLOT statement, 5481	REG procedure, PROC REG statement, 5447
REG procedure, PLOT statement, 5481 AIC option, 5487	REG procedure, PROC REG statement, 5447 ALL option, 5448
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSSCP= option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSEB option, 5449 OUTSTB option, 5449
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488 CVREF= option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSEB option, 5449 OUTSTB option, 5450 OUTVIF option, 5450
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488 CVREF= option, 5488 DESCRIPTION= option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSCP= option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488 CVREF= option, 5488 DESCRIPTION= option, 5488 EDF option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSEB option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450 PLOT option, 5450
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488 CVREF= option, 5488 DESCRIPTION= option, 5488 EDF option, 5488 GMSEP option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSEB option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450 PLOT option, 5450 PLOTS option, 5450 PLOTS option, 5450
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CYREF= option, 5488 CVREF= option, 5488 EDF option, 5488 GMSEP option, 5488 HAXIS= option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSCP= option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450 PLOT option, 5450 PLOT option, 5450 PLOTS option, 5450 PRESS option, 5460
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CYREF= option, 5488 CVREF= option, 5488 DESCRIPTION= option, 5488 EDF option, 5488 GMSEP option, 5488 HAXIS= option, 5488 HAXIS= option, 5488 HPLOTS= option, 5492	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSCP= option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450 PLOT option, 5450 PLOT option, 5450 PLOTS option, 5450 PLOTS option, 5450 PLOTS option, 5450 PRESS option, 5460 RIDGE= option, 5460
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488 CVREF= option, 5488 DESCRIPTION= option, 5488 EDF option, 5488 GMSEP option, 5488 HAXIS= option, 5488 HPLOTS= option, 5488 HPLOTS= option, 5488 HREF= option, 5488	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 NOPRINT option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSEP option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450 PLOT option, 5450 PLOT option, 5450 PLOTS option, 5450 PRESS option, 5460 RIDGE= option, 5460 RSQUARE option, 5460
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488 CVREF= option, 5488 DESCRIPTION= option, 5488 EDF option, 5488 GMSEP option, 5488 HAXIS= option, 5488 HPLOTS= option, 5488 IN option, 5489	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSCP= option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450 PLOT option, 5450 PLOT soption, 5450 PLOTS option, 5450 PRESS option, 5460 RIDGE= option, 5460 RSQUARE option, 5460 SIMPLE option, 5460
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488 CVREF= option, 5488 DESCRIPTION= option, 5488 EDF option, 5488 GMSEP option, 5488 HAXIS= option, 5488 HPLOTS= option, 5488 IN option, 5489 JP option, 5489	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSEB option, 5449 OUTSCP= option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450 PLOT option, 5450 PLOT soption, 5450 PLOTS option, 5450 PRESS option, 5460 RIDGE= option, 5460 SIMPLE option, 5460 SINGULAR= option, 5460
REG procedure, PLOT statement, 5481 AIC option, 5487 ANNOTATE= option, 5487 BIC option, 5487 CAXIS= option, 5487 CFRAME= option, 5487 CHOCKING= option, 5487 CHREF= option, 5487 CLEAR option, 5491 CLINE= option, 5487 CMALLOWS= option, 5488 COLLECT option, 5491 CONF option, 5488 CP option, 5488 CTEXT= option, 5488 CVREF= option, 5488 DESCRIPTION= option, 5488 EDF option, 5488 GMSEP option, 5488 HAXIS= option, 5488 HPLOTS= option, 5488 IN option, 5489	REG procedure, PROC REG statement, 5447 ALL option, 5448 ALPHA= option, 5448 ANNOTATE= option, 5448 CORR option, 5448 COVOUT option, 5448 DATA= option, 5449 EDF option, 5449 GOUT= option, 5449 LINEPRINTER option, 5449 OUTEST= option, 5449 OUTSEB option, 5449 OUTSCP= option, 5449 OUTSTB option, 5450 OUTVIF option, 5450 PCOMIT= option, 5450 PLOT option, 5450 PLOT soption, 5450 PLOTS option, 5450 PRESS option, 5460 RIDGE= option, 5460 RSQUARE option, 5460 SIMPLE option, 5460

