

SAS/STAT® 9.2 User's Guide The PRINCOMP Procedure (Book Excerpt)



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Chapter 69

The PRINCOMP Procedure

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Overview: PRINCOMP Procedure

The PRINCOMP procedure performs principal component analysis. As input you can use raw data, a correlation matrix, a covariance matrix, or a sum-of-squares-and-crossproducts (SSCP) matrix. You can create output data sets containing eigenvalues, eigenvectors, and standardized or unstandardized principal component scores.

Principal component analysis is a multivariate technique for examining relationships among several quantitative variables. The choice between using factor analysis and using principal component

analysis depends in part on your research objectives. You should use the PRINCOMP procedure if you are interested in summarizing data and detecting linear relationships. You can use principal components to reduce the number of variables in regression, clustering, and so on. See Chapter 9, "Introduction to Multivariate Procedures," for a detailed comparison of the PRINCOMP and FACTOR procedures.

You can use ODS Graphics to display the scree plot, component pattern plot, component pattern profile plot, matrix plot of component scores, and component score plots. These plots are especially valuable tools in exploratory data analysis.

Principal component analysis was originated by Pearson (1901) and later developed by Hotelling (1933). The application of principal components is discussed by Rao (1964), Cooley and Lohnes (1971), and Gnanadesikan (1977). Excellent statistical treatments of principal components are found in Kshirsagar (1972), Morrison (1976), and Mardia, Kent, and Bibby (1979).

Given a data set with p numeric variables, you can compute p principal components. Each principal component is a linear combination of the original variables, with coefficients equal to the eigenvectors of the correlation or covariance matrix. The eigenvectors are customarily taken with unit length. The principal components are sorted by descending order of the eigenvalues, which are equal to the variances of the components.

Principal components have a variety of useful properties (Rao 1964; Kshirsagar 1972):

- The eigenvectors are orthogonal, so the principal components represent jointly perpendicular directions through the space of the original variables.
- The principal component scores are jointly uncorrelated. Note that this property is quite distinct from the previous one.
- The first principal component has the largest variance of any unit-length linear combination of the observed variables. The jth principal component has the largest variance of any unit-length linear combination orthogonal to the first j-1 principal components. The last principal component has the smallest variance of any linear combination of the original variables.
- The scores on the first *j* principal components have the highest possible generalized variance of any set of unit-length linear combinations of the original variables.
- The first j principal components provide a least squares solution to the model

$$Y = XB + E$$

where **Y** is an $n \times p$ matrix of the centered observed variables; **X** is the $n \times j$ matrix of scores on the first j principal components; **B** is the $j \times p$ matrix of eigenvectors; **E** is an $n \times p$ matrix of residuals; and you want to minimize trace(**E**'**E**), the sum of all the squared elements in **E**. In other words, the first j principal components are the best linear predictors of the original variables among all possible sets of j variables, although any nonsingular linear transformation of the first j principal components would provide equally good prediction. The same result is obtained if you want to minimize the determinant or the Euclidean (Schur, Frobenious) norm of **E**'**E** rather than the trace.

• In geometric terms, the *j*-dimensional linear subspace spanned by the first *j* principal components provides the best possible fit to the data points as measured by the sum of squared

perpendicular distances from each data point to the subspace. This is in contrast to the geometric interpretation of least squares regression, which minimizes the sum of squared vertical distances. For example, suppose you have two variables. Then, the first principal component minimizes the sum of squared perpendicular distances from the points to the first principal axis. This is in contrast to least squares, which would minimize the sum of squared vertical distances from the points to the fitted line.

Principal component analysis can also be used for exploring polynomial relationships and for multivariate outlier detection (Gnanadesikan 1977), and it is related to factor analysis, correspondence analysis, allometry, and biased regression techniques (Mardia, Kent, and Bibby 1979).

Getting Started: PRINCOMP Procedure

The following data provide crime rates per 100,000 people in seven categories for each of the 50 states in 1977. Since there are seven numeric variables, it is impossible to plot all the variables simultaneously. Principal components can be used to summarize the data in two or three dimensions, and they help to visualize the data. The following statements produce Figure 69.1 through Figure 69.5.

```
data Crime;
   input State $1-15 Murder Rape Robbery Assault
        Burglary Larceny Auto_Theft;
   datalines;
            14.2 25.2 96.8 278.3 1135.5 1881.9 280.7
Alabama
             10.8 51.6 96.8 284.0 1331.7 3369.8 753.3
Alaska
Arizona
             9.5 34.2 138.2 312.3 2346.1 4467.4 439.5
Arkansas
              8.8 27.6 83.2 203.4 972.6 1862.1 183.4
California
            11.5 49.4 287.0 358.0 2139.4 3499.8 663.5
             6.3 42.0 170.7 292.9 1935.2 3903.2 477.1
Colorado
Connecticut
              4.2 16.8 129.5 131.8 1346.0 2620.7 593.2
             6.0 24.9 157.0 194.2 1682.6 3678.4 467.0
Delaware
            10.2 39.6 187.9 449.1 1859.9 3840.5 351.4
Florida
Georgia
            11.7 31.1 140.5 256.5 1351.1 2170.2 297.9
Hawaii
             7.2 25.5 128.0 64.1 1911.5 3920.4 489.4
              5.5 19.4 39.6 172.5 1050.8 2599.6 237.6
Idaho
Illinois
              9.9 21.8 211.3 209.0 1085.0 2828.5 528.6
              7.4 26.5 123.2 153.5 1086.2 2498.7 377.4
Indiana
Towa
              2.3 10.6 41.2 89.8 812.5 2685.1 219.9
              6.6 22.0 100.7 180.5 1270.4 2739.3 244.3
Kansas
Kentucky 10.1 19.1 81.1 123.3 872.2 1662.1 245.4
Louisiana
            15.5 30.9 142.9 335.5 1165.5 2469.9 337.7
             2.4 13.5 38.7 170.0 1253.1 2350.7 246.9
Maine
maine
Maryland
             8.0 34.8 292.1 358.9 1400.0 3177.7 428.5
Massachusetts 3.1 20.8 169.1 231.6 1532.2 2311.3 1140.1
              9.3 38.9 261.9 274.6 1522.7 3159.0 545.5
Michigan
             2.7 19.5 85.9 85.8 1134.7 2559.3 343.1
Minnesota
Mississippi 14.3 19.6 65.7 189.1 915.6 1239.9 144.4
```

```
9.6 28.3 189.0 233.5 1318.3 2424.2 378.4
Missouri
Montana
               5.4 16.7 39.2 156.8 804.9 2773.2 309.2
              3.9 18.1 64.7 112.7 760.0 2316.1 249.1
Nebraska
             15.8 49.1 323.1 355.0 2453.1 4212.6 559.2
Nevada
New Hampshire 3.2 10.7 23.2 76.0 1041.7 2343.9 293.4
New Jersey 5.6 21.0 180.4 185.1 1435.8 2774.5 511.5
              8.8 39.1 109.6 343.4 1418.7 3008.6 259.5
New Mexico
New York
              10.7 29.4 472.6 319.1 1728.0 2782.0 745.8
North Carolina 10.6 17.0 61.3 318.3 1154.1 2037.8 192.1
North Dakota 0.9 9.0 13.3 43.8 446.1 1843.0 144.7
              7.8 27.3 190.5 181.1 1216.0 2696.8 400.4
Ohio
Oklahoma
              8.6 29.2 73.8 205.0 1288.2 2228.1 326.8
Oregon
              4.9 39.9 124.1 286.9 1636.4 3506.1 388.9
Pennsylvania 5.6 19.0 130.3 128.0 877.5 1624.1 333.2
Rhode Island 3.6 10.5 86.5 201.0 1489.5 2844.1 791.4
South Carolina 11.9 33.0 105.9 485.3 1613.6 2342.4 245.1
South Dakota 2.0 13.5 17.9 155.7 570.5 1704.4 147.5
Tennessee 10.1 29.7 145.8 203.9 1259.7 1776.5 314.0
Texas
            13.3 33.8 152.4 208.2 1603.1 2988.7 397.6
Utah
              3.5 20.3 68.8 147.3 1171.6 3004.6 334.5
Vermont
              1.4 15.9 30.8 101.2 1348.2 2201.0 265.2
Virginia
              9.0 23.3 92.1 165.7 986.2 2521.2 226.7
Washington 4.3 39.6 106.2 224.8 1605.6 3386.9 360.3
West Virginia 6.0 13.2 42.2 90.9 597.4 1341.7 163.3
Wisconsin 2.8 12.9 52.2 63.7 846.9 2614.2 220.7
              5.4 21.9 39.7 173.9 811.6 2772.2 282.0
Wyoming
ods graphics on;
title 'Crime Rates per 100,000 Population by State';
proc princomp out=Crime_Components plots= score(ellipse ncomp=3);
   id State;
run:
ods graphics off;
```

Figure 69.1 displays the PROC PRINCOMP output, beginning with simple statistics followed by the correlation matrix. The PROC PRINCOMP statement requests by default principal components computed from the correlation matrix, so the total variance is equal to the number of variables, 7.

Figure 69.1 Number of Observations and Simple Statistics from the PRINCOMP Procedure

```
Crime Rates per 100,000 Population by State

The PRINCOMP Procedure

Observations 50

Variables 7
```

Figure 69.1 continued

			Simple St	atistics			
	Mur	der	Ra	pe	Robbery	i	Assault
Mean	7.444000		25.734000		24.0920000		3000000
StD	3.866768	941	10.759629	95	88.3485672	100.7	2530492
			Simple St	atistics			
		Burgla	ary	Larcen	y Aut	co_Theft	
	Mean	1291.904	000	2671.28800	0 377	.5260000	
	StD	432.455	711	725.90870	7 193	. 3944175	
			Correlati	on Matrix			
							Auto_
	Murder	Rape	Robbery	Assault	Burglary	Larceny	Theft
Murder	1.0000	0.6012	0.4837	0.6486	0.3858	0.1019	0.0688
Rape	0.6012	1.0000	0.5919	0.7403	0.7121	0.6140	0.3489
Robbery	0.4837	0.5919	1.0000	0.5571	0.6372	0.4467	0.5907
Assault	0.6486	0.7403	0.5571	1.0000	0.6229	0.4044	0.2758
Burglary	0.3858	0.7121	0.6372	0.6229	1.0000	0.7921	0.5580
Larceny	0.1019	0.6140	0.4467	0.4044	0.7921	1.0000	0.4442
Auto_Thef	t 0.0688	0.3489	0.5907	0.2758	0.5580	0.4442	1.0000

Figure 69.2 displays the eigenvalues. The first principal component explains about 58.8% of the total variance, the second principal component explains about 17.7%, and the third principal component explains about 10.4%. Note that the eigenvalues sum to the total variance.

The eigenvalues indicate that two or three components provide a good summary of the data, two components accounting for 76% of the total variance and three components explaining 87%. Subsequent components contribute less than 5% each.

Figure 69.2 Results of Principal Component Analysis: PROC PRINCOMP

Eigenvalues of the Correlation Matrix								
	Eigenvalue Difference Proportion Cumulative							
	1	4.11495951	2.87623768	0.5879	0.5879			
	2	1.23872183	0.51290521	0.1770	0.7648			
	3	0.72581663	0.40938458	0.1037	0.8685			
	4	0.31643205	0.05845759	0.0452	0.9137			
	5	0.25797446	0.03593499	0.0369	0.9506			
	6	0.22203947	0.09798342	0.0317	0.9823			
	7	0.12405606		0.0177	1.0000			

Figure 69.3 displays the eigenvectors. From the eigenvectors matrix, you can represent the first principal component Prin1 as a linear combination of the original variables:

```
\begin{aligned} \text{Prin1} &= 0.300279 \times (\text{Murder}) \\ &+ 0.431759 \times (\text{Rape}) \\ &+ 0.396875 \times (\text{Robbery}) \\ &\cdot \\ &\cdot \\ &\cdot \\ &+ 0.295177 \times (\text{Auto\_Theft}) \end{aligned}
```

Similarly, the second principal component Prin2 is

```
\begin{aligned} \text{Prin2} &= -0.629174 \times (\text{Murder}) \\ &- 0.169435 \times (\text{Rape}) \\ &+ 0.042247 \times (\text{Robbery}) \\ &\cdot \\ &\cdot \\ &- 0.502421 \times (\text{Auto\_Theft}) \end{aligned}
```

where the variables are standardized.

Figure 69.3 Results of Principal Component Analysis: PROC PRINCOMP

			Eigenve	ectors			
	Prin1	Prin2	Prin3	Prin4	Prin5	Prin6	Prin7
Murder	0.300279	629174	0.178245	232114	0.538123	0.259117	0.267593
Rape	0.431759	169435	244198	0.062216	0.188471	773271	296485
Robbery	0.396875	0.042247	0.495861	557989	519977	114385	003903
Assault	0.396652	343528	069510	0.629804	506651	0.172363	0.191745
Burglary	0.440157	0.203341	209895	057555	0.101033	0.535987	648117
Larceny	0.357360	0.402319	539231	234890	0.030099	0.039406	0.601690
Auto_Theft	0.295177	0.502421	0.568384	0.419238	0.369753	057298	0.147046

The first component is a measure of the overall crime rate since the first eigenvector shows approximately equal loadings on all variables. The second eigenvector has high positive loadings on variables Auto_Theft and Larceny and high negative loadings on variables Murder and Assault. There is also a small positive loading on Burglary and a small negative loading on Rape. This component seems to measure the preponderance of property crime over violent crime. The interpretation of the third component is not obvious.

The ODS GRAPHICS statement enables the PRINCOMP procedure to produce statistical graphs by using ODS Graphics. See Chapter 21, "Statistical Graphics Using ODS," for more information.

PLOTS=SCORE(ELLIPSE NCOMP=3) in the PROC PRINCOMP statement requests the pairwise component score plots for the first three components with a 95% prediction ellipse overlaid on each of the scatter plot. Figure 69.4 shows the plot of the first two components. It is possible to identify regional trends on the plot of the first two components. Nevada and California are at the extreme right, with high overall crime rates but an average ratio of property crime to violent crime. North and South Dakota are at the extreme left, with low overall crime rates. Southeastern states tend to be at the bottom of the plot, with a higher-than-average ratio of violent crime to property crime. New England states tend to be in the upper part of the plot, with a higher-than-average ratio of property crime to violent crime. Assuming the first two components are from a bivariate normal distribution, the ellipse identifies Nevada as a possible outlier.

Figure 69.4 Plot of the First Two Component Scores

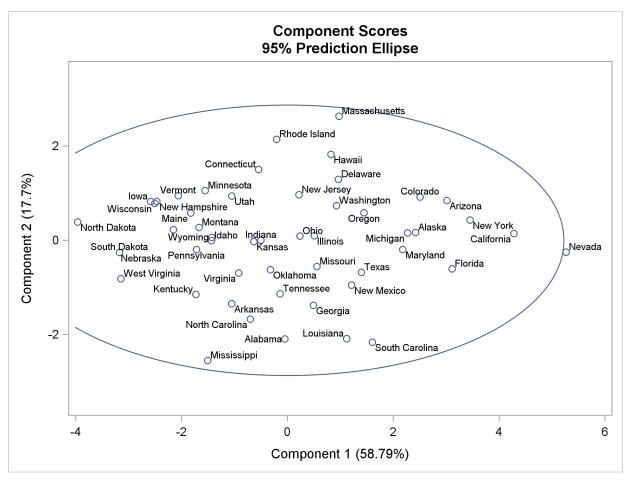


Figure 69.5 shows the plot of the first and third components. Assuming the first and the third components are from a bivariate normal distribution, the ellipse identifies Nevada, Massachusetts, and New York as possible outliers.

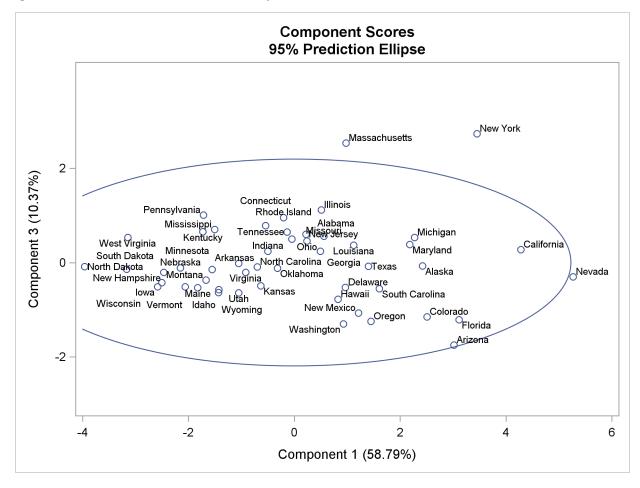


Figure 69.5 Plot of the First and Third Component Scores

The most striking feature of the plot of the first and third principal components is that Massachusetts and New York are outliers on the third component.

Syntax: PRINCOMP Procedure

The following statements are available in PROC PRINCOMP:

```
PROC PRINCOMP < options>;
BY variables;
FREQ variable;
ID variables;
PARTIAL variables;
VAR variables;
WEIGHT variable;
```

Usually only the VAR statement is used in addition to the PROC PRINCOMP statement. The rest of this section provides detailed syntax information for each of the preceding statements, beginning

with the PROC PRINCOMP statement. The remaining statements are described in alphabetical order.

PROC PRINCOMP Statement

PROC PRINCOMP < options> ;

The PROC PRINCOMP statement starts the PRINCOMP procedure and optionally identifies input and output data sets, specifies the analyses performed, and controls displayed output. Table 69.1 summarizes the options.

Table 69.1 Summary of PROC PRINCOMP Statement Options

Option	Description					
Specify data se	Specify data sets					
DATA=	specifies input data set name					
OUT=	specifies output data set name					
OUTSTAT=	specifies output data set name containing various statistics					
Specify details	of analysis					
COV	computes the principal components from the covariance matrix					
N=	specifies the number of principal components to be computed					
NOINT	omits the intercept from the model					
PREFIX=	specifies a prefix for naming the principal components					
RPREFIX=	specifies a prefix for naming the residual variables					
SINGULAR=	specifies the singularity criterion					
STD	standardizes the principal component scores					
VARDEF=	specifies the divisor used in calculating variances and standard deviations					
Suppress the d	isplay of output					
NOPRINT	suppresses the display of all output					
Specify ODS G	Fraphics details					
PLOTS=	specifies options that control the details of the plots					

The following list provides details about these options.

COVARIANCE

COV

computes the principal components from the covariance matrix. If you omit the COV option, the correlation matrix is analyzed. Use of the COV option causes variables with large variances to be more strongly associated with components with large eigenvalues and causes variables with small variances to be more strongly associated with components with small eigenvalues. You should not specify the COV option unless the units in which the variables are measured are comparable or the variables are standardized in some way.

DATA=SAS-data-set

specifies the SAS data set to be analyzed. The data set can be an ordinary SAS data set or a TYPE=ACE, TYPE=CORR, TYPE=COV, TYPE=FACTOR, TYPE=SSCP, TYPE=UCORR, or TYPE=UCOV data set (see Appendix A, "Special SAS Data Sets"). Also, the PRINCOMP procedure can read the _TYPE_='COVB' matrix from a TYPE=EST data set. If you omit the DATA= option, the procedure uses the most recently created SAS data set.

N=number

specifies the number of principal components to be computed. The default is the number of variables. The value of the N= option must be an integer greater than or equal to zero.

NOINT

omits the intercept from the model. In other words, the NOINT option requests that the covariance or correlation matrix not be corrected for the mean. When you use the PRINCOMP procedure with the NOINT option, the covariance matrix and, hence, the standard deviations are not corrected for the mean. If you are interested in the standard deviations corrected for the mean, you can get them by using a procedure such as the MEANS procedure.

If you use a TYPE=SSCP data set as input to the PRINCOMP procedure and list the variable Intercept in the VAR statement, the procedure acts as if you had also specified the NOINT option. If you use NOINT and also create an OUTSTAT= data set, the data set is TYPE=UCORR or TYPE=UCOV rather than TYPE=CORR or TYPE=COV.

NOPRINT

suppresses the display of all output. Note that this option temporarily disables the Output Delivery System (ODS). For more information, see Chapter 20, "Using the Output Delivery System."

OUT=SAS-data-set

creates an output SAS data set that contains all the original data as well as the principal component scores.

If you want to create a permanent SAS data set, you must specify a two-level name. For details about OUT= data sets, see the section "Output Data Sets" on page 5152. See SAS Language Reference: Concepts for more information about permanent SAS data sets.

OUTSTAT=SAS-data-set

creates an output SAS data set that contains means, standard deviations, number of observations, correlations or covariances, eigenvalues, and eigenvectors. If you specify the COV option, the data set is TYPE=COV or TYPE=UCOV, depending on the NOINT option, and it contains covariances; otherwise, the data set is TYPE=CORR or TYPE=UCORR, depending on the NOINT option, and it contains correlations. If you specify the PARTIAL statement, the OUTSTAT= data set contains R squares as well.

If you want to create a permanent SAS data set, you must specify a two-level name. For details about OUTSTAT= data sets, see the section "Output Data Sets" on page 5152. See SAS Language Reference: Concepts for more information about permanent SAS data sets.

```
PLOTS < (global-plot-options) > <= plot-request < (options) > >
```

PLOTS < (global-plot-options) > < = (plot-request < (options) > < ... plot-request < (options) > >) > controls the plots produced through ODS Graphics. When you specify only one plot request, you can omit the parentheses around the plot request. Here are some examples:

```
plots=none
plots=(scatter pattern)
plots(unpack)=scree
plots(ncomp=3 flip)=(pattern(circles=0.5 1.0) score)
```

You must enable ODS Graphics before requesting plots—for example, like this:

```
ods graphics on;
proc princomp plots=all;
  var x1--x10;
run;
ods graphics off;
```

For general information about ODS Graphics, see Chapter 21, "Statistical Graphics Using ODS." If you have enabled ODS Graphics but do not specify the PLOTS= option, PROC PRINCOMP produces the scree plot by default.