REG procedure, REFIT statement, 5494	MODEL statement (REG), 5473
REG procedure, RESTRICT statement, 5494	PLOT statement (REG), 5490
REG procedure, REWEIGHT statement, 5496	SPEC option
ALLOBS option, 5498	MODEL statement (REG), 5473
NOLIST option, 5498	SS1 option
RESET option, 5498	MODEL statement (REG), 5473
STATUS option, 5499	SS2 option
UNDO option, 5499	MODEL statement (REG), 5473
WEIGHT= option, 5499	SSE option
REG procedure, TEST statement, 5500	MODEL statement (REG), 5473
PRINT option, 5500	PLOT statement (REG), 5490
REG procedure, VAR statement, 5501	START= option
REG procedure, WEIGHT statement, 5501	MODEL statement (REG), 5474
RESET option	STATFONT option
PAINT statement (REG), 5480	PLOT statement (REG), 5490
REWEIGHT statement (REG), 5498	STATHT option
RESTRICT statement	PLOT statement (REG), 5491
REG procedure, 5494	STATUS option
REWEIGHT statement, REG procedure, 5496	PAINT statement (REG), 5481
RIDGE= option	REWEIGHT statement (REG), 5499
MODEL statement (REG), 5471	STB option
PROC REG statement, 5460	MODEL statement (REG), 5474
RIDGEPLOT option	STOP= option
PLOT statement (REG), 5490	MODEL statement (REG), 5474
RMSE option	SYMBOL= option
MODEL statement (REG), 5472	PAINT statement (REG), 5480
RSQUARE option	PLOT statement (REG), 5492
MODEL statement (REG), 5472	· · · · · · · · · · · · · · · · · · ·
PROC REG statement, 5460	TABLEOUT option
,	PROC REG statement, 5461
SBC option	TEST statement
MODEL statement (REG), 5472	REG procedure, 5500
PLOT statement (REG), 5490	TOL option
SCORR1 option	MODEL statement (REG), 5474
MODEL statement (REG), 5472	
SCORR2 option	UNDO option
MODEL statement (REG), 5472	PAINT statement (REG), 5481
SELECTION= option	REWEIGHT statement (REG), 5499
MODEL statement (REG), 5472	USEALL option
REG procedure, MODEL statement, 5429	PLOT statement (REG), 5491
SEQB option	USSCP option
MODEL statement (REG), 5473	PROC REG statement, 5461
SIGMA= option	NAD data was
MODEL statement (REG), 5473	VAR statement
SIMPLE option	REG procedure, 5501
PROC REG statement, 5460	VAXIS= option
SINGULAR= option	PLOT statement (REG), 5491
MODEL statement (REG), 5473	VIF option
PROC REG statement, 5460	MODEL statement (REG), 5474
SLENTRY= option	VPLOTS= option
MODEL statement (REG), 5473	PLOT statement (REG), 5493
SLSTAY= option	VREF= option
MODEL statement (REG), 5473	PLOT statement (REG), 5491
SP option	WEIGHT statement

REG procedure, 5501
WEIGHT= option
REWEIGHT statement (REG), 5499
WHITE option
MODEL statement (REG), 5474

XPX option
MODEL statement (REG), 5474

Your Turn

We welcome your feedback.

- If you have comments about this book, please send them to yourturn@sas.com. Include the full title and page numbers (if applicable).
- If you have comments about the software, please send them to suggest@sas.com.

SAS® Publishing Delivers!

Whether you are new to the work force or an experienced professional, you need to distinguish yourself in this rapidly changing and competitive job market. SAS® Publishing provides you with a wide range of resources to help you set yourself apart. Visit us online at support.sas.com/bookstore.

SAS® Press

Need to learn the basics? Struggling with a programming problem? You'll find the expert answers that you need in example-rich books from SAS Press. Written by experienced SAS professionals from around the world, SAS Press books deliver real-world insights on a broad range of topics for all skill levels.

support.sas.com/saspress

SAS® Documentation

To successfully implement applications using SAS software, companies in every industry and on every continent all turn to the one source for accurate, timely, and reliable information: SAS documentation. We currently produce the following types of reference documentation to improve your work experience:

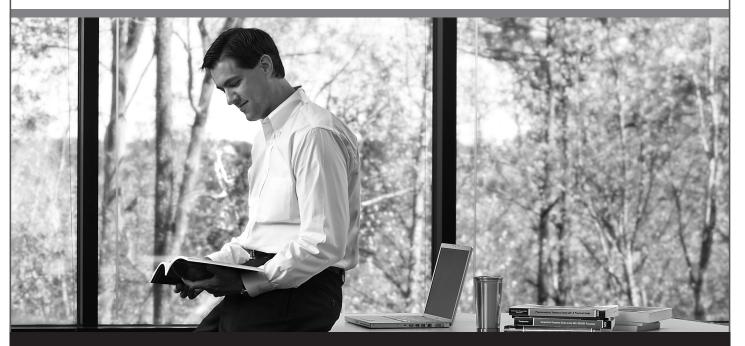
- Online help that is built into the software.
- Tutorials that are integrated into the product.
- Reference documentation delivered in HTML and PDF free on the Web.
- Hard-copy books.

support.sas.com/publishing

SAS® Publishing News

Subscribe to SAS Publishing News to receive up-to-date information about all new SAS titles, author podcasts, and new Web site features via e-mail. Complete instructions on how to subscribe, as well as access to past issues, are available at our Web site.

support.sas.com/spn



Sas THE POWER TO KNOW.