The global plot options include the following:

FLIP

flips or interchanges the X-axis and Y-axis dimension for the component score plots and the component pattern plots. For example, if there are three components, the default plots (y * x) are Component 2 * Component 1, Component 3 * Component 1, and Component 3 * Component 2. When you specify PLOTS(FLIP), the plots are Component 1 * Component 2, Component 1 * Component 3, and Component 2 * Component 3.

NCOMP=n

specifies the number of components $n(\geq 2)$ to be plotted for the component pattern plots and the component score plots. If the NCOMP= option is again specified in an individual plot, such as PLOTS=SCORE(NCOMP= m), the value m will determine the number of components to be plotted in the component score plots. Be aware that the number of plots $(\frac{n \times (n-1)}{2})$ produced grows quadratically when n increases. The default is 5 or the total number of components $m(\geq 2)$, whichever is smaller. If n > m, NCOMP= m will be used.

ONLY

suppresses the default plots. Only plots specifically requested are displayed.

UNPACKPANEL

UNPACK

suppresses paneling in the scree plot. By default, multiple plots can appear in an output panel. Specify UNPACKPANEL to get each plot in a separate panel. You can specify PLOTS(UNPACKPANEL) to unpack the default plots. You can also specify UNPACKPANEL as a suboption with SCREE (such as PLOTS=SCREE(UNPACKPANEL)).

The plot requests include the following:

ALL

produces all appropriate plots. You can specify other options with ALL; for example, to request all plots and unpack only the scree plot, specify PLOTS=(ALL SCREE(UNPACKPANEL)).

EIGEN | EIGENVALUE | SCREE < (UNPACKPANEL) >

produces the scree plot of eigenvalues and proportion variance explained. By default, both plots are output in a panel. Specify PLOTS= SCREE(UNPACKPANEL) to get each plot in a separate panel.

MATRIX

produces the matrix plot of principal component scores.

NONE

suppresses the display of all graphics output.

PATTERN < (pattern-options) >

produces the pairwise component pattern plots. Each variable is plotted as an observation whose coordinates are correlations between the variable and the two corresponding components on the plot. Use the NCOMP= option (for instance, PLOTS=PATTERN(NCOMP=3)) described in the following to control the number of plots to be displayed.

The available *pattern-options* are as follows:

CIRCLES < = number list >

plots the variance percentage circles. Each number in the list must be greater than 0. If the number is greater than or equal to 1, it is interpreted as a percentage and divided by 100; CIRCLES=0.05 and CIRCLES=5 are equivalent. For each number (c) specified, a $(c \times 100\%)$ variance circle is created.

By default, there is no circle for the scatter pattern plot (PLOTS=PATTERN) and a unit circle with a 100% variance circle is plotted for the vector pattern plot (PLOTS=PATTERN (VECTOR)). You can display multiple circles by specifying PLOTS=PATTERN(CIRCLES=). For example, specifying PLOTS=PATTERN(CIRCLES= .3 .6 1.0) will display the 30%, 60%, and 100% variance circles in the pattern plots.

FLIP

flips or interchanges the X-axis and Y-axis dimensions for the component pattern plots. Specify PLOTS=PATTERN(FLIP) to flip the X-axis and Y-axis dimensions.

NCOMP=n

specifies the number of components $n \ge 2$ to be plotted. The default is 5 or the total number of components $m \ge 2$, whichever is smaller. If n > m, NCOMP= m will be used. Be aware that the number of plots $(\frac{n \times (n-1)}{2})$ produced grows quadratically when n increases.

VECTOR

plots pattern in a vector form.

PATTERNPROFILE | PROFILE

produces the pattern profile plot. There is a profile for each component. The Y-axis value represents the correlation between the variable (corresponding to the X-axis value) and the profiled principal component.

SCORE < (score-options) >

produces the pairwise component score plots. Use the NCOMP= option (for instance, PLOTS=SCORE(NCOMP=3)) described in the following to control the number of plots to be displayed.

The available *score-options* are as follows:

ALPHA=number list

specifies a list of numbers for the prediction ellipses to be displayed in the score plots. Each value (α) in the list must be greater than 0. If α is greater than or equal to 1, it is interpreted as a percentage and divided by 100; ALPHA=0.05 and ALPHA=5 are equivalent.

ELLIPSE

requests prediction ellipses for the principal component scores of a new observation to be created in the principal component score plots. See the section "Confidence and Prediction Ellipses" in "The CORR Procedure" (*Base SAS Procedures Guide: Statistical Procedures*), for details about the computation of a prediction ellipse.

FLIP

flips or interchanges the X-axis and Y-axis dimensions for the component score plots. Specify PLOTS=SCORE(FLIP) to flip the X-axis and Y-axis dimensions.

NCOMP=n

specifies the number of components $n \geq 2$ to be plotted. The default is 5 or the total number of components $m \geq 2$, whichever is smaller. If n > m, NCOMP= m will be used. Be aware that the number of plots $(\frac{n \times (n-1)}{2})$ produced grows quadratically when n increases.

PREFIX=name

specifies a prefix for naming the principal components. By default, the names are Prin1, Prin2, ..., Prinn. If you specify PREFIX=ABC, the components are named ABC1, ABC2, ABC3, and so on. The number of characters in the prefix plus the number of digits required to designate the variables should not exceed the current name length defined by the VALIDVARNAME= system option.

PARPREFIX=name

PPREFIX=name

specifies a prefix for naming the residual variables in the OUT= data set and the OUTSTAT= data set. By default, the prefix is R_. The number of characters in the prefix plus the maximum length of the variable names should not exceed the current name length defined by the VALIDVARNAME= system option.

SINGULAR=p

SING=p

specifies the singularity criterion, where 0 . If a variable in a PARTIAL statement has an R square as large as <math>1-p when predicted from the variables listed before it in the statement, the variable is assigned a standardized coefficient of 0. By default, SINGULAR=1E-8.

STANDARD

STD

standardizes the principal component scores in the OUT= data set to unit variance. If you omit the STANDARD option, the scores have variance equal to the corresponding eigenvalue. Note that STANDARD has no effect on the eigenvalues themselves.

VARDEF=DF | N | WDF | WEIGHT | WGT

specifies the divisor used in calculating variances and standard deviations. By default, VARDEF=DF. The following table displays the values and associated divisors.

Value	Divisor		Formula
DF	error degrees of freedom	n-i	(before partialing)
		n-p-i	(after partialing)
N	number of observations	n	
WEIGHT WGT	sum of weights	$\sum_{j=1}^{n} w_j$	
WDF	sum of weights minus one	$\left(\sum_{j=1}^{n} w_{j}\right) - i$ $\left(\sum_{j=1}^{n} w_{j}\right) - p - i$	(before partialing)
		$\left(\sum_{j=1}^{n} w_j\right) - p - i$	(after partialing)

In the formulas for VARDEF=DF and VARDEF=WDF, p is the number of degrees of freedom of the variables in the PARTIAL statement, and i is 0 if the NOINT option is specified and 1 otherwise.

BY Statement

BY variables;

You can specify a BY statement with PROC PRINCOMP to obtain separate analyses on observations in groups defined by the BY variables. When a BY statement appears, the procedure expects the input data set to be sorted in order of the BY variables.

If your input data set is not sorted in ascending order, use one of the following alternatives:

- Sort the data by using the SORT procedure with a similar BY statement.
- Specify the BY statement option NOTSORTED or DESCENDING in the BY statement for PROC PRINCOMP. The NOTSORTED option does not mean that the data are unsorted but rather that the data are arranged in groups (according to values of the BY variables) and that these groups are not necessarily in alphabetical or increasing numeric order.

• Create an index on the BY variables by using the DATASETS procedure.

For more information about the BY statement, see SAS Language Reference: Concepts. For more information about the DATASETS procedure, see the Base SAS Procedures Guide.

FREQ Statement

FREQ variable;

The FREQ statement specifies a variable that provides frequencies for each observation in the DATA= data set. Specifically, if n is the value of the FREQ variable for a given observation, then that observation is used n times.

The analysis produced using a FREQ statement reflects the expanded number of observations. The total number of observations is considered equal to the sum of the FREQ variable. You could produce the same analysis (without the FREQ statement) by first creating a new data set that contains the expanded number of observations. For example, if the value of the FREQ variable is 5 for the first observation, the first 5 observations in the new data set would be identical. Each observation in the old data set would be replicated n_j times in the new data set, where n_j is the value of the FREQ variable for that observation.

If the value of the FREQ variable is missing or is less than one, the observation is not used in the analysis. If the value is not an integer, only the integer portion is used.

ID Statement

ID variables;

The ID statement labels observations with values from the first ID variable in the principal component score plot. If one or more ID variables are specified, their values are displayed in tooltips of the component score plot and the matrix plot of component scores.

PARTIAL Statement

PARTIAL variables;

If you want to analyze a partial correlation or covariance matrix, specify the names of the numeric variables to be partialed out in the PARTIAL statement. The PRINCOMP procedure computes the principal components of the residuals from the prediction of the VAR variables by the PARTIAL variables. If you request an OUT= or OUTSTAT= data set, the residual variables are named by prefixing the characters R_ by default or the string specified in the RPREFIX= option to the VAR variables.

VAR Statement

VAR variables;

The VAR statement lists the numeric variables to be analyzed. If you omit the VAR statement, all numeric variables not specified in other statements are analyzed. If, however, the DATA= data set is TYPE=SSCP, the default set of variables used as VAR variables does not include Intercept so that the correlation or covariance matrix is constructed correctly. If you want to analyze Intercept as a separate variable, you should specify it in the VAR statement.

WEIGHT Statement

WEIGHT variable;

If you want to use relative weights for each observation in the input data set, place the weights in a variable in the data set and specify the name in a WEIGHT statement. This is often done when the variance associated with each observation is different and the values of the weight variable are proportional to the reciprocals of the variances.

The observation is used in the analysis only if the value of the WEIGHT statement variable is nonmissing and is greater than zero.

Details: PRINCOMP Procedure

Missing Values

Observations with missing values for any variable in the VAR, PARTIAL, FREQ, or WEIGHT statement are omitted from the analysis and are given missing values for principal component scores in the OUT= data set. If a correlation, covariance, or SSCP matrix is read, it can contain missing values as long as every pair of variables has at least one nonmissing entry.

Output Data Sets

OUT= Data Set

The OUT= data set contains all the variables in the original data set plus new variables containing the principal component scores. The N= option determines the number of new variables. The

names of the new variables are formed by concatenating the value given by the PREFIX= option (or Prin if PREFIX= is omitted) and the numbers 1, 2, 3, and so on. The new variables have mean 0 and variance equal to the corresponding eigenvalue, unless you specify the STANDARD option to standardize the scores to unit variance. Also, if you specify the COV option, the procedure computes the principal component scores from the corrected or the uncorrected (if the NOINT option is specified) variables rather than the standardized variables.

If you use a PARTIAL statement, the OUT= data set also contains the residuals from predicting the VAR variables from the PARTIAL variables.

An OUT= data set cannot be created if the DATA= data set is TYPE=ACE, TYPE=CORR, TYPE=COV, TYPE=EST, TYPE=FACTOR, TYPE=SSCP, TYPE=UCORR, or TYPE=UCOV.

OUTSTAT= Data Set

The OUTSTAT= data set is similar to the TYPE=CORR data set produced by the CORR procedure. The following table relates the TYPE= value for the OUTSTAT= data set to the options specified in the PROC PRINCOMP statement.

Options	TYPE=
(default)	CORR
COV	COV
NOINT	UCORR
COV NOINT	UCOV

Note that the default (neither the COV nor NOINT option) produces a TYPE=CORR data set.

The new data set contains the following variables:

- the BY variables, if any
- two new variables, _TYPE_ and _NAME_, both character variables
- the variables analyzed (that is, those in the VAR statement); or, if there is no VAR statement, all numeric variables not listed in any other statement; or, if there is a PARTIAL statement, the residual variables as described under the OUT= data set

Each observation in the new data set contains some type of statistic as indicated by the _TYPE_ variable. The values of the _TYPE_ variable are as follows:

MEAN mean of each variable. If you specify the PARTIAL statement, this observation is omitted.

STD standard deviations. If you specify the COV option, this observation is omitted, so the SCORE procedure does not standardize the variables before computing scores. If you use the PARTIAL statement, the standard deviation of a variable is computed as its root mean squared error as predicted from the PARTIAL variables.

USTD

uncorrected standard deviations. When you specify the NOINT option in the PROC PRINCOMP statement, the OUTSTAT= data set contains standard deviations not corrected for the mean. However, if you also specify the COV option in the PROC PRINCOMP statement, this observation is omitted.

N

number of observations on which the analysis is based. This value is the same for each variable. If you specify the PARTIAL statement and the value of the VARDEF= option is DF or unspecified, then the number of observations is decremented by the degrees of freedom for the PARTIAL variables.

SUMWGT

the sum of the weights of the observations. This value is the same for each variable. If you specify the PARTIAL statement and VARDEF=WDF, then the sum of the weights is decremented by the degrees of freedom for the PARTIAL variables. This observation is output only if the value is different from that in the observation with _TYPE_='N'.

CORR

correlations between each variable and the variable specified by the _NAME_ variable. The number of observations with _TYPE_='CORR' is equal to the number of variables being analyzed. If you specify the COV option, no _TYPE_='CORR' observations are produced. If you use the PARTIAL statement, the partial correlations, not the raw correlations, are output.

UCORR

uncorrected correlation matrix. When you specify the NOINT option without the COV option in the PROC PRINCOMP statement, the OUTSTAT= data set contains a matrix of correlations not corrected for the means. However, if you also specify the COV option in the PROC PRINCOMP statement, this observation is omitted.

COV

covariances between each variable and the variable specified by the _NAME_ variable. _TYPE_='COV' observations are produced only if you specify the COV option. If you use the PARTIAL statement, the partial covariances, not the raw covariances, are output.

UCOV

uncorrected covariance matrix. When you specify the NOINT and COV options in the PROC PRINCOMP statement, the OUTSTAT= data set contains a matrix of covariances not corrected for the means.

EIGENVAL

eigenvalues. If the N= option requested fewer than the maximum number of principal components, only the specified number of eigenvalues are produced, with missing values filling out the observation.

SCORE

eigenvectors. The _NAME_ variable contains the name of the corresponding principal component as constructed from the PREFIX= option. The number of observations with _TYPE_='SCORE' equals the number of principal components computed. The eigenvectors have unit length unless you specify the STD option, in which case the unit-length eigenvectors are divided by the square roots of the eigenvalues to produce scores with unit standard deviations.

To obtain the principal component scores, if the COV option is not specified, these coefficients should be multiplied by the standardized data. With the COV option, these coefficients should be multiplied by the centered data. Means obtained from the observation with _TYPE_='MEAN' and standard deviations obtained from the observation with _TYPE_='STD' should be used for centering and standardizing the data.

USCORE	scoring coefficients to be applied without subtracting the mean from the raw
0000112	storing toting to ot applied without suchating the mean from the faw

variables. _TYPE_='USCORE' observations are produced when you specify the

NOINT option in the PROC PRINCOMP statement.

To obtain the principal component scores, these coefficients should be multiplied by the data that are standardized by the uncorrected standard deviations obtained from the observation with _TYPE_='USTD'.

RSQUARED R squares for each VAR variable as predicted by the PARTIAL variables

B regression coefficients for each VAR variable as predicted by the PARTIAL vari-

ables. This observation is produced only if you specify the COV option.

STB standardized regression coefficients for each VAR variable as predicted by the

PARTIAL variables. If you specify the COV option, this observation is omitted.

The data set can be used with the SCORE procedure to compute principal component scores, or it can be used as input to the FACTOR procedure specifying METHOD=SCORE to rotate the components. If you use the PARTIAL statement, the scoring coefficients should be applied to the residuals, not the original variables.

Computational Resources

Let

n = number of observations

v = number of VAR variables

p = number of PARTIAL variables

c = number of components

• The minimum allocated memory required (in bytes) is

$$232v + 120p + 48c + \max(8cv, 8vp + 4(v + p)(v + p + 1))$$

• The time required to compute the correlation matrix is roughly proportional to

$$n(v+p)^2 + \frac{p}{2}(v+p)(v+p+1)$$

- The time required to compute eigenvalues is roughly proportional to v^3 .
- The time required to compute eigenvectors is roughly proportional to cv^2 .

Displayed Output

The PRINCOMP procedure displays the following items if the DATA= data set is not TYPE=CORR, TYPE=COV, TYPE=SSCP, TYPE=UCORR, or TYPE=UCOV:

- simple statistics, including the mean and std (standard deviation) for each variable. If you specify the NOINT option, the uncorrected standard deviation (ustd) is displayed.
- the correlation or, if you specify the COV option, the covariance matrix

The PRINCOMP procedure displays the following items if you use the PARTIAL statement:

- regression statistics, giving the R square and RMSE (root mean squared error) for each VAR variable as predicted by the PARTIAL variables (not shown)
- standardized regression coefficients or, if you specify the COV option, regression coefficients for predicting the VAR variables from the PARTIAL variables (not shown)
- the partial correlation matrix or, if you specify the COV option, the partial covariance matrix (not shown)

The PRINCOMP procedure displays the following item if you specify the COV option:

• the total variance

The PRINCOMP procedure displays the following items unless you specify the NOPRINT option:

- eigenvalues of the correlation or covariance matrix, as well as the difference between successive eigenvalues, the proportion of variance explained by each eigenvalue, and the cumulative proportion of variance explained
- the eigenvectors

ODS Table Names

PROC PRINCOMP assigns a name to each table it creates. You can use these names to reference the table when using the Output Delivery System (ODS) to select tables and create output data sets. These names are listed in Table 69.2. For more information about ODS, see Chapter 20, "Using the Output Delivery System."

All of the tables are created with the specification of the PROC PRINCOMP statement; a few tables need an additional PARTIAL statement.

Table 69.2 ODS Tables Produced by PROC PRINCOMP

ODS Table Name	Description	Statement / Option
Corr	Correlation matrix	default
Cov	Covariance matrix	COV
Eigenvalues	Eigenvalues	default
Eigenvectors	Eigenvectors	default
NObsNVar	Number of observations, variables, and partial variables	default
ParCorr	Partial correlation matrix	PARTIAL statement
ParCov	Uncorrected partial covariance matrix	PARTIAL statement and COV
RegCoef	Regression coefficients	PARTIAL statement and COV
RSquareRMSE	Regression statistics: R squares and RMSEs	PARTIAL statement
SimpleStatistics	Simple statistics	default
StdRegCoef	Standardized regression coefficients	PARTIAL statement
TotalVariance	Total variance	COV

ODS Graphics

To request graphics with PROC PRINCOMP, you must first enable ODS Graphics by specifying the ods graphics on statement. See Chapter 21, "Statistical Graphics Using ODS," for more information. Some graphs are produced by default; other graphs are produced by using statements and options. You can reference every graph produced through ODS Graphics with a name. The names of the graphs that PROC PRINCOMP generates are listed in Table 69.3, along with the required statements and options.

Table 69.3 ODS Graphics Produced by PROC PRINCOMP

ODS Graph Name	Plot Description	Statement and Option
PaintedScorePlot	Score plot of component 3 versus	PLOTS=SCORE when num-
	component 2, painted by component 1	ber of variables ≥ 3
PatternPlot	Component pattern plot	PLOTS=PATTERN
PatternProfilePlot	Component pattern profile plot	PLOTS=PATTERNPROFILE
ScoreMatrixPlot	Matrix plot of component scores	PLOTS=MATRIX
ScorePlot	Component score plot	PLOTS=SCORE
ScreePlot	Scree and variance plots	default and PLOTS=SCREE
VariancePlot	Variance proportion explained plot	PLOTS=SCREE(UNPACKPAN

Examples: PRINCOMP Procedure

Example 69.1: Temperatures

This example analyzes mean daily temperatures in selected cities in January and July. Both the raw data and the principal components are plotted to illustrate how principal components are orthogonal rotations of the original variables.

The following statements create the Temperature data set.

```
data Temperature;
             length Cityid $ 2;
             title 'Mean Temperature in January and July for Selected Cities ';
             input City $1-15 January July;
             Cityid = substr(City, 1, 2);
              datalines;
Mobile 51.2 81.6
Phoenix 51.2 91.2
Little Rock 39.5 81.4
Sacramento 45.1 75.2
Denver 29.9 73.0
Hartford 24.8 72.7
Wilmington 32.0 75.8
Washington DC 35.6 78.7
  Jacksonville 54.6 81.0

      Jacksonville
      54.6 81.0

      Miami
      67.2 82.3

      Atlanta
      42.4 78.0

      Boise
      29.0 74.5

      Chicago
      22.9 71.9

      Peoria
      23.8 75.1

      Indianapolis
      27.9 75.0

      Des Moines
      19.4 75.1

      Wichita
      31.3 80.7

      Louisville
      33.3 76.9

      New Orleans
      52.9 81.9

      Portland
      ME

      21.5 68.0

 Portland, ME 21.5 68.0
 Baltimore 33.4 76.6
Boston 29.2 73.3
 Boston 29.2 73.3
Detroit 25.5 73.3
  Sault Ste Marie 14.2 63.8

      Sault Ste Marie
      14.2
      63.8

      Duluth
      8.5
      65.6

      Minneapolis
      12.2
      71.9

      Jackson
      47.1
      81.7

      Kansas City
      27.8
      78.8

      St Louis
      31.3
      78.6

      Great Falls
      20.5
      69.3

      Omaha
      22.6
      77.2

      Reno
      31.9
      69.3

      Concord
      20.6
      69.7
```

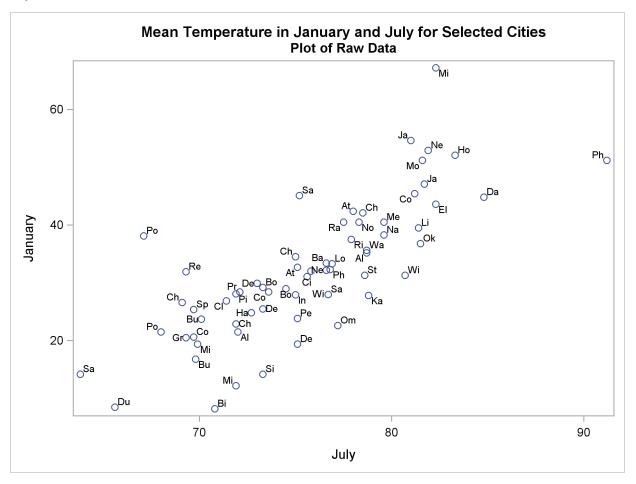
```
Atlantic City
Albuquerque
Albany
Buffalo
Buffalo
Charlotte
Raleigh
Albinarck
Cincinnati
Cleveland
Columbus
Oklahoma City
Portland, OR
Philadelphia
Pittsburgh
Providence
Columbia
Sioux Falls
Nashville
Dallas
El Paso
Norfolk
Richmond
Spokane
Cheyenne
Cheyenne
Cheyenne
Salt City
Portland, OR
Columbia
C
```

The following statements plot the temperature data set. The Cityid variable instead of City is used as a data label in the scatter plot for possible label clashing.

```
title 'Mean Temperature in January and July for Selected Cities';
title2 'Plot of Raw Data';
proc sgplot data=Temperature;
    scatter x=July y=January / datalabel=Cityid;
run;
```

The results are displayed in Output 69.1.1, which shows a scatter diagram of the 64 pairs of data points with July temperatures plotted against January temperatures.

Output 69.1.1 Plot of Raw Data



The following statement requests a principal component analysis on the Temperature data set:

```
ods graphics on;
title 'Mean Temperature in January and July for Selected Cities';
proc princomp data=Temperature cov plots=score(ellipse);
  var July January;
  id Cityid;
run;
ods graphics off;
```

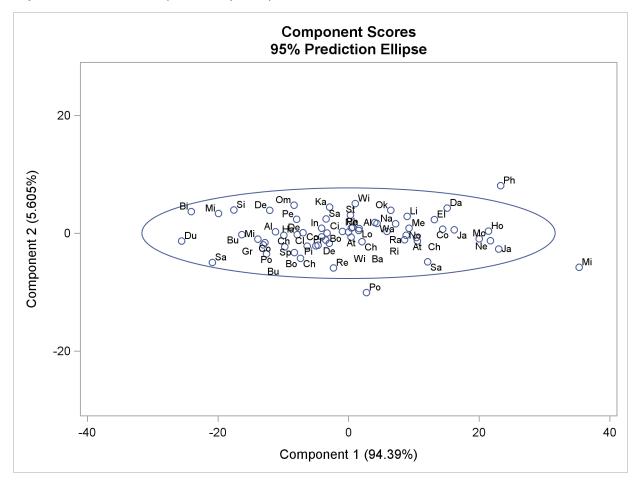
Output 69.1.2 displays the PROC PRINCOMP output. The standard deviation of January (11.712) is higher than the standard deviation of July (5.128). The COV option in the PROC PRINCOMP statement requests the principal components to be computed from the covariance matrix. The total variance is 163.474. The first principal component explains about 94% of the total variance, and the second principal component explains only about 6%. The eigenvalues sum to the total variance.

Note that January receives a higher loading on Prin1 because it has a higher standard deviation than July, and the PRINCOMP procedure calculates the scores by using the centered variables rather than the standardized variables.

Output 69.1.2 Results of Principal Component Analysis

Mean	Temperature i	n January and	July for Select	ted Cities
	Т	he PRINCOMP Pro	ocedure	
		servations		
	Va	riables	2	
		Simple Statist	cics	
		July	Janua	ry
	Mean	75.60781250	32.095312	50
	StD	5.12761910	11.712433	09
		Covariance Mat	crix	
		July	Janua	ary
		26.2924777		
	January	46.8282912	137.1810	888
	Total	Variance 16	53.47356647	
	Eigenval	ues of the Cova	ariance Matrix	
	Eigenvalue	Difference	Proportion	Cumulative
1	154.310607	145.147647		0.9439
2	9.162960		0.0561	1.0000
		Eigenvectors	5	
		Prin1	Prin2	
	July	0.343532	0.939141	
		0.939141		

PLOTS=SCORE in the PROC PRINCOMP statement requests a plot of the second principal component against the first principal component as shown in Output 69.1.3. It is clear from this plot that the principal components are orthogonal rotations of the original variables and that the first principal component has a larger variance than the second principal component. In fact, the first component has a larger variance than either of the original variables July and January. The ellipse indicates that Miami, Phoenix, and Portland are possible outliers.



Output 69.1.3 Plot of Component 2 by Component 1

Example 69.2: Basketball Data

The data in this example are rankings of 35 college basketball teams. The rankings were made before the start of the 1985–86 season by 10 news services.

The purpose of the principal component analysis is to compute a single variable that best summarizes all 10 of the preseason rankings.

Note that the various news services rank different numbers of teams, varying from 20 through 30 (there is a missing rank in one of the variables, WashPost). And, of course, not all services rank the same teams, so there are missing values in these data. Each of the 35 teams is ranked by at least one news service.

The PRINCOMP procedure omits observations with missing values. To obtain principal component scores for all of the teams, it is necessary to replace the missing values. Since it is the best teams that are ranked, it is not appropriate to replace missing values with the mean of the nonmissing values. Instead, an ad hoc method is used that replaces missing values with the mean of the unassigned ranks. For example, if 20 teams are ranked by a news service, then ranks 21 through 35 are unassigned. The mean of ranks 21 through 35 is 28, so missing values for that variable are replaced

by the value 28. To prevent the method of missing-value replacement from having an undue effect on the analysis, each observation is weighted according to the number of nonmissing values it has. See Example 70.2 in Chapter 70, "The PRINQUAL Procedure," for an alternative analysis of these data.

Since the first principal component accounts for 78% of the variance, there is substantial agreement among the rankings. The eigenvector shows that all the news services are about equally weighted; this is also suggested by the nearly horizontal line of the pattern profile plot in Output 69.2.3. So a simple average would work almost as well as the first principal component. The following statements produce Output 69.2.1.

```
/*----*/
/*
                                                            */
/★ Pre-season 1985 College Basketball Rankings
                                                            */
/* (rankings of 35 teams by 10 news services)
/*
/* Note: (a) news services rank varying numbers of teams;
                                                            */
         (b) not all teams are ranked by all news services; */
/*
       (c) each team is ranked by at least one service;
                                                            */
/*
       (d) rank 20 is missing for UPI.
                                                            */
/*
                                                            */
data HoopsRanks;
   input School $13. CSN DurSun DurHer WashPost USAToday
         Sport InSports UPI AP SI;
   label CSN = 'Community Sports News (Chapel Hill, NC)'
        DurSun = 'Durham Sun'
         DurHer = 'Durham Morning Herald'
         WashPost = 'Washington Post'
         USAToday = 'USA Today'
         Sport = 'Sport Magazine'
         InSports = 'Inside Sports'
         UPI = 'United Press International'
         AP
               = 'Associated Press'
                = 'Sports Illustrated'
   format CSN--SI 5.1;
   datalines;
Louisville 1 8 1 9 8 9 6 10 9 9
Georgia Tech 2 2 4 3 1 1 1 2 1 1
Kansas 3 4 5 1 5 11 8 4 5 7
Michigan
            4 5 9 4 2 5 3 1 3 2
             5 6 7 5 4 10 4 5 6 5
Duke
UNC 6 1 2 2 3 4 2 3 2 3 Syracuse 7 10 6 11 6 6 5 6 4 10
Notre Dame 8 14 15 13 11 20 18 13 12 .

Kentucky 9 15 16 14 14 19 11 12 11 13

LSU 10 9 13 . 13 15 16 9 14 8

DePaul 11 . 21 15 20 . 19 . . 19
Georgetown 12 7 8 6 9 2 9 8 8 4
Navy 13 20 23 10 18 13 15 . 20 . Illinois 14 3 3 7 7 3 10 7 7 6
```

```
15 16 . . 23 . . 14 . 20
Iowa
Arkansas
            16 . . . 25 . . . . 16
Memphis State 17 . 11 . 16 8 20 . 15 12
Washington 18 . . . . . . 17 . .
           19 13 10 . 12 17 . 16 16 15
UAB
UNLV
           20 18 18 19 22 . 14 18 18 .
NC State 21 17 14 16 15 . 12 15 17 18 Maryland 22 . . . 19 . . . 19 14
Pittsburgh 23 . . . . . . . . .
           24 19 17 17 17 12 17 . 13 17
Oklahoma
Indiana
           25 12 20 18 21 . . .
            26 . 22 . . 18
Virginia
Old Dominion 27 . . . .
Auburn 28 11 12 8 10 7 7 11 10 11
St. Johns
UCLA
           29 . . . . 14
            30 . . . . . . . 19
St. Joseph's . . 19 . . . . . .
           . . 24 . . 16 . . .
Tennessee
             . . . 20 .
Montana
Houston
             . . . . 24 . . . . .
/* PROC MEANS is used to output a data set containing the
                                                         */
/* maximum value of each of the newspaper and magazine
                                                          */
/* rankings. The output data set, maxrank, is then used
                                                          */
/* to set the missing values to the next highest rank plus
                                                          */
/* thirty-six, divided by two (that is, the mean of the
                                                          */
/* missing ranks). This ad hoc method of replacing missing
                                                         */
/* values is based more on intuition than on rigorous
                                                         */
/* statistical theory. Observations are weighted by the
                                                          */
/* number of nonmissing values.
                                                          */
/*
                                                          */
title 'Pre-Season 1985 College Basketball Rankings';
proc means data=HoopsRanks;
  output out=MaxRank
         max=CSNMax DurSunMax DurHerMax
            WashPostMax USATodayMax SportMax
             InSportsMax UPIMax APMax SIMax;
run;
```

Output 69.2.1 Summary Statistics for Basketball Rankings Using PROC MEANS

		Pre-Season 1985 College Basketball F	Rankings		
		The MEANS Procedure			
Variable		bel	N	Ме	an
CSN	 Co	mmunity Sports News (Chapel Hill, NC)	30	15.50000	000
DurSur	n Du	rham Sun	20	10.50000	000
DurHer	. Du	rham Morning Herald	24	12.50000	000
WashPo		shington Post	19	10.42105	26
USAToo	lay US	A Today	25	13.00000	000
Sport	- Sp	ort Magazine	20	10.50000	000
-	_	side Sports	20	10.50000	000
UPI		ited Press International	19	10.00000	000
AP		sociated Press	20	10.50000	
SI	_	orts Illustrated	20	10.50000	
Variable 	raper		Std D	ev 	Minimu
CSN	Commun	ity Sports News (Chapel Hill, NC)	8.80340	84 1.	000000
DurSun	Durham	Sun	5.91607	98 1.	000000
DurHer	Durham	Morning Herald	7.07106	78 1.	000000
WashPost	Washin	gton Post	6.06736	07 1.	000000
USAToday	USA To	day	7.35980	07 1.	000000
Sport	Sport	Magazine	5.91607	98 1.	000000
InSports	Inside	Sports	5.91607	98 1.	000000
UPI	United	Press International	5.62731	43 1.	000000
AP	Associ	ated Press	5.91607	98 1.	000000
SI	Sports	Illustrated	5.91607	98 1.	000000
Var	able	Label		Maximum	
		Community County Navy (Charal Will	NG) 3		
CSN	: :Sun	Community Sports News (Chapel Hill,		0.0000000	
		Durham Sun		0.0000000	
	Her	Durham Morning Herald		4.0000000	
	shPost	3		0.0000000	
		Today USA Today		5.0000000	
0	ort Sport Magazine			0.0000000	
-	ports	-		0.0000000	
Ins	•	United Press International		9.000000	
Ins UPI					
Ins		Associated Press Sports Illustrated		0.0000000	

The following statements produce Output 69.2.2 and Output 69.2.3:

```
data Basketball;
     set HoopsRanks;
     if _n_=1 then set MaxRank;
     array Services{10} CSN--SI;
     array MaxRanks{10} CSNMax--SIMax;
     keep School CSN--SI Weight;
     Weight=0;
     do i=1 to 10;
         if Services{i}=. then Services{i}=(MaxRanks{i}+36)/2;
         else Weight=Weight+1;
      end;
  run;
ods graphics on;
proc princomp data=Basketball n=1 out=PCBasketball standard
              plots=patternprofile;
  var CSN--SI;
  weight Weight;
run;
ods graphics off;
```

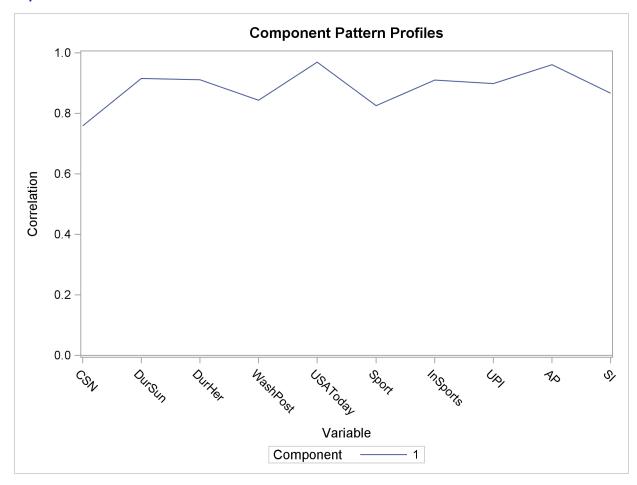
Output 69.2.2 Principal Components Analysis of Basketball Rankings Using PROC PRINCOMP

	Pre	-Season 1985 Col	llege Basketba	ll Rankings			
The PRINCOMP Procedure							
		Observati	ions	35			
		Variables	5	10			
		Simple	e Statistics				
	CSN	DurSun	DurHer	WashPost	USAToday		
Mean	13.33640553	13.06451613	12.88018433	13.83410138	12.55760369		
StD	22.08036285	21.66394183	21.38091837	23.47841791	20.48207965		
Simple Statistics							
	Sport	InSports	UPI	AP	SI		
Mean	13.83870968	13.24423963	13.59216590	12.83410138	13.52534562		
StD	23.37756267	22.20231526	23.25602811	21.40782406	22.93219584		

Output 69.2.2 continued

		(Correlation	Matrix				
					CSN	DurSun	DurHer	
					CSN	Dursun	Durner	
CSN	Commun	ity Sports Ne	ews (Chapel	Hill, NC	1.0000	0.6505	0.6415	
DurSun	Durham	Sun			0.6505	1.0000	0.8341	
DurHer	Durham Morning Herald				0.6415	0.8341	1.0000	
WashPost	Washington Post 0.612					0.7667	0.7035	
USAToday	USA Today 0.745					0.8860	0.8877	
Sport	Sport 1	Magazine	0.4806	0.6940	0.7788			
InSports	Inside	Sports	0.6558	0.7702	0.7900			
UPI	United	Press Intern	0.7007	0.9015	0.7676			
AP	Associ	ated Press	0.6779	0.8437	0.8788			
SI	Sports	Illustrated	0.6135	0.7518	0.7761			
		C	Correlation	Matrix				
	Wash			In				
	Post	USAToday	Sport	Sports	UPI	AP	SI	
CSN	0.6121	0.7456	0.4806	0.6558	0.7007	0.6779	0.6135	
DurSun	0.7667	0.8860	0.6940	0.7702	0.9015	0.8437	0.7518	
DurHer	0.7035	0.8877	0.7788	0.7900	0.7676	0.8788	0.7761	
WashPost	1.0000	0.7984	0.6598	0.8717	0.6953	0.7809	0.5952	
USAToday	0.7984	1.0000	0.7716	0.8475	0.8539	0.9479	0.8426	
Sport	0.6598	0.7716	1.0000	0.7176	0.6220	0.8217	0.7701	
InSports	0.8717	0.8475	0.7176	1.0000	0.7920	0.8830	0.7332	
UPI	0.6953	0.8539	0.6220	0.7920	1.0000	0.8436	0.7738	
AP	0.7809	0.9479	0.8217	0.8830	0.8436	1.0000	0.8212	
SI	0.5952	0.8426	0.7701	0.7332	0.7738	0.8212	1.0000	
		Eigenvalu	ues of the (Correlati	on Matrix			
	:	Eigenvalue	Difference	e Prop	ortion (Cumulative		
	1	7.88601647			0.7886	0.7886		
			Eigenvect	tors				
						Pr	in1	
2000		Cammu		/Ch ?	m:11 va\	0.070	205	
CSN	!un	Durham Sun	Sports News	0.270205 0.326048				
DurSun DurHer		Durham Morning Herald				0.326048		
WashPost		Washington Post				0.324392		
WashPost USAToday		USA Today				0.345200		
Sport		Sport Magazine				0.293881		
InSports		Inside Sports				0.324088		
UPI	-		United Press International				0.319902	
AP		Associated Press				0.342151		
SI	SI		Sports Illustrated				0.308570	
	•							

Output 69.2.3 Pattern Profile Plot



The following statements produce Output 69.2.4:

```
proc sort data=PCBasketball;
   by Prin1;
run;

proc print;
  var School Prin1;
  title 'Pre-Season 1985 College Basketball Rankings';
  title2 'College Teams as Ordered by PROC PRINCOMP';
run;
```

Output 69.2.4 Basketball Rankings Using PROC PRINCOMP

Pre-Season 1985 College Basketball Rankings							
College Teams as Ordered by PROC PRINCOMP							
OBS	School	Prin1					
1	Georgia Tech	-0.58068					
2	UNC	-0.53317					
3	Michigan	-0.47874					
4	Kansas	-0.40285					
5	Duke	-0.38464					
6	Illinois	-0.33586					
7	Syracuse	-0.31578					
8	Louisville	-0.31489					
9	Georgetown	-0.29735					
10	Auburn	-0.09785					
11	Kentucky	0.00843					
12	LSU	0.00872					
13	Notre Dame	0.09407					
14	NC State	0.19404					
15	UAB	0.19771					
16	Oklahoma	0.23864					
17	Memphis State	0.25319					
18	Navy	0.28921					
19	UNLV	0.35103					
20	DePaul	0.43770					
21	Iowa	0.50213					
22	Indiana	0.51713					
23	Maryland	0.55910					
24	Arkansas	0.62977					
25	Virginia	0.67586					
26	Washington	0.67756					
27	Tennessee	0.70822					
28	St. Johns	0.71425					
29	Virginia Tech	0.71638					
30	St. Joseph's	0.73492					
31	UCLA	0.73965					
32	Pittsburgh	0.75078					
33	Houston	0.75534					
34	Montana	0.75790					
35	Old Dominion	0.76821					
33							

Example 69.3: Job Ratings

This example uses the PRINCOMP procedure to analyze job performance. Police officers were rated by their supervisors in 14 categories as part of standard police departmental administrative procedure.

The following statements create the Jobratings data set:

```
options validvarname=any;
data Jobratings;
   input ('Communication Skills'n
          'Problem Solving'n
          'Learning Ability'n
          'Judgment Under Pressure'n
          'Observational Skills'n
          'Willingness to Confront Problems'n
          'Interest in People'n
          'Interpersonal Sensitivity'n
          'Desire for Self-Improvement'n
          'Appearance'n
          'Dependability'n
          'Physical Ability'n
          'Integrity'n
          'Overall Rating'n) (1.);
   datalines;
26838853879867
74758876857667
56757863775875
67869777988997
99997798878888
89897899888799
89999889899798
87794798468886
35652335143113
89888879576867
76557899446397
97889998898989
76766677598888
... more lines ...
99899899899899
76656399567486
```

The data set Jobratings contains 14 variables. Each variable contains the job ratings, using a scale measurement from 1 to 10 (1=fail to comply, 10=exceptional). The last variable Overall Rating contains a score as an overall index on how each officer performs.

The following statements request a principal component analysis on the Jobratings data set, output the scores to the Scores data set (OUT= Scores), and produce default plots. Note that variable Overall Rating is excluded from the analysis.

```
ods graphics on;
proc princomp data=Jobratings(drop='Overall Rating'n);
run;
```

Figure 69.3.1 and Figure 69.3.2 display the PROC PRINCOMP output, beginning with simple statistics followed by the correlation matrix. By default, the PROC PRINCOMP statement requests

principal components computed from the correlation matrix, so the total variance is equal to the number of variables, 13. In this example, it would also be reasonable to use the COV option, which would cause variables with a high variance (such as Dependability) to have more influence on the results than variables with a low variance (such as Learning Ability). If you used the COV option, scores would be computed from centered rather than standardized variables.

Output 69.3.1 Simple Statistics and Correlation Matrix from the PRINCOMP Procedure

			College Basket	_				
	College Teams as Ordered by PROC PRINCOMP							
The PRINCOMP Procedure								
Observations 103								
		Varia	bles	13				
		Si	mple Statistics					
Judgment								
	Communication	on Probl	.em Learnin	g Under	Observational			
	Skill	ls Solvi	ng Abilit	y Pressure	Skills			
Mean	6.65048543	6.6310679	6.99029126	2 6.737864078	6.932038835			
StD	1.76406803	36 1.5903526	1.33941123	8 1.731830976	1.761584269			
		Si	mple Statistics					
	Willingness							
	to Confront	Interest	Interpersonal	Desire fo	r			
	Problems	in People	Sensitivity	Self-Improvemen	t Appearance			
Mean	7.291262136	6.708737864	6.621359223	6.57281553	4 7.00000000			
StD	1.525155524	1.892353385	1.760773587	1.72979621	2 1.798692335			
		Si	mple Statistics					
			Physica	1				
	De	ependability	Abilit	y Integr	ity			
	Mean	6.825242718	7.20388349	5 7.213592	233			
	StD	1.917040123	1.55525184	5 1.845240	223			

Output 69.3.1 continued

-				
Cori	relation Matrix			
				Judgment
	Communication	Problem	Learning	
	Skills	Solving	Ability	Pressure
Communication Skills	1.0000	0.6280	0.5546	0.5538
Problem Solving	0.6280	1.0000	0.5690	0.6195
Learning Ability	0.5546	0.5690	1.0000	0.4892
Judgment Under Pressure	0.5538	0.6195	0.4892	1.0000
Observational Skills	0.5381	0.4284	0.6230	0.3733
Willingness to Confront Problems	0.5265	0.5015	0.5245	0.4004
Interest in People	0.4391	0.3972	0.2735	0.6226
Interpersonal Sensitivity	0.5030	0.4398	0.1855	0.6134
Desire for Self-Improvement	0.5642	0.4090	0.5737	0.4826
Appearance	0.4913	0.3873	0.3988	0.2266
Dependability	0.5471	0.4546	0.5110	0.5471
Physical Ability	0.2192	0.3201	0.2269	0.3476
Integrity	0.5081	0.3846	0.3142	0.5883
_				
Con	rrelation Matrix			
		Will:	ingness	Interest
	Observational		onfront	in
	Skills	P	roblems	People
Communication Skills	0.5381		0.5265	0.4391
Problem Solving	0.5381		0.5265	0.4391
Learning Ability	0.4284		0.5015	0.3372
Judgment Under Pressure	0.3733		0.4004	0.6226
Observational Skills	1.0000		0.7300	0.2616
Willingness to Confront Problems			1.0000	0.2233
Interest in People	0.7500		0.2233	1.0000
Interpersonal Sensitivity	0.1655		0.1291	0.8051
Desire for Self-Improvement	0.5985		0.5307	0.4857
Appearance	0.3303		0.4825	0.2679
Dependability	0.5626		0.4870	0.6074
Physical Ability	0.4274		0.4872	0.3768
Integrity	0.3906		0.3260	0.7452
Corr	relation Matrix			
	Interpersonal	De	sire for	
	Sensitivity	Self-Imp	rovement	Appearance
Communication Skills	0.5030		0.5642	0.4913
Problem Solving	0.4398		0.3042	0.3873
Learning Ability	0.4356		0.5737	0.3988
Judgment Under Pressure	0.1833		0.3737	0.2266
oudgment onder rressure	0.0134		0.4040	0.2200

Output 69.3.1 continued

Correlation Matrix						
	Interpersonal	Desire for				
	Sensitivity	Self-Improvement	Appearance			
Observational Skills	0.1655	0.5985	0.4177			
Willingness to Confront Problems	0.1291	0.5307	0.4825			
Interest in People	0.8051	0.4857	0.2679			
Interpersonal Sensitivity	1.0000	0.3713	0.2600			
Desire for Self-Improvement	0.3713	1.0000	0.4474			
Appearance	0.2600	0.4474	1.0000			
Dependability	0.5408	0.5981	0.5089			
Physical Ability	0.2182	0.3752	0.3820			
Integrity	0.6920	0.5664	0.4135			
	rrelation Matrix	Physical				
	Dependability	-	Integrity			
Communication Skills	0.5471	0.2192	0.5081			
Problem Solving	0.4546	0.3201	0.3846			
Learning Ability	0.5110	0.2269	0.3142			
Judgment Under Pressure	0.5471	0.3476	0.5883			
Observational Skills	0.5626	0.4274	0.3906			
Willingness to Confront Problems	o.4870	0.4872	0.3260			
Interest in People	0.6074	0.3768	0.7452			
Interpersonal Sensitivity	0.5408	0.2182	0.6920			
Desire for Self-Improvement	0.5981	0.3752	0.5664			
Appearance	0.5089	0.3820	0.4135			
Dependability	1.0000	0.4461	0.6536			
Physical Ability	0.4461	1.0000	0.3810			
Integrity	0.6536	0.3810	1.0000			

Figure 69.3.2 displays the eigenvalues. The first principal component explains about 50% of the total variance, the second principal component explains about 13.6%, and the third principal component explains about 7.7%. Note that the eigenvalues sum to the total variance. The eigenvalues indicate that three to five components provide a good summary of the data, with three components accounting for about 71.7% of the total variance and five components explaining about 82.7%. Subsequent components contribute less than 5% each.

Output 69.3.2 Eigenvalues and Eigenvectors from the PRINCOMP Procedure

Eigenvalues of the Correlation Matrix							
	Eigenvalue	Difference	Proportion	Cumulative			
1	6.54740242	4.77468744	0.5036	0.5036			
2	1.77271499	0.76747933	0.1364	0.6400			
3	1.00523565	0.26209665	0.0773	0.7173			
4	0.74313901	0.06479499	0.0572	0.7745			
5	0.67834402	0.22696368	0.0522	0.8267			
6	0.45138034	0.06922167	0.0347	0.8614			
7	0.38215866	0.08432613	0.0294	0.8908			
8	0.29783254	0.02340663	0.0229	0.9137			
9	0.27442591	0.01208809	0.0211	0.9348			
10	0.26233782	0.01778332	0.0202	0.9550			
11	0.24455450	0.04677622	0.0188	0.9738			
12	0.19777828	0.05508241	0.0152	0.9890			
13	0.14269586		0.0110	1.0000			

Output 69.3.2 continued

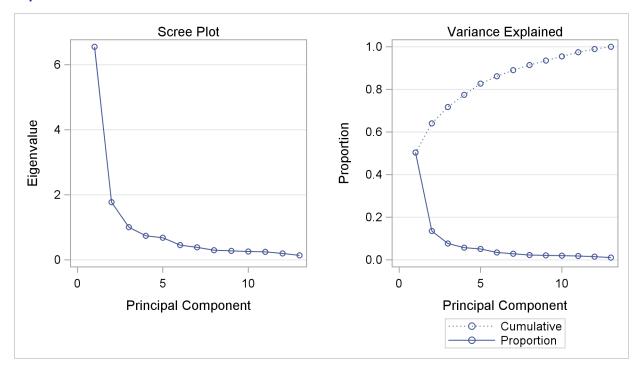
	Eigenvectors	;		
	Prin1	Prin2	Prin3	Prin4
Communication Skills	0.303548	0.052039	329181	227039
Problem Solving	0.278034	0.057046	400112	0.300476
Learning Ability	0.266521	0.288152	354591	020735
Judgment Under Pressure	0.294376	199458	255164	0.397306
Observational Skills	0.276641	0.366979	0.065959	0.035711
Willingness to Confront Problems	0.267580	0.392989	0.098723	0.184409
Interest in People	0.278060	432916	0.118113	0.046047
Interpersonal Sensitivity	0.253814	495662	064547	060000
Desire for Self-Improvement	0.299833	0.099077	0.061097	211279
Appearance	0.237358	0.190065	0.248353	544587
Dependability	0.319480	049742	0.169476	156070
Physical Ability	0.213868	0.097499	0.614959	0.514519
Integrity	0.298246	301812	0.190222	169062
	Eigenvectors	;		
	Prin5	Prin6	Prin7	Prin8
Communication Skills	0.181087	416563	0.143543	0.333846
Problem Solving	0.453604	0.096750	0.048904	0.199259
Learning Ability	219329	0.578388	114808	0.064088
Judgment Under Pressure	030188	0.102087	0.068204	591822
Observational Skills	325257	301254	297894	0.163484
Willingness to Confront Problems	0.038278	458585	044796	365684
Interest in People	111279	0.030870	011105	0.154829
Interpersonal Sensitivity	0.107807	170305	088194	0.192725
Desire for Self-Improvement	427477	0.105369	0.689011	0.087453
Appearance	0.568044	0.221643	0.049267	257497
Dependability	130575	0.202301	594850	0.081242
Physical Ability	0.203995	0.173168	0.169247	0.302536
Integrity	130757	100039	0.029456	317545
	Eigenvectors	;		
	Prin9	Prin10	Prin11	Prin12
Communication Skills	430955	0.375983	0.028370	252778
Problem Solving	0.256098	372914	434417	0.069863
Learning Ability	0.224706	0.287031	0.210540	284355
Judgment Under Pressure	358618	0.178270	0.118318	0.306490
Observational Skills	0.258377	0.223793	079692	0.565290
Willingness to Confront Problems	0.129976	330710	0.275249	386151
Interest in People	0.321200	081470	0.393841	210915
Interpersonal Sensitivity	0.137468	074821	0.285447	0.276824
Desire for Self-Improvement	121474	363854	052085	0.151436
Appearance	0.087395	0.061890	0.168369	0.236655

Output 69.3.2 continued

	Eigenvectors			
	Prin9	Prin10	Prin11	Prin12
Dependability	495598	377561	164909	090904
Physical Ability	149625	0.258321	006202	055828
Integrity	0.271060	0.297010	612497	276273
	Eigenvectors			
		Pr	rin13	
	Communication Skills	12	2809	
	Problem Solving	11	6642	
	Learning Ability	0.248555 126636		
	Judgment Under Pressure			
	Observational Skills	16	8555	
	Willingness to Confront Proble	ems 0.17	7688	
	Interest in People	61	.0215	
	Interpersonal Sensitivity	0.64	3410	
	Desire for Self-Improvement	0.05	3834	
	Appearance	11	3705	
	Dependability	01	8094	
	Physical Ability	0.13	3430	
	Integrity	0.11	4965	

When the ods graphics on statement is specified, PROC PRINCOMP produces the scree plot as shown in Figure 69.3.3 by default, which helps to visualize and choose the number of components. You can obtain more plots by specifying the PLOTS= option in the PROC PRINCOMP statement.

The "Scree Plot" on the left shows that the eigenvalue of the first component is approximately 6.5 and the eigenvalue of the second component is largely decreased to under 2.0. The "Variance Explained" plot on the right shows that you can explain a near 80% of total variance with the first four principal components.



Output 69.3.3 Scree Plot from the PRINCOMP Procedure

The first component reflects overall performance since the first eigenvector shows approximately equal loadings on all variables. The second eigenvector has high positive loadings on the variables Observational Skills and Willingness to Confront Problems but even higher negative loadings on the variables Interest in People and Interpersonal Sensitivity. This component seems to reflect the ability to take action, but it also reflects a lack of interpersonal skills. The third eigenvector has a very high positive loading on the variable Physical Ability and high negative loadings on the variables Problem Solving and Learning Ability. This component seems to reflect physical strength, but also shows poor learning and problem-solving skills.

In short, the three components represent the following:

First Component: overall performance

Second Component: smart, tough, and introverted

Third Component: superior strength and average intellect

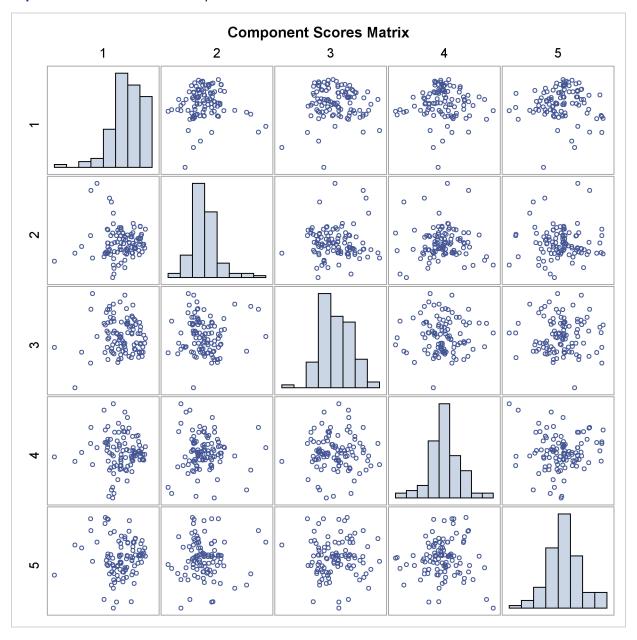
PROC PRINCOMP also produces other plots besides the scree plot, which are helpful while interpreting the results. The following statements request plots from the PRINCOMP procedure:

PLOTS=ALL(NCOMP=3) in the PROC PRINCOMP statement requests all plots to be produced but limits the number of components to be plotted in the component pattern plots and the component score plots to three. The N=5 option sets the number of principal components to be computed to

five. Besides a scree plot similar to the one shown before, the rest of plots are displayed in the following context.

Output 69.3.4 shows a matrix plot of component scores between the first five principal components. The histogram of each component is displayed in the diagonal element of the matrix. The histograms indicate that the first principal component is skewed to the left and the second principal component is slightly skewed to the right.

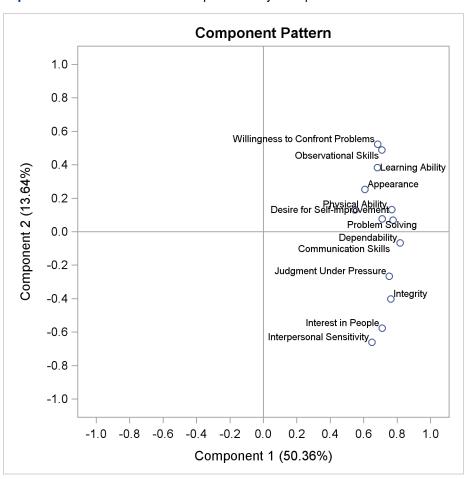
Output 69.3.4 Matrix Plot of Component Scores



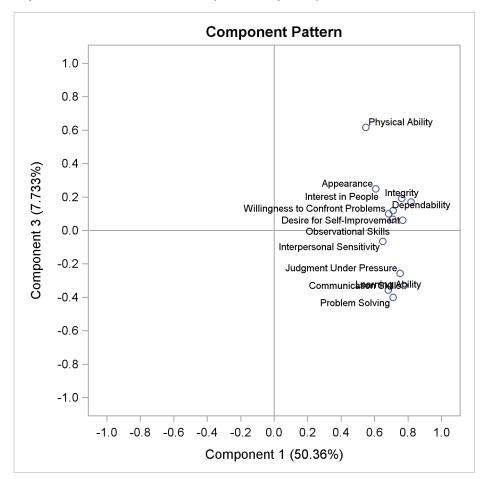
The pairwise component pattern plots are shown in Output 69.3.5 to Output 69.3.7. The pattern plots show the following:

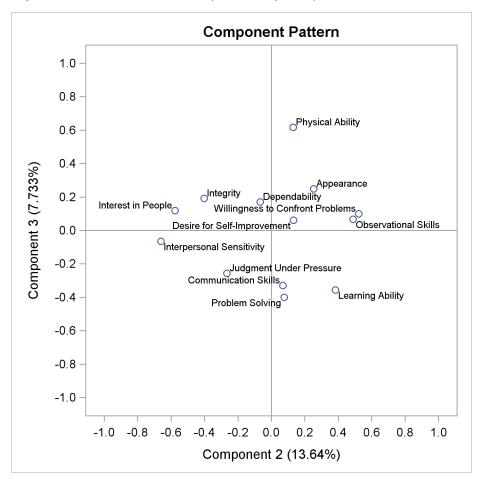
- All variables positively and evenly correlate with the first principal component (Output 69.3.5 and Output 69.3.6).
- The variables Observational Skills and Willingness to Confront Problems correlate highly with the second component, and the variables Interest in People and Interpersonal Sensitivity correlate highly but negatively with the second component (Output 69.3.5).
- The variable Physical Ability correlates highly with the third component, and the variables Problem Solving and Learning Ability correlate highly but negatively with the third component (Output 69.3.6).
- The variable Observational Skills, Willingness to Confront Problems, Interest in People, and Interpersonal Sensitivity correlate highly (either positively or negatively) with the second component, but all have very low correlations with the third component; the variables Physical Ability and Problem Solving correlate highly (either positively or negatively) with the third component, but both have very low correlations with the second component (Output 69.3.7).

Output 69.3.5 Pattern Plot of Component 2 by Component 1



Output 69.3.6 Pattern Plot of Component 3 by Component 1





Output 69.3.7 Pattern Plot of Component 3 by Component 2

Output 69.3.8 shows a component pattern profile. As it was shown in the pattern plots, the nearly horizontal profile from the first component indicates that the first component is mostly correlated evenly across all variables.

Component Pattern Profiles

0.5

Control Profiles

Control Profiles

Control Profiles

Control Profiles

Control Profiles

Variable

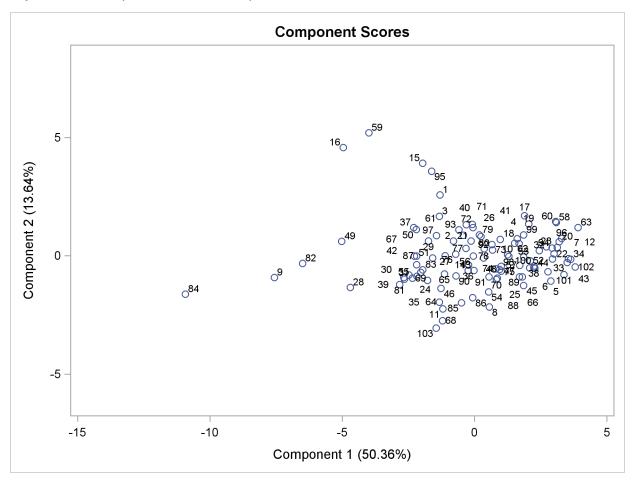
Component 1 - - 2 - - 3 - 4 - - 5

Output 69.3.8 Component Pattern Profile Plot from the PRINCOMP Procedure

Output 69.3.9 through Output 69.3.11 display the pairwise component score plots. Observation numbers are used as the plotting symbol.

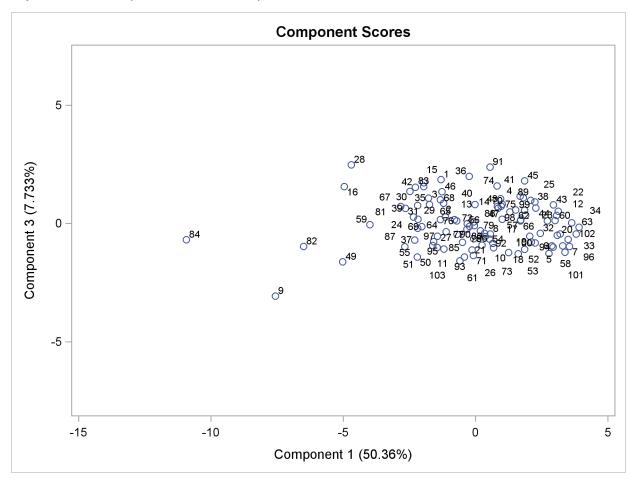
Output 69.3.9 shows a scatter plot of the first and third components. Observations 82, 9, and 84 seem like outliers on the first component; Observations 16 and 59 can be potential outliers on the second component.

Output 69.3.9 Component 2 versus Component 1



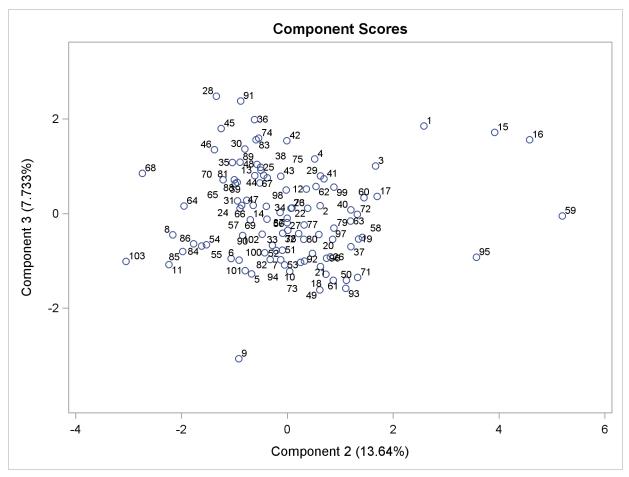
Output 69.3.10 shows a scatter plot of the first and third components. Observations 82, 9, and 84 seem like outliers on the first component.

Output 69.3.10 Component 3 versus Component 1

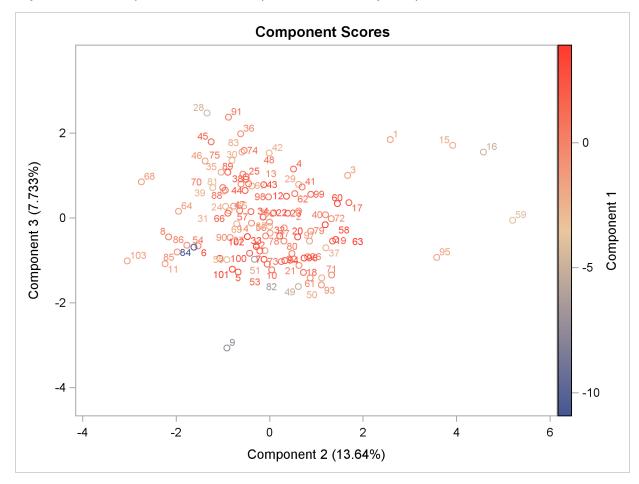


Output 69.3.11 shows a scatter plot of the second and third components. Observations 95, 15, 16, and 59 can be potential outliers on the second component.





Output 69.3.12 shows a scatter plot of the second and third components, displaying density with color. Color interpolation is based on the first component, such as in the statistical style, going from blue (minimum density) to tan (median density) and to red (maximum density).



Output 69.3.12 Component 3 versus Component 2, Painted by Component 1

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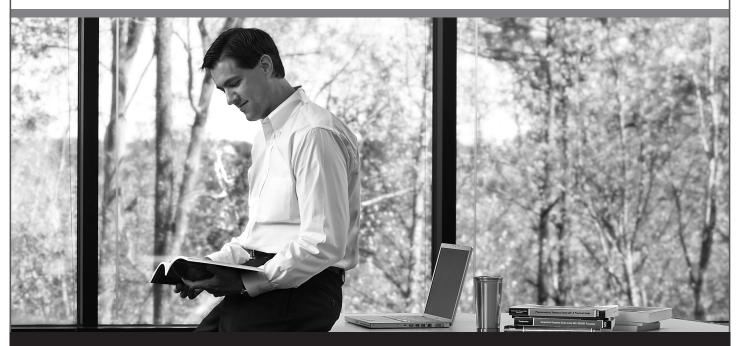
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